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Rapid and precise determination of zero-field splittings by terahertz time-domain electron paramagnetic resonance spectroscopy

A simple tabletop method for the direct measurement of zero-field splittings between the magnetic sublevels of high-spin transition metal compounds is demonstrated. Single-cycle pulses of THz-frequency light irradiate the sample, which emits a characteristic free-induction decay signal that is easily measured. The signal reveals zero-field splittings which are highly sensitive to molecular geometry, symmetry, and electronic structure. Electron paramagnetic resonance (EPR) spectroscopic measurements of zero-field splittings in the THz frequency range should now be broadly accessible.

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Introduction

Transition-metal or rare-earth molecular complexes and biological molecules assume well-defined symmetries, and may undergo structural distortion to lower symmetries due to interactions of the central metal ions with each ligand.¹ The molecular orbitals consequently undergo crystal field splitting, and valence electrons rearrange to form an energetically stable ground state. Zero-field splitting (ZFS) refers to the magnetic sublevel fine structure of unpaired electrons in such molecular orbitals in the absence of an external magnetic field. ZFS originates from spin–spin interactions mediated by the ligand field and from spin–orbit coupling.¹ The behavior of ZFS can be adequately captured by two parameters, D and E, which are the axial and transverse components of the magnetic anisotropy, respectively.²

Accurate determination of the ZFS parameters for atomic centers with unpaired spins is critical in many research fields.

Rapid and precise determination of zero-field splittings by terahertz time-domain electron paramagnetic resonance spectroscopy[†]

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Zero-field splitting (ZFS) parameters are fundamentally tied to the geometries of metal ion complexes. Despite their critical importance for understanding the magnetism and spectroscopy of metal complexes, they are not routinely available through general laboratory-based techniques, and are often inferred from magnetism data. Here we demonstrate a simple tabletop experimental approach that enables direct and reliable determination of ZFS parameters in the terahertz (THz) regime. We report time-domain measurements of electron paramagnetic resonance (EPR) signals associated with THz-frequency ZFSs in molecular complexes containing high-spin transition-metal ions. We measure the temporal profiles of the free-induction decays of spin resonances in the complexes at zero and nonzero external magnetic fields, and we derive the EPR spectra *via* numerical Fourier transformation of the time-domain signals. In most cases, absolute values of the ZFS parameters are extracted from the measured zero-field EPR frequencies, and the signs can be determined by zero-field measurements at two different temperatures. Field-dependent EPR measurements further allow refined determination of the ZFS parameters and access to the *g*-factor. The results show good agreement with those obtained by other methods. The simplicity of the method portends wide applicability in chemistry, biology and material science.

For instance, in nanoscale thermometry based on nitrogen vacancy centers in diamond, the temperature dependence of D, the axial magnetic anisotropy, enables precise measurements of local temperature.³ In metalloproteins, ZFS parameters are essential for interpreting EPR signals and understanding the electronic structure of metallo-cofactors.4 In molecular magnets, D and E are related to both magnetic susceptibility and magnetization;5 measuring these parameters independently anchors the structure-function relationship that enables the design of molecules with higher effective barriers for spin inversion. Indeed, in such molecules, a negative D parameter indicates Ising-type magnetic anisotropy, and the potential energy surface of the spin sublevels has a double-well shape, with a spin inversion barrier that is proportional to D.⁶ Due to their long relaxation and coherence times at low temperatures, single-molecule and single-ion magnets have been proposed to serve as the smallest units in high-density memory, quantum information processing and spintronics,7 as such systems have two stable states that can be switched reversibly by magnetic fields, analogous to nitrogen vacancy centers in diamond.8

Conventional pulsed EPR spectroscopy using microwave technology has been widely applied to measure ZFS parameters between 1 and 100 GHz in the time domain. However, ZFS parameters of many metalloproteins and molecular complexes, in particular molecules with high magnetic anisotropy, lie in

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the THz frequency range between 0.1 and 10 THz (1 THz = 33.3 cm^{-1}). Access to these higher frequencies is not available currently with routine magnetic resonance techniques. In highfrequency, high-field EPR (HFEPR), an external magnetic field is continuously swept to shift the spin resonances to the frequencies of the narrowband THz radiation sources used.9,10 Leading work in this area is conducted with magnetic fields that typically can be varied continuously from 0 to 25 T.11 Compounds with particularly large values of the ZFS parameters would require even higher magnetic fields which scale up with increasing ZFS parameters.12 Because these measurements are conducted with applied magnetic fields, they also do not allow for direct measurements of the ZFS parameters, which are instead inferred from fitting the field-swept resonance data at discrete frequencies. Alternatively, frequency-domain Fouriertransform (FT) EPR using THz sources from coherent synchrotron radiation¹³ or blackbody radiation^{14,15} has been used to measure ZFS parameters in single-molecule magnets13,16 and biological systems14,17 at zero and nonzero external magnetic field. Although this allows direct and broadband measurements of ZFS parameters and enhanced precision when the field-swept broadband spectra are fitted by theoretical modeling,18 the synchrotron THz sources employed thus far place severe limitations on wide applicability in the community. Inelastic neutron scattering has been used to directly measure ZFSs, but a typical experiment requires large amounts of sample (often more than 1 g), and is only available at specialized facilities with neutron sources. Most commonly, temperature-dependent magnetometry measurements have been used to determine ZFS parameters. Although more widely available, this technique is also arguably the most imprecise, because the measurements inevitably convolve ZFS parameters with other magnetic responses (e.g., exchange coupling, which is often of similar frequency to ZFS) and average over the temperature variation of ZFS values. Indeed, ZFS parameters determined by magnetometry often deviate from those measured by other methods. Clearly, the development of a simple technique employing benchtop equipment to directly and reliably measure absolute values of ZFS parameters could have a transformative effect in physical inorganic and organic chemistry, leading to more facile development of new magnetic materials and greatly facilitating the understanding of structure and function in metalloenzymes.

In this work, we present direct characterization of THzfrequency ZFSs in transition-metal complexes by measuring their EPR spectra using THz time-domain spectroscopy both at zero and nonzero external magnetic fields.¹⁹ The broadband spectral coverage of our THz generation and detection methods readily allows for the measurement of EPR signals in transitionmetal complexes with THz-frequency ZFSs at zero field. In cases where there is more than one spin transition, the ZFS parameter absolute values can be derived from a single EPR spectrum, and the spectral linewidths are typically narrower than those at nonzero magnetic fields, yielding optimal resolution.²⁰ The sign of the *D* parameter can be determined by zero-field EPR measurements at two different temperatures. The measurements can be supplemented in important ways with the addition of an applied magnetic field. Field-dependent EPR measurements allow the determination of ZFS parameters in spin systems where only one spin transition is present at zero field. Refined determination of the ZFS parameter values as well as access to the *g*-factor are also provided by field-dependent measurements. At the qualitative level, field-dependent measurements can unambiguously distinguish spin transitions from other low-frequency resonances including molecular or lattice vibrational transitions.

EPR spectra in zero and nonzero magnetic fields

The Hamiltonian^{4,21} for a single electron spin includes the ZFS and electron Zeeman interaction (EZI) terms given by,

$$\hat{H}_0 = \hat{H}_{\text{EZI}} + \hat{H}_{\text{ZFS}}.$$
(1a)

The ZFS Hamiltonian is commonly written as,

$$\hat{H}_{ZFS} = D\left[\hat{S}_{z}^{2} - \frac{1}{3}S(S+1)\right] + E\left(\hat{S}_{x}^{2} - \hat{S}_{y}^{2}\right), \quad (1b)$$

where \hat{S}_i (i = x, y, z) are spin matrices, S is the total spin quantum number, and D and E are the axial and transverse ZFS parameters ($E \le D/3$).²¹ Diagonalization of the ZFS Hamiltonian yields the eigenenergies and eigenvectors of the magnetic sublevels of the spin system at zero static magnetic field. With a nonzero E value, the eigenstates are linear combinations of $|M_S\rangle$ states. Though M_S is a "good" quantum number only when E is zero, the magnetic sublevels are usually denoted by M_S . For integer spin systems, the degeneracy among the magnetic sublevels is completely removed by nonzero D and E. For halfinteger spin systems, degeneracy between $\pm M_S$ doublets remains, but can be removed by applying an external static magnetic field.

The static EZI term accounts for the spin system under a static magnetic field B_0 . The EZI term is usually written as

$$\hat{H}_{\text{EZI}} = \mu_{\text{B}}(\hat{S}_{x}g_{x}B_{0x} + \hat{S}_{y}g_{y}B_{0y} + \hat{S}_{z}g_{z}B_{0z}), \quad (1c)$$

where $\mu_{\rm B}$ is the Bohr magneton, B_{0i} (i = x, y, z) is the static magnetic field, and g_i (i = x, y, z) is the *g*-factor along each molecular axis. The application of a field induces splittings and shifts of the magnetic sublevels derived from the ZFS Hamiltonian. The new eigenenergies and eigenvectors of the spin system under a static external magnetic field can be sufficiently described by $\hat{H}_{\rm ZFS}$ and $\hat{H}_{\rm EZI}$.

The magnetic field of electromagnetic radiation $B_1(t)$ interacts with the spin system also *via* the Zeeman interaction. It induces resonant magnetic dipole-allowed transitions between the magnetic sublevels. By measuring the transition frequencies, the ZFS parameters in the static spin Hamiltonian can be accessed at zero field. The Zeeman splittings and frequency shifts of the magnetic dipole-allowed transitions under a nonzero static magnetic field can also be measured, allowing determination of the *g*-factor.

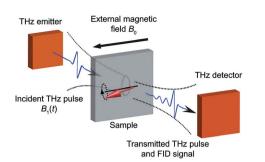


Fig. 1 Schematic illustration of experimental geometry. Single-cycle THz pulses are generated by illuminating the THz emitter with fs laser pulses. The THz pulses are incident onto the sample to excite the spin transitions. The transmitted THz pulses and FID signals are directed into the THz detector. Fs laser pulses are overlapped with the THz fields at the THz detector for phase-resolved detection of the THz signals. The sample is placed in a cryostat with an external magnetic field B_0 perpendicular to the THz magnetic field B_1 (e.g. the Voigt geometry shown here). Fourier transformation of the THz signals yields the EPR spectra. In this work, the THz emitter and detector are both ZnTe crystals as described in the ESI.†

Experimental

The experimental setup is a free-space THz time-domain spectroscopy system in transmission geometry as shown schematically in Fig. 1. (Details of the experimental setup are presented in the ESI Fig. S1[†]) The THz emitter, which was a 1 mm thick (110)-cut zinc telluride (ZnTe) crystal, was illuminated by 800 nm pulses with 100 fs duration from a commercial Ti : sapphire amplifier at a 5 kHz repetition rate. Single-cycle THz pulses with usable bandwidths spanning from 0.1 to 2.5 THz were generated by optical rectification of the laser pulses in the ZnTe crystal.22 The broadband, linearly polarized THz pulses were focused onto the sample where the THz magnetic fields induced magnetic dipole-allowed transitions between the magnetic sublevels.23 The resulting spin coherences radiated electromagnetic signals, known as free-induction decays (FIDs), at the resonance frequencies. We determined the electric field profiles of the FID signals with sub-ps resolution in the time domain by measuring the THz field-induced depolarization of a variably delayed 800 nm probe pulse in another ZnTe crystal.^{22,24} The sample was placed in a helium cryostat with a split superconducting magnet that could be used to apply a static magnetic field B_0 in the 0–5.5 T range. The orientation of B_0 was perpendicular to the polarization of the THz magnetic field B_1 .

We derive the THz FT amplitude spectra $|E_{sig}(v)|$ of the sample both at zero field and at discrete B_0 levels through numerical Fourier transformation of the FID signals. Absorbance spectra A(v) of the samples are obtained by comparing the sample spectra with the reference spectra $|E_{ref}(v)|$ which were measured in the absence of the sample. The absorbance A(v) in units of optical density (OD) is given by

$$A(\nu) = -2 \log_{10}(|E_{\rm sig}(\nu)|/|E_{\rm ref}(\nu)|).$$
(2)

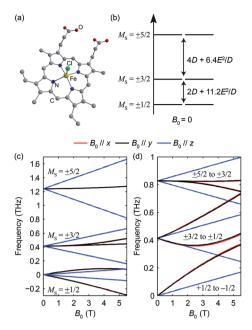


Fig. 2 (a) The structure of hemin. Hydrogen atoms are omitted for clarity. (b) Zero-field magnetic sublevel energy diagram of the HS Fe(III) in hemin (S = 5/2 spin system), where a positive D value is assumed. The magnetic dipole-allowed transitions are shown by the arrows. (c) Calculated Zeeman splitting of the magnetic sublevels as a function of B_0 in hemin. (d) Calculated frequencies of magnetic dipole-allowed transitions as functions of B_0 in hemin. In (c) and (d), the color coding indicates the direction of B_0 with respect to the molecular axes as shown by the legend. The black and red curves ($B_0//x$ and y) are too closely overlapped to distinguish in these plots.

Results and discussion

To demonstrate the utility of the method, we chose prototypical samples that cover all of the common transition metal highspin (HS) states and that are of interest in a diverse spectrum of research fields in which the knowledge of ZFS parameters is crucial. The following proof-of-principle samples were chosen: hemin, a compound that is related to heme-based enzymes, containing HS Fe(m) in a square-pyramidal environment;^{14,17} $CoX_2(PPh_3)_2$ (X = Cl or Br, PPh₃ = triphenylphosphine), a known series of compounds exhibiting single-ion singlemolecule magnetic behavior stemming from HS Co(II) in a pseudo-tetrahedral coordination environment;²⁵; [Fe(H₂O)₆] $(BF_4)_2$, a well-known integer-spin compound with HS Fe(II) in an octahedral environment;²⁶ and NiCl₂(PPh₃)₂, an integer-spin compound with HS Ni(II) in pseudo-tetrahedral rather than the usual square planar geometry.18 Microcrystalline powders of each compound were pressed into pellets which were used in the measurements (for details see ESI[†]).

High-spin Fe(m): spin-5/2 system

Hemin has been under extensive study in EPR, as it is related to heme, which is the functional group in heme-based metalloproteins such as hemoglobin and myoglobin. The squarepyramidal structure of hemin is shown in Fig. 2(a). The valence electrons (d^5) of the HS Fe(m) in hemin indicate a total

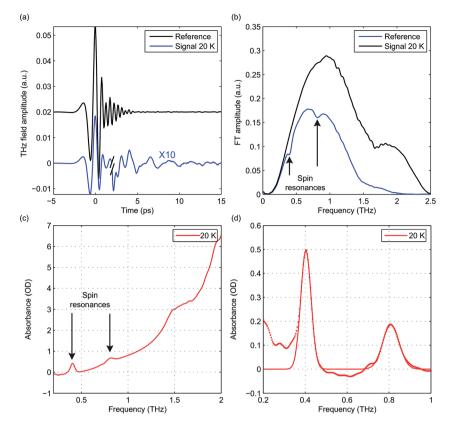


Fig. 3 (a) Time-domain waveforms of the reference THz pulse (black) and the THz pulse transmitted through the sample followed by the FID signal (blue) at zero field. The traces are separated vertically and the FID signal is magnified by 10 for clarity. (b) FT amplitude spectra of the THz reference pulse (black) and the THz pulse and FID signal transmitted through the sample (blue). Two spin resonances are indicated by arrows. (c) Raw absorbance spectrum of hemin at 20 K. (d) Absorbance spectrum after background subtraction (dots) and a fit to two Gaussian functions (solid line).

spin number S = 5/2. The magnetic sublevels derived by diagonalizing the ZFS Hamiltonian with S = 5/2 are shown in Fig. 2(b), where the eigenstates are denoted by $M_{\rm S}$. Magnetic dipole-allowed transitions are denoted by the double-sided arrows, and the transition frequencies shown as functions of D and E are calculated through second-order perturbation theory.10 Measuring the frequencies of these two transitions at zero field readily allows determination of both the D and E parameter values. Zero-field measurements at two temperatures where the intermediate $M_{\rm S} = \pm 3/2$ doublet states are either populated or not allows determination of the sign of D. The Zeeman interaction under nonzero applied field B_0 lifts the Kramers degeneracy and shifts the energies of the $M_{\rm S}$ states as shown in eqn (1c) and Fig. 2(c). The frequencies of the magnetic dipole-allowed transitions as functions of B_0 are plotted in Fig. 2(d). By measuring the frequency shifts of the transitions as a function of applied field strength, the values of the g-factor components can be obtained. The crystallites in the pellet sample are oriented randomly with respect to the applied magnetic field, so all three components can be determined.

The raw time-domain FID signal E(t) and the FT amplitude spectrum $|E(\nu)|$ measured from hemin at zero field and 20 K are shown in Fig. 3. The time-domain waveform of the THz pulse transmitted through the sample shows attenuation and slight

broadening due to the THz absorption and dispersion in the sample. The FID signal is identified as the complex waveform profile following the transmitted THz pulse shown in Fig. 3(a). Numerical Fourier transformation of the THz time-domain signals yielded the complex FT spectra of the reference and

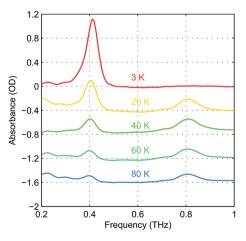


Fig. 4 Temperature-dependent zero-field absorbance spectra of hemin after background subtraction. The data are color-coded according to the temperatures. The higher-frequency peak disappears and the lower-frequency peak shifts slightly at reduced temperatures.

sample. The amplitude spectra are shown in Fig. 3(b), where two dips are assigned as the magnetic dipole-allowed transitions indicated in Fig. 2(b). The absorption spectrum of hemin at 20 K is plotted in Fig. 3(c). In the raw spectrum, these two peaks sit on the wing of broad higher-lying absorptions that may be due to low-frequency vibrations. The background was subtracted manually to yield Fig. 3(d). The lineshapes were fitted to two Gaussian functions, yielding the peak frequencies 0.404 ± 0.001 THz and 0.809 ± 0.001 THz. The S = 5/2 spin Hamiltonian was used to calculate the frequencies with variable ZFS parameters *D* and *E* to determine the absolute values |D| = 6.74 ± 0.01 cm⁻¹ and $|E| = 0.048 \pm 0.048$ cm⁻¹ which show good agreement with previous measurements using frequencydomain FT THz EPR.¹⁸

The absorbance spectra of hemin at several temperatures are shown in Fig. 4. The time-domain data and FT spectra from which the absorbance spectra were determined are shown in Fig. S2 of the ESI.† At temperatures above 20 K, both peaks resulting from the two magnetic dipole-allowed transitions are present. As the temperature decreases to 3 K, the lowerfrequency peak becomes more pronounced while the higherfrequency peak disappears. This shows that at low temperature the spin populations are concentrated in the $M_{\rm S} = \pm 1/2$ states which must therefore be lowest in energy, indicating that the sign of *D* is positive. If *D* were negative, the $M_{\rm S} = \pm 5/2$ states would be lowest in energy and the higher-frequency transition would predominate at low temperature. Details about determination of the sign of *D* can be found in the ESI.[†] The spectral peak at ~0.40 THz at 20 K shifts to ~0.41 THz at 3 K. This shift indicates a change in the ZFS parameter that may arise from subtle changes in the geometric or electronic structure of hemin at different temperatures.

Field-dependent measurements were conducted at 3 K and 20 K. B_0 was oriented along the THz propagation direction (*i.e.*, Faraday geometry). The experimental absorbance spectra at zero field and six discrete B_0 levels are shown in Fig. 5(a) and (b) at 3 K and 20 K, respectively. The background was manually subtracted from all spectra. The time-domain data and FT amplitude spectra are shown in Fig. S3 of the ESI.† The Kramers degeneracy is lifted and the $\pm M_s$ doublets are split at nonzero B_0 . Due to the anisotropy in the g-factor, the spectral peaks are shifted by the Zeeman interaction along all three molecular axes in the powder sample used, corresponding to the fielddependent frequency shifts shown in Fig. 2(d). A new magnetic dipole-allowed transition between the $M_{\rm S} = \pm 1/2$ states emerges at nonzero B_0 and is shifted from zero frequency to the spectral window shown as B_0 increases. The spectra at 20 K become somewhat crowded due to the presence of two peaks at zero field which both split to produce four peaks, plus the new peak starting from zero frequency, with some

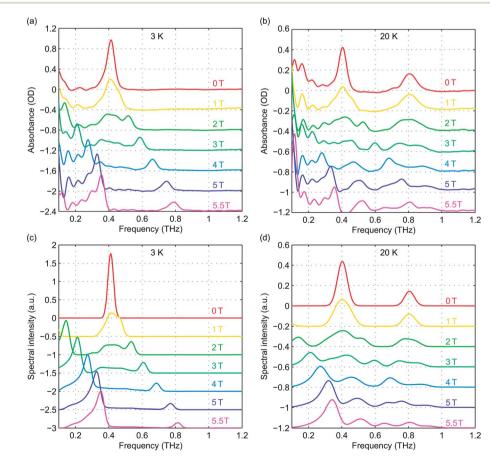


Fig. 5 (a) and (b) Experimental absorbance spectra of hemin as a function of B_0 at 3 K (a) and 20 K (b). (c) and (d) Simulated absorbance spectra at 3 K (c) and 20 K (d). The spectra are color-coded based on the values of B_0 indicated in the figure.

peaks merging to produce complicated lineshapes as the field strength is increased. The spectra at 3 K are simpler since only transitions originating from the $M_{\rm S} = \pm 1/2$ states appear.

To quantitatively analyze the field-dependent spectra of our pellet samples with randomly oriented crystallites, we employed *Easyspin*, an EPR simulation software package.²⁷ A frequency-domain EPR simulation program was used to calculate the spectra for an S = 5/2 spin system at the experimental temperatures and magnetic field levels. The input parameters include the total spin quantum number (set to 5/2), the ZFS parameters *D* and *E*, the *g*-factor elements g_x , g_y , and g_z , and the spectral line-shape and linewidth. The simulated spectra are shown in Fig. 5(c) and (d) for comparison with the experimental data. The frequency shifts and spectral lineshapes show good agreement between the experimental and simulated EPR spectra.

To eliminate possible errors introduced by the background subtraction, we plot in Fig. 6(a) and (b) the difference absorbance spectra between the spectra (without background subtraction) at successive B_0 levels. The difference absorbance spectra can also provide enhanced sensitivity to spectral changes induced by B_0 . The *Easyspin* simulation results at both temperatures are plotted in thick dashed lines and are overlaid

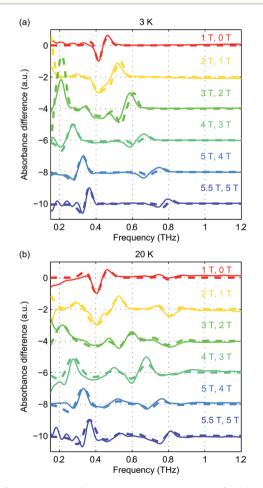


Fig. 6 Experimental difference absorbance spectra (solid lines) and simulated difference intensity spectra (dashed lines) at 3 K (a) and 20 K (b) at various B_0 levels. The spectra are color-coded according to the values of B_0 indicated in the figure.

Table 1Spin Hamiltonian parameters determined through simula-tions of the field-dependent difference EPR spectra for thecompounds

	$D\left(\mathrm{cm}^{-1} ight)$	$E\left(\mathrm{cm}^{-1}\right)$	g_x	g_y	g _z
Hemin, 3 K	6.90	0	1.91	1.91	2.05
Hemin, 20 K	6.73	0.02	1.91	1.91	2.05
$CoCl_2(PPh_3)_2, 6 K$	-14.76	1.61	2.20	2.18	2.23
$CoBr_2(PPh_3)_2$, 2 K	-13.90	0.96	2.10	2.10	2.22
$Fe(H_2O)_6(BF_4)_2$, 1.8 K	10.82	1.00	2.10	2.10	2.10
$NiCl_2(PPh_3)_2$, 2 K	13.27	2.00	2.20	2.17	2.17

with the experimental difference spectra plotted in thin solid lines in Fig. 6(a) and (b). The simulation results at 20 K show good agreement with the experimental data in terms of the frequency shifts and the lineshapes. The simulation results at 3 K capture the transition peak between the $M_{\rm S} = \pm 1/2$ doublets due to g_x and g_y . However, the blue-shifted spectral peak originating from the transitions between $M_{\rm S} = \pm 1/2$ and $M_{\rm S} = \pm 3/2$ states due to g_x and g_y shows slightly smaller frequency shifts than the simulated ones. This discrepancy warrants further study. Based on the comparison between the simulated and experimental field-dependent EPR spectra, we can refine the quantitative determination of the parameters in the spin Hamiltonian of hemin. The parameters of the spin Hamiltonian determined by the simulations of the difference spectra are summarized in Table 1.

High-spin Co(II): spin-3/2 systems

The pseudo-tetrahedral structure of $CoX_2(PPh_3)_2$ (X = Cl or Br) is shown in Fig. 7(a).²⁵ The valence electrons (d^7) of the HS Co(II) indicate a total spin quantum number S = 3/2 due to three unpaired electrons. The magnetic sublevels are derived by diagonalization of the ZFS Hamiltonian with S = 3/2 and are shown in Fig. 7(b) where a negative D value is assumed. The eigenstates are denoted by $M_{\rm S}$. Magnetic dipole-allowed transitions are denoted by the double-sided arrows, and the frequency is given by $2\sqrt{D^2+3E^2}$. Due to Kramers degeneracy between the $\pm M_{\rm S}$ states, only one transition is observable at zero field, which is insufficient for separate determination of D and E or determination of the sign of D. The application of B_0 lifts the Kramers degeneracy and shifts the energies of the $M_{\rm S}$ states as shown in Fig. 7(c). The field-dependent transition frequencies are calculated and plotted in Fig. 7(d). Several magnetic dipole-allowed transitions emerge under a nonzero B_0 and allow separate determination of D and E. Measuring the transition between $M_{\rm S} = \pm 1/2$ states at different temperatures allows determination of the sign of D.

The zero-field absorbance spectra of the two compounds at low temperatures are shown in Fig. 8(a) and (b). The timedomain signals and FT amplitude spectra are shown in Fig. S4 of the ESI.† Several strong spectral peaks are all due to vibrations. One spectral peak due to the spin transition is indicated by the arrow in each figure. The magnetic origin of the transitions is confirmed in the field-dependent measurements

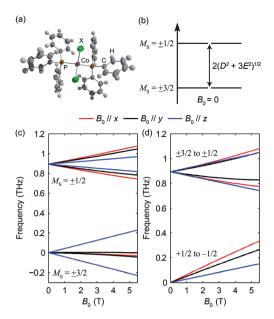
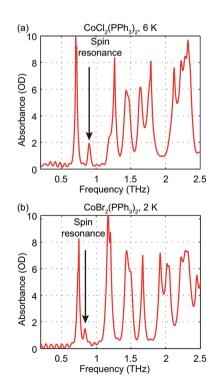


Fig. 7 (a) The structure of $CoX_2(PPh_3)_2$. (b) Zero-field magnetic sublevel energy diagram of the HS Co(III) in $CoX_2(PPh_3)_2$ (S = 3/2 spin systems), where a negative D is assumed. The magnetic dipoleallowed transition is shown by the arrow. (c) Zeeman splitting of the magnetic sublevels as a function of B_0 . (d) Frequencies of magnetic dipole-allowed transitions as functions of B_0 . In (c) and (d), the color coding indicates the direction of B_0 with respect to the molecular axes as shown by the legend.

discussed later. Each spectral peak is fitted to a Lorentzian function, with central frequencies 0.901 \pm 0.001 THz for $CoCl_2(PPh_3)_2$ and 0.838 \pm 0.001 THz for $CoBr_2(PPh_3)_2$. The combination of the ZFS parameters $\sqrt{D^2 + 3E^2}$ can be determined from the peak frequency in each case, yielding 15.01 \pm 0.03 cm⁻¹ and 13.96 \pm 0.03 cm⁻¹ for the Cl and Br compounds respectively at their experimental temperatures. The ZFS parameter values D = -14.76 cm⁻¹ and E = 1.141 cm⁻¹ of $CoCl_2(PPh_3)_2$ have been measured by HFEPR,²⁸ yielding $\sqrt{D^2 + 3E^2} = 14.89$ cm⁻¹ in good agreement with our measurement.

Field-dependent measurements from 0 to 5.5 T were conducted on each sample. B_0 was oriented perpendicular to the THz propagation direction (i.e., Voigt geometry). The timedomain FID data and spectra are shown in Fig. S4 of the ESI.† The field-dependent absorbance spectra are shown in Fig. 9 for the two compounds. The modulations are artifacts from the Fourier transformation as discussed in the ESI.† At 1 T, the spin resonance peak in each compound exhibits a decrease in amplitude and broadening due to the anisotropic Zeeman interaction. At higher B_0 levels, the peaks split into several peaks, following the trends shown in Fig. 7(d). The transition between the $M_{\rm S} = \pm 1/2$ doublets emerges at nonzero B_0 and is expected to be around 0.3 THz at 5.5 T. The absence of these absorption peaks at 5.5 T at such low temperatures implies that the populations in the $M_{\rm S}=\pm 1/2$ states are depleted and the populations are concentrated in the lower-energy $M_{\rm S} = \pm 3/2$ states. The sign of the D parameter is therefore determined to be negative in each compound.



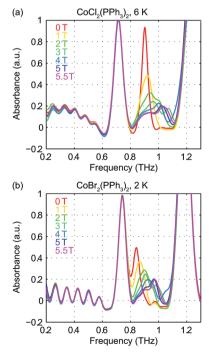


Fig. 8 Zero-field absorbance spectra of $CoCl_2(PPh_3)_2$ at 6 K (a) and $CoBr_2(PPh_3)_2$ at 2 K. The spin resonance peak in each figure is indicated by the arrow. Other strong absorption peaks are due to vibrations.

Fig. 9 Field-dependent absorbance spectra of $CoCl_2(PPh_3)_2$ at 6 K (a) and $CoBr_2(PPh_3)_2$ at 2 K (b). The spectral modulations are artifacts of Fourier transformation. The spectra are color-coded based on the values of B_0 shown in the legends.

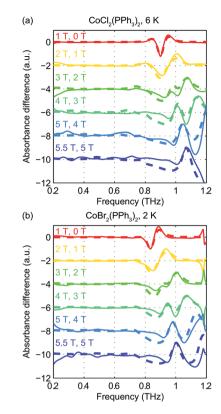


Fig. 10 Experimental difference absorbance spectra (solid lines) and simulated difference intensity spectra (dashed lines) for $CoCl_2(PPh_3)_2$ at 6 K (a) and $CoBr_2(PPh_3)_2$ at 2 K (b). The spectra are color-coded according to the values of B_0 indicated in the figure. Additional features around 1.2 THz are due to the strong nearby vibrational absorption peak in each compound.

Quantitative analysis of the field-dependent spectra is conducted by comparing the experimental difference absorbance spectra with the simulated ones. The results are shown in Fig. 10. The simulation assumes negative D values for both compounds, which further confirms the determination of the sign of the D parameter. Separate determination of the D and E parameters is possible by analyzing the field-dependent spectra for S = 3/2 systems. The relevant parameters of the spin Hamiltonian determined by the simulation are listed in Table 1. The measurements yield $\sqrt{D^2 + 3E^2}$ values of 15.02 cm⁻¹ for $CoCl_2(PPh_3)_2$ at 6 K and 14.00 cm⁻¹ for $CoBr_2(PPh_3)_2$ at 2 K. In these two compounds, the spin transition peaks lie between two stronger absorptions due to vibrations. The peak vibrational absorptions are so strong that even small imperfections in their subtraction result in artifacts in the difference absorbance spectra.

High-spin Fe(II): spin-2 system

The structure of $Fe(H_2O)_6^{2+}$ is shown in Fig. 11(a).²⁹ The HS Fe(II) ion is in octahedral coordination with six water ligands. Four unpaired electrons of the valence electrons (d⁶) indicate a total spin quantum number S = 2. The magnetic sublevel energy diagram assuming a positive *D* and a nonzero *E* is shown in Fig. 11(b). The new eigenstates are denoted by Φ_i with their

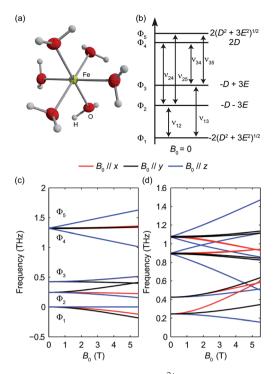


Fig. 11 (a) The structure of $Fe(H_2O)_6^{2+}$. (b) Zero-field magnetic sublevel diagram of the HS Ni(II) in NiCl₂(PPh₃)₂ (S = 1 spin system), where a positive *D* value is assumed. The magnetic dipole-allowed transitions are shown by the arrows. (c) Zeeman splitting of the magnetic sublevels as a function of B_0 . (d) Frequencies of magnetic field. In (c) and (d), the color coding indicates the direction of B_0 with respect to the molecular axes, as shown by the legend.

eigenenergies labeled in Fig. 11(b). Magnetic dipole-allowed transitions are denoted by the double-sided arrows. As the Φ_i states are superpositions of the M_s states, six magnetic dipoleallowed transitions exist at zero field. As $D \gg E$ is typical, the splitting between Φ_4 and Φ_5 is small. The transitions to Φ_4 and Φ_5 states are often merged, which results in four distinct

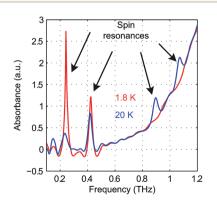


Fig. 12 Zero-field absorbance spectra of $Fe(H_2O)_6(BF_4)_2$ at 1.8 K (red) and 20 K (blue). At 1.8 K, two strong peaks are assigned as the spin resonances resulting from two transitions. At 20 K, four peaks are assigned as the spin resonances resulting from six transitions. In this case the peak frequencies could be determined accurately without subtraction of the background absorption.

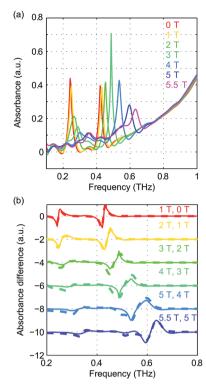


Fig. 13 (a) Field-dependent absorbance spectra of $Fe(H_2O)_6(BF_4)_2$ at 1.8 K. The two spin resonance peaks show splittings and shifts as a function of the applied magnetic field. (b) Experimental difference absorbance spectra (solid lines) and simulated difference intensity spectra (dashed lines) for $Fe(H_2O)_6(BF_4)_2$ at 1.8 K. The spectra are color-coded according to the magnetic field values indicated in each figure.

transitions. The values of the ZFS parameters *D* and *E* are adequately determined by a zero-field measurement of the frequencies v_{12} and v_{13} . The sign of *D* can be determined by temperature-dependent measurements at zero field. The application of B_0 further shifts the magnetic sublevels as shown in Fig. 11(c). The frequency shifts of the magnetic dipole-allowed transitions as a function of B_0 are shown in Fig. 11(d).

The zero-field absorbance spectra of $Fe(H_2O)_6(BF_4)_2$ at 1.8 K and 20 K are shown in Fig. 12. The time-domain signals and FT amplitude spectra are shown in Fig. S5 of the ESI.[†] At 1.8 K, only the lowest state Φ_1 is populated. Two absorption peaks located through Lorentzian fits at 0.243 \pm 0.001 THz and 0.423 \pm 0.001 THz are assigned as the spin transitions at frequencies v_{12} and v_{13} between Φ_1 and Φ_2 and between Φ_1 and Φ_3 , respectively, as shown in Fig. 11(b). The assignments were confirmed by fielddependent measurements discussed below. Based on the values of v_{12} and v_{13} , the ZFS parameters are calculated to be |D| $= 10.82 \pm 0.03$ cm⁻¹ and $|E| = 1.00 \pm 0.01$ cm⁻¹. At 20 K, four transitions are observed as the intermediate states Φ_2 and Φ_3 are also populated. The two absorption peaks at frequencies v_{12} and v_{13} become weaker, and two additional spectral peaks at ${\sim}0.90$ THz and ${\sim}1.07$ THz emerge due to the transitions between the higher-lying states. Hence the sign of the D parameter is determined to be positive.

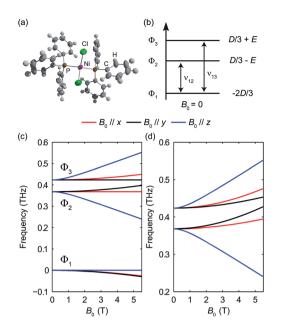


Fig. 14 (a) The structure of NiCl₂(PPh₃)₂. (b) Zero-field magnetic sublevel diagram of the HS Fe(II) in Fe(H₂O)₆(BF₄)₂ (S = 2 spin system), where a positive *D* value is assumed. The magnetic dipole-allowed transitions are shown by the arrows. (c) Zeeman splitting of the magnetic sublevels as a function of *B*₀. (d) Frequencies of magnetic dipole-allowed transitions as functions of *B*₀. In (c) and (d), the color coding indicates the direction of *B*₀ with respect to the molecular axes, as shown by the legend.

Due to the relative simplicity of the zero-field EPR spectra at 1.8 K where only two transitions appear, field-dependent measurements from 0 to 5.5 T were conducted at 1.8 K in the Voigt geometry. The experimental absorbance spectra are shown in Fig. 13(a). The time-domain signals and FT amplitude spectra are shown in Fig. S6 of the ESI.[†] The spectral peaks assigned as spin resonances show splittings and shifts as a function of B_0 , which confirm their magnetic origins. To eliminate the background due to the wing of higher-lying absorptions by vibrations, difference absorbance spectra are overlapped with simulated ones for comparison, which show excellent agreement. The spin Hamiltonian parameters determined by the simulations are listed in Table 1.

High-spin Ni(II): spin-1 system

The pseudo-tetrahedral structure of NiCl₂(PPh₃)₂, which is similar to the structure of CoCl₂(PPh₃)₂, is shown in Fig. 14(a). Two unpaired electrons of the valence electrons (d⁸) of the HS Ni(II) indicate a total spin quantum number S = 1. Similar to the case of the S = 2 spin system, with a zero E value, the degeneracy between the $\pm M_S$ states remains and the eigenstates are the M_S states. With a nonzero E value, the degeneracy between the $M_S = \pm 1$ states is lifted and the new eigenstates are superpositions of the M_S states. The magnetic sublevel energy diagram with positive D and nonzero E values is shown in Fig. 14(b) with new eigenstates denoted by Φ_i whose eigenenergies are indicated. Magnetic dipole-allowed transitions are denoted by the double-

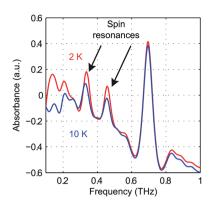


Fig. 15 Zero-field absorbance spectra of $NiCl_2(PPh_3)_2$ at 2 K (red) and 10 K (blue). The two spin resonance peaks are shown by the arrows and are present at both temperatures. The stronger peak is due to a vibration.

sided arrows. At zero field, two transitions are observable with frequencies denoted as v_{12} and v_{13} . The values of the ZFS parameters *D* and *E* are adequately determined by measuring v_{12} and v_{13} . The sign of *D* can be determined by temperature-dependent measurements at zero field. The application of B_0 shifts the magnetic sublevels as shown in Fig. 14(c). The frequency shifts of the magnetic dipole-allowed transitions as a function of B_0 are shown in Fig. 14(d) which allows the determination of the *g*-factor.

The zero-field absorbance spectra of $NiCl_2(PPh_3)_2$ at 2 K and 10 K are shown in Fig. 15. The time-domain signals and FT amplitude spectra are shown in Fig. S7 of the ESI.† The dominant peak is likely due to a lattice vibrational mode. It is at a frequency similar to that of a peak in the spectra of CoCl₂ (PPh₃)₂ due to their similar molecular structures and atomic masses. Two weaker absorption peaks are assigned as the spin resonances. The ZFS parameters can be calculated based on the frequencies of these two peaks, which correspond to the transitions at v_{12} and v_{13} in Fig. 14(b). The frequencies were obtained by fitting the spectral lineshapes to two Gaussian functions, yielding $\nu_{12}=0.337\pm0.001$ THz and $\nu_{13}=0.459\pm$ 0.001 THz. The ZFS parameters were calculated to be |D| = $13.27 \pm 0.03 \text{ cm}^{-1}$ and $|E| = 2.03 \pm 0.03 \text{ cm}^{-1}$ at 2 K, which show good agreement with previous HFEPR results28 yielding D = 13.196 cm⁻¹ and E = 1.848 cm⁻¹. The appearance of two peaks at both 2 K and 10 K implies that the lowest energy state is Φ_1 , where the population is concentrated. If Φ_3 were the lowest energy state, the population at Φ_2 would be mostly depleted and only one transition peak would be expected at 2 K. Hence the sign of the D parameter is determined to be positive.

The field-dependent absorbance spectra of $NiCl_2(PPh_3)_2$ at 2 K (Voigt geometry) are shown in Fig. 16(a). The time-domain signals and FT amplitude spectra are shown in Fig. S8 of the ESI.[†] The two spin resonance peaks show field-dependent frequency shifts. The dependence of the spectral peaks on the magnetic field is analyzed by comparing the difference absorbance spectra with those obtained from simulations. The results are shown in Fig. 16(b), which shows excellent agreement between the experimental and simulated spectra.

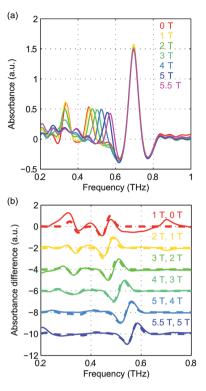


Fig. 16 (a) Field-dependent absorbance spectra of NiCl₂(PPh₃)₂ at 2 K. The two spin resonance peaks show splittings and shifts as a function of B_0 . The strong absorption peak is likely due to lattice vibrations. (b) Experimental difference absorbance spectra (solid lines) and simulated difference intensity spectra (dashed lines) for NiCl₂(PPh₃)₂ at 2 K. The spectra are color-coded according to the values of B_0 indicated in each figure.

spin Hamiltonian parameters determined by the simulations are listed in Table 1.

Conclusions

We demonstrate using four representative molecules a fast, facile, and reliable technique to measure ZFS parameters directly, in the absence of a magnetic field, and to refine the determination through field-dependent measurements. We use THz time-domain FID measurements to obtain EPR signals associated with THz-frequency ZFSs in molecular complexes. We fully characterized the values and signs of the ZFS parameters for several compounds belonging to S = 1, S = 3/2, S = 2and S = 5/2 spin systems based on the zero-field and/or fielddependent EPR spectra. Values of the g-factor are also obtained from the field-dependent measurements. This technique permits unambiguous assignment of THz-frequency ZFS parameters at different temperatures, which is difficult to accomplish by magnetometry measurements. More specifically, integer THz-frequency spin systems were termed "EPR silent" as the magnetic dipole-allowed transitions are not accessible in traditional EPR measurements due to the large ZFS parameters. HFEPR can access complexes with moderate ZFSs that are shifted into the excitation bandwidth via the Zeeman interaction, but the magnetic fields required for such measurements with monochromatic excitation sources can be quite large for complexes with high ZFS. The THz time-domain EPR measurement provides a direct way to measure large ZFSs in the THz-frequency region which is characteristic for molecular magnets.

In our current experiments, the spin number density was on the order of 10^{21} cm⁻³. Considering the \sim 5 mm THz beam diameter throughout the 2 mm thick pellet samples, the measured signals emerged from $\sim 10^{20}$ spins (see ESI[†] for details). The estimated sensitivity of our current measurement configuration is 10¹⁹ spins which is close to that required from a reasonable amount of large biomolecules.15,17 In this work, the THz source and detector utilized allow us to measure resonances between about 6 and 80 cm⁻¹. The ranges of D and E that are accessible in this work depend on the specific spin system under study. Although we used homebuilt THz systems for our measurements, existing THz technologies³⁰ including some commercially available tabletop instruments can provide broader THz spectral coverage throughout the far-infrared range,³¹ higher resolution,³² higher sensitivity,³³⁻³⁶ and faster data acquisition times.32,37 These will allow determination of ZFS parameters and other magnetic fine structure revealed through THz-frequency spin transitions.

Because the technique is independent of the identity of the spin center and of the spin value, it can be applied broadly to systems with non-zero ZFS. We expect that the general approach in using THz time-domain spectroscopy to characterize transitions in the spin manifold of open-shell systems can be further elaborated to include other magnetic interactions, including magnetic exchange, for instance. Apart from the demonstrated advantages of THz time-domain spectroscopy over its frequency-domain counterpart,38 the time-domain oscillation periods of ~ 1 ps will allow measurement of the dynamic evolution of unpaired electron spins as revealed by timedependent changes in the ZFS spectra following, for example, pulsed optical excitation of a molecular state from which charge transfer or spin crossover occurs.39,40 Two-dimensional (2D) THz magnetic resonance spectroscopy of collective spin waves (magnons) has recently been demonstrated,⁴¹ and 2D THz EPR measurements of HS compounds may also prove possible. THz EPR echoes (as observed in the 2D THz measurements of magnons) could prove useful for separation of spin transitions in biomolecules from low-frequency vibrations which may undergo very rapid dephasing, after which echo signals may be dominated by otherwise obscured spin coherences. The methodology presented herein and its future developments will find wide-ranging applications in characterizing magnetic properties of molecules, biological systems, and condensed matter.

Conflicts of interest

There are no conflicts to declare.

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