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# Single-particle measurements of electrochemical kinetics in NMC and NCA cathodes for Li-ion batteries†

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The electrochemical kinetics of battery electrodes at the single-particle scale are measured as a function of state-of-charge, and interpreted with the aid of concurrent transmission X-ray microscopy (TXM) of the evolving particle microstructure. An electrochemical cell operating with near-picoampere current resolution is used to characterize single secondary particles of two widely-used cathode compounds, NMC333 and NCA. Interfacial charge transfer kinetics are found to vary by two orders of magnitude with state-of-charge (SOC) in both materials, but the origin of the SOC dependence differs greatly. NCA behavior is dominated by electrochemically-induced microfracture, although thin binder coatings significantly ameliorate mechanical degradation, while NMC333 demonstrates strongly increasing interfacial reaction rates with SOC for chemical reasons. Micro-PITT is used to separate interfacial and bulk transport rates, and show that for commercially relevant particle sizes, interfacial transport is rate-limiting at low SOC, while mixed-control dominates at higher SOC. These results provide mechanistic insight into the mesoscale kinetics of ion intercalation compounds, which can guide the development of high performance rechargeable batteries.

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## Broader context

The performance of high performance Li-ion batteries, central to both electric transportation and grid scale storage, is ultimately reliant on the performance of critical components such as their cathode and anode compounds. For ease of manufacturing, the prevailing technological forms of these materials are secondary particles of nearly spherical morphology containing many nanocrystallites. The electrochemical kinetics at this critical length scale have been difficult to assess; particle-level behavior has primarily been deduced from macroscale cell measurements. Thus the microelectrode technique developed in this work, combined with state-of-the-art TXM imaging, allows for the first time the direct measurement of electrochemical kinetics of particles as they are charged and discharged. Surprising behavior is revealed – interfacial charge transfer kinetics are found to vary greatly with state-of-charge and cycling history, both for intrinsic chemical reasons (in NMC333) and because of massively damaging “electrochemical shock” (in NCA). Moreover, a thin coating of polymer binder is found to ameliorate fracture damage. These results, and the techniques demonstrated, provide a bridge between macroscopic battery function and microscale electrode kinetics as influenced by electrochemomechanical stress and charging history.

## Introduction

High energy density lithium-ion batteries (LIBs) have emerged as the leading energy storage technology for consumer electronics,

electric vehicles, and grid-scale storage. The continuing need for higher rate capability, especially during charge, and higher energy density, by increasing the upper limit of charge voltage, requires detailed understanding of lithium transport kinetics in battery electrodes at multiple length scales.<sup>1</sup> In a typical composite electrode, there are many possible rate-limiting transport paths; measurements of macroscopic electrodes can be especially difficult to deconvolute into processes occurring at smaller length scales. There exists a need for techniques that can probe electrochemical kinetics of battery electrode materials in a manner that allows separation of individual transport parameters, including their dependence on state-of-charge (SOC) and cycling.

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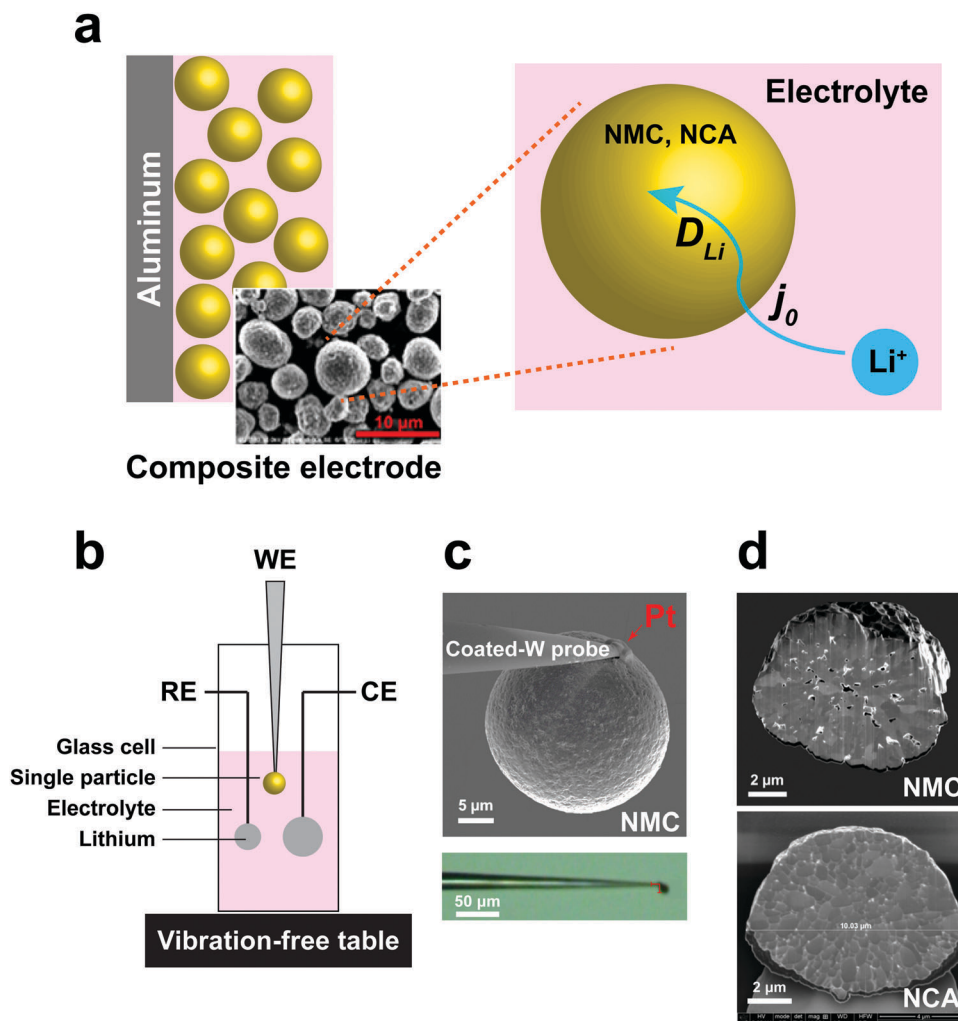
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**Fig. 1** (a) Schematic of electrochemical kinetics for cathode particles in composite electrodes. Key steps are charge-transfer at the particle–electrolyte interface, and bulk transport of lithium within particles. (b) Schematic of the electrochemical cell for the single-particle measurements. (c) Microelectrodes made by attaching a spherical polycrystalline NMC/NCA particle to an insulating resin-coated tungsten probe tip using Pt deposition in a focused ion beam (FIB) apparatus. (d) SEM of FIB cross-section of NMC and NCA single particles, showing polycrystalline microstructure.

At the particle scale, electrochemical kinetics involve the liquid phase diffusion of Li ions within the electrolyte to each individual cathode particle, the charge-transfer reaction at the cathode–electrolyte interface, and transport of Li ions and electrons (*i.e.*, ambipolar or chemical diffusion) within particles,<sup>2,3</sup> as illustrated in Fig. 1a. Understanding of the charge-transfer reaction and bulk ion diffusion is desired to reveal the limiting factors of rate performance. However, in a conventional lithium ion cell, the composite electrodes are composed of active materials, binders, conductive agents, and current collectors. Due to the multicomponent mixture and complex architecture, which includes variations in particle shape and size distribution, it is challenging to extract intrinsic kinetic parameters from cell measurements.<sup>4,5</sup> Particle-level characterization of electrochemical kinetics or microstructural changes during cycling have been separately conducted, but not directly correlated with each other.<sup>6–10</sup> Moreover, the experimental designs in prior work have involved either “open” electrochemical cells or use of low-vapor pressure ionic liquid electrolytes, which do not represent a realistic Li ion battery environment.

To address these challenges, we developed a sealed single-particle wet cell operating in an argon-filled glovebox to measure the electrochemical kinetics of single cathode particles in a half-cell configuration, and using alkyl carbonate based electrolyte (Fig. 1). To ensure practical relevance of the results, we selected intercalation compounds in the  $\text{LiNi}_{1-x-y}\text{Mn}_x\text{Co}_y\text{O}_2$  (NMC)<sup>11–13</sup> and  $\text{LiNi}_{1-x-y}\text{Co}_x\text{Al}_y\text{O}_2$  (NCA)<sup>1,14</sup> composition families, which are leading cathodes for current and future LIBs. Specifically,  $\text{LiNi}_{1/3}\text{Mn}_{1/3}\text{Co}_{1/3}\text{O}_2$  (NMC333) and  $\text{LiNi}_{0.8}\text{Co}_{0.15}\text{Al}_{0.05}\text{O}_2$  (NCA) were studied, being two model compositions that are in widespread use today. These cathodes are commercially produced as spherical secondary particles (Fig. 1), a morphology that simplifies handling as well as data analysis in this work.

Electrochemical impedance spectroscopy (EIS) and potentiostatic intermittent titration tests (PITT) were carried out using the single-particle cell. In addition, we used *ex situ* transmission X-ray microscopy (TXM) to characterize fracture at the particle level as a function of state-of-charge. Using these combined techniques, the rate-limiting transport processes at the particle



level, their variation across a wide range of state-of-charge, and their dependence on electrochemomechanical stress induced by cycling, are characterized together for the first time.

## Results and discussion

### Design and fabrication of the single-particle test cell

A three-electrode cell with a single particle as the working electrode (Fig. 1b) was developed to meet critical requirements of sealing against electrolyte loss, thereby permitting long-duration experiments, and ultra-low background vibration and electromagnetic noise. The apparatus was operated in an argon-filled glovebox, and achieved background current noise of < 30 pA, compared to measurement currents of 200 pA to 1 nA. The working electrode was assembled by physically isolating and attaching a polycrystalline cathode particle to a tungsten (W) nanoparticle manipulator used in an FIB instrument (Fig. 1c). The tungsten probe was coated with an insulating resin that suppressed the tungsten oxidation side-reaction (see Fig. S1, ESI†). A thin layer of platinum (Pt) was sputter-deposited where the cathode particle contacts the conductive probe, using the sputtering capabilities of the FIB, to ensure a low-resistance, stable electrical contact between the particle and probe. The area of deposited Pt is less than 0.5% of the cathode particle surface area. The reference and counter electrodes are both Li foils with an area of ~0.2 cm<sup>2</sup> and ~1 cm<sup>2</sup>, respectively. Fig. 1d shows SEM cross-sections of as-received NMC and NCA particles after ion-beam cross-sectioning in the FIB. It is observed that each of the individual particles is a secondary particle composed of primary crystallites of 0.5–1 μm diameter. The NMC particle contains a few percent internal porosity, generally concentrated towards the center of the particle, while the NCA particles appear to be fully dense.

### EIS measurements of single-particle interfacial kinetics

The interfacial current density at the electrode–electrolyte in a system with single-electron transfer is described by the Butler–Volmer equation:<sup>15</sup>

$$j = j_0 \left( e^{\frac{-\alpha F}{RT} \eta} - e^{\frac{(1-\alpha)F}{RT} \eta} \right) \quad (1)$$

where  $j_0$  is the exchange current density (mA cm<sup>-2</sup>);  $\eta$  is the interfacial overpotential (V);  $\alpha$  is the transfer coefficient (typically assumed to be 0.5);<sup>16</sup>  $R$  is the universal gas constant (8.314 J mol<sup>-1</sup> K<sup>-1</sup>);  $F$  is Faraday's constant (96 485 C mol<sup>-1</sup>); and  $T$  is temperature (K).  $j_0$  is the relevant materials property that characterizes the charge-transfer reaction at the electrode–electrolyte interface,<sup>15</sup> which we seek to quantify and understand. At high overpotentials, bulk diffusion of Li may also contribute to the measured current. Therefore, we limited the measurements of  $j_0$  to low overpotentials (< 15 mV), where  $j_0$  is readily obtained from the simplified Butler–Volmer equation:

$$j_0 = \frac{RT}{FA R_{ct}} \quad (2)$$

here,  $A$  is the interfacial area of the single particle (cm<sup>2</sup>), which can be calculated from the observed spherical particle diameter

in SEM; and  $R_{ct}$  is the charge-transfer resistance at the electrode–electrolyte interface, which can be calculated from electrochemical impedance spectroscopy (EIS). In previous work,<sup>17–19</sup> the simplified planar geometry of silicon wafers has been used to measure  $j_0$  for silicon anodes without geometric ambiguity. Here, we similarly take advantage of the nearly ideal spherical morphology of the NMC333 and NCA particles.

The exchange current density,  $j_0$ , is a materials-dependent parameter that in principle may vary with cathode type and composition, electrolyte composition, the state of charge (SOC), and sample history.<sup>16,19–21</sup> We used 1 M LiPF<sub>6</sub> in EC/DMC (1 : 1) as a model lithium-ion electrolyte. In order to maximize signal-to-noise ratio during the electrochemical tests, larger particles of ~25 μm diameter with higher absolute charge/discharge currents were used. For TXM analysis, somewhat smaller particles of ~10 μm diameter were characterized, as these proved better able to survive shocks experienced during shipping to the instrument facility, which tended to cause fracture or separation of the larger particles from the probe.

To measure  $j_0$  as a function of SOC, a polycrystalline NMC333 or NCA single particle was first charged (electrochemically delithiated) at C/20 rate to a specified voltage, followed by open-circuit relaxation for three hours, or when the rate of voltage change was less than 3 mV hour<sup>-1</sup>, whichever occurred first. A typical NMC charge voltage profile is shown in Fig. 2a, and a typical NCA profile is shown in Fig. S2 (ESI†). The relaxed OCV and the corresponding SOC at each charge voltage step are summarized in the inset of Fig. 2a. Hereafter, we will use the relaxed OCV as a measure of the SOC of the particle. After relaxation at each voltage step, EIS measurements were performed. Fig. 2b shows the EIS spectrum obtained for an NMC single particle charged to 4.6 V and then relaxed to an OCV of 4.53 V. The equivalent circuit used to fit the EIS data, shown in the inset of Fig. 2b, consists of 5 circuit elements as follows. The high-frequency intercept,  $R_s$ , represents the ohmic resistance of the system. A first semicircle corresponds to  $R_c/CPE_c$ , where  $R_c$  is the contact resistance between NMC and Pt and  $CPE_c$  is the corresponding capacitance. This small feature remained relatively unchanged throughout the measurement of a particle. The second semicircle  $R_{ct}/CPE_{ct}$  is attributed to the charge-transfer resistance,  $R_{ct}$ , at the electrode–electrolyte interface, and its corresponding capacitance,  $CPE_{ct}$ .  $j_0$  associated with each OCV (and SOC) was then calculated from this resistance using eqn (2). The EIS spectra for NMC and NCA as a function of relaxed OCV upon first charging to 4.8 V are shown in Fig. S3a and b (ESI†). The charge voltage, steady OCV,  $R_{ct}$ , and  $j_0$  values for NMC333 and NCA particles are summarized in Tables S1–S5 (ESI†).

Measurements were made on three single particles for each of NMC333 and NCA, amongst which the results were in good agreement, as Fig. 2c and d show. There are three characteristic features of these results: (1) the  $j_0$  values at low SOC (< 4.0 V charge voltage) before the onset of any cycling-related effects; (2) the variation in  $j_0$  with SOC; and (3) the hysteresis in  $j_0$  between the first charge and first discharge. From these results and the TXM observations below, we are able to understand the





**Fig. 2** A representative example of the cell voltage vs. time and the exchange current density vs. state-of-charge, and its hysteresis, for NMC333 and NCA particles, obtained via single particle EIS measurements. (a) Example of the test protocol, here for a NMC333 particle of 26.5  $\mu\text{m}$  diameter, in which the particle was galvanostatically step-charged (delithiated) to a desired voltage and held under open circuit conditions to reach a relaxed voltage. The table shows the voltage reached during each step, the relaxed OCV, and the corresponding SOC. (At the highest OCV, the SOC exceeds 100%, which is attributed to an irreversible contribution to the measured current from electrolyte oxidation.) (b) Single-particle EIS data and fitting using the equivalent circuit shown, NMC333 particle charged to 4.6 V. The dependence of  $j_0$  on (relaxed) OCV shown for three particles each of (c) NMC333 and (d) NCA. (e) Hysteresis is observed in  $j_0$  between charge and discharge, and is markedly different for NMC333 and NCA charged to the same maximum voltage (4.8 V).

extent to which interfacial charge transfer rates are determined by composition and SOC, as opposed to microstructure, including microstructure changes due to electrochemically induced stresses.

At low SOC (corresponding to charge voltage 3.8–4.0 V), NCA has more than ten times higher  $j_0$  than does NMC333,  $\sim 10^{-1}$  vs.  $\sim 3 \times 10^{-3} \text{ mA cm}^{-2}$ . Literature data for NCA are not available, to our knowledge. For NMC333, a published set of  $j_0$  values<sup>22</sup>



measured on composite electrodes is over an order of magnitude higher than those we obtain here, but since the assumptions about the microstructural geometry were not stated in the previous work (most critically, whether the assumed area is the particle surface area or the electrode area), direct comparison with our results is difficult. Considering next the SOC dependence, we see that for NMC333,  $j_0$  increases dramatically, by about a factor of  $10^2$ , from the lowest to highest OCV tested, ultimately reaching  $\sim 0.3 \text{ mA cm}^{-2}$ . The NCA results show a markedly different OCV dependence with two apparent maxima in  $j_0$ , the first appearing at OCV of 4.0 V, which corresponds to about 50% SOC. Newman<sup>15,20</sup> proposed that  $j_0$  depends on the concentration of lithium on both sides of the electrode–electrolyte interface through the function:

$$j_0 = F(k_c)^{\alpha}(k_a)^{(1-\alpha)}(c_s)^{\alpha}(c_{s,\max} - c_s)^{(1-\alpha)}(c_l)^{\alpha} \quad (3)$$

where  $F$  is Faraday constant ( $96485 \text{ C mol}^{-1}$ ),  $k_c$  and  $k_a$  are reaction rate constants for the anodic and cathodic reactions,  $\alpha$  is the transfer coefficient,  $c_s$  is the lithium concentration in active materials ( $\text{mol cm}^{-3}$ ),  $c_{s,\max}$  is the maximum lithium concentration in active materials ( $\text{mol cm}^{-3}$ ),  $c_{s,\max} - c_s$  is the concentration of unoccupied lithium sites in active materials ( $\text{mol cm}^{-3}$ ), and  $c_l$  is the salt concentration in electrolyte ( $\text{mol cm}^{-3}$ ). According to this model,  $j_0$  should exhibit a maximum at some intermediate composition (the exact value depending on the value of  $\alpha$ ) and tend towards zero as the lithium concentration approaches either 0 or  $c_{s,\max}$ . It is tempting to interpret the first maximum in Fig. 2d in terms of eqn (3); we return to this point later. However,  $j_0$  for NMC333 clearly does not exhibit such a maximum over the measured OCV values, which correspond to the practical SOC range for this cathode.

The  $j_0$  for NCA also drops precipitously at OCV above 4.5 V. There is furthermore a large hysteresis in  $j_0$ , the values measured during charge being over an order of magnitude higher than those measured upon discharge (Fig. 2e). In contrast, the NMC333 exhibits both a much smaller hysteresis and a higher  $j_0$  during the first discharge than during the first charge (by a factor of 2–5, depending on the OCV). The results in the following section show that the irreversibility in  $j_0$  for NCA is primarily due to electrochemically induced fracture.

### TXM observations of 3D microstructural evolution

One potential cause of capacity loss during electrochemical cycling is irreversible mechanical failure.<sup>23–27</sup> This phenomenon has been termed “electrochemical shock” in analogy to the thermal shock of brittle materials, which exhibits similar dependences on crystalline properties and microstructure.<sup>28–32</sup> Capacity fade and impedance growth in various lithium ion intercalation materials have been correlated to post-cycling observations of mechanical fracture.<sup>24,26,27,33</sup> Acoustic emission from electrochemical shock has also been directly recorded during charging and discharging.<sup>28–32,34–36</sup> Here, TXM was used to non-destructively generate 3D tomographs of the single particles at different states of charge, which we correlate with the electrochemical measurements. Individual NMC333 and NCA single particles having  $\sim 10 \mu\text{m}$  diameter were charged

at C/3 rate to 3.9 V, 4.1 V, and 4.5 V, respectively. Fig. 3 shows 2D slices at the midpoint of the 3D morphologies of as-received and charged NMC333 and NCA particles as a function of charge voltage. Some internal pores are observed in the starting NMC333 particle (Fig. 3a), while no internal defects were apparent in the starting NCA particle. The TXM slices are consistent with the SEM cross-sectional images of the starting NMC333 and NCA particles in Fig. 1d. It is worth noting that the fine microstructural features due to grain boundaries observed in NCA by SEM are below the spatial resolution of TXM ( $\sim 30 \text{ nm}$ ). Fig. 3a and b show sequentially increasing severity of cracks as charge voltage increases. Visible microcracking starts at about 4.1 V for NMC333 and 3.9 V for NCA. Based on these observations, we conclude that microcracks initiate close to the center of particles and propagate outward. At 4.5 V, dramatic radial cracking and particle separation are observed for NCA; the mechanical damage is considerably less for NMC333. The difference in behavior between the two systems can be correlated with the change in their respective unit cell volumes and c/a ratios as a function of SOC, Fig. 3c.<sup>27,37,38</sup> Both show a similar linear decrease in unit cell volume with increasing SOC (increasing delithiation) at low SOC. However, the unit cell volume for NCA decreases sharply at higher SOC. The c/a ratio increases monotonically with SOC for NMC333, while that for NCA first increases and then decreases with SOC. As explained by Woodford *et al.*,<sup>28</sup> an SOC-dependent crystalline anisotropy (c/a ratio) creates misfit stresses between grains that can lead to microfracture; the criteria for fracture include the change in c/a, elastic constants and fracture toughness of the compound, and the crystallite size, but is independent of (dis)charge rate. The present results highlight the different electrochemical shock behaviors of NMC333 and NCA.

The morphology of the particles as a function of SOC can be used to understand the evolution in  $j_0$  in Fig. 2c–e. For NMC333, the TXM images suggest that despite microfracture, electrical continuity is maintained within the particle, which may explain the reasonably reversible  $j_0$  between charging and discharging as shown in Fig. 2e. In contrast, NCA shows massive fracture at and above a charge voltage of 4.5 V, which should disrupt electrical continuity, consistent with both the decrease in  $j_0$  at high SOC (Fig. 2d) and the large hysteresis between charge (to 4.8 V) and discharge (Fig. 2e). The extreme change in unit cell dimensions that NCA experiences at charge voltage above 4.5 V seems critical to this damage, since we found that an NCA particle charged to only 4.5 V has much more reversible  $j_0$ , as shown in Fig. S4 (ESI†). We did not image by TXM the NCA particles charged to 4.8 V, since the particles could not be handled and shipped intact. Nonetheless, even for particles charged to 4.5 V, the structural integrity of all particles was greatly compromised, and one out of the three NCA particles tested had separated leaving only a portion attached to the probe.

Particle cracking may allow penetration of the liquid electrolyte into the interior of particles, increasing the active surface area. If so, the observed  $R_{ct}$  may decrease and the apparent  $j_0$  increase; in Fig. 2 all values have been calculated assuming that the active surface is the outer surface area of the particle.





**Fig. 3** TXM tomograms showing slices at their midpoints of individual particles of (a) NMC333 and (b) NCA, all particles having  $\sim 10 \mu\text{m}$  diameter. Images are shown for the particles in their pristine state and after charging at C/3 rate to 3.9 V, 4.1 V, and 4.5 V, respectively. The evolution in particle fracture correlates to (c) the percentage change in unit cell volume and c/a ratio of NMC333 and NCA as a function of capacity (*i.e.*, SOC). The data are replotted from ref. 37 and 38.). (d) The measured exchange current density,  $j_0$ , for an NCA particle vs. SOC, corrected for total surface area obtained from the TXM results after charging to 4.5 V (red points), shows that the fracture surface area correction is small compared to the variation in  $j_0$  with OCV (and SOC).

The true  $j_0$  should depend on the actual exposed surface area. To estimate the value of the area correction factor, we analyzed the

TXM results for the more severely fractured case of NCA. Otsu's method<sup>39</sup> was applied to segment the 3D TXM images of the



particles. Allen–Cahn dynamics was used to generate a field with diffuse (*i.e.*, not discontinuous) interface from the resulting binary data to obtain smooth isosurface renderings and corresponding surface mesh of the particle.<sup>40</sup> The areas of the triangular patches of the surface mesh corresponding to the particle–electrolyte interface were summed to obtain the electrochemically active surface area of each particle. Along with the corresponding solid particle volumes calculated from the segmented image data, the surface/volume ratios for the NCA particles (Table S6, ESI†) were obtained. The surface/volume ratios of fractured NCA particles are normalized to that of the pristine particle (taken to be unity). Since the particle volume does not change, the increase in fracture surface area can be used to correct  $j_0$ . In Fig. 3d, we show the corrected  $j_0$  (red open circles) at three different OCV values, calculated assuming that all of the quantified fracture surface area is exposed to liquid electrolyte and available for charge transfer. The correction factor naturally increases with OCV, and in the most extreme case is about a factor of 3 for charging to 4.5 V (Fig. 3b). Compared to the variation in  $j_0$  with OCV, the area correction is modest. For NMC333, the correction factor would be even smaller. We conclude that the monotonic increase in  $j_0$  with OCV of a factor of  $\sim 10^2$  for NMC333 cannot be explained by fracture surface area changes, and are most likely due to (electro)-chemical changes at the cathode–electrolyte interface occurring with changes in SOC. For NCA, despite extensive fracture, the decrease in  $j_0$  by over a factor of 10 above 4.5 V also cannot be explained by the surface area change alone. The large hysteresis in  $j_0$  (Fig. 2e) suggests that this is most likely due to a loss of electrical continuity between fractured regions of the particle.

### Binder effects on particle separation

Typical LIB electrodes are formulated with polymer binders that promote adhesion of the cathode particles and conductive additives to each other and to the current collector foil. Thus, it is reasonable to ask whether such binders, which are usually soluble in the processing solvent (*e.g.*, *N*-methyl-2-pyrrolidone, NMP), influence either  $j_0$  or the electrochemical shock we observed in the NCA particles. Polyvinylidene fluoride (PVdF),

a common binder, was dissolved in NMP, forming a solution into which the attached NCA particles were dipped and then allowed to dry. The coated particles were subjected to the same test protocol as discussed above for the bare NCA. Fig. 4a shows a TXM slice of the PVdF-coated NCA after charging to 4.8 V. Although radial cracks still appear, these are not open cracks, and particle separation is not observed, unlike the bare NCA particles (Fig. 3b). Clearly, a thin surface layer of binder is sufficient to prevent the disintegration that occurs for unconstrained particles. Fig. 4b shows  $j_0$  as a function of OCV measured for a PVdF-coated NCA single particle during the first charge and first discharge. The absolute value of  $j_0$  on first charge is similar to that measured for the bare NCA (Fig. 2d and e), and again shows a double maximum. This indicates that the PVdF coating does not impose a significant charge transfer barrier between the NCA surface and the electrolyte. However, upon discharge the binder-coated NCA did not exhibit the large hysteresis in  $j_0$  seen for the bare NCA (Fig. 2e), and in fact reached a higher peak  $j_0$ . This supports the interpretation that irreversibility in  $j_0$  is due to fracture-induced loss of electrical contact, although a reversible increase in the cathode SEI resistance at high SOC cannot be strictly ruled out. While the PVdF-coated NCA particle exhibits, upon discharge, a  $j_0$  curve with a single maximum, further investigation is necessary before it can be concluded that the experimental result corresponds to the theoretical relationship in eqn (3).

### Single-particle PITT of NMC333

In order to understand the relative contributions of interfacial charge transfer and bulk diffusion to electrochemical kinetics at the single-particle level, we performed potentiostatic intermittent titration tests (PITT) as a function of SOC on the NMC333 particles. Corresponding measurements were not made for the NCA particles, due to the uncertainty in interpreting bulk diffusion when particles are heavily cracked. The measurements were performed during discharge, after first charging the particles to 4.8 V. The particles were then galvanostatically discharged to a specified voltage, corresponding to a desired SOC, and allowed



Fig. 4 (a) TXM slice of a PVdF-coated NCA particle charged to 4.8 V shows evident radial cracking, but with less crack-opening than observed for the bare NCA particle charged to 4.5 V (Fig. 3b). (b) The PVdF-coated NCA exhibits  $j_0$  vs. OCV behavior upon charging that is similar to the bare NCA (Fig. 2d and e), but has greatly improved retention of  $j_0$  during discharge.



to relax under open-circuit conditions for 3 h. The PITT measurement was then performed by stepping up the voltage by 15 mV, and measuring the resulting current as a function of time. The PITT analysis<sup>41,42</sup> used here takes into account a finite interfacial reaction rate, allowing  $j_0$  and the lithium chemical diffusivity,  $D_{\text{Li}}$ , to be obtained simultaneously. PITT therefore provides an independent measurement of  $j_0$  that can be compared with the EIS measurements presented above. In the current experimental configuration, transport of lithium in the liquid electrolyte is not rate-limiting. Note that due to the sufficiently high electronic conductivity of NMC333 which ranges from  $\sim 10^{-6} \text{ S cm}^{-1}$  to  $\sim 10^{-2} \text{ S cm}^{-1}$  over Li concentrations  $x = 0.00$  to  $0.75$ ,<sup>43</sup> the chemical diffusion coefficient is mainly limited by lithium diffusion rather than electron transport. In addition to  $j_0$  and  $D_{\text{Li}}$ , the PITT analysis also yields the electrochemical Biot number ( $B$ ), which characterizes the relative rates of interfacial reaction and bulk diffusion, and is given by:

$$B = -\frac{rj_0}{D_{\text{Li}}RT} \frac{\partial U}{\partial C} \quad (4)$$

where  $r$  is the radius of the electrode particle,  $\frac{\partial U}{\partial C}$  is the slope of the equilibrium potential ( $U$ ) vs. lithium concentration ( $C$ ) curve

at the given SOC,  $R$  is the gas constant, and  $T$  is the absolute temperature. The current response under PITT measurement is fitted using eqn (5) to obtain  $D_{\text{Li}}$  and  $B$ :<sup>41,42</sup>

$$I(t) = -\frac{3D_{\text{Li}}Q}{r^2} \left\{ -\frac{B}{B-1} \left( 1 - \operatorname{erfc} \frac{r}{\sqrt{D_{\text{Li}}t}} \right) + \frac{B^2}{B-1} \exp \left[ \frac{D_{\text{Li}}t}{r^2} (B-1)^2 \right] \operatorname{erfc} \left[ (B-1) \sqrt{\frac{D_{\text{Li}}t}{r^2}} \right] + \frac{B^2 - 2B}{B-1} \exp \left[ 2(B-1) + \frac{D_{\text{Li}}t}{r^2} (B-1)^2 \right] \times \operatorname{erfc} \left[ \frac{r}{\sqrt{D_{\text{Li}}t}} + (B-1) \sqrt{\frac{D_{\text{Li}}t}{r^2}} \right] \right\} \quad (5)$$

where  $I$  is the current for the electrode particle,  $t$  is the time, and  $Q$  is the total charge transferred during the potential step for the electrode particle. The exchange current density is calculated as  $i_0 = -\frac{BDRT}{r} \frac{\partial U}{\partial C}$ . The term  $\frac{\partial U}{\partial C}$  was determined

from the slope of the relaxed OCV vs. Li concentration curves for NMC333.

Fig. 5a shows the PITT current response obtained from a  $26.5 \mu\text{m}$  diameter NMC333 particle upon stepping the voltage



Fig. 5 (a) PITT current vs. time data, and corresponding least-squares fit to eqn (5), from which kinetic parameters are obtained, for an NMC333 particle of  $26.5 \mu\text{m}$  diameter, measured for a +15 mV voltage step from a relaxed OCV of 4.45 V. (b) The dependence of  $j_0$  on OCV from PITT (black squares) is in good agreement with those obtained from EIS (red circles). (c) Chemical diffusion coefficient  $D_{\text{Li}}$  vs. OCV, based on PITT measurements.





**Fig. 6** (a) The electrochemical Biot number,  $B$ , is shown against OCV for a measured 26.5 μm diameter NMC333 particle (top curve), and is scaled to 10, 5 and 2 μm diameter particles (lower curves). At commercially relevant average particle sizes of 5–10 μm, there is mixed-control kinetics across the OCV range from 3.8 V to 4.5 V. (b) The maximum C-rate obtainable for an overpotential of 100 mV is shown, assuming respectively that  $j_0$  or  $D_{Li}$  is rate-limiting. A typical average particle size of 10 μm is assumed. At charge voltages < 4.2 V, interfacial charge transfer is rate-limiting, while at higher charge voltage, mixed control prevails.

by +15 mV from an OCV of 4.45 V. Current ( $i$ )-time ( $t^{-1/2}$ ) profiles such as these were fitted to obtain  $D_{Li}$ ,  $j_0$ , and  $B$ . Raw PITT current vs. time curves for several OCV values are shown in Fig. S5 (ESI†). The measured  $D_{Li}$ ,  $j_0$ , and  $B$  values are summarized in Table S7 (ESI†). Fig. 5b compares the  $j_0$  vs. OCV results for NMC333 from the PITT measurements with those from EIS. The good agreement for the two methods is apparent, and further reinforces the observation that for NMC333,  $j_0$  increases monotonically with OCV. Fig. 5c shows the voltage dependence of  $D_{Li}$ . Amin *et al.*<sup>43</sup> previously measured  $D_{Li}$  in single-phase sintered NMC333 at various SOC, and obtained values similar to those obtained here, of order 10<sup>-10</sup> cm<sup>2</sup> s<sup>-1</sup>.

The electrochemical Biot number,  $B$ , for the NMC particle in Fig. 5 is plotted vs. OCV as the top curve in Fig. 6a. In general,  $B < 0.1$  corresponds to interfacial reaction-limited kinetics  $B > 10$  corresponds to bulk diffusion-limited kinetics, while  $0.1 < B < 10$  is considered to represent mixed-control. According to this criterion, the 26.5 μm particle exhibits mixed-control at lower OCV transitioning to diffusion-limited control at higher OCV, due to the steeper increase in  $j_0$  than in  $D_{Li}$  with OCV. Since  $B$  scales linearly with particle radius  $r$  (eqn (4)), the top curve in Fig. 6a is readily scaled to various (assumed) particle sizes. For commercially-relevant NMC particle sizes of 5–10 μm, mixed-control kinetics are expected across the OCV range from 3.8 V to 4.5 V. Another useful metric by which the impact of a given  $j_0$  and  $D_{Li}$  can be viewed is the maximum C-rate that is permitted before the overpotential,  $\eta$ , becomes unacceptably high. For example, a reasonable limit for  $\eta$  in a Li-ion cell may be about 100 mV. The maximum C-rate limited by interfacial kinetics for a particle with volume  $V$ , surface area  $A$ , and volumetric capacity  $C_p$  is:

$$C_j = \frac{I}{Q} = A \times j_0 \times \left[ \exp\left(\frac{F}{2RT}\eta\right) - \exp\left(-\frac{F}{2RT}\eta\right) \right] / (V \times C_p) \quad (6)$$

where  $C_j$  is interfacial-reaction limited C-rate,  $I$  is the current (in mA), and  $Q$  is the charge passed (in coulombs). For NMC333,

$C_p$  is 1097 mA h cm<sup>-3</sup>. Similarly, the maximum C-rate when bulk diffusion is rate-limiting corresponds approximately to the time constant for diffusion ( $\tau_D$ ) across an electrode particle with radius  $r$  is the diffusion length:

$$\tau_D = \frac{r^2}{D_{Li}} \quad (7)$$

Assuming  $D_{Li}$  to be size-independent, the maximum C-rate is given by:

$$C_D = \frac{3600D_{Li}}{r^2} \quad (8)$$

where  $C_D$  is bulk diffusion-limited C-rate. Fig. 6b shows the maximum C-rate vs. OCV when interfacial kinetics or bulk diffusion are rate-limiting, respectively, assuming a commercial NMC333 cathode with spherical particles of 10 μm average diameter. Across the OCV range from 3.8 V to 4.5 V, the bulk diffusion-limited C-rate, denoted by  $C_D$ , is about 2C, while the interfacial-reaction limited C-rate, denoted by  $C_j$  is 0.5C to 2C. These C-rate values are consistent with experimentally measured rate-capabilities.<sup>11–13</sup>

## Conclusions

The electrochemical kinetics and concurrent microstructural changes of single secondary cathode particles used in Li-ion batteries are characterized for the first time, using a novel high current resolution wet cell and TXM tomography, respectively. With increasing state-of-charge, both NMC333 and NCA undergo electrochemically induced fracture, but with much greater damage occurring in the latter. Quantification of the 3D TXM images shows that even at high charge voltages (4.5–4.8 V), the increase in surface area cannot account for the observed changes in interfacial charge-transfer kinetics, indicating that the main cause of performance degradation in NCA is loss of electrical contact. NMC333 undergoes a factor of 10<sup>2</sup> increase in exchange current density with state-of-charge, which also cannot be explained by microstructure change, and is ascribed to (electro)-chemical changes at the cathode-electrolyte interface, which



may include reversible changes in cathode surface composition or SEI composition with SOC. Micro-PITT measurements show that at commercially relevant particle sizes of  $\sim 10\ \mu\text{m}$ , NMC333 kinetics are interface-limited at low SOC and mixed interfacial/bulk-diffusion limited at higher SOC.

## Materials and methods

### Materials

$\text{LiNi}_{1/3}\text{Mn}_{1/3}\text{Co}_{1/3}\text{O}_2$  (NMC333) and  $\text{LiNi}_{0.8}\text{Co}_{0.15}\text{Al}_{0.05}\text{O}_2$  (NCA) polycrystalline particles were purchased from BASF and TODA America, respectively. Lithium foil, polyvinylidene fluoride (PVdF), and *N*-methyl-2-pyrrolidone (NMP) were purchased from Alfa Aesar. A conventional electrolyte consisted of 1 M  $\text{LiPF}_6$  dissolved in a 1:1 weight ratio of ethylene carbonate (EC) and dimethyl carbonate (DMC) was purchased from BASF. Tungsten (W) probes were purchased from Ted Pella. The Amorphous Fluoropolymer CYTOP was purchased from Asahi Glass. Anti-vibration table was purchased from Technical Manufacturing Corporation.

### Single-particle electrode cell

The tungsten probe was first coated with an amorphous fluoropolymer, CYTOP, to prevent the tungsten oxidation side reaction (Fig. S1, ESI†). To attach a cathode particle, the coating on the probe tip was removed using a silicon ion source in FIB to allow electrical connection. An individual cathode particle was then manipulated into position in the FIB and attached to the tungsten probe by sputtering platinum. Prior to cell assembly, the microelectrode was dried at  $100\ ^\circ\text{C}$  for  $\sim 8\ \text{h}$  under vacuum. To prepare a PVdF-coated NCA microelectrode, PVdF was dissolved in NMP solution at 6 wt%. Afterwards, a bare NCA single-particle microelectrode was dipped into the PVdF/NMP solution and immersed for half an hour. The PVdF-coated NCA single-particle microelectrode was dried at room temperature for  $\sim 8\ \text{h}$ , at  $60\ ^\circ\text{C}$  in air for  $\sim 3\ \text{h}$ , and then for  $\sim 12\ \text{h}$  at  $100\ ^\circ\text{C}$  under vacuum. The single-particle measurement was performed in an argon-filled glovebox at ambient temperature. A conventional electrolyte of 1 M  $\text{LiPF}_6$  in EC/DMC (1:1 weight ratio) was used. The reference and counter electrodes were both Li foils with area of  $\sim 0.1\ \text{cm}^2$  and  $\sim 1\ \text{cm}^2$ , respectively. The three-electrode cell was placed on a vibration-free table (Everstill™ K-400) and in a Faraday cage to minimize vibrational and electromagnetic noise. These cells underwent galvanostatic cycling using a Biologic VMP3 potentiostat with low current capability.

### EIS and PITT measurements

After charging or discharging a single-particle electrode to selected voltage at a rate of C/20 ( $11.5\ \text{mA g}^{-1}$ ), the cell was relaxed under OCV conditions for 3 h until or the voltage changed less than  $3\ \text{mV hour}^{-1}$ , whichever occurred first. The EIS measurements were performed at each relaxed OCV over the frequency range 200 kHz to 10 mHz. Three oscillation amplitudes (5 mV, 10 mV, and 20 mV) were tested to verify the linearity of the impedance response. The PITT measurements

were then performed at each relaxed OCV with 15 mV applied overpotential.

### TXM measurements

*Ex situ* TXM was performed on individual NMC333 and NCA particles of  $\sim 10\ \mu\text{m}$  size in the pristine state and after charging to 3.9 V, 4.1 V, and 4.5 V at C/3 rate. Full-field X-ray transmission tomograms were collected at beamline 32-ID-C at the Advanced Photon Source and beamline 6-2c at the Stanford Synchrotron Light Source. Beamline 32-ID-C operates on a 3.30 cm undulator source. Energy selection was accomplished with a liquid-nitrogen-cooled double-crystal monochromator set to 8400 eV in order to achieve strong nickel absorbance contrast. Single particles were mounted in the microscope still attached to the tungsten tip. A series of  $2048 \times 2048$  transmission micrographs were collected at angles between  $0^\circ$  and  $180^\circ$  with a  $0.25^\circ$  angular step and 2 s exposure time. The field-of-view for each projection is  $25.90\ \mu\text{m}$ , resulting in a pixel-size of 12.65 nm. Ten white-field and five dark-field images were also collected and used for conversion from transmission to optical-depth contrast. Projections were first down-sampled by a factor of two in each dimension. A three-dimensional optical density volume was then reconstructed using tomopy<sup>44</sup> with a combination of simultaneous iteration and filtered back-projection algorithms *via* the “SIRT-FBP” plugin.<sup>45</sup>

Beamline 6-2c operates on a 56-pole wiggler end-station. Energy selection is accomplished with a liquid-nitrogen-cooled double-crystal monochromator, which was set to 9000 eV in order to be significantly above the nickel K-edge to achieve strong absorbance contrast. Single particles were mounted in the microscope still attached to the tungsten tip and a series of  $2048 \times 2048$  transmission micrographs were collected at angles between  $0^\circ$  and  $180^\circ$  with a  $0.5^\circ$  angular step and 0.5 s exposure time. Reference images were collected both before and after tomogram acquisition to allow for conversion to optical-depth projections. A three-dimensional optical-density volume was reconstructed using “TXM-Wizard” and the iterative algebraic reconstruction technique algorithm.<sup>46</sup> In order to account for motor jitter, an iterative alignment technique was used that is built into “TXM-wizard”: the reconstructed volume was forward-projected to calculate a series of projections, which was then compared with the collected projections *via* image registration techniques. In all cases, segmentation of the internal fractures was done using the scikit-image library:<sup>47</sup> morphological opening and black top-hat filters were applied using spherical kernels. Visualization of 3D volumes was done using “ParaView”.<sup>48</sup>

## Conflicts of interest

There are no conflicts to declare.

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