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Introduction

As one of the minor actinides (neptunium, americium, and curium) in spent nuclear fuel (SNF),¹⁻³ neptunium (Np) is considered to be one of the major issues in nuclear waste management owing to its high radioactivity and long half-lifetime. Np has an electronic configuration of $[Rn]5f^57s^2$ (or $[Rn]5f^46d^17s^2$) with multiple known oxidation states, *i.e.* III, IV, V, VI and VII, among which the most stable one in aqueous solutions is the penta-valent state,^{4,5} and predominantly exists as neptunyl cations (NpO_2^+) . The NpO_2^+ ion does not form strong complexes with the commonly used ligands and is hard to extract during spent fuel reprocessing. In the development of advanced SNF reprocessing protocols, the efficient separation of Np remains a challenge, and calls for extensive study, from

Influence of denticity and combined soft-hard strategy on the interaction of picolinic-type ligands with NpO_2^+ ⁺

Hongcai Ling,^{ab} Miaoren Xia,^b Wenkai Chen,^{*ac} Zhifang Chai^{bd} and Donggi Wang^{*b}

The interaction of neptunyl ions (NpO₂⁺) with three picolinic type ligands (L), including the deprotonated picolinic acid anion (PA⁻), the deprotonated dipicolinic acid anion (DPA²⁻) and the 1,10-phenanthroline-2,9-dicarboxylic acid anion (PADA²⁻), was investigated by using a density functional theory method with various stoichiometric ratios of Np : L = 1 : 1, 1 : 2, and 1 : 3. The coordination modes, the influence of the denticity of the ligands, and the stoichiometry of the complexes were evaluated in terms of geometry, electronic structure, and thermodynamics. The calculations show that the coordination of NpO₂⁺ to tetradentate ligands is more stable than that to tridentate and bidentate ones, and the coordination ability of the three deprotonated ligands follows the order: PADA²⁻ > DPA²⁻ > PA⁻. Quantum theory of atoms-in-molecules (QTAIM) analysis, charge decomposition analysis (CDA) and natural atomic orbital (NAO) analysis were used to understand the bonding nature and electronic properties of the coordination modes and the distinct ability of the ligands in binding to neptunyl, we conclude that the denticity of the ligands and the combined hard–soft donor strategy work cooperatively in the coordination of NpO₂⁺ with ligands. This work is expected to contribute to the rational design of new types of ligand with enhanced ability to extract neptunyl.

both the experimental and theoretical sides, to shed light on the chemical behavior of Np in the condensed phase.⁶⁻¹¹

In spent nuclear fuel reprocessing using extraction techniques, extractants containing heterocyclic N donors are attractive owing to their compositions of only C, H, O and N, thus being completely incinerable to avoid secondary waste in nuclear waste treatment. The N donor ligands developed in recent years, such as bis(-triazinyl)pyridines (BTPs),^{12,13} bis(triazinyl) bipyridines (BTBPs),¹⁴⁻¹⁶ bis(triazinyl)-1,10-phenanthrolines (BTPhens),^{9,17-19} have been considered as promising extractants for minor actinides. These earlier studies mainly focused on the efficient separation of trivalent lanthanides and actinides, and neptunyl was rarely considered due to its weak extractability by organic ligands.

In recent years, Rao et al.²⁰⁻²⁶ and other groups^{27,28} conducted a series of experimental studies to evaluate the performance of ligands containing O and N in their binding with neptunyl. These cover the determination of the thermodynamic parameters (stability constants, enthalpy, and entropy) by spectrophotometry and microcalorimetry, and X-ray crystallographic studies of neptunyl complexes with dicarboxylic acids as well as the diamide derivatives, such as oxydiacetic acid (ODA), N,N-dimethyl-3-oxa-glutaramic acid (DMOGA) and, N,N,N',N'tetramethyl-3-oxa-glutaramide (TMOGA), and 1,10phenanthrolin-2,9-dicarboxylic acid (H₂PADA). In their recent work of H₂PADA, Rao et al. compared²⁵ it with picolinic acid (HPA)²⁹ and dipicolinic acid (H₂DPA),²³ and found

^aCollege of Chemistry, Fuzhou University, Fuzhou 350116, P. R. China. E-mail: qc2008@fzu.edu.cn

^bMultidisciplinary Initiative Center, Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, P. R. China. E-mail: dwang@ihep.ac.cn

^cKey Laboratory of Applied Nuclear Techniques in Geosciences Sichuan, Chengdu University of Technology, Chengdu 610059, P. R. China

^dSchool of Radiation Medicine and Interdisciplinary Sciences (RAD-X), Soochow University, Suzhou 215123, P. R. China

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that the complexation of neptunyl ions with the tetradentate H_2PADA ligand is much stronger than with other ligands (HPA and H_2DPA), and proposed that it could be an excellent extractant in the separation of neptunyl ions. Note that, both H_2DPA and H_2PADA , comparing to some other κ^3 and κ^4 chelating ligands, have preorganized planar structures with their donor atoms, *i.e.* O and N, aligned on the same side to prepare for the coordination with neptunyl in the equatorial plane, thus save the energy cost that may be needed for the ligands with backbone dihedral freedoms.³⁰

In earlier work, we have reported B3LYP studies on the coordination chemistry and thermodynamics of neptunyl with the ligands of N, N, N', N'-tetramethyl-3-oxa-glutaramide (TMOGA), N,N-dimethyl-3-oxa-glutaramic acid (DMOGA), deprotonated oxydiacetic analog (ODA), and BTPs, BTBPs, BTPhens.9,31 which show that the denticity of the chelating ligands is key to their interaction with neptunyl. In this work, we extend our study and aim to understand the influence of denticity of ligands and the importance to consider the combined soft-hard donor strategy in developing new types of ligands to extract actinides. For this purpose, we investigated the complexation behavior of NpO₂⁺ with H₂PADA and its two picolinic derivatives by using density functional theory method. The geometries of the complexes have been optimized, and the free energy change of ligand exchange processes have been calculated and analyzed to find the most probable coordination modes of each ligands. To understand the coordination modes and bonding nature of NpO2⁺ with these ligands, the quantum theory of atoms-in-molecules (QTAIM) topological analysis, charge decomposition analysis (CDA), and natural atomic orbital (NAO) analysis were carried to reveal the feature of the metal-ligand dative bonds. The results were compared to the experimental data to show that the computational work may complement experimental studies by providing molecular level of details.

Methods

The ligands in experimental studies,²⁵ HPA, H_2DPA , and H_2PADA , as shown in Scheme 1, were used as the prototype models to investigate the complexation of neptunyl ion (NpO₂⁺) with the deprotonated picolinic acid anion (PA⁻), the



Scheme 1 Schematic elucidation of the three ligands discussed in this paper.

All geometry optimization and frequency calculations were carried out by using the B3LYP functional³²⁻³⁴ as implemented in the Gaussian 09 program.35 Frequency analysis was done for all of the optimized stationary points to identify their nature as minima, and to obtain the thermodynamic parameters (enthalpy (ΔH), Gibbs free energy (ΔG), and entropy (ΔS)), which were used to evaluate the thermodynamic feasibility of the binding process^{36,37} of hydrated neptunyl with the picolinic-type ligands. Two combined basis sets have been used differing in the treatment of C, H, O and N, one with the 6-31+G* (ref. 38) basis set (BS1), which was used for geometry optimization and frequency calculations, and another one with the larger basis set 6-311++G(d,p) (BS2) to refine energies.³⁹⁻⁴¹ In both basis sets, the Np atom was treated by a small-core quasi-relativistic effective core potentials (5f-in-valence RECPs) for the 60 core electrons, and the corresponding valence basis set adopted contraction scheme of (14s13p10d8f6g)/[10s9p5d4f3g] а (ECP60MWB basis)⁴²⁻⁴⁴ to describe the valence shells.

The solvent effect of water was taken into account with the polarizable continuum model (PCM).^{45,46} GaussView 5.0 program⁴⁷ was used for visualization of structures and molecular orbitals. The Multiwfn 3.2 program⁴⁸ was used to carry out the quantum theory of atoms-in-molecules (QTAIM)^{49–52} topological analysis to understand the coordination modes and bonding nature of complexes⁵³ described by five parameters at the (3, -1) bond critical point (BCP), *i.e.* the electron density at BCP (ρ_b), the Laplacian of electron density at BCP ($\nabla^2 \rho_b$), the total energy density at BCP (H_b), the delocalization index ($\delta(A,B)$), and the bond ellipticity (ε). Charge decomposition analysis (CDA) and natural atomic orbital (NAO) analysis were also done to evaluate the ionic interaction in complex formation and the covalency of the metal-ligand dative bond.

Results and discussion

A. Geometries and relative energies

As shown in Scheme 1, the three ligands differ in their denticities when coordinating to metal ions, which are 2, 3, and 4 for PA⁻, DPA²⁻ and PADA²⁻, respectively. As all of the three ligands may interact with neptunyl with their carboxyl groups, it is also possible for them to coordinate with neptunyl in a η^1 (with one of the two O^{carb} atoms) or κ^2 (with both O^{carb} atoms) manner. Thus, in this work, we have done an exhaustive search of coordination modes that the neptunyl-ligand complexes may take. In these complexes, a coordination number (C.N.) of neptunyl in its equatorial plane as 5 or 6 is retained, and the excess coordination sites may be occupied by additional same ligand, either in the identical or distinct coordination modes, or water molecules. This results in 17, 10, and 4 possible complexes for PA⁻, DPA²⁻ and PADA²⁻, respectively. The representative stationary points with the lowest energy in each set of stoichiometric ratio from the calculations in the aqueous phase are shown in Fig. 1, and the rest complexes are collected in the ESI.†



Fig. 1 Representative conformations of the complexes obtained at the B3LYP level in the aqueous phase. (P1C: $[NpO_2(PA)(H_2O)_3]_C$, P1N: $[NpO_2(PA)(H_2O)_3]_N$, P2CN: $[NpO_2(PA)_2(H_2O)]^-_C_N$, P2NN: $[NpO_2(PA)_2(H_2O)]^-_N_N$, P3CNN: $[NpO_2(PA)_3]^2^-_C_N_N$, P3NNN: $[NpO_2(PA)_3]^2^-_N_N_N$, D1N: $[NpO_2(\kappa^3-DPA)(H_2O)_2]^-_N$, D2CN: $[NpO_2(\kappa^3-DPA)(\kappa^2-DPA)]^3^-_C_N$, D2NN: $[NpO_2(\kappa^3-DPA)_2]^3^-_N_N$, H1W1: $[NpO_2(\kappa^4-PADA)(H_2O)_2]^-_N$.

As a bidentate ligand, PA⁻ may coordinate with neptunyl either in the manner of end-on with its carboxyl group (denoted as _C) or side-on with its N and one O^{1A} of the carboxyl group (denoted as _N). In Fig. 1, six complexes of neptunyl-PA⁻ are shown, differing in the coordination mode and the stoichiometric ratio, which is up to $Np : PA^- = 1 : 3$ with Np atom remaining penta- or hex-coordinated in its equatorial plane. In addition, in Fig. 1, three complexes of DPA²⁻, with one, two and two DPA^{2-} in the complex, respectively, and two of $PADA^{2-}$ are also shown. In the complexes with $Np: DPA^{2-} = 1:2$, one DPA²⁻ appears as a tridentate ligand, and another one may coordinate with Np either in κ^2 (D2CN) or κ^3 (D2NN) manner. In the case of PADA²⁻, as the ligand binds with Np in κ^4 manner, and constitutes substantial steric hindrance to prevent the coappearance of additional PADA²⁻, here we only considered the stoichiometric ratio of Np : $DAPA^{2-} = 1:1$ (H1W1 and

H2W2, differing in the presence of one or two water molecules respectively).

The averaged bond lengths d (Å) of Np–O^{vl}, Np–N^{py}, Np–O^{carb}, and Np–O^{wat} bonds were summarized in Table 1 and ESI.[†] In bare neptunyl, the Np–O^{vl} bond distance is calculated to be 1.737 and 1.781 Å in gas phase and in aqueous phase, respectively. This value increase to 1.780 and 1.794 Å in its pentahydrated form (**N1** in Table 1), which suggests that the coordination of water ligands to neptunyl in its equatorial plane weakens the Np–O^{vl} bonds. Upon its coordination to the three negatively charged organic ligands, the Np–O^{vl} bond is perturbed and elongated to 1.81–1.83 Å, suggesting a stronger perturbation brought by these ligands than by water.

We also note that for the dative bonds in the complexes, in general the bond length of Np–O^{carb} is about 0.1–0.2 Å shorter than that of Np–N^{py} and Np–O^{wat} bonds. This may be

	Np-O ^{yl}	Np-N ^{py}	Np-O ^{carb}	Np-O ^{wat}		Np-O ^{yl}	Np-N ^{py}	Np-O ^{carb}	Np-O ^{wat}
N1 ^a	1.794	_	_	2.555	P1C	1.802	_	2.555	2.597
D1N	1.812	2.593	2.487	2.658	P1N	1.804	2.644	2.444	2.574
D2CN	1.823	2.594	2.524	_	P2CN	1.821	2.662	2.542	2.686
D2NN	1.824	2.786	2.581		P2NN	1.814	2.667	2.458	2.686
H1W1	1.823	2.621	2.480	2.603	P3CNN	1.827	2.917	2.578	_
H1W2	1.812	2.690	2.524	2.714	P3NNN	1.821	3.006	2.454	_

^{*a*} **N1**: $[NpO_2(H_2O)_5]^+$.

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determined by the stronger electrostatic interaction between Np and O^{carb} than between Np and the other two types of coordinating atoms.

In aqueous phase, neptunyl exists in its hydrated form with five water molecules bound in the first coordination shell. Starting from $[NpO_2(H_2O)_5]^+$, the thermodynamics of the formation of the above-mentioned complexes was evaluated *via* ligand exchange process to replace the water ligands by corresponding organic ligands. The data are collected in Table 2.^{23,25,29}

In Table 2, the eqn (1) to (6) were used to calculate the thermodynamics for the formation of the neptunyl-PAcomplexes with the stoichiometric ratio of Np: L varies from 1:1 to 1:2 to 1:3. It can be seen that the NpL₂ (P2CN and P2NN) complexes is thermodynamically more stable than NpL (P1C and P1N) and comparable with NpL₃ (P3CNN and P3NNN) both in the gas phase (data in ESI[†]) and in water, suggesting that neptunyl has stronger affinity to PA⁻ than to water ligand, but with an optimal stoichiometric ratio of 1:2. Regarding to the coordination mode, with one PA⁻ bound, neptunyl favors the _N mode to benefit from both the excess negative charge of the carboxyl group (P1C: C-O^{1A} = 1.269 Å, C-O^{1B} = 1.273 Å vs. **P1N:** $C-O^{1A} = 1.286$ Å, $C-O^{1B} = 1.242$ Å) and pyridine N atom which is relatively "softer" than the carbonyl O^{1B} atom according to Pierson's Hard-Soft-Acid-Base (HSAB) principle.54,55 This rule holds with one or two more PA⁻ bound, and neptunyl does not favor to bind with all of the PA⁻ ligands in the _N mode, but rather with one PA⁻ in the _C mode and the rest in the _N mode.

The DPA²⁻ ligand behaves similarly to PA⁻, and in the 1 : 1 complex, it binds with neptunyl in the κ^3 (_N) mode rather than the κ^2 (_C) mode. The presence of one more DPA²⁻ ligand brings additional stabilization energy to the complexes, with the κ^3 mode (-53.32 kcal mol⁻¹) moderately more favorable than the κ^2 mode (-51.41 kcal mol⁻¹).

The PADA²⁻ ligand displays exceptional binding affinity to neptunyl and the substitution of four water ligands by one PADA²⁻ is calculated to be exothermic by 55.10 kcal mol⁻¹. This suggests that at the same stoichiometric ratio, PADA²⁻ is superior over the other two ligands toward to the coordination with neptunyl. This trend is consistent with the experimental observations^{23,25,29} as shown in Table 2.

In summary, the thermodynamic stability of the complexes of NpO₂⁺ with the three pyridine-based carboxylate ligands follow the order: PADA²⁻ ($-55.1 \text{ kcal mol}^{-1}$) > DPA²⁻ ($-53.32 \text{ kcal mol}^{-1}$) > PA⁻ ($-41.24 \text{ kcal mol}^{-1}$) in the aqueous phase, suggesting that the phenanthroline-based tetradentate ligand (PADA²⁻) has the best binding affinity with neptunyl than the other two ligands. The calculations also show that the binding mode with combined "hard–soft" donors brings more stabilization energy to the complexes than that with only "hard" donors. The former binding mode gains enthalpy without the loss of entropic contribution. This is reasonable concerning that the carboxylate group builds stronger hydrogen bonding with water solvent than the N^{Py} does, thus the _C binding mode requires more energy to reorganize solvent environment than the _N mode does.

Table 2 The thermodynamics (kcal mol⁻¹) of selected ligand exchange reactions towards the formation of the NpO₂⁺ complexes with the three ligands at 298.15 K in the aqueous phase

	Aqueous		Exp.	Exp.			
Complexation reactions	ΔG	ΔH	$T\Delta S$	ΔG	ΔH	$T\Delta S$	
(1) $\left[\operatorname{NpO}_2(\operatorname{H}_2\operatorname{O})_5\right]^+ + \operatorname{PA}^- \rightarrow \operatorname{P1C} + 2\operatorname{H}_2\operatorname{O}$	-16.09	-7.54	8.55		_	_	
(2) $[NpO_2(H_2O)_5]^+ + PA^- \rightarrow P1N + 2H_2O$	-20.75	-11.6	4 9.12	-4.90^{a}	-0.72^{a}	4.18^{a}	
(3) $[NpO_2(H_2O)_5]^+ + 2PA^- \rightarrow P2CN + 4H_2O$	-41.24	-25.2	4 16.00	-8.91^{a}	—	—	
(4) $[NpO_2(H_2O)_5]^+ + 2PA^- \rightarrow P2NN + 4H_2O$	-36.78	-21.5	8 15.20	—	—	—	
(5) $[NpO_2(H_2O)_5]^+ + 3PA^- \rightarrow P3CNN + 5H_2O$	-41.03	-23.9	7 17.07	—	—	—	
(6) $[NpO_2(H_2O)_5]^+ + 3PA^- \rightarrow P3NNN + 5H_2O$	-30.91	-17.1	2 13.79	—	—	—	
$(7) \left[NpO_2(H_2O)_5 \right]^+ + DPA^{2-} \rightarrow D1N + 3H_2O$	-40.71	-24.3	7 16.33	-11.85^{b}	-6.02^{b}	5.83 ^b	
(8) $\left[\operatorname{NpO}_{2}(\operatorname{H}_{2}\operatorname{O})_{5}\right]^{+} + 2\operatorname{DPA}^{2-} \rightarrow \mathbf{D2NN} + 5\operatorname{H}_{2}\operatorname{O}$	-53.32	-27.5	5 25.78	-16.75^{b}	-10.99^{b}	5.76 ^b	
(9) $\left[\operatorname{NpO}_2(\operatorname{H}_2\operatorname{O})_5\right]^+ + 2\operatorname{DPA}^{2-} \rightarrow \mathbf{D2CN} + 5\operatorname{H}_2\operatorname{O}$	-51.41	-24.1	1 27.30	_	_	—	
(10) [NpO ₂ (H ₂ O) ₅] ⁺ + PADA ²⁻ \rightarrow H1W1 + 4H ₂ O	-55.10	-32.1	1 23.00	-15.99^{c}	-6.86^{c}	9.13 ^{<i>c</i>}	
$(11)^{"}[NpO_2(H_2O)_5]^+ + PADA^{2-} \rightarrow H1W2 + 3H_2O$	-39.27	-27.4	5 11.80	_	_	—	
(12) $[NpO_2(H_2O)_5]^+ + H_2O \rightarrow [NpO_2(H_2O)_6]^+$	4.47	-4.48	-8.95	—	—	—	

^a Data from ref. 29. ^b Data from ref. 23. ^c Data from ref. 25.

QTAIM topological analysis В.

The quantum theory of atoms-in-molecules (QTAIM) topological analysis of Bader^{49,52} and Matta and Boyd⁵⁶ et al. were used to understand the bonding nature and electronic properties of the complexes. Five descriptors in the framework of AIM, *i.e.* the density $\rho_{\rm b}$ at the (3, -1) bond critical point (BCP), the Laplacian of electron density at BCP ($\nabla^2 \rho_b$), the total energy density at BCP

($H_{\rm b}$), the delocalization index ($\delta(A,B)$), and the bond ellipticity (ε) , were used to characterize the interactions between Np and ligands. The values of these descriptors are tabulated in Table 3 and ESI.†

In a bare neptunyl ion (N0), for the Np– O^{yl} bond, the electron density $\rho_{\rm b}$, the Laplacian of electron density ($\nabla^2 \rho_{\rm b}$), and the total energy density (H_b) at the (3, -1) bond critical point (BCP) were

Table 3 Electron density $\rho_{\rm b}$ (e bohr⁻³) and its Laplacian $\nabla^2 \rho_{\rm b}$ (e bohr⁻⁵), the energy density $H_{\rm b}$ (a.u.) at the bond critical point, and the averaged delocalization indices $\bar{\delta}$ (a.u.) and averaged bond ellipticity $\bar{\epsilon}$ (a.u.) of the Np–O^{yl}, Np–N^{py}, Np–O^{carb}, and Np–O^{water} bonds of the complexes obtained from QTAIM analysis (N0: NpO₂⁺, N1: [NpO₂(H₂O)₅]⁺)

	$\rho_{\rm b}$	$ abla^2 ho_{ m b}$	$H_{\rm b}$	$ar{\delta}$	$\overline{\varepsilon}$	$ ho_{ m b}$	$ abla^2 ho_{ m b}$	$H_{\rm b}$	$ar{\delta}$	$\overline{\varepsilon}$
	Np-O ^{yl}			Np-N ^{py}						
NO	0.294	0.179	-0.269	2.860	0.000	_	_	_	_	_
N1	0.283	0.215	-0.249	2.823	0.000	_	_	_	_	
P1C	0.278	0.223	-0.239	2.810	0.001	_	_	_	_	
P1N	0.276	0.229	-0.236	2.808	0.002	0.042	0.131	-0.001	0.869	0.392
P2CN	0.266	0.247	-0.218	2.792	0.004	0.040	0.126	-0.001	0.851	0.390
P2NN	0.270	0.242	-0.225	2.794	0.004	0.039	0.126	-0.001	0.846	0.392
P3CNN	0.261	0.256	-0.209	2.782	0.001	0.023	0.070	0.000	0.683	0.265
P3NNN	0.264	0.249	-0.215	2.784	0.000	0.019	0.058	0.001	0.624	0.192
D1N	0.271	0.237	-0.227	2.795	0.002	0.046	0.149	-0.001	0.891	0.375
D2CN	0.265	0.273	-0.215	2.777	0.005	0.045	0.158	-0.001	0.875	0.132
D2NN	0.262	0.253	-0.212	2.779	0.001	0.030	0.096	0.001	0.747	0.299
H1W1	0.266	0.264	-0.216	2.789	0.004	0.043	0.145	-0.001	0.867	0.226
H1W2	0.270	0.239	-0.226	2.796	0.002	0.037	0.120	0.000	0.822	0.361
	Np-O ^{carb}			Np-O ^{water}						
NO	_	_	_	_	_	_	_	_	_	
N1	_	_	_	_	_	0.041	0.164	0.001	0.864	0.220
P1C	0.044	0.158	0.001	0.918	0.357	0.037	0.146	0.001	0.827	0.305
P1N	0.054	0.214	-0.001	1.073	0.363	0.039	0.157	0.001	0.848	0.249
P2CN	0.046	0.168	0.001	0.973	0.332	0.031	0.115	0.001	0.741	0.327
P2NN	0.053	0.208	-0.001	1.070	0.345	0.032	0.115	0.000	0.732	0.337
P3CNN	0.041	0.155	0.001, -0.001	0.952	0.304		_	_		_
P3NNN	0.051	0.209	0.001	1.084	0.292	_	_	_	_	
D1N	0.049	0.192	-0.000	1.019	0.343	0.034	0.123	0.001	0.751	0.345
D2CN	0.047	0.180	-0.001	1.003	0.069	_	_	_	_	_
D2NN	0.039	0.148	0.001	0.952	0.331	_	_	_		_
H1W1	0.050	0.199	-0.000	1.078	0.289	0.037	0.147	0.001	0.839	0.151
H1W2	0.045	0.175	0.000	0.977	0.334	0.030	0.106	-0.000	0.690	0.355



Fig. 2 The bond length d (Å), and the electron density $\rho_{\rm b}$ (e⁻ bohr⁻³) at BCP of Np–O^{yl} bond in complexes from calculations in the aqueous phase. The values of NpO₂⁺ in its hydrated and bare forms are also shown for comparison (bare: NpO₂⁺, water: [NpO₂(H₂O)₅]⁺, PA[n(L) = 1]: P1N, PA[n(L) = 2]: P2CN, PA[n(L) = 3]: P3CNN, DPA[n(L) = 1]: D1N, DPA[n(L) = 2]: D2NN, PADA[n(L) = 1]: H1W1).

[0.335, 0.120, -0.347] and [0.294, 0.179, -0.269] respectively in the gas phase and in the aqueous phase, $\rho_{\rm b} > 0.20$, $\nabla^2 \rho_{\rm b} > 0$, $H_{\rm b} <$ 0. According to Matta and Boyd,⁵⁶ a $\rho_{\rm b}$ greater than 0.20 e bohr⁻³, a positive $\nabla^2 \rho_{\rm b}$, and a negative $H_{\rm b}$ are the feature of a shared bond. This means that the interactions between Np and O^{yl} has strong covalent feature.

In contrast, the interaction between Np and the coordinating atoms, both for the $O^{\rm carb}$ and $N^{py},$ displays predominant ionic



Fig. 3 Electron density $\rho_{\rm b}$ (e⁻ bohr⁻³) and bond length d (Å, in parenthesis) of NpO₂⁺ complexes from calculations in aqueous phase.

feature. For these dative bonds, the electronic density ρ_b is close to 0, $\nabla^2 \rho_b$ is positive, and $H_b \approx 0$, indicating a depleted nature.

The $\delta(A,B)$ and ε provides consistent results for the nature of the Np–O^{yl} and the coordination bonds. In the bare neptunyl ion, the delocalization index ($\delta(A,B)$) and the bond ellipticity (ε) were calculated to be 2.970 and 0.002 in the gas phase and 2.860 and 0.000 in the aqueous phase, respectively, which suggests a triple bond feature for the Np–O^{yl} bond and is consistent with previous work.³¹ The explicit consideration of water ligands in the first coordination shell of neptunyl ([NpO₂(H₂O)₅]⁺, **N1**) caused a marginal decrease of $\delta(A,B)$ of Np–O^{yl} bonds of about 0.04, suggesting a weakening of the Np–O^{yl}, while this does not change its triple bond feature.

Upon its coordination with the organic ligands studied here, the $\delta(Np, O^{yl})$ decreases further by 0.01–0.04 with a slight increase of the bond ellipticity (ε), indicating a stronger perturbation of the organic ligands to the bond nature of Np–O^{yl} than the water ligands.

For the dative bonds of the complexes, *i.e.* Np–N^{py}, Np–O^{carb}, and Np–O^{water}, the delocalization indices ($\delta(A,B)$) are in the range of 0.62–1.08, and the bond ellipticity (ε) values are in the range of 0.06–0.39. Among the dative bonds, the Np–O^{carb} bonds appear with the largest $\delta(A,B)$, and for the same coordination mode, the more ligands coordinated to Np, the lower the $\delta(A,B)$ value (P1C and P1N *vs.* P2CN and P2NN *vs.* P3CNN and P3NNN, D1N *vs.* D2CN and D2NN, H1W1 *vs.* H1W2), indicating the saturation in the coordination of neptunyl and the competition of the ligands in interacting with neptunyl.

In Fig. 2, the distance and the ρ_b at BCP of Np–O^{yl} bond as a function of the type of ligand are plotted. As seen in Fig. 2, the bond length *d* increase from 1.781 Å to 1.823 Å, and the electron density ρ_b decrease from 0.294 e bohr⁻³ to 0.266 e bohr⁻³ at BCP of Np–O^{yl} bond in NpO₂L_n (L = H₂O, PA⁻, DPA²⁻, PADA²⁻, n(L) = 0, 1) complexes in the aqueous phase, which indicates enhanced perturbation on the strength of Np–O^{yl} bond by the coordination of the organic ligands in the complexes with the same stoichiometric ratio M : L = 1 : 1, suggesting the binding affinity of neptunyl to the ligands decreases in the order: PADA²⁻ > DPA²⁻ > PA⁻ > H₂O. The higher presence of the ligands brings more perturbation to the Np–O^{yl} bond.

In Fig. 3, the electron density in the equatorial plane transverse to the axis of neptunyl through Np is shown for the representative complexes complexes $(NpO_2L_n(H_2O)_m)^j$ (L = PA⁻, DPA²⁻, and PADA²⁻, n = 0-3, m = 0-3, 5, j = 1+, 0, 1-, 2-, 3-), and the bond lengths of the dative bonds in the plane are also given. The data of Np–O^{yl} for the bare neptunyl are also shown. In these complexes, the ρ_b of Np–N bond is always smaller than that of Np–O^{carb}, suggesting a larger accumulation of electron density of the latter than the former. This is consistent with their delocalization indices collected in Table 3.

C. Charge transfer in the complexes

The charge decomposition analysis (CDA) proposed by Dapprich and Frenking,^{57,58} and the extended charge decomposition analysis (ECDA) by Gorelsky^{59,60} are used to calculate charge transfer between neptunyl and the ligands upon the ligand exchange. In CDA, the overall reorganization of electronic density is calculated which includes both the contributions of charge transfer (CT) and electronic polarization (PL). These are separated in ECDA, and the transferred charge can be directly obtained as $CT(A \rightarrow B) - CT(B \rightarrow A) = [PL(A) + CT(A \rightarrow B)] - [PL(A) + CT(B \rightarrow A)].$

Here we consider the net charge transfer from the ligands to neptunyl in selected complexes by the CDA and ECDA methods at the B3LYP level, and the data are tabulated in Table 4. For Np : L = 1 : 1 type complexes, the net charge transfer from the ligands to neptunyl decreases in the order of PADA²⁻ > DPA²⁻ > PA⁻ > H₂O (in the range of 0.610–0.648, 0.594–0.615, 0.585– 0.591, 0.573, and 0.900–0.999, 0.880–0.941, 0.871–0.878, 0.816, obtained by CDA and ECDA, respectively). This coincides the sequence of the relative stabilities, which suggests that the ligand-to-metal-charge-transfer (LMCT) plays an important role in the higher binding affinity of PADA²⁻ and DPA²⁻ than that of PA⁻ and H₂O.

We note that the charge transfer is also correlated to the coordination mode. According to ECDA results, for each pair of isomers, *e.g.* **P2CN** *vs.* **P2NN**, **P3CNN** *vs.* **P3NNN**, and **D2CN** *vs.* **D2CN**, the co-presence of the _C and the _N coordination modes causes more charge transfer from ligands to neptunyl. In the complexes with a single organic ligands, *i.e.* **P1C** *vs.* **P1N**, **D1C** *vs.* **D1N**, and **H1C** *vs.* H1N, the latter appears with more charge transfer than the former. These results suggest that the combined hard–soft strategy, *i.e.* the harder O^{carb} and the softer N^{py}, favors to stabilize the complexes with stronger electrostatic interaction between neptunyl and the ligands compared to the other coordination modes. This offers theoretical supports on the combined hard–soft strategy to develop extractants with higher selectivity towards the actinides.^{19,61,62}

D. Molecular orbital (MO) and NAO analysis

The natural atomic orbital (NAO)⁶³ was analyzed to understand the bonding of NpO_2^+ with ligands, and the representative α -spin frontier orbitals of **P1C**, **P1N**, **D1N** and **H1W1** are shown

Table 4 Charge transfer (e⁻) in the complexes from the ligands to NpO₂⁺ by the CDA and ECDA methods calculated at the B3LYP level

Complexes	Charge transfer	CDA	ECDA
$(N1) [NpO_2(H_2O)_5]^+$	$5H_2O \rightarrow NpO_2^+$	0.5734	0.8157
$(P1C) [NpO_2 (PA)(H_2O)_3]_C$	$L + 3H_2O \rightarrow NpO_2^+$	0.5908	0.8713
$(P1N) [NpO_2 (PA)(H_2O)_3]_N$	$L + 3H_2O \rightarrow NpO_2^+$	0.5852	0.8780
$(P2CN) [NpO_2(PA)_2(H_2O)]^- C_N$	$2L + H_2O \rightarrow NpO_2^+$	0.6542	0.9885
$(P2NN) [NpO_2(PA)_2(H_2O)]^N_N$	$2L + H_2O \rightarrow NpO_2^+$	0.6315	0.9681
$(P3CNN) [NpO_2(PA)_3]^{2-} C_N_N$	$3L \rightarrow NpO_2^+$	0.7408	1.1201
$(P3NNN) [NpO_2(PA)_3]^{2-}N_N_N$	$3L \rightarrow NpO_2^+$	0.6970	1.0751
$(D1C) [NpO_2(DPA)(H_2O)_3]^-C$	$L + 3H_2O \rightarrow NpO_2^+$	0.5942	0.8799
$(D1N) [NpO_2(DPA)(H_2O)_2]^-N$	$L + 2H_2O \rightarrow NpO_2^+$	0.6152	0.9411
$(D2CN) [NpO_2(DPA)_2]^{3-}C_N$	$2L \rightarrow NpO_2^+$	0.7429	1.1310
$(D2NN) [NpO_2(DPA)_2]^{3-} N_N$	$2L \rightarrow NpO_2^+$	0.7897	1.2131
$(H1C) [NpO_2(PADA)(H_2O)_3]^-C$	$L + 3H_2O \rightarrow NpO_2^+$	0.6097	0.8996
$(H1W1) [NpO_2(PADA)(H_2O)]^-N$	$L + H_2O \rightarrow NpO_2^+$	0.6211	0.9770
(H1W2) $[NpO_2(PADA)(H_2O)_2]^N$	$L + 2H_2O \rightarrow NpO_2^+$	0.6483	0.9987



Fig. 4 Representative α -spin frontier orbitals of NpO₂⁺ complexes. The isosurface value of MO is 0.02 a.u.

in Fig. 4 and their compositions are tabulated in Table 5. These MOs are mainly contributed by the 2p atomic orbital of the O/N atoms and 5f or 6d atomic orbital of neptunium.

As shown in Fig. 4, for all of the four complexes, the two singly occupied molecular orbitals (SOMO) are contributed by the Np and the O^{yl} atoms, which is consistent with the observations that the unpaired electrons are localized within the

P1C	HOMO-2		HOMO-	3	HOMO-4		HOMO-5		HOMO-9	
Np	4.1		30.2		23.0		9.2		9.3	
5f/6d O ^{1A} /O ^{1B}	$5f_{y(3x^2-y^2)}$: 1.6 O ^{1B} : 7.0 (2p _x), 17.7 (2p _y) O ^{1A} : 30.1 (2p _x), 25.8 (2p _y)		O^{1B} : 13.9 (2p _z)		$5f_{z^{3}}$: 18.1, $5f_{xyz}$: 1.3 O ^{1B} : 22.3 (2p _z) O ^{1A} : 25.7 (2p _z)		$5f_{xz^2}$: 3.9 O ^{1B} : 29.3 (2p _x), 2.7 (2p _y) O ^{1A} : 11.9 (2p _x)		$6d_{yz}$: 8.8 O^{1B} : 1.8 $(2p_z)$ O^{1A} : 1.9 $(2p_z)$	
P1N	HOMO-1 HOMO-4		HOMO-6			HOMO-8			HOMO-10	
Np 5f/6d N ¹ /O ^{1A}	$5f/6d$ $5f_{z^3}$: 4.5 $5f_{z^3}$: 32.8		11.0 $5f_{z^3}$: 1.0, $5f_{xz^2}$: 2.9, $5f_{yz^2}$: 1.4 N ¹ : 26.4 (2p _x), 4.6 (2p _z), O ^{1A} : 1			21.4 $5f_{xz^2}$: 15.6, $5f_{yz^2}$: 3.3 1.4 (2p _y) N ¹ : 1.6 (2s), 16.2 (2p _x)			13.9 6d _{xz} : 11.3, 6d _{yz} : 2.2 N ¹ : 1.2 (2p _z)	
D1N	НОМО-2 НОМО-5		HOMO-8			HOMO-11		HOMO-12		
Np 5f/6d	18.8 5.5 $5f_{z'}$: 14.6 $5f_{yz^2}$: 1.3, $6d_{xy}$: 1.		$\begin{array}{c} 23.9\\ 4 \qquad 5f_{xz^2}: 21.2 \end{array}$			5.8 $5f_{xz^2}$: 1.4, $5f_{x(x^2-3y^2)}$: 1.3, $6d_{x^2y^2}$: 1.6		10.8 6d _{yz} : 9.8		
N ¹ /O ^{2A} /O ^{1A}	$O^{1A} = O^{2A}$: 16.2 (2p _z), O^{2A} : 2.1 (2p _x), 29. O^{1A} : 16.2 (2p _z) O^{1A} : 2.1 (2p _x), 29.				$O^{2A}: 2.5 (2p_y),$			N ¹ : 0.9 (2p _x), O ^{2A} : 1.8 (2p _z) O ^{1A} : 1.8 (2p _z)		
H1W1	HOMO-4	I	HOMO-8	HOM	IO-12	H	IOMO-14	Н	OMO-17	
Np 5f/6d N ¹ /N ² /O ^{2A} /O	$\begin{array}{c} 19.4 \\ 5f_{z^3}: 13.5, \\ 0^{2A}: 15.9 \\ 0^{1A} \\ 0^{1A}: 17.3 \end{array}$	$5f_{z(x^2-y^2)}: 2.5$ (2p _z), (2p _z	36.2 $5f_{z^3}$: 29.8 D^{2A} : 6.3 (2p D^{1A} : 6.5 (2p	v_z), $N^2 : 5$	1.6, 6d _{xz} : 2.7 .7 (2p _x), 4.8 (2p _y). .4 (2p _x), 2.5 (2p _y)	5), N .) 2	.55 $f_{y(3x^2-y^2)}$: 2.0, $6d_{xy}$: 2.3 t^2 : 13.3 (2p _x), 6.1 (2p _y), .2 (2p _z), N ¹ : 16.4 (2p _x), .1 (2p _y), 2.7 (2p _z)	N	3 d ₂ : 1.0 : 4.8 (2p _x), 4.4 (2p _y), 1: 6.0 (2p _x), 3.2 (2p _y)	

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neptunyl moiety indicated by the spin density distribution. For the orbitals that constituted from both the neptunyl and the ligands, it is shown that from **P1C** to **P1N** to **D1N** and **H1W1**, there is increasing orbital overlap from these fragments, suggesting stronger ionic feature in **P1C** while more covalency in the other complexes. This indicates that the excess stabilization brought by _N coordination mode (**P1N**, **D1N**, and **H1W1**), compared to the _C mode (**P1C**), may be contributed by the enhanced covalent interaction between the neptunyl and the ligands.

As listed in Table 5, the compositions of the representative orbitals display localized feature, *i.e.* the major contribution comes from the Np and the ligand atoms coordinated to Np. For the complex **P1C**, some frontier MOs contains significant contributions from the two O^{carb} atoms of the same carboxylate group. It is conceivable that this perturbs the delocalization feature of electrons in the carboxylate group. In the other complexes, the N atoms and one O^{carb} atom of each carboxylate group have noticeable contributions. This avoids significant perturbation to the ligands and maintains the aromaticity of the hetero-rings and the local electronic feature of the carboxylate groups of the ligands.

E. Comparison with the experimental work

In Rao *et al.*'s work,²⁵ the trends in the protonation constants of H_2PADA and related ligands and the thermodynamic data for

Np^V complexes with three ligands were discussed. The first protonation constants of the ligands were observed to decrease in the order: HPA > H₂DPA > H₂PADA. This trend was explained by the intramolecular hydrogen bonding between the carboxylate group and the nitrogen atom which became weaker along the series. Though the preparation of the crystals of the $Np^{V/}$ PADA²⁻ complex was not successful, the spectrophotometric and calorimetric data undoubtedly indicated that the 1:1 complex formed in solution and appeared to be much stronger than complexes formed by the other two ligands. This is reasonable concerning the increase in denticity from HPA to H_2 DPA and H_2 PADA that stabilizes the Np^V complexes: PA⁻ < DPA^{2-} < $PADA^{2-}$. Our calculations are consistent with the experimental observations on the variation of the stability constants of the complexes in view of the relative free energies of complexation, which are tabulated in Table 2.

The calculated entropic and enthalpic contributions are plotted in Fig. 5. For Np : L = 1 : 1 type complexes, based on our calculations, their formation of relative Gibbs free energies decreased by the order: PADA²⁻ ($-55.10 \text{ kcal mol}^{-1}$) > DPA²⁻ ($-40.71 \text{ kcal mol}^{-1}$) > PA⁻ ($-20.75 \text{ kcal mol}^{-1}$) in the aqueous phase. This trend is consistent with the experimental data which report the free energy changes of $-15.99 \text{ kcal mol}^{-1}$ for PADA²⁻, $-11.85 \text{ kcal mol}^{-1}$ for DPA²⁻, and $-4.90 \text{ kcal mol}^{-1}$ for PA⁻. We note that there is substantial difference in the values between the calculated and the experimentally derived ones,



Fig. 5 Thermodynamic trends of NpO₂⁺ complexes from calculations in the aqueous phase (left) and from experiment (right).



Fig. 6 The relative electronic energies of NpO_2^+ complexes calculated using basis set BS1 and larger basis set BS2 in the gas phase and aqueous phase.

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which may be due to the treatment of the model systems in this work, *e.g.* the insufficient sampling of the model systems, the implicit treatment of solvent effect, and the omitting of the counterion effect. This makes it hard to make a direct comparison between them, and molecular dynamic simulations at first-principle level are needed which is beyond the scope of this work.

The energies were refined by using more sophisticated treatment (BS2) of the atoms where a larger basis set 6-311++G(d,p) was used for the atoms except for Np, and the results were plotted in Fig. 6. The data show that for the three ligands, when they form complexes with neptunyl with the same stoichiometric ratio, higher denticity brings more stabilization energy, *i.e.* the stability of the complexes decrease in the order of PADA²⁻ > DPA²⁻ > PA⁻. This trend is consistent with the data from the calculations at the B3LYP/BS1 level, and agrees with the reported experimental observations.

Conclusions

In the present work, we report a DFT study of the interactions between neptunyl ion (NpO_2^+) and the deprotonated 1,10-phenanthrolin-2,9-dicarboxylic acid anion $(PADA^{2-})$. Its analogs, the deprotonated picolinic acid anion (PA^-) and dipicolinic acid anion (DPA^{2-}) , were also investigated and compared. The geometries, thermodynamics of the complexation reactions, and the electronic structures of the complexes were analyzed to evaluate the coordination modes and stoichiometry ratio of neptunyl ion with ligands. The calculations indicate that the coordination of NpO_2^+ to tetradentate chelators is more favorable than that to tridentate and bidentate ones, and the coordination ability of three deprotonated ligands follows the order: $PADA^{2-} > DPA^{2-} > PA^-$.

The QTAIM analysis showed that the metal-ligand interactions have strong ionic feature. In addition to the QTAIM analysis, the charge decomposition analysis (CDA) and extended charge decomposition analysis (ECDA) were performed to quantify the charge donation and back-donation between the metal and ligand fragments in complexes. For Np : L = 1 : 1 type complexes, the net charge transfer from the ligands to neptunyl decreases in the order of PADA²⁻ > DPA²⁻ > PA⁻ > H₂O, which is in good agreement with the relative thermodynamic stabilities of the corresponding complexes. The natural atomic orbital (NAO) analysis revealed that the 5f orbitals of Np participated in the metal-ligand dative bond and contribute to its covalency.

In summary, our calculations show that the denticity of ligand and the combined hard-soft donor strategy work cooperatively in the coordination of Np with ligands, which should be taken into account in the rational design of new type of extractants for the separation of Np.

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