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# First-principles calculation of lithium insertion into homogeneous a-SiC<sub>2/5</sub>O<sub>6/5</sub> as high performance anode

Ningbo Liao, \* Beirong Zheng, Miao Zhang and Wei Xue

Amorphous silicon oxycarbide is considered as a promising anode material for new generation of lithium-ion batteries, and figuring out the lithiation mechanism is crucial for its application. In this work, first principle calculations are performed to study the atomic structures, formation energy and lithiation voltage of homogeneous SiC<sub>2/5</sub>O<sub>6/5</sub>. The interpretation of radial distribution, angular distribution and coordinate number suggests that the Si–O bond tends to break and the Li<sub>2</sub>O will form at the beginning of lithiation, then the Li<sub>x</sub>O and the Li<sub>y</sub>Si form with increasing Li concentration, which makes a major contribution to the capacity of SiC<sub>2/5</sub>O<sub>6/5</sub>. By the Li content dependence of the formation energies curve, the theoretical specific capacity of SiC<sub>2/5</sub>O<sub>6/5</sub> is predicted as 1415 mA h g<sup>−1</sup>, which is comparable to the reversible capacity of 900 mA h g<sup>−1</sup> in experiments. Both the formation energies and the voltage curves suggest lithium is preferable in incorporation with SiC<sub>2/5</sub>O<sub>6/5</sub>, and this is attributed to the formation of Li<sub>x</sub>O and Li<sub>y</sub>Si.

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## 1. Introduction

Graphite is widely used as an anode material for commercial lithium-ion batteries (LIBs), however, the low capacity (372 mA h g<sup>−1</sup>) has limited its further applications. Silicon is a promising material to replace graphite with lower cost and around 10 times the gravimetric capacity.<sup>1,2</sup> But silicon exhibits about a 300% volume expansion during cycling, which will lead to mechanical failure, poor cycling performance and irreversible capacity.<sup>3,4</sup> Therefore, research efforts are being made to search for new anode materials with high capacities and long life cycle.

Amorphous silicon oxycarbide (a-SiCO) presents a high reversible capacity (larger than 800 mA h g<sup>−1</sup>) and is a promising anode material for LIBs.<sup>5–12</sup> Amorphous SiCO ceramics generally include SiCO glass and SiCO glass with free carbon phase, corresponding to homogeneous structure and inhomogeneous structure respectively. Current experiments<sup>13</sup> suggested that both the SiCO structures have a very high first insertion capacity, the concentration of lithium residing at the mixed bonds is much greater than the concentration sequestered in the free carbon,<sup>7</sup> and the reversible capacity of these mixed bonds is severely diminished when oxygen is substituted by nitrogen.<sup>6</sup> Although the experiments provide some information on how the nano-structure influences the electrochemical properties of SiCO, the mechanism for lithium

insertion into a-SiCO is still not clearly understood. More insight needs to be gained in terms of atomistic structure and energy, which could be very challenging for current experimental technologies.

First principles calculations can obtain the atomic structure, electronic properties and lithiation characters of anode materials, and were successfully used in analyzing LIB electrodes such as Si,<sup>14</sup> SiO,<sup>15</sup> Nb<sub>2</sub>C<sup>16</sup> and graphene sheets.<sup>3</sup> In our previous studies,<sup>17,18</sup> SiCO models containing mixed-bond tetrahedron were proposed based on crystalline SiO<sub>2</sub> configuration,<sup>17</sup> the influence of tetrahedron on the performance of SiCO was studied. Moreover, in order to gain deeper insight into amorphous SiCO structure, a more realistic model was established by molecular dynamics simulation of melt-quench, and the effect of carbon segregation on performance of inhomogeneous SiCO was studied.<sup>18</sup> In this work, the performance of homogeneous a-SiCO is investigated by first principles calculations, the atomic structures, formation energy and lithiation voltage of SiC<sub>2/5</sub>O<sub>6/5</sub> are calculated and discussed.

## 2. Methods

Classical molecular dynamics (CMD) based melt quench simulations were used to obtain the initial structures of SiC<sub>2/5</sub>O<sub>6/5</sub>. Tersoff potential<sup>19</sup> and the potential parameters for SiC<sup>19</sup> and SiO<sub>2</sub> (ref. 20) were used to describe the atomic interaction in SiC<sub>2/5</sub>O<sub>6/5</sub>. The melt-quench procedure proposed in our previous study<sup>21</sup> was used to generate the amorphous structures of SiC<sub>2/5</sub>O<sub>6/5</sub> from random atomic configuration, the system temperature was adjusted by velocity scaling and

College of Mechanical & Electrical Engineering, Wenzhou University, Wenzhou, 325035, P.R.China. E-mail: nliao@wzu.edu.cn; lnb55@163.com; Fax: +86-577-86689138; Tel: +86-577-86689138



canonical ensemble (NVT) using a Nosé–Hoover thermostat. The CMD simulations were implemented by LAMMPS (Large-scale Atomic/Molecular Massively Parallel Simulator) code.<sup>22</sup>

The first principles simulations were then performed to optimize the  $\text{SiC}_{2/5}\text{O}_{6/5}$  structures further. The systems were annealed at 1800 K by 8 ps of NVT simulations, and were then quenched to 300 K at a rate of  $0.3 \text{ K fs}^{-1}$  by NPT simulations. Finally the amorphous structures are relaxed fully by geometry optimization of lattice parameters and atomic position. A plane-wave cut-off of 300 eV and a  $2 \times 2 \times 2 \kappa$ -points mesh were found to give sufficient convergence. The geometry optimization was conducted by: residual force  $< 0.01 \text{ eV \AA}^{-1}$ , convergence of energy change per atom  $< 2 \times 10^{-6} \text{ eV}$ , stress  $< 0.01 \text{ GPa}$ . The electronic broadening width was 0.1 eV in a variable occupancy calculation, and the same orbitals for alpha and beta spins were used. The generalized gradient approximation following the Perdew–Bueke–Ernzerhof scheme (GGA-PBE)<sup>23</sup> was used. The first principles simulations according to the density functional theory (DFT) ultra-soft pseudo-potential method were conducted in CASTEP code<sup>24,25</sup> in Materials Studio 5.5.

The  $\text{SiC}_{2/5}\text{O}_{6/5}$  studied here refers to the stoichiometric glass composed of  $1/3(\text{SiC})$  and  $2/3(\text{SiO}_2)$ . The formation energy of  $\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5}$  is obtained by subtracting the reference energies of  $\text{SiC}_{2/5}\text{O}_{6/5}$  and Li from the energy of  $\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5}$  model. The formation energy per Si atom is given by:<sup>15</sup>

$$E_f = E(\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5}) - (xE(\text{Li}) + E(\text{SiC}_{2/5}\text{O}_{6/5})) \quad (1)$$

where  $x$  is the ratio of number of Li atoms per Si atoms,  $E(\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5})$  and  $E(\text{SiC}_{2/5}\text{O}_{6/5})$  are the per Si atom energies for the lithiated  $\text{SiC}_{2/5}\text{O}_{6/5}$  and the original  $\text{SiC}_{2/5}\text{O}_{6/5}$ , and  $E(\text{Li})$  is the per Li atom energy of bcc-Li. The average intercalation voltage  $V(x)$  is the chemical potential of Li ion in electrodes and is calculated by<sup>15</sup>

$$V(x) = -\frac{d(E_f)}{dx} \quad (2)$$

### 3. Results and discussion

The calculated properties of  $\text{SiC}_{2/5}\text{O}_{6/5}$  are listed in Table 1 and compared to the experimental data. The peaks values in radial distribution functions (RDFs) and angular distribution are obtained by Gaussian multi-peak fitting.<sup>26</sup> The bond length of Si–O, Si–C and C–C are obtained by the sharp peaks of RDFs, observed at  $r_{\text{SiO}} = 1.64 \text{ \AA}$ ,  $r_{\text{SiC}} = 1.89 \text{ \AA}$  and  $r_{\text{CC}} = 1.51 \text{ \AA}$  respectively, correspond to the experimental data of  $r_{\text{SiO}} = 1.62 \text{ \AA}$ ,  $r_{\text{SiC}} = 1.88 \text{ \AA}$  and  $r_{\text{CC}} = 1.49 \text{ \AA}$ .<sup>27,28</sup> The tetrahedrons are mainly linked to each other by vertex and form a broad angular distribution Si–O–Si, centered approximately at  $146^\circ$ , it corresponds to the peak of  $140\text{--}144^\circ$  in experiments.<sup>27</sup> The Young's modulus ( $E$ ) of  $\text{SiC}_{2/5}\text{O}_{6/5}$  is 99 GPa and within the range of 90–110 GPa in experiments.<sup>29,30</sup> The glass transition temperature ( $T_g$ ) is determined by the temperature corresponds to the change in slope of temperature-dependent Young's modulus curve. The obtained  $T_g$  of  $\text{SiC}_{2/5}\text{O}_{6/5}$  is 1460 K and is closed to the range of 1573–1673 K in experiments.<sup>31–33</sup>

Table 1 Computed properties compared to reported experimental data

	This work	Experimental results <sup>27,28,30–36</sup>
Si–O [ $\text{\AA}$ ]	1.64	1.62
Si–C [ $\text{\AA}$ ]	1.89	1.88
C–C [ $\text{\AA}$ ]	1.51	1.49
Si–O–Si [deg]	146	140–144
$E$ [GPa]	99	90–110
$T_g$ [K]	1460	1573–1673
Density [ $\text{g m}^{-3}$ ]	2.58	2.4–2.64

In order to describe the structural evolution of  $\text{SiC}_{2/5}\text{O}_{6/5}$  under Li insertion, a series of configuration snapshots of  $\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5}$  are presented in Fig. 1. At low Li concentration, the Si atoms are slightly displaced from their tetrahedral positions, and formation of  $\text{Li}_x\text{SiO}_y$ -like structures can be observed. With increasing Li concentration, some of the silicon-centered tetrahedrons are destroyed, which leads to the breaking of Si–O bonds and the formation of  $\text{Li}_x\text{O}$ .

The atomic correlations of the lithiated  $\text{SiC}_x\text{O}_{6/5}$  are inferred by means of RDFs, as shown in Fig. 2. The bond length of Si–O and C–C for lithiated  $\text{SiC}_{2/5}\text{O}_{6/5}$  are determined by the first peaks of RDFs around 1.64  $\text{\AA}$  and 1.51  $\text{\AA}$  respectively. With increasing Li concentration, the first peak of Si–O slightly shift to a larger value and its long distance correlation becomes more predominate, this is an indicative of stretched Si–O bonds and rupture of Si–O–Si units, which is accorded with the above observations. The small peak of Si–O around 1.85  $\text{\AA}$  corresponds to the Si–O bond near the edge of free carbon. The C–C network tends to be more close together after the rupture of Si–O–Si units, it results in a very slight decrease on C–C bond length, which proves the structural stability of free carbon during lithiation.

The coordination numbers are obtained by integrating the first peak of radial distribution function, as shown in Fig. 3. Based on the average bond length of O–Si, Si–Li and O–Li,<sup>15,37–40</sup> 1.85  $\text{\AA}$ , 3.08  $\text{\AA}$  and 2.16  $\text{\AA}$  are chosen as maximum cutoff radii for the calculations of  $\text{CN}_{\text{O–Si}}$ ,  $\text{CN}_{\text{Si–Li}}$  and  $\text{CN}_{\text{O–Li}}$  respectively. Consisting with the above results, with increasing concentration of lithium atoms in the mixture, a quasi-linear drop of

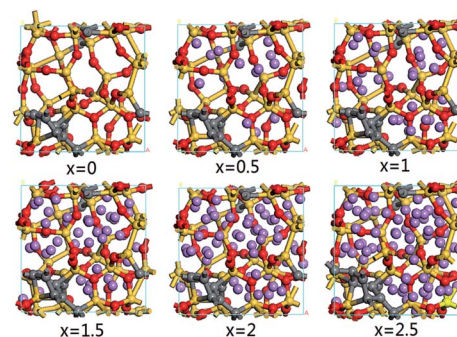


Fig. 1 Atomic configurations of  $\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5}$  with increasing Li concentration. The yellow, grey, red and purple spheres represent the silicon, carbon, oxygen and lithium atoms respectively.



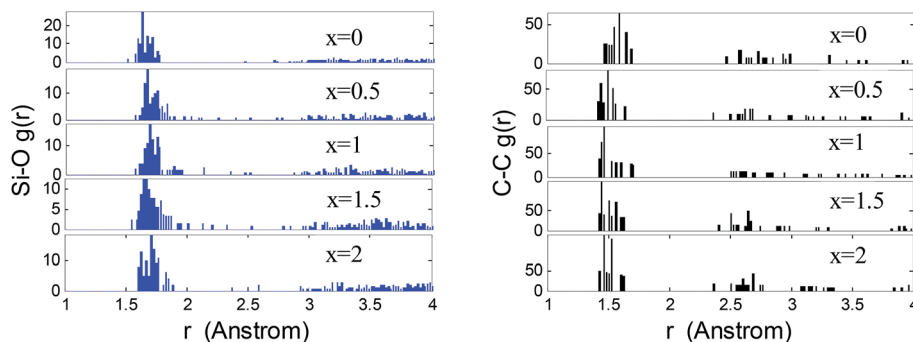


Fig. 2 Calculated Si–O and C–C RDFs of a-SiC<sub>2/5</sub>O<sub>6/5</sub> at several degrees of lithiation.

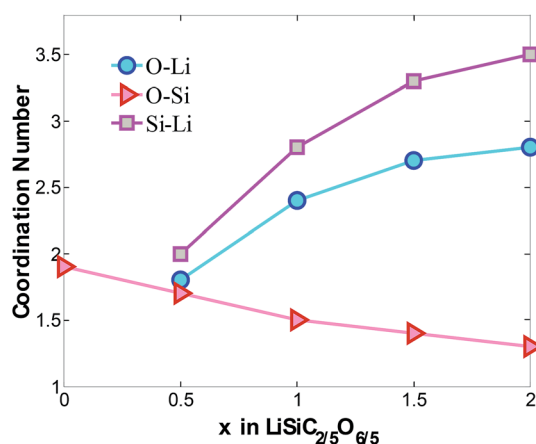


Fig. 3 Average coordinate number of O–Li, O–Si and Si–Li atom pairs in Li<sub>x</sub>SiC<sub>2/5</sub>O<sub>6/5</sub>. The cutoff radii for CN<sub>O–Si</sub>, CN<sub>Si–Li</sub> and CN<sub>O–Li</sub> are 1.85 Å, 3.08 Å and 2.16 Å respectively.

CN<sub>O–Si</sub> from 1.9 to 1.4 confirm the disintegration of Si–O bonds. The increasing of CN<sub>Si–Li</sub> and CN<sub>O–Li</sub> is attributed to increasing Li atoms surround the Si and O atoms, it indicates the formation of Li<sub>x</sub>O and Li<sub>y</sub>Si structures. The Si and O atoms prefer to interact with the Li atoms rather than with each other, specially at high Li concentration. When  $x = 2$ , the insertion of Li

gradually disintegrates the a-SiC<sub>2/5</sub>O<sub>6/5</sub> host mixture with O and Si atoms coordinating to 2.8 and 3.5 Li atoms.

Detailed views on formation of Li<sub>x</sub>O and Li<sub>y</sub>Si complexes in lithiated SiC<sub>2/5</sub>O<sub>6/5</sub> ( $x = 2$ ) are shown in Fig. 4. As the Li concentration increases, more O atoms are involved in formation of Li<sub>x</sub>O ( $x = 2, 3, 4$ ) and Li<sub>y</sub>Si ( $y = 3, 4, 5$ ) complexes. Stable formation of both Li<sub>x</sub>O and Li<sub>y</sub>Si complexes in high Li concentration structure is attributed to the Si–C/O mixed-bond tetrahedrons in the original structure. According to the first-principle calculation of silicon dioxide,<sup>41</sup> after lithiation and some of the Si–O bonds broke, only Li<sub>x</sub>O was found in the lithiated structure, indicating the broken Si atoms still connected with other O atoms and could not form Li<sub>y</sub>Si compound in silicon dioxide. While the mixed bond tetrahedrons in SiCO provide the possibility to generate broken Si and O for the formation of Li<sub>x</sub>O and Li<sub>y</sub>Si complexes.

The total density of states (TDOS) and partial density of states (PDOS) of SiC<sub>2/5</sub>O<sub>6/5</sub> and lithiated SiC<sub>2/5</sub>O<sub>6/5</sub> around the Fermi level are shown in Fig. 5. The insertion of Li makes two main contributions to the TDOS: one is located at around  $-4$  eV while the other is near  $1.2$  eV, which can be viewed as bonding and anti-bonding states introduced by Li insertion. The TDOS around the Fermi level is mainly composed of Si-s, Si-p, C-p, O-p and a little Li-p components. In particular, the non-zero s component of Li PDOS is almost the same as the p orbit of Si atoms. Above Fermi level, Si-p makes a major contribution to

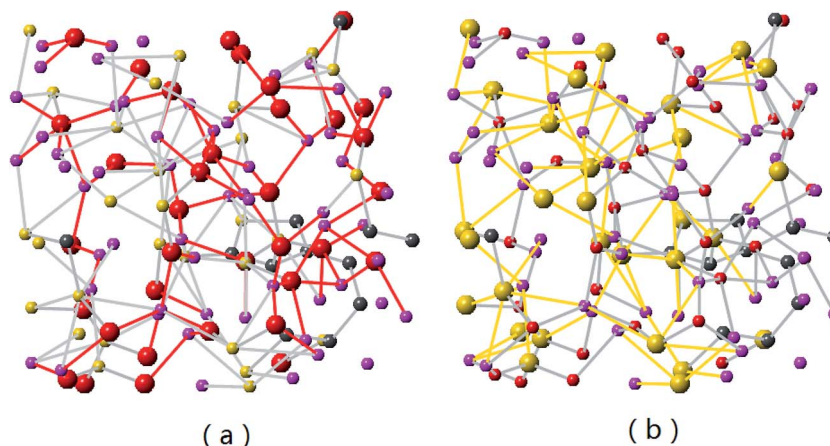


Fig. 4 Formation of Li<sub>x</sub>O and Li<sub>y</sub>Si in Li<sub>2</sub>SiC<sub>2/5</sub>O<sub>6/5</sub> (the Li–O and Li–Si bonds are presented by red and yellow colors respectively).



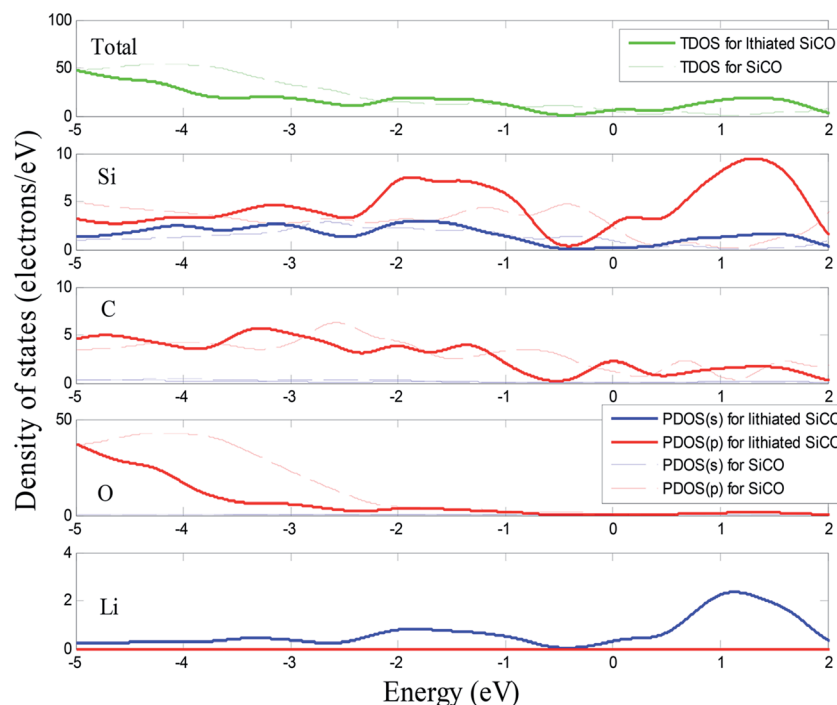


Fig. 5 Calculated total and partial density of states of  $\text{SiC}_{2/5}\text{O}_{6/5}$  and lithiated  $\text{SiC}_{2/5}\text{O}_{6/5}$ .

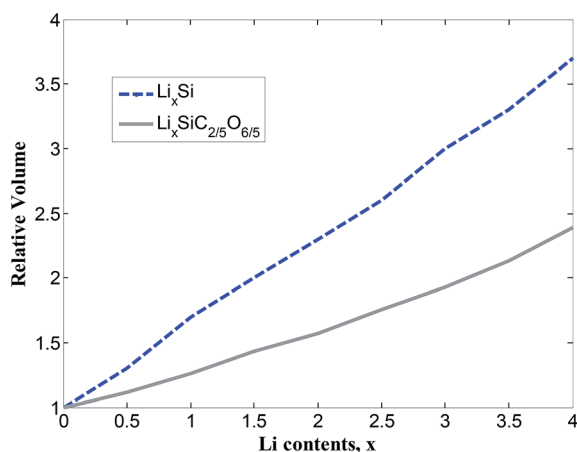


Fig. 6 Evolution of relative volume of  $\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5}$  and  $\text{Li}_x\text{Si}$  14.

TDOS with some Li-s, Si-s and C-p components, it means that the bond of Li-Si is mainly covalency with little ionicity. The relative volumes of  $\text{SiC}_{2/5}\text{O}_{6/5}$  with different degree of lithiation were calculated and compared with those of Si,<sup>14</sup> as shown in Fig. 6. The results show that the profile of relative volume for  $\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5}$  is considerably lower compared to the value of  $\text{Li}_x\text{Si}$ ,  $\text{SiC}_{2/5}\text{O}_{6/5}$  presented a better expansion performance than Si.

Fig. 7 showed the formation energies of  $\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5}$  as a function of  $x$ . The formation energies decrease with increasing Li concentration and reach the minimum when the structure is fully lithiated. The lithiation is favorable until a Li concentration of  $x = 2.75$ , an additional Li insertion is thermodynamically unfavorable. It corresponds to a specific capacity of  $1415 \text{ mA h g}^{-1}$ , considering that the ratio of irreversible and

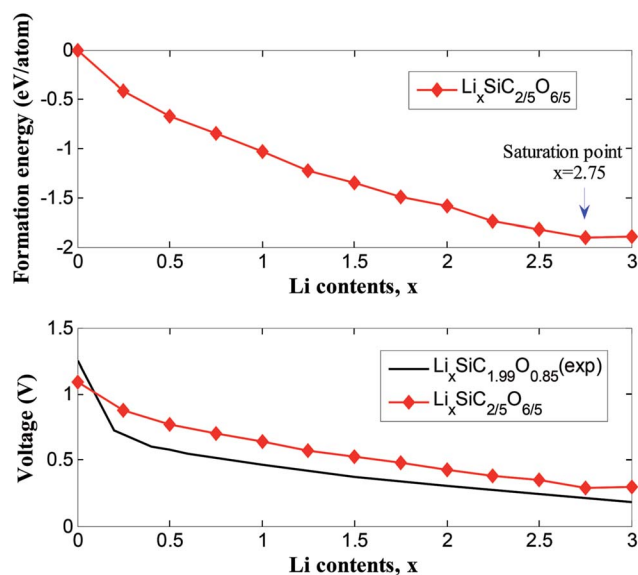


Fig. 7 Formation energy and voltage profiles for  $\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5}$  in comparison to experimental results of  $\text{Li}_x\text{SiC}_{1.99}\text{O}_{0.85}$  (ref. 5).

reversible capacity is about 1/3 for the SiCO with similar composition,<sup>42</sup> a reversible capacity of  $1061 \text{ mA h g}^{-1}$  is expected and this is comparable to reversible capacity of  $900 \text{ mA h g}^{-1}$  in experiments.<sup>42</sup> The composition-voltage curve if  $\text{Li}_x\text{SiC}_{2/5}\text{O}_{6/5}$  is also calculated and compared to the experimental data.<sup>5</sup> The lithiation voltage relative is given by the negative of the reaction free energy per Li.<sup>43</sup> The lithiation voltage for  $\text{SiC}_{2/5}\text{O}_{6/5}$  is predicted to be around 0.42 to 1.12 V.



## 4. Conclusions

The present first-principle simulations offer an insights into the lithiated structures and lithiation mechanism of  $\alpha$ - $\text{SiC}_{2/5}\text{O}_{6/5}$ . Our interpretation of radial distribution, angular distribution and coordinate number suggests that the Si-O bond tends to break and the  $\text{Li}_2\text{O}$  will forms at the beginning of lithiation, then  $\text{Li}_x\text{O}$  and  $\text{Li}_y\text{Si}$  form with increasing of Li concentration, which make major contribution to the capacity of the  $\alpha$ - $\text{SiC}_{2/5}\text{O}_{6/5}$ . The Li concentration dependent of formation energies curve indicates that the lithiation of  $\text{SiC}_{2/5}\text{O}_{6/5}$  is favorable until a Li concentration of  $x = 2.75$ , which corresponds to a specific capacity of  $1415 \text{ mA h g}^{-1}$ . Both the formation energies and the voltage curves suggest lithium is preferable in incorporation with  $\text{SiC}_{2/5}\text{O}_{6/5}$ , and this is attributed to the formation of  $\text{Li}_x\text{O}$  and  $\text{Li}_y\text{Si}$ .

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