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## Alkyl-nitrile adlayers as probes of plasmonically induced electric fields†

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Vibrational Stark shifts observed from mercaptoalkyl monolayers on surface enhanced Raman (SERS) active materials are reported to provide a direct measurement of the local electric field around plasmonic nanostructures. Adlayers of CN<sup>−</sup>, *p*-mercaptobenzonitrile, and *n*-mercaptobutylnitrile were adsorbed to a heterogeneous nanostructured Ag surface. The frequency of the CN moiety was observed to shift in a correlated fashion with the SERS intensity. These shifts are attributed to a vibrational Stark shift arising from rectification of the optical field, which gives rise to a DC potential on the surface. All three molecules showed CN Stark shifts on the plasmonic surfaces. *p*-Mercaptobenzonitrile is observed to be a well-behaved probe of the electric field, providing a narrow spectral line, suggesting a more uniform orientation on the surface. The utility of *p*-mercaptobenzonitrile was demonstrated by successfully assessing the electric field between gold nanoparticles adsorbed to a monolayer of the nitrile on a flat gold surface. A model is presented where the Stark shift of the alkyl-nitrile probe can be correlated to optical field, providing an intensity independent measurement of the local electric field environment.

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## Introduction

The excitation of plasmon resonances in metal nanostructures results in confined electric fields that have been exploited in research areas ranging from chemical catalysis to trace detection.<sup>1–4</sup> Plasmonic nanostructures increase the rate of reactions on their surfaces when illuminated at their plasmon resonance frequency.<sup>4–9</sup> On nanostructure arrays, heterogeneous reactivity has been observed, implicating “hotspots”, areas of intense electric fields, as important for catalysis.<sup>10</sup> The excitation of plasmons has long been associated with nanostructure enhanced spectroscopies,<sup>11</sup> such as surface enhanced (SERS) and tip enhanced (TERS) Raman scattering. The increased electric field promote optical processes by increasing the magnitude of the excitation field ( $E_{\text{exc}}$ ) and the emitted electric field ( $E_{\text{emm}}$ ) leading to an increased response as shown in eqn (1):

$$\text{EF} = \frac{|E_{\text{exc}}|^2}{|E_0|^2} \frac{|E_{\text{emm}}|^2}{|E_0|^2} \approx E^4 \quad (1)$$

where the excitation and emission fields are normalized to the incident electric field ( $E_0$ ), this equation is known as the  $E^4$  approximation.<sup>12</sup> For isolated spherical particles, the approximation is rigorous and predicts an electric field enhancement (EF) on the order of  $10^5$  when optimized. When two particles align to form a hotspot, the resulting electric field is amplified

and, given the  $E^4$  dependence (eqn (1)), is attributed with single molecule detection in Raman spectroscopy.<sup>13,14</sup>

Experimental measurement of the electric fields that arise from plasmonic excitation is challenging and has been determined in different ways. In surface enhanced Raman scattering, the relationship between the observed Raman scattering intensity and the electromagnetic enhancements provides an indirect method to assess the electric fields using the  $E^4$  approximation.<sup>12</sup> If one can calculate the number of molecules on the plasmonic surface, an analytical enhancement factor can be determined from the increased Raman scattering observed from the molecules relative to the normal Raman cross-section.<sup>3,15</sup> It has been shown that hotspots dominate the SERS signal,<sup>16</sup> and from eqn (1), the electric field can be backed out. Uncertainty with molecular orientation and surface coverage are problematic for this intensity-based determination of the electric field.<sup>17–20</sup> An alternative approach was demonstrated by combining theory with electron energy loss spectroscopy (EELS) to indirectly probe electromagnetic hotspots.<sup>21</sup> The use of finite element models with experiment is a common approach. These calculations seem to oversimplify the electric fields in small junctions, and to accurately model the electric fields at the nanoparticle surface requires the inclusion of quantum effects.<sup>22</sup>

A measurement directly associated with the electric field would provide increased understanding of the electric fields at the surface of nanoparticles arising from plasmon excitation. It has been shown that the intense electric fields associated with excited plasmon resonances can drive nonlinear optical phenomena.<sup>23</sup> Specifically, optical rectification results in a DC field at interfaces under the influence of high intensity electric

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fields.<sup>24</sup> This second order nonlinear process has been associated with the variation of second harmonic generation intensities with applied potential.<sup>25,26</sup> It has also been shown that exciting a plasmonic junction at the resonant frequency induces a tunneling current,<sup>23</sup> and that biasing these plasmonic junctions will modulate nonlinear optical processes.<sup>27</sup>

The DC field arising from plasmonic excitation has been reported by several groups to generate a Stark shift in a molecule located in the plasmonic junction.<sup>28,29</sup> The vibrational Stark effect is a change in the vibrational frequency that arises from a perturbation to the electronic environment of a chemical bond.<sup>30</sup> Measurement of the change in vibrational frequency of the bond can thus be used to determine the magnitude of the electric field. The vibrational Stark effect has been used to measure electric fields in a variety of chemical systems including the electrochemical double layer,<sup>31–33</sup> catalysts,<sup>34</sup> proteins,<sup>30,35–37</sup> biomembranes,<sup>38</sup> and the energy levels of molecules.<sup>39–41</sup>

Apkarian and coworkers correlated the vibrational Stark shift from a CO molecule between two spherical particles to an electric field enhancement on the order of  $10^{12}$ , substantiating single molecule detection.<sup>29</sup> Results from our laboratory showed a  $130\text{ cm}^{-1}$  Stark shift in the CN stretch frequency when adsorbed CN was detected in a plasmonic junction formed between a nanoparticle TERS tip and a roughened Au surface.<sup>28</sup> Plasmonic coupling between the nanoparticle and the gold surface generates a combined plasmon that oscillates in phase preserving the break in symmetry required for the second order nonlinear process. Only the CN in the confined region is observed to shift, and the CN outside the plasmonic junction was observed to persist at the unshifted frequency.

The ability to determine electric fields on plasmonic surfaces suggests a direct method to map electric field distributions on these materials. In this manuscript we demonstrate the use of adsorbed alkyl-nitrile molecules as Stark reporters of the local electric fields. We use the observed Stark shift to determine the local electric field that gives rise to optical rectification. In particular, we note that *p*-mercaptobenzonitrile appears to be a well-suited probe that can be readily adsorbed to metal structures.

## Experimental

### Materials and reagents

The copper wire used was of 99.995% purity (Alfa Aesar). The silver electroplating solution used was 1025 RTU (Technic, Inc.). Ethanol (90%) and *n*-mercaptobutylnitrile (98%) were obtained from Sigma Aldrich (St. Louis, MO) and were used as received. *p*-Mercaptobenzonitrile was synthesized by the Notre Dame Chemical Synthesis Core and verified to be of >98% pure by NMR. Gold nanoparticle colloid (80 nm citrate NanoXact™ gold) was purchased from nanoComposix (San Diego, CA). Template stripped gold chips used as ultraflat gold surface were from Platypus (100 nm Au thickness, RMS roughness =  $3.6\text{ Å}$ ). UltraNanopure water ( $18.2\text{ MΩ cm}$ ) was obtained from a Barnstead Nanopure filtration system (Thermo Scientific).

### Raman

Raman maps were acquired using a Renishaw inVia Raman microscope. The excitation laser was either a 632.8 nm HeNe laser (ThorLabs) for the *n*-mercaptobutylnitrile and *p*-mercaptobenzonitrile monolayer experiments or a 660 nm diode laser (Laser Quantum) for the  $\text{CN}^-$  adsorbed to Ag experiments. The acquisition time per spectrum was adjusted with the incident laser power to generate spectra with sufficient signal to noise ratios for analysis. For  $\text{CN}^-$  experiments, the scattering between  $1940\text{--}2348\text{ cm}^{-1}$  Raman shift was collected; otherwise, the spectral range was  $2016\text{--}2470\text{ cm}^{-1}$ . Raman spectra for gold nanoparticles on ultraflat gold films were taken using a home-built Raman microscope equipped with dark field microscopy (BD objective, Olympus, LMPlanFLN, NA = 0.5). A 632.8 nm HeNe laser (Melles Griot) was used to irradiate the sample in a top illumination geometry and a Horiba Jobin Yvon iHR320 spectrometer was used to resolve the Raman scattering. The laser power measured at the sample was 0.75 mW, and the acquisition time was 1 s. The spectral data was analyzed using MATLAB and an open-source peak-fitting routine.<sup>42</sup> Spectra were fit to a Gaussian lineshape 5 times, and the fit with the lowest % RMS error was selected.

### Sample preparation

The SERS substrate was fabricated using a modified procedure for embedding electrodes in polystyrene.<sup>43</sup> A 100 cm length of approximately  $25\text{ μm}$  diameter copper wire was held vertically so that the tip was in contact with a glass disk with copper tape edges. Polystyrene powder was added to the mold and melted at a temperature of  $300\text{ °C}$ .<sup>43</sup> The filled mold was allowed to cool and harden, after which the polystyrene disk with embedded wire was removed from the mold. The polystyrene was polished using successively finer grit alumina-embedded paper to expose and polish the Cu surface; the dark field scattering of the surface was observed before continuing with the sample preparation, indicating a relatively flat surface with intermittent small, rough areas.

Silver was electrodeposited onto the Cu surface using a commercial plating solution containing  $\text{CN}^-$ . A deposition potential of  $-1\text{ V vs. Ag/AgCl}$  was applied to the wire for 150–300 s, controlled with a CHI660D potentiostat (CH Instruments). Following electroplating, the substrates were washed sequentially with water and ethanol. The deposited surface had CN adsorbed to the surface. The Ag substrates were sized using optical microscopy in the range of  $25\text{--}50\text{ μm}$  in diameter and were roughly circular.

Monolayers of *n*-mercaptobutylnitrile and *p*-mercaptobenzonitrile were prepared by standard monolayer deposition chemistry. First to remove the adsorbed  $\text{CN}^-$ , 10 oxidation–reduction cycles (ORC) were performed in 0.1 M NaOH.<sup>44</sup> In the ORC, the potential was swept from  $-0.6\text{ V}$  to  $0.4\text{ V}$  at rate of  $10\text{ mV s}^{-1}$ . The removal of  $\text{CN}^-$  was confirmed by Raman spectroscopy, after which the substrate was soaked for 24 h in a 0.01 M ethanolic solution of the appropriate thiol. Following this, the substrates were sequentially washed with water and



ethanol. The substrates were stored covered under ambient conditions when not in use.

On template stripped gold films, a layer of *p*-mercaptobenzonitrile was self-assembled by immersing the ultraflat surface in the *p*-mercaptobenzonitrile ethanolic solution overnight. The film was then rinsed with ethanol and ultrapure water for 3 cycles each. The gold film with the self-assembled monolayer was subsequently immersed in 2 mL of a mono-dispersed gold nanoparticle colloid (80 nm, 0.05 mg mL<sup>-1</sup>) suspension in a Petri dish (35 × 10 mm) for 1 hour, after which the gold film was dipped into ultrapure water multiple cycles to remove weakly bound nanoparticles. The prepared film was then dried and used for dark-field microscopy and Raman spectroscopy.

## Results

To assess the electric fields present on the electrodeposited silver surfaces, three different CN containing molecules were adsorbed to freshly prepared surfaces: cyanide, *p*-mercaptobenzonitrile, and *n*-mercaptobutylnitrile.

Fig. 1 shows the results obtained from an electrodeposited Ag surface, with CN<sup>-</sup> detectable on it. The bright field image (Fig. 1A) indicates a heterogeneous surface topography, which correspond to regions of high and low Raman scattering from the adsorbed CN (Fig. 1B). Previously, it was shown that the frequency of the CN stretch on a Au surface correlated with the observed SERS intensity.<sup>28</sup> By fitting the CN stretch mode to a Gaussian lineshape (Fig. 1C), we are able to extract changes in the mode across the silver surface. In Fig. 1D we see that the CN

frequency varies by ~10 to 12 cm<sup>-1</sup> across the mapped region. The correlation between the CN frequency shift and Raman intensity is less apparent than in previous reports; however, the magnitude of the shift is consistent with low levels of enhancement. In our previous work on Au surfaces, shifts of this magnitude were also observed at low enhancement levels, thus variations in the amount of CN adsorbed may also generate significant signal changes in addition to the plasmonic enhancement. It should be pointed out that atomic level defects may impact the observed rectification associated with tunneling. It has been reported that tunneling can diminish the observed electric fields and resulting SERS response,<sup>45</sup> that may account for some variation. It is well established that SERS enhancements are sensitive to nanoscale structure, which is quite heterogeneous in our system (Fig. S-1†).

To further assess the observed Stark shift on the electrode surface, the region was mapped at increasing laser power. We mapped the Ag surface at five different excitation powers, from 0.02 mW to 2.0 mW, using 660 nm laser excitation. Fig. 2 shows three representative maps obtained at 0.1 mW (Fig. 2A), 0.2 mW (Fig. 2B), and 2.0 mW (Fig. 2C), which display a general trend of increasing CN frequency with increasing laser power.

While the CN stretching frequency was observed to vary across the mapped region of the Ag surface, we chose two distinct regions: one with a lower stretching frequency (blue to light blue region), denoted (1) and one region of higher stretching frequency (yellow to red region), denoted (2). The average frequency shift was calculated over these two regions of interest in the power dependent maps and plotted against the

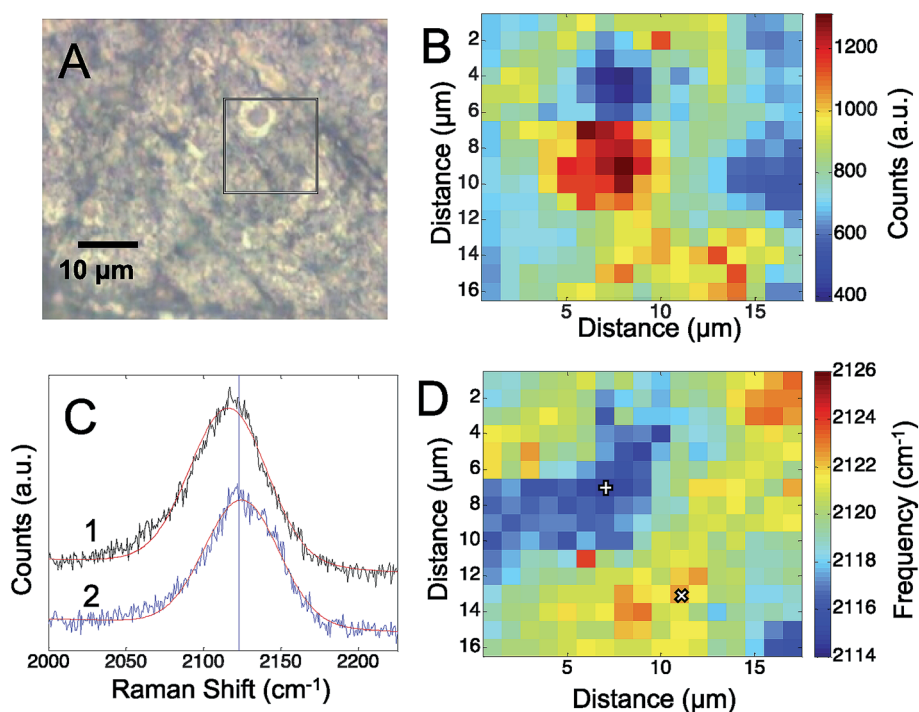


Fig. 1 (A) The optical image of the roughened silver surface is shown. The box indicates the approximate area where the Raman map of the CN stretch intensity (B) was acquired. The CN stretch frequency was determined by fitting a Gaussian lineshape to spectrum at each pixel. Sample spectra from areas with high and low Raman intensity are shown (C). The frequency of the CN stretch is plotted (D), showing a variation of up to 12 cm<sup>-1</sup> across the electrode. The pixels plotted in C are marked by + = 1 and × = 2.



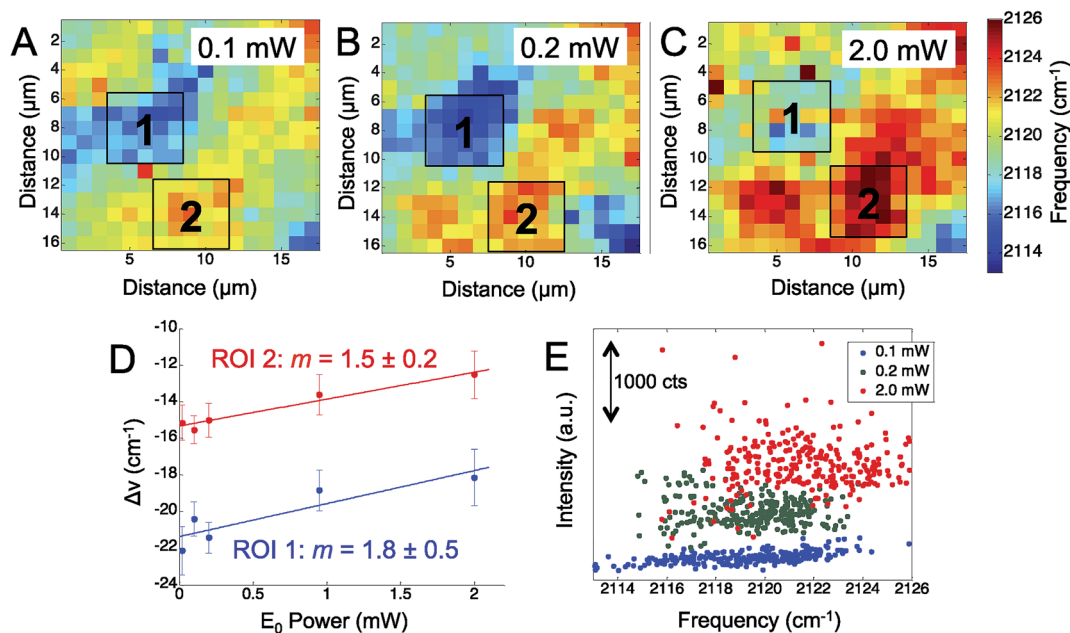


Fig. 2 The observed CN stretch frequency observed on a roughened silver surface is plotted at increasing incident laser power: (A) 0.1 mW, (B) 0.2 mW, and (C) 2.0 mW. (D) The average frequency shift observed in each region of interest (ROI) was plotted against the incident laser power ( $E_0$ ). The slope ( $m$ ) for each is reported. (E) The intensity of the CN mode was plotted against the observed CN frequency.

incident laser power (Fig. 2D). The shift in the CN frequency,  $\Delta\nu_{\text{CN}}$ , was calculated by comparing the observed frequency to a reference value of crystalline AgCN at  $2139 \text{ cm}^{-1}$ .<sup>46</sup> A positive linear relationship was observed between  $\Delta\nu_{\text{CN}}$  and the laser power in agreement with the visual inspection of the maps. The

slope in each ROI was determined to be  $1.8 \pm 0.5 \text{ cm}^{-1} \text{ mW}^{-1}$  and  $1.5 \pm 0.2 \text{ cm}^{-1} \text{ mW}^{-1}$ , suggesting a similar change in the CN stretch frequency is observed in both regions. The positive slope observed for the CN frequency *versus* incident power suggests increasing positive charge on the surface. It is worth

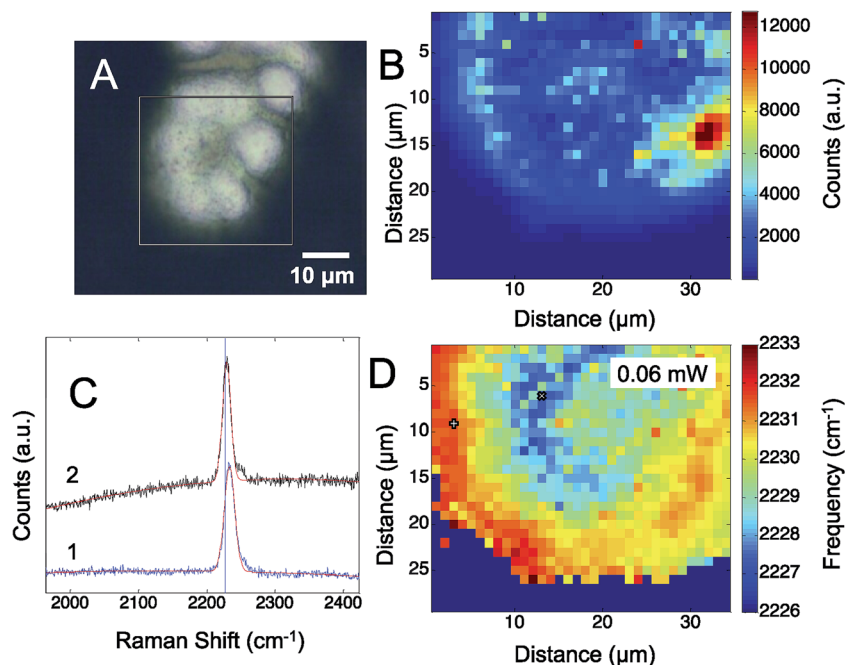


Fig. 3 (A) The optical image of the electrodeposited silver surface with *p*-mercaptobenzonitrile is shown. The box indicates the area where the Raman map (B) was acquired. The CN stretch frequency was determined by fitting a Gaussian lineshape to each pixel. Sample spectra from areas with high and low Raman intensity are shown (C). The observed CN stretch frequency is plotted (D), showing a variation of up to  $7 \text{ cm}^{-1}$  across the electrode. The pixels plotted in C are marked by + = 1 and x = 2.





noting that the isotropic frequency for CN is greater than the frequencies observed in Fig. 1 and 2. This suggests an induced positive DC field that shifts the CN stretch to a higher frequency. These data suggest the Ag surface potential is initially negative and may affect the Ag–CN interaction compared to CN adsorbed on Au.

Fig. 2E shows a map of the SERS intensity *versus* frequency of the CN band at the indicated incident field powers. The overall intensity of the CN stretch mode across the entire Raman map is observed to increase with the increased laser power (Fig. 2E). In agreement with the data in Fig. 2D, the range of high and low observed CN frequencies also trend positive with increasing incident power. The SERS intensity is expected to show a nonlinear,  $E^4$ , correlation to the electric field; however, the data show increasing spread in the intensity, further suggesting the adsorbed CN is located in heterogeneous plasmonic environments.

The CN stretch frequency is highly dependent upon the bonds formed to the nitrile. Earlier work reported difficulty establishing a Stark tuning rate for CN on metals, arising from coupling of the metal–carbon and nitrile bond.<sup>47</sup> However, alkyl nitriles have been used successfully as probes of local electric fields.<sup>30,37,38,48–50</sup> To further investigate CN Stark shifts in plasmonic environments, we adsorbed *p*-mercaptobenzonitrile and *n*-mercaptobutylnitrile to SERS active surfaces.

Fig. 3 shows the results obtained from a self-assembled monolayer of *p*-mercaptobenzonitrile on the silver SERS surface. To remove any CN from the silver surface, the electrochemical potential was cycled in flowing NaOH.<sup>44</sup> The CN band was monitored before and after to insure CN was removed. Similar to the results with adsorbed CN, a heterogeneous structured Ag surface is obtained that shows SERS activity. The Raman map shows areas that suggest hotspots based on the intensity of the adsorbed CN. The greatest SERS intensity is observed in the region between two Ag hemispherical structures. A single Gaussian lineshape was fit to the CN band (Fig. 3C) to determine variation in the CN frequency over the surface (Fig. 3D).

The CN stretch frequency observed from *p*-mercaptobenzonitrile is different from adsorbed  $\text{CN}^-$ . In Fig. 3C the FWHM of the CN stretch frequency is observed to be 18 and 19  $\text{cm}^{-1}$ , whereas adsorbed  $\text{CN}^-$  exhibited a FWHM of 55–58  $\text{cm}^{-1}$ . Additionally, the frequency of *p*-mercaptobenzonitrile (Fig. 3D) is centered around 2230  $\text{cm}^{-1}$ , *versus* 2120  $\text{cm}^{-1}$  in Fig. 1D. The shift in the absolute frequency is consistent with CN frequency of neat *p*-mercaptobenzonitrile, which we observe at 2223  $\text{cm}^{-1}$  (Fig. S-2†). The change in CN frequency supports the formation of the benzonitrile adlayer on the surface. The narrower peak width observed suggests a more homogeneous environment for nitrile.

Similarly to the  $\text{CN}^-$  adsorbed to Ag experiment above, the CN stretching mode of *p*-mercaptobenzonitrile was mapped across the Ag surface at five excitation laser powers, ranging from 0.06 mW to 6.4 mW. In these experiments a 633 nm HeNe laser was used. Fig. 4 shows representative maps of the CN frequency at laser powers of 0.06 mW (Fig. 4A), 0.65 mW (Fig. 4B), and 6.4 mW (Fig. 4C). At the lowest laser power, the CN frequency appeared to cluster into three ROIs. The shift in the CN frequency was calculated against the CN frequency of neat

*p*-mercaptobenzonitrile (2223  $\text{cm}^{-1}$ ). The averaged  $\Delta\nu_{\text{CN}}$  of three ROI were plotted *versus* the laser power (Fig. 4D). The trend with increased incident power is different than that observed for adsorbed  $\text{CN}^-$ . Initially, a positive trend was observed for the first three maps, suggesting that the Stark shift was increasing with the incident power as before with  $\text{CN}^-$  on Ag; however, at higher incident power the CN stretch frequency levels off and decreases.

Examining the change in the CN stretch frequency suggests at least two different trends. Fitting a line to the initial rise for each ROI, the calculated slopes were  $1.4 \pm 0.5 \text{ cm}^{-1} \text{ mW}^{-1}$  (ROI 1),  $0.3 \pm 0.1 \text{ cm}^{-1} \text{ mW}^{-1}$  (ROI 2), and  $0.6 \pm 0.2 \text{ cm}^{-1} \text{ mW}^{-1}$  (ROI 3). The slope observed in ROI 1 is similar to that observed

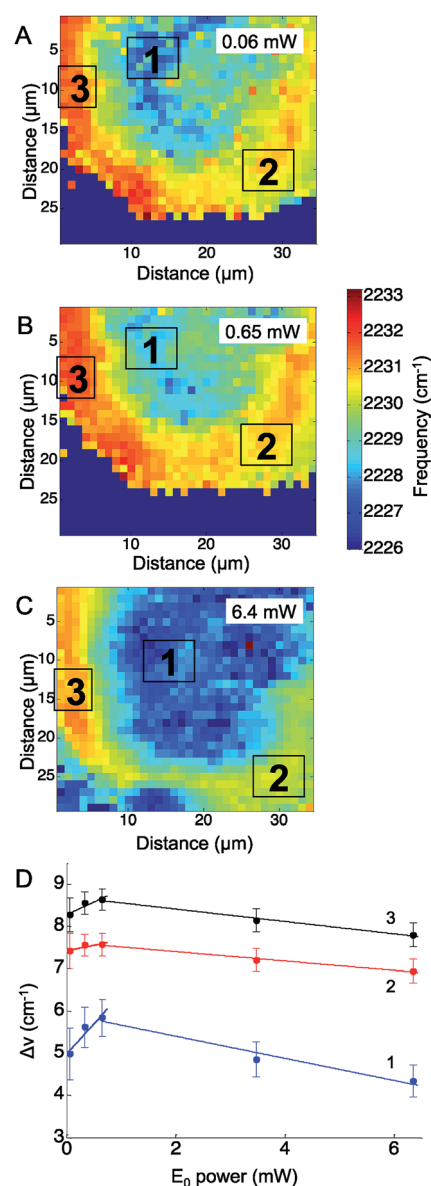


Fig. 4 The observed CN stretch frequency of *p*-mercaptobenzonitrile on a roughened silver surface is plotted at increasing incident laser power: (A) 0.06 mW, (B) 0.65 mW, and (C) 6.4 mW. (D) The average frequency shift observed in each region of interest (ROI) was plotted against the incident laser power ( $E_0$ ). The lines in D are guides for the eye.



with changes in incident power for adsorbed  $\text{CN}^-$  (Fig. 2). The slope observed in ROI 2 and ROI 3 is significantly lower, and suggests something else is involved. It is known that organic molecules can be photodecomposed at higher laser powers.<sup>16,51</sup> Photodamage may explain the decrease in the observed CN stretch at higher laser powers. This trend correlates with laser powers  $>1$  mW, which are known to damage molecules. The lower initial slopes in ROIs 2 and 3 are also the areas that have the highest initial CN stretch frequencies, which would correlate with the greatest plasmonic fields and increased likelihood of damage. This agrees with work by Dlott and coworkers that suggests molecules in the highest enhancement region are most likely to be photodamaged.<sup>16</sup> The *p*-mercaptobenzonitrile experiment explored higher powers than in the adsorbed  $\text{CN}^-$  experiments, and at excitation powers  $>1$  mW, all three regions show a decrease in average CN stretch frequency, which suggests only molecules adsorbed in lower enhancement regions have survived.

In Fig. 5, the CN stretch frequency shows excellent agreement with our previous results from adsorbed  $\text{CN}^-$  on Au.<sup>28</sup> There is a nonlinear trend in intensity that correlates with the observed CN stretch frequency. Interestingly, the intensity data shows a minimum in Fig. 5 near  $2227\text{ cm}^{-1}$ , which may indicate the isoelectric point for the CN on the Ag surface.

Fig. 6 compares the spectra obtained from *p*-mercaptobenzonitrile with those from *n*-mercaptobutylnitrile. The SERS activity of the Ag surface appears similar to that observed above; however, the observed nitrile spectrum is different than observed for either adsorbed  $\text{CN}^-$  or *p*-mercaptobenzonitrile. The spectrum of *n*-mercaptobutylnitrile shows 2 peaks in the CN stretch region centered at  $2245\text{ cm}^{-1}$ . This is in contrast to the single peak observed in the spectrum of the crystalline compound (Fig. S-2†). A lower energy band has been previously attributed to a Fermi resonance in *n*-butylnitrile;<sup>52</sup> however, the

band observed here is at a considerably lower frequency. As shown in Fig. 6, we attribute the spectral variation observed in *n*-mercaptobutylnitrile to the flexible C–C backbone which enables rotation and multiple interactions between the CN and the surface. Such interactions are not observed with *p*-mercaptobenzonitrile because of the rigid phenyl ring structure.

Analysis of the *n*-mercaptobutylnitrile spectra was performed (Fig. S-3 and S-4†) and the higher intensity peak appears to shift in manner consistent with a vibrational Stark shift. Interestingly, the spectral variation observed for *n*-mercaptobutylnitrile appears to be time dependent. Fig. S-5† shows the time varying fluctuations of the CN signal on the SERS substrate. This was not observed in the *n*-mercaptobenzonitrile, further implicating the flexible C–C backbone and multiple surface interactions as the origin of the spectral heterogeneity. This interpretation is also consistent with the broader full-width half maximum observed for adsorbed CN, which may also interact in a variety of conformations.

These results suggest that *p*-mercaptobenzonitrile is the optimal probes of those examined. To further evaluate this, a monolayer of *p*-mercaptobenzonitrile was adsorbed onto a thin

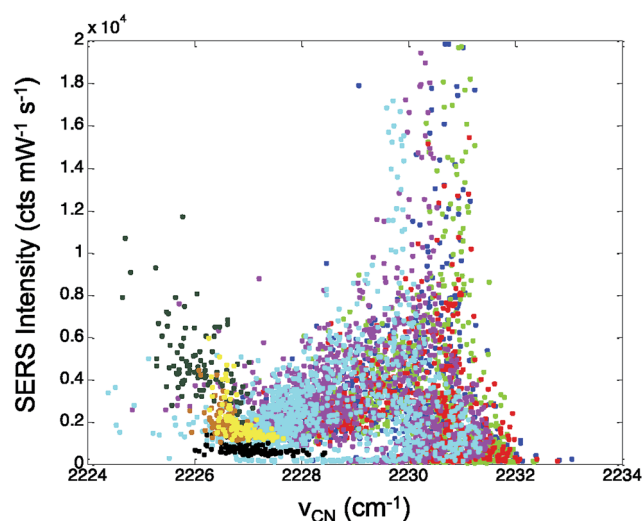


Fig. 5 The intensity of the CN mode in mercaptobenzonitrile was plotted against the observed CN frequency across multiple data sets. The colors represent data sets at different incident powers. The reported intensity has been normalized for power and acquisition time.

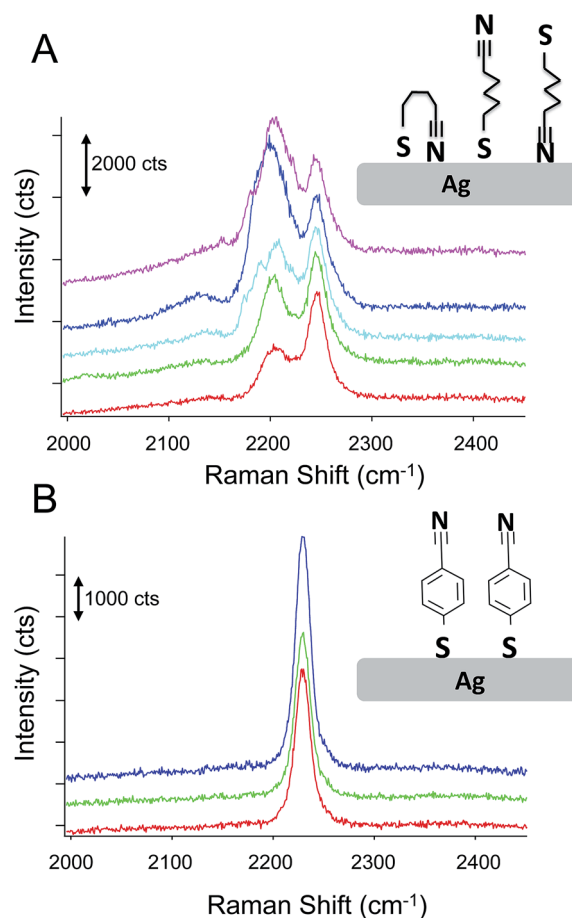


Fig. 6 The SERS spectra observed from an adsorbed layer of *n*-mercaptobutylnitrile (A) show significant spectra to spectra variation compared to the spectra observed from *p*-mercaptobenzonitrile (B). The insets show possible binding configurations that may explain the differences in observed lineshape.



Au film. Citrate capped Au nanoparticles were then deposited onto this film. Fig. 7 shows the dark field image and SERS results obtained from isolated NPs. Brighter scattering particles gave rise to more intense SERS spectra, which may indicate dimers or aggregates on the surface, which would give rise to larger field enhancements.

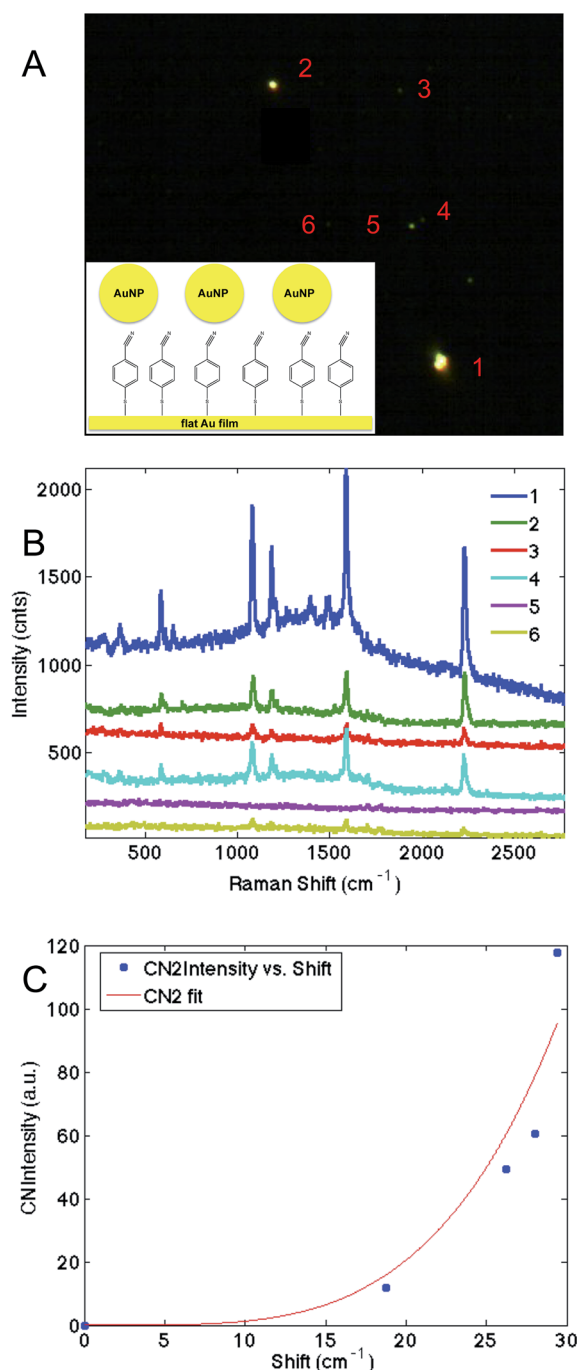


Fig. 7 The dark-field image (A) shows the location of nanoparticles, from which SERS spectra (B) were obtained. The numbers in A correspond to the spectra in (B). The CN region was fit to two Gaussian lineshapes, and the higher energy component's frequency is plotted against its intensity, which shows a nonlinear increase (C). The line in (C) is guide for the eye.

The CN region was fit (Fig. S-6†) and a higher energy feature is observed in the CN stretching regions whose frequency correlates with intensity (Fig. 7C). Similar to our previous TERS experiment,<sup>28</sup> only a portion of the molecules are shifted, implying that the hotspot is localized. Nonetheless, the agreement between SERS intensity and CN frequency in this more controlled experiment further supports the utility of *p*-mercaptobenzonitrile as an electric field reporter.

## Discussion

The observed shift in the CN stretch frequency is attributed to a Stark effect arising from optical rectification of the optical field to produce a DC component experienced by the adsorbed molecules. The linear dependence on the incident power observed in Fig. 2, and at low powers in Fig. 4 and S-4,† are consistent with optical rectification. This linear trend supports the hypothesis of an optically rectified DC field acting on the CN bond and giving rise to a vibrational Stark shift.

A DC field arising from optical rectification suggests a means to calculate the optical field generated by the localized plasmon resonance and determine an enhancement factor independent of signal intensity. It has been shown that the static, or DC, electric field ( $E_{DC}$ ) experienced by a chemical bond can be related to the change in frequency ( $\Delta\nu$ ) through the Stark tuning coefficient ( $\mu$ ) as follows:<sup>30</sup>

$$E_{DC} = \Delta\nu\mu \quad (2)$$

Using the vibrational frequency of the neat, or crystalline, nitrile as the reference frequency, the  $\Delta\nu$  observed on a plasmonic surface is straightforward to calculate.

In optical rectification, the magnitude of the DC field ( $E_{DC}$ ) is proportional to the time invariant component of the second order polarizability:<sup>53</sup>

$$P(0)^{(2)} \approx 2\chi^{(2)}EE \quad (3)$$

where  $\chi^{(2)}$  is the second order susceptibility and  $E$  is the optical field at the interface. While, the incident and Raman emitted electric fields are slightly shifted in wavelength, it is commonly assumed that these fields are the same. Eqn (3) provides a direct connection to the optical field associated with the observed Stark shift.

The exact values for the  $\chi^{(2)}$  tensor for nanostructured plasmonic surfaces are not well documented in the literature.<sup>27</sup> However, there are approaches that let us approximate values for  $\chi^{(2)}$ . It is straightforward to estimate  $\chi^{(2)}$  from literature values of  $\chi^{(3)}$ .<sup>54</sup> A first order approximation is:

$$\chi^{(2)} = \chi^{(3)}E_{AU} \quad (4)$$

where  $E_{AU}$  is the atomic unit of electric field strength,  $5.1 \times 10^{11}$  V m<sup>-1</sup>.<sup>54,55</sup> Using literature values reported for  $\chi^{(3)}$  of silver nanoparticle dispersions,<sup>56–58</sup> we obtain a  $\chi^{(2)}$  on the order of  $10^4$  cm MV<sup>-1</sup>. An alternative approach is to use  $\chi^{(3)}$  values reported for planar Ag surfaces and to correct for enhancements associated with nanostructure. The  $\chi^{(3)}$  values found in the literature



for planar Ag films suggest a  $\chi^{(2)}$  of approximately  $20 \text{ cm MV}^{-1}$ .<sup>54,59</sup> Roughened Ag surfaces, similar to those prepared in this experiment, are reported to enhance second order nonlinear processes by  $10^3$  to  $10^4$ . This combination of this enhancement with the  $\chi^{(2)}$  determined for planar Ag films again corresponds to a  $\chi^{(2)}$  on the order of  $10^4$  to  $10^5 \text{ cm MV}^{-1}$ .

There are reports of the hyperpolarizabilities for silver and gold,<sup>60,61</sup> however, these values are determined on per atom basis. Determining the number of metal atoms that give rise to the enhanced field is unclear. For instance, how do the electrons from adjacent nanostructures alter the hyperpolarizability? Additionally, other factors are needed to properly convert molecular hyperpolarizabilities into susceptibilities for determining the nonlinear response of the larger material.<sup>62</sup>

The calculation of  $\chi^{(2)}$  further indicates the importance of the localized plasmon resonance for generating the intense local field that drives the optical rectification. Nonlinear susceptibility measurements performed as a function of wavelength show the susceptibility increases dramatically at wavelengths associated with plasmon resonances.<sup>56,58,63–65</sup> Interestingly previous work measuring second harmonic excitation on Ag nanoparticle arrays exhibited a maximum response near 650 nm, similar to the laser wavelengths used in this experiment.<sup>64</sup> We have previously measured the extinction spectrum of heterogeneous Ag surface and observed a resonance at these wavelengths.<sup>66</sup> These observations are consistent with our hypothesis that the enhanced local fields drive the optical rectification that gives rise to the observed Stark shift.

Using an approximate  $\chi^{(2)} = 10^4 \text{ cm MV}^{-1}$ , the enhanced electromagnetic fields that generate the SERS response, and thus the electromagnetic enhancement factor can be calculated for this system. Literature values for the Stark tuning coefficient for butylnitrile [ $0.5 \text{ cm}^{-1} (\text{MV cm}^{-1})^{-1}$ ] and benzonitrile [ $0.6 \text{ cm}^{-1} (\text{MV cm}^{-1})^{-1}$ ] can convert the frequency shift into a field intensity.<sup>67,68</sup> The exact Stark tuning coefficient for  $\text{CN}^-$  is not known, but the value  $2.9 \text{ cm}^{-1} (\text{MV cm}^{-1})^{-1}$  is consistent with our previous work.<sup>28</sup> Recognizing the  $E_{\text{DC}}$  (eqn (2)) is equivalent to the  $P(0)^{(2)}$  (eqn (3)), we can establish:

$$E_{\text{DC}} = \chi^{(2)} E E \quad (5)$$

From the measured power and laser spot size, the electric field incident on the surface can be calculated. For low laser powers (0.06 mW, 0.06 mW, and 0.02 mW for *p*-mercaptobenzonitrile, *n*-mercaptobutylnitriles, and  $\text{CN}^-$ , respectively) we observe electric field enhancements of  $4\text{--}6\times$  (*p*-mercaptobenzonitrile),  $2\text{--}3\times$  (*n*-mercaptobutylnitriles), and  $6\text{--}9\times$  ( $\text{CN}^-$ ). Using the standard  $E^4$  approximation, these local electric fields correspond to quite modest SERS enhancement factors of  $\sim 10^2$  to  $10^3$ , which seem low given the observed SERS intensity. Interestingly, the shift observed from gap modes formed between Au nanoparticles and a Au surface are twice the magnitude observed on the Ag substrates, which is consistent with the large electric fields found in this geometry.

There are sources of uncertainty that may explain the low fields calculated. For example, one possible source of difference is the distance of CN bond from the surface. The plasmonic field

is reported to decay quickly from the surface, on the length scale of a few nanometers.<sup>69,70</sup> Another source of uncertainty is the orientation of the CN bond with respect to the electric field. However, it is worth noting that the calculated electric fields agree fairly well for all three probes given the heterogeneous surface examined in these experiments. As mentioned above, the heterogeneous nanostructure may result in differences between the SERS enhancement, related to the AC optical field, and the observed Stark Shift, which we attribute to the rectified field.

A more fundamental source of uncertainty involves how  $\chi^{(2)}$  is determined. In the methods above,  $\chi^{(2)}$  is determined from an experimental measurement of  $\chi^{(3)}$ . With planar Ag substrates, the enhancement of second order processes involves both an increase in the susceptibility associated with the plasmon resonance of the nanostructure but also enhanced local fields arising from exciting this LSPR. Similarly, the  $\chi^{(3)}$  values measured from Ag nanoparticles determine  $\chi^{(3)}$  from the response and the incident electric fields. Again, local field enhancements associated with excited LSPRs are convoluted into the response. This suggests the methods we have used to determine  $\chi^{(2)}$  underestimate the fields giving rise to the optically rectified field. A more accurate value for  $\chi^{(2)}$  would clearly clarify possible discrepancies.

## Conclusions

Vibrational Stark shifts in nitriles are shown to correlate with the electric field present on plasmonically excited structures, thus providing a direct indicator of the enhanced electric field's magnitude. Optical rectification gives rise to a DC field that perturbs the CN stretch frequency. This optical rectification also arises from the optically enhanced field and thus can be used to determine electric field enhancements associated with plasmons. Mercaptobenzonitrile was shown to be an advantageous probe of electric field strength for several reasons. First, sulfur-metal bonding makes it straightforward to assemble the probe on many plasmonic surfaces in contrast to  $\text{CN}^-$ , which requires electrochemical deposition. The *p*-mercaptobenzonitrile appears to adsorb in a more uniform fashion, which is evidenced by a narrower FWHM for the CN stretch. As shown above, the CN stretch mode for adsorbed  $\text{CN}^-$  exhibited a FWHM of  $\sim 55 \text{ cm}^{-1}$ , while FWHM associated with *p*-mercaptobenzonitrile probe was approximately  $20 \text{ cm}^{-1}$ . By physically separating the nitrile bond from the metal surface, a more reliable Stark tuning coefficients can be determined. The rigid linker provided by the phenyl ring maintains the CN group in a consistent orientation with respect to the surface, which results in a spectrum with a clear nitrile stretch, unlike *n*-mercaptobutylnitrile's spectrum that is obscured by multiple spectroscopic features. Additionally, the higher Stark tuning coefficient of *p*-mercaptobenzonitrile relative to *n*-mercaptobutylnitrile means larger frequency shifts are observed from small changes in the electric field. The results with Au nanoparticles further demonstrate that this probe can be used on different metals and provides a measurement of the electric field strength associated with plasmonic excitation.





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