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Complete List of Authors:	Gerber, Robert; The Hebrew University of Jerusalem , Chemistry; University of California, Irvine, McCaslin, Laura; University of California Irvine Department of Ecology and Evolutionary Biology Karimova, Natalia; University of California, Irvine,

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Ion Reactions in Atmospherically-Relevant Clusters: Mechanisms, Dynamics and Spectroscopic Signatures

Natalia V. Karimova^{1*}, Laura M. McCaslin^{2*} and R. Benny Gerber^{1,2**}

¹Department of Chemistry, University of California, Irvine, CA 92697, USA

²Institute of Chemistry and Fritz Haber Research Center, Hebrew University of Jerusalem, Jerusalem 91904, Israel

Abstract

Reactions of nitrogen oxides with seawater are of major atmospheric importance, but microscopic understanding of these processes is still largely unavailable. In this paper we explore models of reactions of N_2O_4 with ions in water in order to provide molecular-level understanding into the processes. Presented here are studies of N_2O_4 interacting with two ions, SO_4^{2-} and Cl^- , in small water clusters. Reactions of the asymmetric conformer of N_2O_4 with SO_4^{2-} ions in water clusters are studied via *ab initio* molecular dynamics (AIMD) simulations in order to unravel the microscopic mechanism of the processes and predict the timescales of different steps. Spectroscopic signatures of the reaction are proposed. The mechanisms of chloride substitution and hydrolysis of symmetric and asymmetric N_2O_4 are explored via intrinsic reaction coordinate (IRC) calculations. Spectroscopic calculations for relevant species suggest possible experimental signatures for the processes. The results of these model ion- N_2O_4 reactions in water throw light on the molecular-level mechanisms of the reactions of nitrogen oxides with seawater.

1. Introduction

Nitrogen oxides, including NO_2 , NO_3 , N_2O_4 and N_2O_5 , play key roles in the chemistry of the atmosphere.¹ In addition to gas phase reactions, much of the importance of these molecules is due to heterogeneous processes that several of these species undergo in aqueous environments, including liquid water, aerosols and cloud drops.

One key heterogeneous reaction of nitrogen oxides in the atmosphere is the hydrolysis of N_2O_5 in aqueous aerosols, the main removal process of this molecule from the atmosphere at nighttime that produces the acid HNO_3 .²⁻⁵ In addition to hydrolysis, N_2O_5 is known to react with halide-containing salty water, to form XNO_2 ($\text{X}=\text{Cl}, \text{Br}, \text{I}$), which is a source of reactive halogen atoms in the atmosphere.⁵⁻⁹ The microscopic mechanisms of halide substitution in N_2O_5 have not yet been unraveled, and work on this topic is currently underway.¹⁰ More is presently known on non-reactive interaction between N_2O_5 and water, partly due to recent extensive molecular dynamics simulations.¹¹

In this paper, we investigate the molecular-level mechanisms of the reactions between atmospherically relevant anions in water and the nitrogen oxide N_2O_4 . Present knowledge on this

topic is very incomplete, and the challenges are similar to those encountered for the N_2O_5 reactions. Theoretically, a major difficulty is that the interaction potentials that govern the reactions are complicated due to strong electrostatic interactions and charge transfer processes, and require description by *ab initio* methods of a suitable level. Furthermore, the actual atmospheric systems are extended, nanosize aerosols at the very least, so models must be introduced that enable computationally feasible calculations while still representing the correct chemical mechanisms.

N_2O_4 has two isomers that are believed to play a role in atmospheric processes.¹²⁻¹⁷ Symmetric N_2O_4 is the more stable isomer, but the barrier for conversion into the asymmetric, more active form of the molecule that is written as ONONO_2 can be overcome, e.g. on water and other surfaces.¹³⁻¹⁸ The possibility of such conversion depends on the specific system and on the temperature, and has not yet been unraveled in detail. We will rely here on the experimental evidence on the formation and chemical activity of asymmetric N_2O_4 on water and ice surfaces in atmospheric conditions.¹⁵⁻¹⁶

In this paper, we computationally explore the reactions of sulfate ions in water clusters with ONONO_2 at the surface, as well as the reactions of chloride with both asymmetric and with symmetric N_2O_4 in the small cluster $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$. We additionally explore the hydrolysis of ONONO_2 in the presence of Cl^- . Previously reported studies include exploration of the hydrolysis of ONONO_2 in small water clusters to produce HONO and HNO_3 ¹⁹, the reaction of ONONO_2 with HCl in the cluster $(\text{ONONO}_2)(\text{HCl})(\text{H}_2\text{O})$,^{20, 21} and the reaction of HCl following collision with ONONO_2 absorbed on a slab of water.²² As will be discussed later, there are close connections between the mechanisms of these processes and the reactions considered here, especially that of the Cl^- ion.

The structure of the paper is as follows: Section 2 presents computational studies of ONONO_2 at the surface of the cluster $(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$, yielding the dynamics and the reaction pathways of the processes, unraveling the microscopic mechanisms, and suggesting possible spectroscopic signatures for future experiments. Section 3 explores the reaction pathways of the cluster $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$ both for asymmetric ONONO_2 and symmetric N_2O_4 . Conclusions of the reactions of N_2O_4 with ions in the presence of water, and the connections to reactions of N_2O_5 , are brought in Section 4.

2. Reactions of N_2O_4 with $(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$

2.1. System and Methods.

Sulfate ions are some of the most abundant ions present in seawater, making their reactions quite important in the atmosphere. Here we present the highly symmetric and compact $(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$ cluster to model the hydrated ion.^{23,24} The structure, shown in Fig. 1a, is computed at the PBE0-D/6-31+G* level of theory.²⁵⁻²⁸ All calculations were carried out in the QChem program package.²⁹

The shell of 12 water molecules shields the sulfate ion by four strongly bound trimer water rings. We aim to understand whether a reagent such as N_2O_4 can penetrate the water layer and react with the sulfate ion. The structures of the symmetric and the asymmetric isomers, computed at

the same level of theory, are shown in Fig. 1b and 1c, respectively. N_2O_4 is calculated to be 11.0 kcal/mol more stable than ONONO_2 at their equilibrium structures shown in Fig. 1. The equilibrium structures of $(\text{N}_2\text{O}_4)(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$ and $(\text{ONONO}_2)(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$ are shown in Fig. 2. The energy difference between the two clusters is only 1.8 kcal/mol, indicating that ONONO_2 is significantly stabilized upon clustering with the hydrated sulfate, although the symmetric isomer remains the more stable structure.

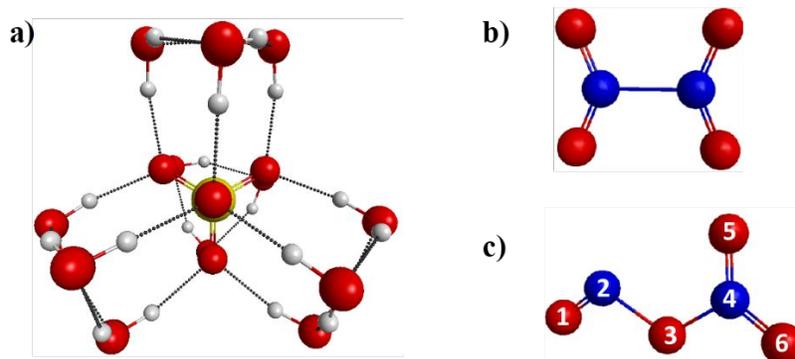


Figure 1 Structures of a) $(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$, b) the symmetric N_2O_4 molecule, and c) the asymmetric *trans*- ONONO_2 molecule. Atom colors: red – oxygen, yellow – sulfur, white – hydrogen, and blue – nitrogen.

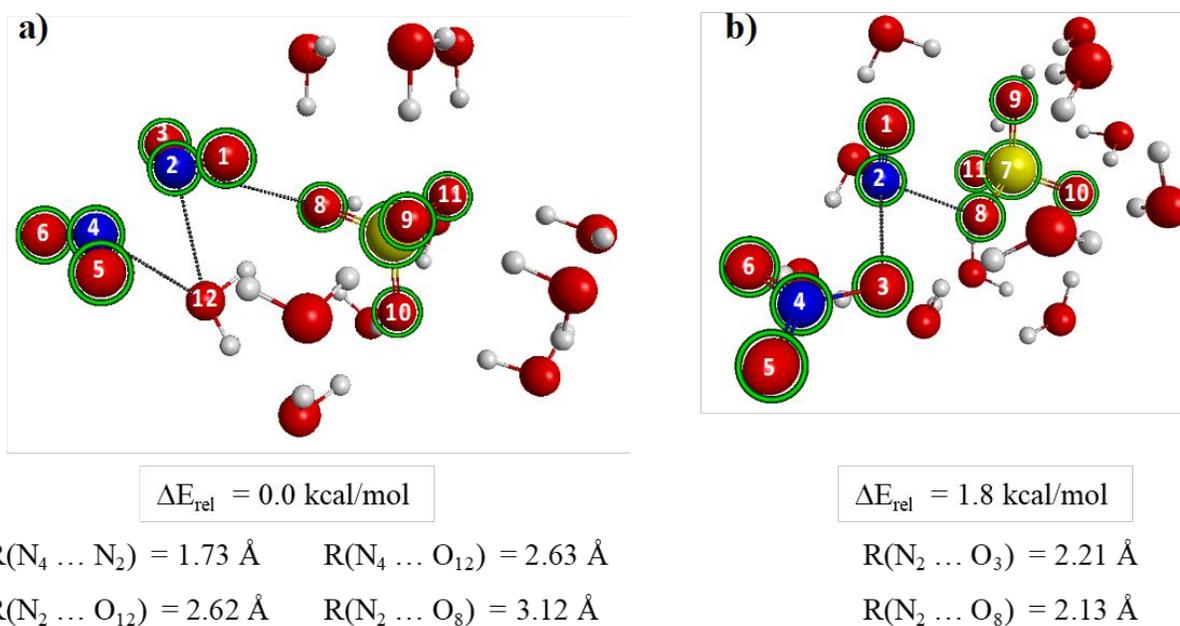


Figure 2 Structures, relative energies, and distances in a) $(\text{N}_2\text{O}_4)(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$, b) $(\text{ONONO}_2)(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$. Atom colors: red – oxygen, yellow – sulfur, white – hydrogen, and blue – nitrogen. The atoms of N_2O_4 and SO_4^{2-} are marked by green circles.

The relatively large stabilization of ONONO_2 by the water cluster is compatible with experimental evidence, noted previously, that polar ONONO_2 is formed and stabilized on ice surfaces due to interactions with free OH groups of amorphous ice.^{15,16} Finally, we note that the

binding energy of ONONO_2 to the $(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$ cluster, 21.7 kcal/mol, is significantly larger than that of N_2O_4 , 12.5 kcal/mol.

To explore the reaction at room temperature between N_2O_4 and the hydrated ion, we used *ab initio* molecular dynamics (AIMD),^{30–32} with potentials at the PBE0-D/6-31+G* level of theory. We find that $(\text{ONONO}_2)(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$ reacts very quickly while the reaction of $(\text{N}_2\text{O}_4)(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$ requires much longer timescales. This can be expected due to the relative ease to break the ON–ONO₂ bond compared to the strong N–N bond in N_2O_4 . Additionally, the reactions of the asymmetric ONONO_2 are sterically favored. It is quite possible that $(\text{N}_2\text{O}_4)(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$ must first undergo isomerization to the asymmetric isomer before reaction, though the timescales needed to observe such a process are much longer than were studied here. We therefore focus only on clusters containing the asymmetric isomer, $(\text{ONONO}_2)(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$, in the dynamics simulations.

2.2. Evolution in Time of Reaction between N_2O_4 and $(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$

Initial velocities were sampled for the equilibrium structure of $(\text{ONONO}_2)(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$ from a Boltzmann distribution at room temperature ($T = 298$ K). A total of 10 reactive trajectories were propagated for up to 7.5 ps using a time-step of 0.4 fs. All the trajectories showed the formation of SO_4NO^- and separation of NO_3^- ion. The product SO_4NO^- was obtained in one of two conformer structures, *cis*- SO_4NO^- and *trans*- SO_4NO^- shown in Fig. 3.

Snapshots of a trajectory leading to *cis*- SO_4NO^- are shown in Fig. 4. Trajectories leading to *trans*- SO_4NO^- are quite similar in character and timescales. In the initial complex $(\text{ONONO}_2)(\text{SO}_4^{2-})(\text{H}_2\text{O})_{12}$ at 0 ps (Fig. 2b, Fig. 4), the ONONO_2 molecule is coordinated to the sulfate ion between the ONONO_2 terminal nitrogen ($\text{N}^{(2)}$) and nearby oxygen ($\text{O}^{(8)}$) of the sulfate with distance 2.13 Å (labels given in Fig. 2b). It should be additionally noted that the distance between the NO and NO_3 groups in the ONONO_2 molecule increases by 0.67 Å in the presence of the hydrated sulfate ion in comparison to the ON–ONO₂ distance in isolated, gas phase ONONO_2 .

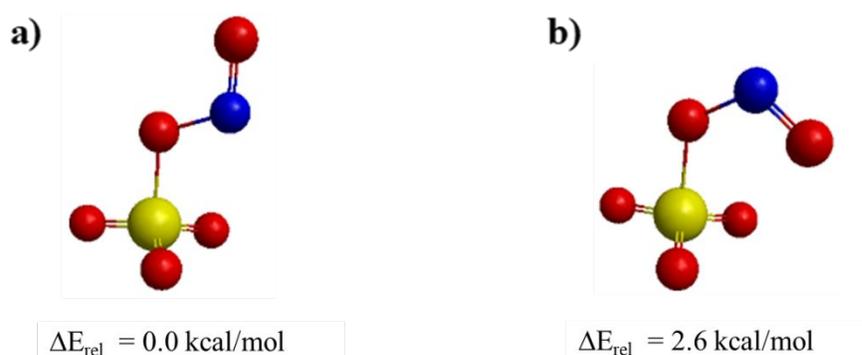


Figure 3 Structures and relative energies of a) *trans*- SO_4NO^- and b) *cis*- SO_4NO^- . Atom colors: red – oxygen, yellow – sulfur, white – hydrogen, and blue – nitrogen.

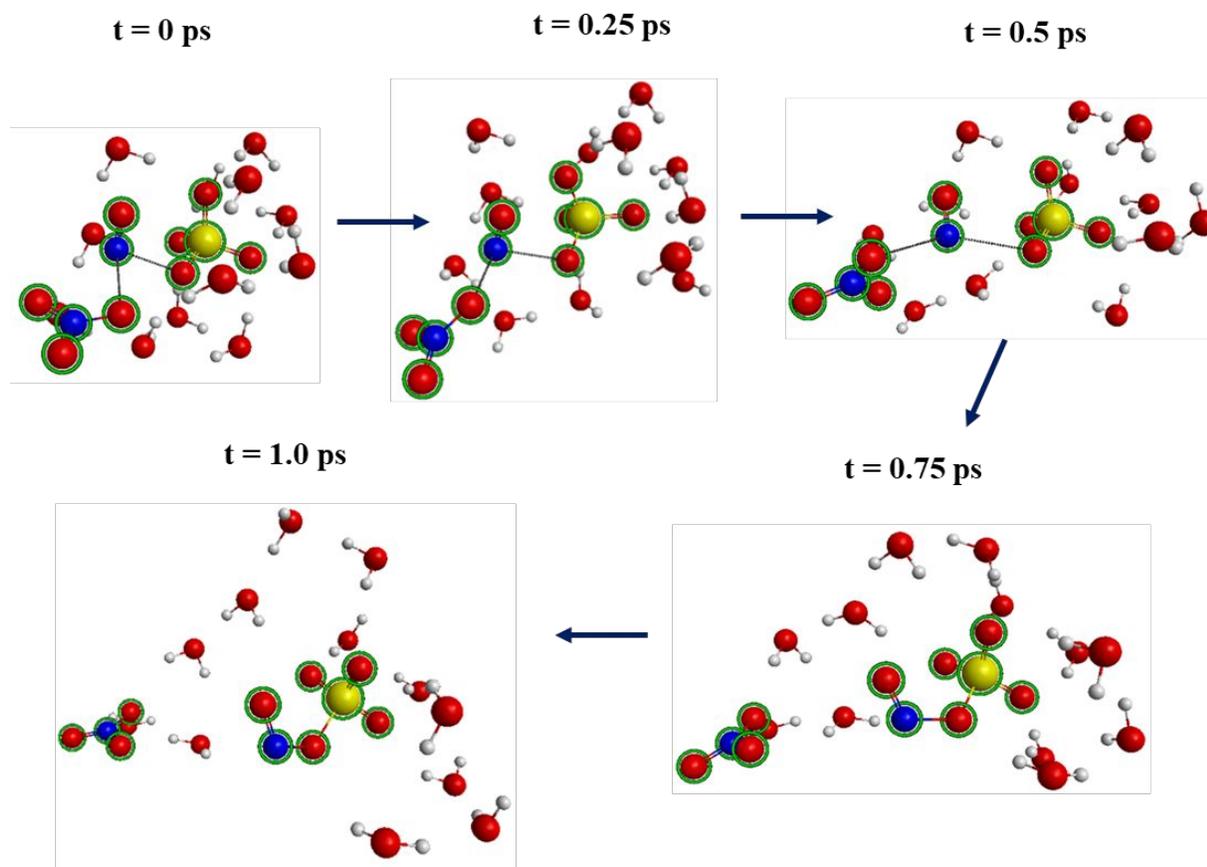


Figure 4 AIMD trajectory configurations with final structure of *cis*-SO₄NO⁻. Atom colors: red – oxygen, yellow – sulfur, white – hydrogen, and blue – nitrogen.

In the first 0.5 ps of the process, the distances between the NO and NO₃ groups increase up to 2.65 Å, whereas the distance between the NO and SO₄²⁻ groups remains without significant change at ~ 2.12 Å. In this time, the bond angle $\angle O^{(3)}N^{(2)}O^{(8)}$ increases from 85° to 115° (Fig. 2b). Between 0.5 ps and 0.75 ps, the SO₄NO⁻ forms via additional shortening of the O⁽²⁾–N⁽⁸⁾ bond distance to 1.76 Å and separation of the NO₃ group, with a O⁽³⁾...N⁽²⁾ coordination distance of 3.41 Å. It should be noted that we considered the average distances and angles for all 10 trajectories at time = 0.5 ps.

In order to consider the changes in partial charge of the SO₄, NO, and NO₃ groups in time, NBO calculations³³ were performed along the trajectories, as shown in Fig. 5 for formation of *cis*-SO₄NO⁻. The partial charge of the SO₄ group is seen to decrease from ~ -1.5 a.u. in the initial structure to ~ -1 a.u. after formation of *cis*-SO₄NO⁻ (Fig. 5a). The positive partial charge on the NO group falls from ~ 0.5 a.u. to ~ 0 a.u. throughout the trajectory. The partial charge on NO₃ group changes very little, from ~ -0.75 a.u. to ~ -1 a.u. (Fig. 5a). Additionally, the evaluation of the charge separation between groups NO⁺ and NO₃⁻ in time is present in Fig. 5b. The results show that initially (from 0 to 0.75 ps), the charge separation between NO and NO₃ moieties is quite substantial (values range from 1.20 – 1.55). After 0.75 ps, this charge separation quickly drops to values around ~1.0, representing the new products. Formation of the SO₄NO⁻ species is quite fast and occurs due to the attraction of an ion pair (SO₄²⁻/NO⁺). Overall, the trajectories,

including analysis of the charges, indicate that the reaction occurs from the minimum structure indicated in Fig. 2b within 0.5 to 1.0 ps at 298 K. Inspection of the detailed geometries along the trajectories strongly suggests that the mechanism is of the S_N2 type: as the $ONONO_2$ approaches the SO_4^{2-} , the NO_3^- group is removed from the NO^+ moiety, and a resulting SO_4NO^- species is formed.

The results from these trajectories motivate experimental cluster studies of S_N2 -type reactions of $ONONO_2$ in water clusters. Very cold clusters with the structure $(ONONO_2)(SO_4^{2-})(H_2O)_{12}$ can be experimentally isolated. Rapid temperature change to 298K will induce a reaction, such that $ONONO_2$ readily penetrates the water layer around SO_4^{2-} , and an S_N2 type process will take place within 0.5 - 1 ps via charge transfer between the SO_4 and NO groups.

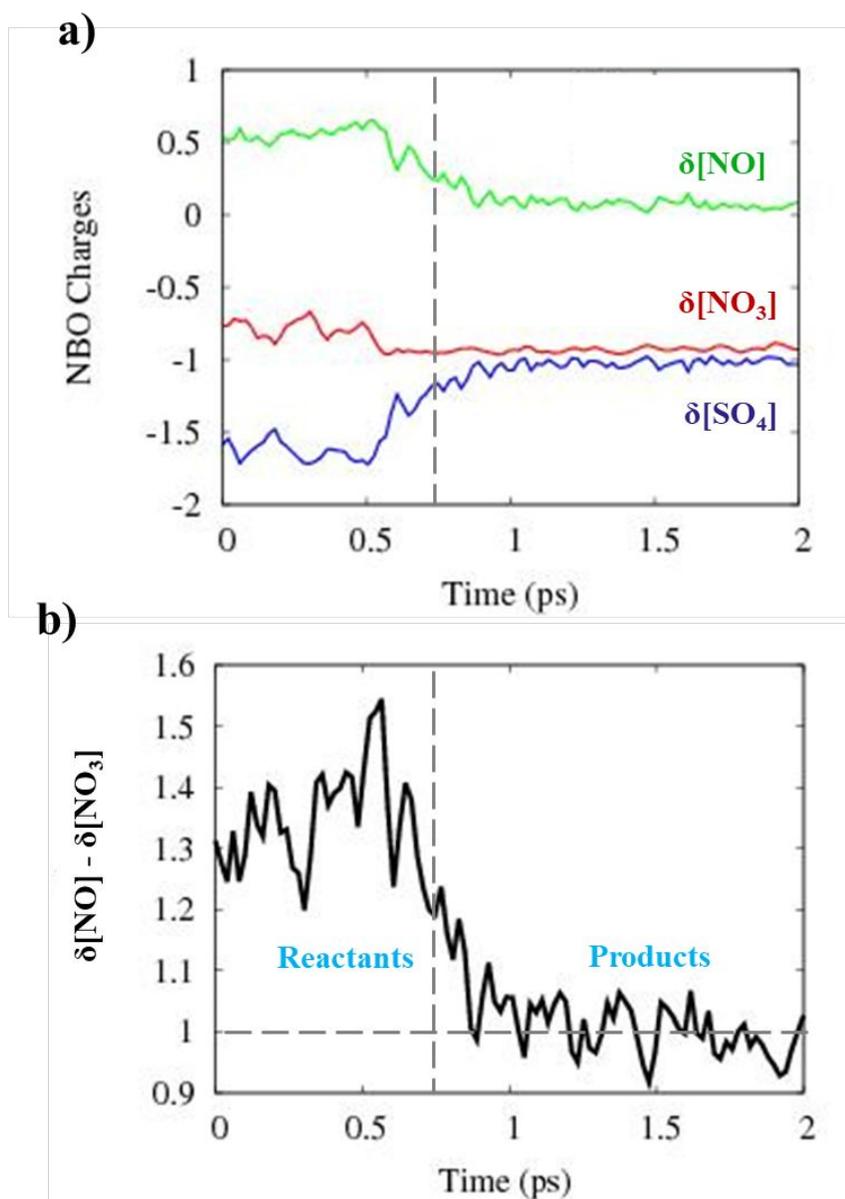


Figure 5 a) Evolution of NBO charges in time along a sample trajectory forming the *cis*-SO₄NO⁻ product, and b) charge separation between NO⁺ and NO₃⁻ groups.

2.3. IR spectra of *cis/trans*-SO₄NO⁻

Infrared (IR) spectroscopy can provide very useful spectroscopic signatures for reaction products and intermediate species for systems including the clusters studied in this work. For instance, the vibrational spectra in the mid-IR range (4000–200 cm⁻¹) may be used to study the fundamental vibrations and associated rotational-vibrational structure.^{34,35} One recent and related example is found in the study by P.J. Kelleher et al.³⁴ on the reactions of N₂O₅ with halide-water clusters, where key intermediates are spectroscopically observed.

In this work, the mid-IR spectrum is simulated for the *cis*- and *trans*- conformers of the SO₄NO⁻ ion, which may be products or intermediates. A theoretically predicted IR spectrum of the conformers of SO₄NO⁻ can be useful to experimentalists for detection of this ion in reactions of N₂O₄ and SO₄²⁻ in water. The energy difference between the *cis*- and *trans*- conformers of two forms of SO₄NO⁻ is 2.6 kcal/mol (Fig. 3). Because both were formed in the dynamical trajectories shown in the previous section, it is important to be able to distinguish the *cis*-SO₄NO⁻ and *trans*-SO₄NO⁻ forms in the IR spectra. Additionally, to understand the different contributions of reagent molecules, the vibrational spectra of *trans*-ONONO₂ and sulfate ion were calculated. Fig. 6 presents the vibrational spectra of *cis*-SO₄NO⁻, *trans*-SO₄NO⁻, *trans*-ONONO₂ and SO₄²⁻, with band positions summarized in Tables 1 and 2. Beckers and co-workers³⁵ showed that the B3LYP³⁶ functional gives good agreement between theory and experiment for IR spectra of the *trans*-ONONO₂ molecule. In this study, the theoretical IR spectra were simulated using the B3LYP method combined with a fairly large basis set 6-311++G**.²⁷ The IR spectra were calculated for the isolated *trans*-ONONO₂ molecule and ions SO₄²⁻ and *cis/trans*-SO₄NO⁻ (i.e. no water molecules were included). The B3LYP method was also used to obtain geometrical structures for related isolated species.^{37,38} In order to compare the two conformers, we aim to identify and compare IR bands with intensities higher than 100 km/mol.

The IR signals of the *cis*- and *trans*-SO₄NO⁻ conformers exhibit 15 vibrational modes in the interval 1500 – 900 cm⁻¹ (Fig. 6a, 6b and Table 1). Here we will focus on five strong bands in each conformer's spectrum (Fig. 6). The obtained bands I, II, III and V are very similar between the vibrational spectra of *cis*- and *trans*-SO₄NO⁻. However, the main difference between their spectra, making them distinguishable, is the intensity and position of band IV (Fig. 6a, 6b and Table 1). This band is a bending mode for the bond angle ∠O–N=O shown in Fig. 3. A band with this character is located at 775.35 cm⁻¹ in the case of the *trans*-isomer, whereas for the *cis*-product, the band is blue-shifted by ~50 cm⁻¹. The differences in intensity and position of IR band IV between the *cis*- and *trans*- isomers can be explained by the steric interaction between the N=O and –SO₃ fragments in the *cis*-SO₄NO⁻ product.

An additional comparison of the IR spectra of the *cis*- and *trans*-SO₄NO⁻ structures with isolated *trans*-ONONO₂ and SO₄²⁻ is performed. Band I of the *cis*- and *trans*-SO₄NO⁻ is the NO stretch of the terminal group (–NO). This same band is observed in the *trans*-ONONO₂ but blue-shifted by 300 cm⁻¹ (with respect to *cis*-SO₄NO⁻) and 280 cm⁻¹ (with respect to *trans*-SO₄NO⁻) (Fig. 6a, 6c and Table 1, 2). The stretch of the N=O bond in the case of *cis*-SO₄NO⁻ is ~20% stronger than

obtained for the *trans*-isomer. Band II in the IR spectrum of *cis*- and *trans*-SO₄NO⁻ is the doubly degenerate asymmetric stretch of the S=O bonds at ~1210 and 1217 cm⁻¹ (vibrational modes 2 and 3 in Table 1). This vibrational band is observed in the IR spectrum of isolated sulfate ion at 980 cm⁻¹ (Fig. 3d), but the presence of –N=O group shifts this band to the blue by ~240 cm⁻¹. The third strong band (III, mode 5 in Table 1) in the IR signal of the SO₄NO⁻ ions is a hybrid band. It arises due to a combination of the single N–O bond stretch and symmetric stretch of S=O (Fig. 3, Table 1).

Table 1. Theoretical vibrational frequencies and IR intensities of *cis/trans*-SO₄NO⁻ at the B3LYP/6-311++G** level of theory.

Mode	<i>trans</i> -SO ₄ NO ⁻		<i>cis</i> -SO ₄ NO ⁻		Description
	Frequencies, cm ⁻¹	IR intensity, km/mol	Frequencies, cm ⁻¹	IR intensity, km/mol	
1	1567.44	215.357	1547.9	264.472	N ⁽¹⁾ =O ⁽²⁾ stretch
2	1219.61	362.303	1213.37	342.627	S=O asym
3	1213.12	344.291	1207.61	309.888	S=O asym
4	1014.97	45.354	975.45	42.73	-
5	938.04	255.065	932.49	262.489	N ⁽²⁾ O ⁽³⁾ , S=O sym
6	775.35	250.395	825.68	48.545	∠O ⁽¹⁾ N ⁽²⁾ O ⁽³⁾ bend
7	559.09	446.848	556.15	336.759	SO ₃ torsion
8	523.78	29.452	526.78	30.221	-
9	520.75	61.825	495.48	16.951	-
10	374.02	40.84	391.51	0.205	-
11	338.16	0.027	345.41	64.523	-
12	299.36	40.296	281.18	0.962	-
13	210.7	3.025	224.39	0.418	-
14	178.49	3.878	163.9	4.081	-
15	104.14	0.002	116.91	0.002	-

(*) Superscripted numbers denote atom labels shown in Fig. 3.

Table 2. Theoretical and experimental³⁵ vibrational frequencies and IR intensities of *trans*-ONONO₂ at the B3LYP/6-311++G** level of theory.

Mode	Experiment ³⁵	Theory		Description
	Frequencies, cm ⁻¹	Frequencies, cm ⁻¹	IR intensity, km/mol	
1	1824.9	1848.24	352.946	N ⁽¹⁾ =O ⁽²⁾ stretch
2	1656.2	1654.94	422.157	NO ₂ asym
3	1293.2	1289.67	299.688	NO ₂ sym
4	903.3	940.76	30.734	-
5	792.9	807.46	186.169	∠O ⁽⁵⁾ N ⁽⁴⁾ O ⁽⁶⁾ bend
6	784.1	769.9	32.951	-
7	639	635.9	117.037	∠O ⁽⁶⁾ N ⁽⁴⁾ O ⁽³⁾ bend
8	488.2	489.41	229.82	N ⁽⁴⁾ O ⁽³⁾ stretch
9	306.0	295.24	315.794	N ⁽²⁾ O ⁽³⁾ stretch
10	-	250.54	1.056	-

11	-	204.31	3.432	-
12	-	92.49	1.154	-

(*) Superscripted numbers denoted the atom labels shown in Fig. 1c.

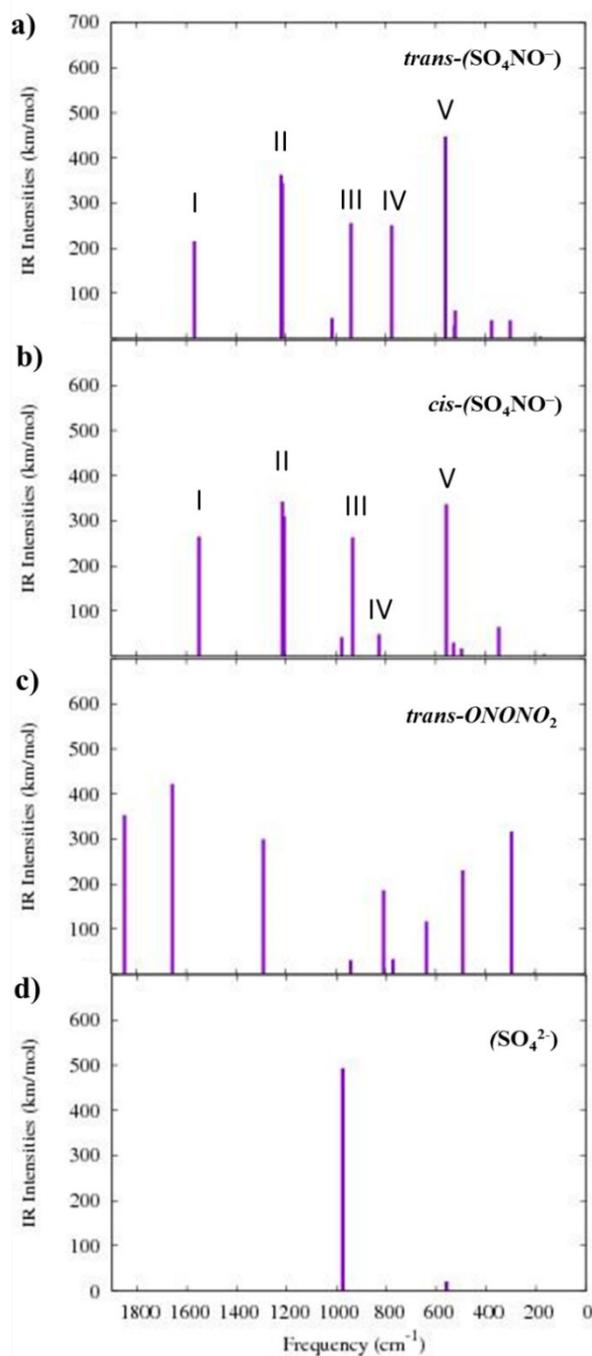


Figure 6 IR spectra of a) $\text{trans-SO}_4\text{NO}^-$, b) $\text{cis-SO}_4\text{NO}^-$ c) trans-ONONO_2 , and d) SO_4^{2-} at the B3LYP/6-311++G** level of theory.

3. Reactions of N_2O_4 with $(\text{Cl}^-)(\text{H}_2\text{O})$

3.1. System and Methods

The reactive mechanisms of ONONO_2 with Cl^- in water have been widely debated. Theoretically, small cluster studies of the system $(\text{ONONO}_2)(\text{HCl})(\text{H}_2\text{O})$ present a minimum structure of ONONO_2 electrostatically bound to HCl and H_2O , with a hydrogen bond between the H of HCl and the oxygen of the water. The chlorine atom sits 3.09 Å from the nitrogen available for attack.^{20,21} The HCl bond must break for transfer of the H to the water, which in turn transfers an H to $\text{NO}_3^{\delta+}$ for the Cl to be free to attack the nitrogen, breaking the $\text{ON}-\text{ONO}_2$ bond, and forming ClNO , H_2O , and NO_3^- . The proton thus plays an integral role in stabilizing the chlorine atom from attacking the nitrogen. Later theoretical studies model a thin film of water with ONONO_2 stabilized on the surface.²² HCl is scattered from the surface of the water, which ionizes quickly. The Cl^- leads the attack on ONONO_2 , forming ClNO and NO_3^- . This larger model system indicates that the mechanism of chloride substitution of ONONO_2 is of the $\text{S}_{\text{N}}2$ -type and thus not a proton-led attack. Due to this substantial difference in mechanism between the proton-led attack of the $(\text{ONONO}_2)(\text{HCl})(\text{H}_2\text{O})$ cluster studies and the $\text{S}_{\text{N}}2$ -type substitution of the water slab studies, it is quite desirable to identify model systems that allow one to study the $\text{S}_{\text{N}}2$ -type mechanism in detail. Previous cluster studies of the $(\text{ONONO}_2)(\text{HCl})(\text{H}_2\text{O})$ system will be contrasted with the work here: cluster studies of the negatively charged $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$ system. The negatively charged cluster studied here has an additional advantage in that it can be isolated using mass spectrometric techniques.

One major reason that the mechanisms of ONONO_2 reactions with Cl^- in water have been so widely debated is lack of clear experimental insights into the atomistic mechanistic details of the processes. In theory, experimental studies of the reactions of ONONO_2 in chloride-water clusters could be performed to characterize intermediates of these reactions spectroscopically, as was recently performed by Kelleher et al.³⁴ It is thus of interest to theoretically identify model cluster systems that contain the key elements for accurately describing atmospherically relevant reactions of ONONO_2 in chloride-containing water.

Here we present a study of the small cluster system $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$ in order to gain insights into the competition between halide substitution and hydrolysis of asymmetric N_2O_4 . We additionally identify barriers and mechanisms for formation of symmetric N_2O_4 from ONONO_2 . We lastly aim to characterize key intermediates and their spectroscopic signatures for future cluster studies of this system.

In order to characterize reactions of the small cluster system $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$, we present intrinsic reaction coordinates (IRC) for key steps in the halide substitution and hydrolysis processes³⁹. These were computed at the $\omega\text{B97X-D/aug-cc-pVDZ}$ level of theory and zero point energy (ZPE) corrected^{40,41}. ZPE were calculated in the harmonic approximation. Vibrational frequencies and intensities, also computed in the harmonic approximation, are reported at the same level of theory for key intermediates. This level of theory was used due to its success in previous studies of $(\text{N}_2\text{O}_5)(\text{Cl}^-)(\text{H}_2\text{O})$ clusters and related systems^{10,34}. All calculations in Section 3 were performed in the QChem program package²⁹.

3.2. Reaction Pathway of $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$

Here we present a study of the reaction pathway of $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$ for both symmetric and asymmetric conformers of N_2O_4 . It is the aim of this study to compare and contrast the reaction pathways and possible mechanisms between the $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$ studied here and previous cluster studies of $(\text{ONONO}_2)(\text{HCl})(\text{H}_2\text{O})$. Previous studies of the neutral cluster containing HCl indicate that a proton-led attack of ONONO_2 prevails. However, HCl is known to rapidly ionize in solution, making a Cl^- -led $\text{S}_{\text{N}}2$ -type attack more likely in the environment. The present studies of the $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$ cluster will allow for detailed information on the microscopic configurations of the cluster for halide substitution and hydrolysis reactions.

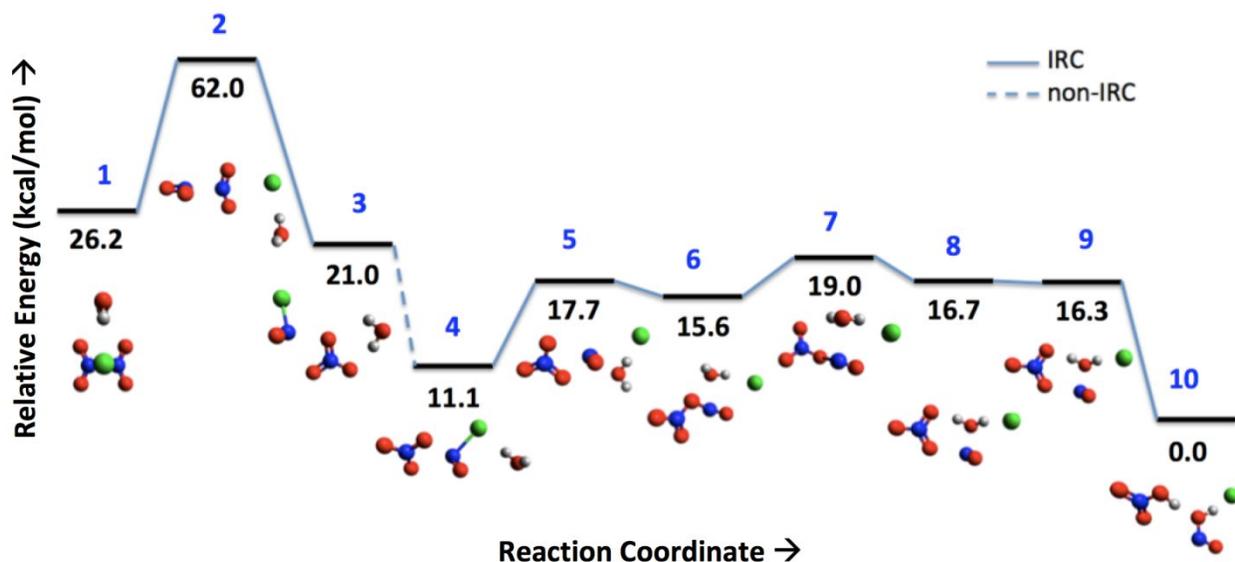


Figure 7 Low-lying reaction pathway of $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$. Solid blue lines represent an intrinsic reaction coordinate (IRC), while dotted blue lines do not.

The low-lying reaction pathway for halide substitution and hydrolysis reactions of $\text{N}_2\text{O}_4 + \text{Cl}^- + \text{H}_2\text{O}$ is shown in Fig. 7. The far left structure with relative energy of 26.2 kcal indicates symmetric N_2O_4 interacting with Cl^- , directly above the N-N bond, and water, forming a hydrogen bond with Cl^- . Section 2 shows that isolated symmetric N_2O_4 is 11.0 kcal/mol more stable than ONONO_2 . Here it is shown that the low-lying conformer of $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$ (1) is 10.6 kcal/mol higher in energy than the minimum structure $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$ with relative energy of 15.6 kcal/mol (6). This is quite an interesting result, as it indicates that ONONO_2 is highly stabilized by the presence of H_2O and Cl^- . This stabilization of ONONO_2 by water and SO_4^{2-} was also observed in Section 2, though the cluster containing symmetric N_2O_4 remained more stable by 1.8 kcal/mol. The chloride substitution reaction of symmetric N_2O_4 has a barrier of 35.8 kcal/mol, indicating that symmetric N_2O_4 requires additional water molecules for this reaction to occur. We therefore focus the majority of our attention on reactions of asymmetric ONONO_2 with H_2O and Cl^- in this study.

Two minimum configurations of $(\text{ClNO})(\text{NO}_3^-)(\text{H}_2\text{O})$ (3 and 4) are shown in Fig. 7, though they are not connected via IRC due to the many complex pathways that connect the structures. Interestingly, the difference in relative energy between the two structures is quite large: 9.9 kcal/mol. The main difference between these configurations is the hydrogen bonding of the

water. In the higher energy configuration, the water forms a hydrogen bond with an oxygen atom on the NO_3^- . Conversely, the lower energy configuration reveals a hydrogen bond between the water and chlorine atom of ClNO . It is clear from the differences in energy that the hydrogen bonding between water and ClNO is very strong and stabilizes this intermediate.

Fig. 7 indicates a minimum geometry of ONONO_2 interacting with Cl^- and H_2O at a relative energy of 15.6 kcal/mol (6). On the left of this lies a barrier to chloride substitution of 2.1 kcal/mol. Right of this is a two-step process to hydrolysis. The first step, a barrier of 3.4 kcal/mol indicates formation of a hydrogen bond between the water and an oxygen atom of ONONO_2 . The pathway continues to a minimum structure at 16.7 kcal/mol (8), revealing the water molecule having two hydrogen bonds: one with the Cl^- and one with the ONONO_2 . The IRC calculations performed indicate a nearby transition state (at 16.3 kcal/mol) that is lowered in relative energy when the ZPE correction is included. Without the correction, the process is, to numerical accuracy, barrierless. Finally, the hydrolysis product, $(\text{HNO}_3)(\text{cis-HONO})(\text{Cl}^-)$ (10) is found to be the most stable structure in the reaction pathway. Here, the hydrogen atom of HNO_3 makes a hydrogen bond with the adjacent oxygen of *cis*-HONO. The hydrogen atom of *cis*-HONO also makes a hydrogen bond with Cl^- . Both hydrogen bonds greatly stabilize this structure.

3.3. IR Spectra of Key Species in Reactions of $\text{N}_2\text{O}_4 + \text{Cl}^- + \text{H}_2\text{O}$

In order to make connections between the theoretical reaction pathways described in this section and future experimental studies, we present calculations and analysis of the IR spectra for key species in the processes. The four species with frequencies and intensities presented here are symmetric $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$, asymmetric $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$, substitution products $(\text{ClNO})(\text{NO}_3^-)(\text{H}_2\text{O})$, and hydrolysis products $(\text{HNO}_3)(\text{HONO})(\text{Cl}^-)$, labeled 1, 4, 6, and 10, respectively in Fig. 7. The harmonic frequencies and intensities of these minima, as well as characteristic descriptions for the strongest bands, are given in Tables 3 - 6. The simulated spectra for these clusters are presented in Fig. 8. We aim to identify the key features of the spectra, especially bands that differentiate the four species.

All four species have at least one strong OH stretch, though these bands span over 600 cm^{-1} . The highest energy OH stretch (3648 cm^{-1}) is determined for the $(\text{ClNO})(\text{NO}_3^-)(\text{H}_2\text{O})$ cluster (4 in Fig. 7). The next highest OH stretch is found at 3568 cm^{-1} in the symmetric $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$ cluster (1 in Fig. 7). The asymmetric $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$ species (6 in Fig. 7) has a strong OH stretch at 3296 cm^{-1} , while the $(\text{HNO}_3)(\text{HONO})(\text{Cl}^-)$ cluster (10 in Fig. 7) has a strong OH stretch at 3032 cm^{-1} . All four of these stretches indicate hydrogen stretching toward the chlorine atom, indicating a wide range of hydrogen bonding strengths between these species.

The symmetric $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$ species (Table 3 and Fig. 8a) is the most different in structure from the other species studied here. This structure has strong NO stretching bands at 1874 and 1368 cm^{-1} . This species also has a fairly strong water bend at 1674 cm^{-1} , though this is difficult to differentiate from the NO stretching region. The characteristic band in the symmetric $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$ structure is a fairly strong ONO bend at 787 cm^{-1} , which is not observed in the other three structures' spectra.

Three of the five strongest bands of the asymmetric $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$ species (Table 4 and Fig. 8b) are NO stretches. The band at 2194 cm^{-1} is the terminal NO stretch, decoupled from NO stretches of the NO_3 subspecies. The NO stretches of the NO_3 subspecies are found at 1582 and 1373 cm^{-1} . The decoupled nature of these stretches as well as the large blue shift of the terminal NO stretch indicates that the asymmetric ONONO_2 has the character of an ion pair ($\text{NO}_3^-/\text{NO}^+$) in this structure. The band at 492 cm^{-1} is a mixed mode with character of the free OH wag and stretch between NO and NO_3 subgroups, indicating significant interaction between the subgroups.

The spectrum for the species $(\text{ClNO})(\text{NO}_3^-)(\text{H}_2\text{O})$, formed as a result of the halide substitution reaction, contains two strong bands that indicate formation of the ClN bond. The NO stretch in the ClNO is found at 2079 cm^{-1} , a 115 cm^{-1} red shift from the terminal NO stretch observed in the $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$ cluster. This shift is most likely due to the ClN bond perturbing this stretch more than the NO_3 does in the asymmetric ONONO_2 cluster. Secondly, the ClN bond stretch is a fairly strong band at 452 cm^{-1} , characterizing the formation of ClNO. The strong NO bands at 1546 and 1384 cm^{-1} are almost identical in character and frequency as those observed in the $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$ cluster, indicating that the NO_3 subgroup behaves similarly in the two systems.

The fourth spectrum represented in Fig. 8d is the cluster resulting from a hydrolysis reaction in $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$ to form $(\text{HNO}_3)(\text{HONO})(\text{Cl}^-)$. The five strongest bands in this spectrum all have mixed character and are quite different from the bands of the $(\text{ONONO}_2)(\text{Cl}^-)(\text{H}_2\text{O})$ and $(\text{ClNO})(\text{NO}_3^-)(\text{H}_2\text{O})$ clusters. Two mixed modes involving the OH stretch of the HONO and the terminal NO stretch of the HONO are found at 1771 and 1525 cm^{-1} . At 1270 and 1083 cm^{-1} , two strong bands are present that represent in sync wagging motion of the hydrogen atoms, having the character of a water bend. The band at 1083 cm^{-1} is also coupled to the stretching motion of the central NO bond of HONO.

Due to the significant changes in structure between the four species described here, characteristic bands appear in each spectrum. The studies presented in this work aim to guide future spectroscopic investigation of the halide substitution and hydrolysis reactions of symmetric and asymmetric N_2O_4 . Future theoretical and experimental studies involving additional water molecules will greatly enhance understanding of how the microscopic configurations of the species affect the reactivity of N_2O_4 , stabilization of the asymmetric vs. symmetric forms, and product yields of HONO vs. ClNO. The studies of this small cluster presented here provide detailed microscopic information on the potential energy surface and mechanisms of the hydrolysis and halide substitution processes of ONONO_2 .

Table 3. Harmonic frequencies (above 200 cm^{-1}) of $(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$ cluster at the $\omega\text{B97X-D/aug-cc-pVDZ}$ level of theory

Mode	$(\text{N}_2\text{O}_4)(\text{Cl}^-)(\text{H}_2\text{O})$ cluster		Description
	Frequencies, cm^{-1}	IR intensity, km/mol	
1	3935.10	25.248	-
2	3567.88	562.144	OH stretch toward Cl
3	1872.68	651.435	NO stretch

4	1836.36	0.688	-
5	1674.98	188.730	H ₂ O bend
6	1466.25	55.023	-
7	1368.36	381.788	NO stretch
8	862.26	3.286	-
9	787.01	196.224	NO ₂ bend
10	686.99	3.681	-
11	671.20	40.455	-
12	542.89	0.006	-
13	487.17	96.033	-
14	347.87	0.828	-
15	344.04	57.652	-
16	278.38	0.028	-
17	202.60	26.194	-

Table 4. Harmonic frequencies (above 200 cm⁻¹) of (ONONO₂)(Cl)(H₂O) cluster at the ωB97X-D/aug-cc-pVDZ level of theory

Mode	(ONONO ₂)(Cl)(H ₂ O) cluster		Description
	Frequencies, cm ⁻¹	IR intensity, km/mol	
1	3921.44	44.523	-
2	3296.07	837.972	OH stretch toward Cl
3	2194.43	270.317	Terminal NO stretch
4	1621.56	27.007	-
5	1581.67	596.368	NO stretch on NO ₃
6	1372.64	619.712	NO stretch on NO ₃
7	1097.96	76.654	-
8	840.73	12.564	-
9	734.50	45.648	-
10	720.15	0.579	-
11	492.32	106.525	Mixed: free OH wag + terminal NO stretch
12	419.95	78.811	-
13	382.76	74.435	-
14	346.24	22.322	-
15	244.00	83.225	-
16	227.56	33.241	-

Table 5. Harmonic frequencies (above 200 cm⁻¹) of (ClNO)(NO₃⁻)(H₂O) cluster at the ωB97X-D/aug-cc-pVDZ level of theory

Mode	(ClNO)(NO ₃ ⁻)(H ₂ O) cluster		Description
	Frequencies, cm ⁻¹	IR intensity, km/mol	
1	3950.87	55.682	-
2	3648.38	645.594	OH stretch between water and Cl

3	2078.80	517.849	NO stretch on ClNO
4	1665.22	90.060	-
5	1545.58	602.341	Asym. NO stretch on NO ₃ ⁻
6	1383.64	713.300	Asym. NO stretch on NO ₃ ⁻
7	1109.99	35.225	-
8	853.52	9.381	-
9	746.67	25.914	-
10	724.17	1.681	-
11	633.62	75.946	-
12	451.63	295.631	CIN stretch and ClNO bend
13	426.64	18.013	-
14	306.21	54.832	-
15	265.85	27.220	-
16	222.63	187.260	CIN stretch

Table 6. Harmonic frequencies (above 200 cm⁻¹) of (HNO₃)(HONO)(Cl⁻) cluster at the ωB97X-D/aug-cc-pVDZ level of theory

Mode	(HNO ₃)(HONO)(Cl ⁻) cluster		Description
	Frequencies, cm ⁻¹	IR intensity, km/mol	
1	3031.53	1977.156	Mixed: OH stretch on HNO ₃ + OH stretch on HONO
2	1771.41	994.356	Mixed: OH stretch on HONO + terminal NO stretch on HONO
3	1754.20	369.008	-
4	1524.73	1395.559	Mixed: OH stretch on HONO + terminal NO sym. stretch on HONO
5	1471.42	189.612	-
6	1412.16	440.936	-
7	1270.22	2598.159	Mixed: H wag on HONO + H wag on HNO ₃
8	1082.93	559.807	Mixed: H wag on HONO + H wag on HNO ₃ + central ON stretch on HONO
9	1062.23	73.142	-
10	1036.64	147.098	-
11	951.75	220.485	-
12	823.14	8.826	-
13	755.38	57.965	-
14	714.71	16.536	-
15	657.41	3.811	-
16	350.88	181.787	-

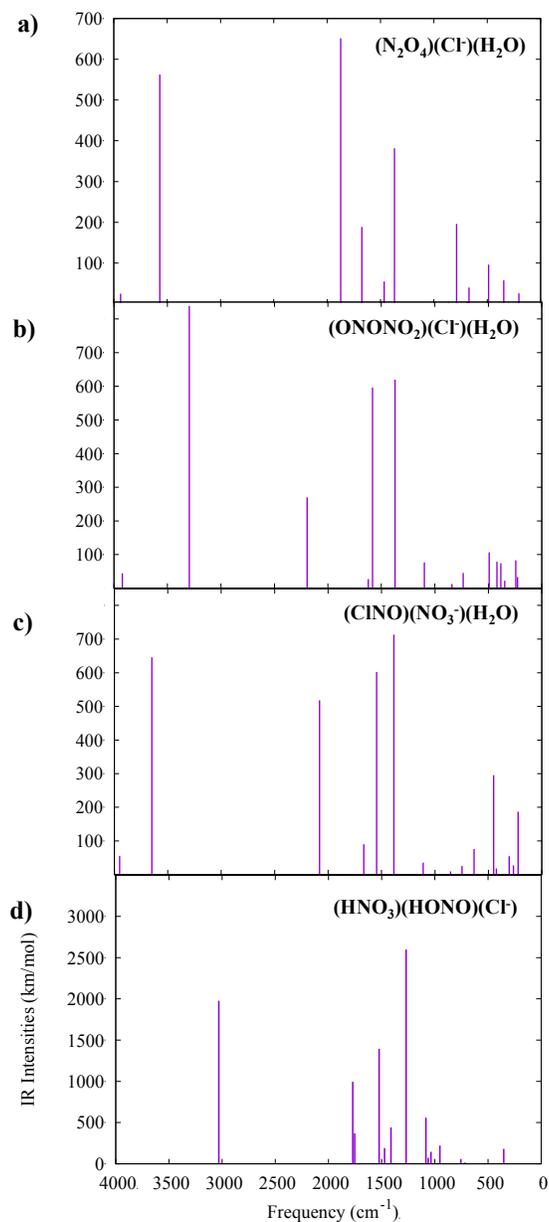


Figure 8 IR spectra of a) symmetric (N₂O₄)(Cl⁻)(H₂O), b) asymmetric (ONONO₂)(Cl⁻)(H₂O), c) (ClNO)(NO₃⁻)(H₂O), and d) (HNO₃)(HONO)(Cl⁻) at the ωB97X-D/aug-cc-pVDZ level of theory.

4. Conclusions

This paper explores the reactions of ONONO₂ with the ions SO₄²⁻ and Cl⁻ in water clusters. For both anions, an S_N2-type mechanism involving the terminal nitrogen of the ONONO₂ is observed. This suggests that for ONONO₂ and related species (including N₂O₅), S_N2-type

substitution reactions are more likely than the electrophilic reactions predicted in previous studies including cluster studies of (ONONO₂)(HCl)(H₂O). The S_N2 reactions of ions with ONONO₂ in a water environment described in this work are quite efficient. In a recent study, we also found efficient S_N2 reactions of Cl⁻ interacting with N₂O₅ and one water molecule. In calculations of IR frequencies and intensities, we identify spectroscopic signatures of key reaction intermediates and products that may be identified in future experiments.

Author contributions

N.V.K. and L.M.M. performed the calculations, provided interpretation of the results, and contributed to the writing of paper. R.B.G. suggested the project, participated in analysis of results, and contributed to the writing of the paper. N.V.K. and L.M.M. made equal contributions to the work as first authors.

Conflicts of interest

There are no conflicts to declare.

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References

- 1 B.J. Finlayson-Pitts and J.N. Pitts, Jr. "Chemistry of the Upper and Lower Atmosphere", Academic Press, San Diego, 2000.
- 2 N. Riemer, *J. Geophys. Res.*, 2003, 108, 4144.
- 3 U.F. Platt, A.M. Biermann, R. Atkinson and J.N. Pitts, Jr. *Environ. Sci. Technol.* 1984, 18, 365-369.
- 4 M. Mozurkewich and J.G. Calvert, *J. Geophys. Res. Atoms.* 1988, 93, 15889-15896.
- 5 J.A. Thornton and J.P.D. Abbatt, *J. Phys. Chem. A*, 2005, 109, 10004-10012.
- 6 B.J. Finlayson-Pitts, M.J. Ezell and J.N. Pitts, Jr. *Nature*, 1989, 337, 2412-44.
- 7 R.C. Hoffmann, M.E. Gebel, B.S. Fox and B.J. Finlayson-Pitts, *Phys. Chem. Chem. Phys.* 2003, 5, 1780-1789.
- 8 J.A. Thornton, J.P. Korcher, T.P. Riedel, N.L. Wagner, J. Cozic, J.S. Holloway, W.P. Dube, G.M. Wolfe, P.K. Quin, A.M. Middlebrook, B. Alexander and S.S. Brown, *Nature*, 2010, 464, 2712-74.
- 9 A.D. Hammerich, B.J. Finlayson-Pitts and R.B. Gerber, *Phys. Chem. Chem. Phys.*, 2015, 17, 19360-19370.
- 10 L.M. McCaslin, M.A. Johnson and R.B. Gerber, "Mechanisms and Competition of Halide Substitution and Hydrolysis in Reactions of N₂O₅ with Seawater", (In review).
- 11 B. Hirshberg, E. Rossich Molina, A.W. Goetz, A.D. Hammerich, G.M. Nathanson, T.H. Bertram, M.A. Johnson and R.B. Gerber, *Phys. Chem. Chem. Phys.*, 2018, 20, 17961-17976.

- 12 B.J. Finlayson-Pitts, L.M. Wingen, A.L. Summer, D. Syomin and K.A. Ramazan, *Phys. Chem. Chem. Phys.*, 2003, 5, 223.
- 13 D. de Jesus Medeiros and A.S. Pimentel, *J. Phys. Chem. A*, 2011, 115, 6357-6365.
- 14 A. Givan and A. Loewenschuss, *J. Chem. Phys.*, 1991, 94, 7562.
- 15 J. Wang and B.E. Koel, *J. Phys. Chem. A*, 1998, 102, 8573.
- 16 J. Wang and B.E. Koel, *Surf. Sci.*, 1999, 436, 15.
- 17 A.S. Pimentel, F.C.A. Lima and A.B.F. de Silva, *J. Phys. Chem. A*, 2007, 111, 2913.
- 18 H. Lignell, M.E. Varner, B.J. Finlayson-Pitts and R.B. Gerber, *Chem. Phys.*, 2012, 403, 52-59.
- 19 M.E. Varner, B.J. Finlayson-Pitts and R.B. Gerber, *Phys. Chem. Chem. Phys.*, 2014, 16, 4483-4487.
- 20 J.D. Raff, B. Njegic, W.L. Chang, M.S. Gordon, D. Dabdub, R.B. Gerber and B.J. Finlayson-Pitts, *Proc. Natl. Acad. Sci. (USA)*, 2009, 106, 13647-13654.
- 21 B. Njegic, J.D. Raff, B.J. Finlayson-Pitts, M.S. Gordon and R.B. Gerber, *J. Phys. Chem. A*, 2010, 114, 4609-4618.
- 22 A.D. Hammerich, B.J. Finlayson-Pitts and R.B. Gerber, *J. Phys. Chem. Lett.*, 2012, 3, 3405-3410.
- 23 J.C. Hey, L.C. Smeeton, M.T. Oakley, and R.L. Johnston, *J. Phys. Chem. A*, 2016, 120, 4008-4015.
- 24 L.C. Smeeton, J.D. Farrell, M.T. Oakley, D.J. Wales, and R.L. Johnston, *J. Chem. Theory Comput.*, 2015, 11, 2377-2384.
- 25 C. Adamo and V. Barone, *J. Chem. Phys.*, 1999, 110, 6158.
- 26 P.M.W. Gill, B.G. Johnson, J.A. Pople and M.J. Frisch, *Chem. Phys. Lett.*, 1992, 197, 499.
- 27 M.M. Francl, W.J. Pietro, W.J. Hehre, J.S. Binkley, M.S. Gordon, D.J. DeFrees and J.A. Pople, *J. Chem. Phys.*, 1982, 77, 3654.
- 28 S. Grimme, *J. Comput. Chem.*, 2006, 27, 1787.
- 29 Y. Shao, Z. Gan, E. Epifanovsky, A. T. B. Gilbert, M. Wormit, J. Kussmann, A. W. Lange, A. Behn, J. Deng, X. Feng, D. Ghosh, M. Goldey P. R. Horn, L. D. Jacobson, I. Kaliman, R. Z. Khaliullin, T. Kúš, A. Landau, J. Liu, E. I. Proynov, Y. M. Rhee, R. M. Richard, M. A. Rohrdanz, R. P. Steele, E. J. Sundstrom, H. L. Woodcock III, P. M. Zimmerman, D. Zuev, B. Albrecht, E. Alguire, B. Austin, G. J. O. Beran, Y. A. Bernard, E. Berquist, K. Brandhorst, K. B. Bravaya, S. T. Brown, D. Casanova, C.-M. Chang, Y. Chen, S. H. Chien, K. D. Closser, D. L. Crittenden, M. Diedenhofen, R. A. DiStasio Jr., H. Dop, A. D. Dutoi, R. G. Edgar, S. Fatehi, L. Fusti-Molnar, A. Ghysels, A. Golubeva-Zadorozhnaya, J. Gomes, M. W. D. Hanson-Heine, P. H. P. Harbach, A. W. Hauser, E. G. Hohenstein, Z. C. Holden, T.-C. Jagau, H. Ji, B. Kaduk, K. Khistyayev, J. Kim, J. Kim, R. A. King, P. Klunzinger, D. Kosenkov, T. Kowalczyk, C. M. Krauter, K. U. Lao, A. Laurent, K. V. Lawler, S. V. Levchenko, C. Y. Lin, F. Liu, E. Livshits, R. C. Lochan, A. Luenser, P. Manohar, S. F. Manzer, S.-P. Mao, N. Mardirossian, A. V. Marenich, S. A. Maurer, N. J. Mayhall, C. M. Oana, R. Olivares-Amaya, D. P. O'Neill, J. A. Parkhill, T. M. Perrine, R. Peverati, P. A. Pieniazek, A. Prociuk, D. R. Rehn, E. Rosta, N. J. Russ, N. Sergueev, S. M. Sharada, S. Sharma, D. W. Small, A. Sodt, T. Stein, D. Stück, Y.-C. Su, A. J. W. Thom, T. Tsuchimochi, L. Vogt, O. Vydrov, T. Wang, M. A. Watson, J. Wenzel, A. White, C. F. Williams, V. Vanovschi, S. Yeganeh, S. R. Yost, Z.-Q. You, I. Y. Zhang, X. Zhang, Y. Zhou, B. R. Brooks, G. K. L. Chan, D. M. Chipman, C. J. Cramer, W. A. Goddard III, M. S. Gordon, W. J. Hehre, A. Klamt, H. F. Schaefer III, M. W. Schmidt, C. D. Sherrill, D. G.

- Truhlar, A. Warshel, X. Xua, A. Aspuru-Guzik, R. Baer, A. T. Bell, N. A. Besley, J.-D. Chai, A. Dreuw, B. D. Dunietz, T. R. Furlani, S. R. Gwaltney, C.-P. Hsu, Y. Jung, J. Kong, D. S. Lambrecht, W. Liang, C. Ochsenfeld, V. A. Rassolov, L. V. Slipchenko, J. E. Subotnik, T. Van Voorhis, J. M. Herbert, A. I. Krylov, P. M. W. Gill, and M. Head-Gordon, *Mol. Phys.*, 2015, 113, 184–215.
- 30 D. Matx and J. Hutter, “Ab Initio Molecular Dynamics: Basic Theory and Advanced Methods”, Cambridge University Press, New York, 2009.
- 31 R.B. Gerber, D. Shemesh, M.E. Varner, J. Kalinowski, B. Hirshberg, *Phys. Chem. Chem. Phys.*, 2014, 16, 9760-9775.
- 32 R.B. Gerber, M.E. Varner, A.D. Hammerich, S. Riikonen, G. Murdachaew, D. Shemesh, B.J. Finlayson-Pitts, *Accts. Chem. Res.*, 2015, 48, 399-406.
- 33 E. D. Glendening, C. R. Landis, and F. Weinhold, *J. Comput. Chem.*, 2013, 34, 1429.
- 34 P.J. Kelleher, F.S. Menges, J.W. DePalma, J.K. Denton, and M.A. Johnson, G.H. Weddle, B. Hirshberg, R.B. Gerber, *J. Phys. Chem. Lett.*, 2017, 8, 4710–4715.
- 35 H. Beckers, X. Zeng, and H. Willner, *Chem. Eur. J.*, 2010, 16, 1506-1520.
- 36 A. D. Becke, *J. Chem. Phys.*, 1993, 98, 1372.
- 37 W.-G. Liu, W.A. Goddard III, *J. Am. Chem. Soc.*, 2012, 134, 12970–12978.
- 38 R. S. Zhu, K.-Y. Lai, M.C. Lin, *J. Phys. Chem. A*, 2012, 116, 4466–4472.
- 39 K. Fukui, *J. Phys. Chem.*, 1970, 74, 4161-4163.
- 40 J.D. Chai and M. Head-Gordon, *Phys. Chem. Chem. Phys.*, 2008, 10, 6610-6615.
- 41 R.A. Kendall, T.H. Dunning, and R.J Harrison, *J. Chem. Phys.*, 1992, 96, 6796-6806.
- 42 J. Towns, T. Cockerill, M. Dahan, I. Foster, K. Gaither, A. Grimshaw, V. Hazlewood, S. Lathrop, D. Lifka, G. D. Peterson, R. Roskies, J. R. Scott, N. Wilkins-Diehr, *Comput. Sci. Eng.*, 2014, 16, 62-74.