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# Alloying effects of Ag on grain boundaries and alumina interfaces in copper: a first principles prediction

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The mechanical properties of oxide dispersion-strengthened copper are largely dictated by its internal interfaces, *i.e.* the oxide interfaces and the grain boundaries (GBs). Here we present a systematic first-principles study for evaluating the potential impact of Ag alloying on adhesion of Cu/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> interfaces and Cu grain boundaries as well. The results suggest that, in contrast to the strong segregation of S that is always detrimental, Ag only slightly segregates to the Al<sub>2</sub>O<sub>3</sub> interfaces, strengthens the weak stoichiometric interface, and slightly weakens the strong Al-rich interface. Ag cannot pin S inside the matrix. The co-segregation of Ag with S modestly negates the detrimental influence of S on adhesion, but can hardly occur. Ag segregation to most of the GBs is found also to be weak, and reduces the adhesion slightly. The only one exception is on the  $\Sigma 9$  GB. Based on the gained insights, we suggest that Ag alloying has only limited benefits but can still be encouraged.

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## 1. Introduction

The alumina dispersion-strengthened copper (ADSC) alloys, also called alumina particle-reinforced copper matrix composites Cu(Al<sub>2</sub>O<sub>3</sub>)p, have excellent comprehensive properties of high electrical/thermal conductance and high strength. They are highly advantageous for uses in many electrical applications at elevated temperatures, such as electrical connectors, spot-welding electrodes, heat sink devices, and high pressure heat exchangers for power generations.<sup>1</sup> ADSC alloys are often fabricated by *in situ* internal oxidation. During fabrication, a small number of solute Al atoms are first pre-alloyed with solvent Cu atoms. The mixture is heat-treated, either by using Cu<sub>2</sub>O powder as an internal oxidizer or by directly heating in an oxygen-rich gaseous atmosphere, followed by densification in vacuum. During the process, Al atoms are preferentially oxidized *in situ*, forming ultra-fine Al<sub>2</sub>O<sub>3</sub> dispersoids with a uniform distribution inside the Cu matrix. Performance and reliability of such alloys are largely determined by the oxide interfaces as well as grain boundaries. Both interfaces can be

significantly affected by trace amount of impurities and alloying elements.

It is known from the literature that S segregation not only significantly degrades the grain boundary adhesion in Ni,<sup>2–4</sup> but also provokes the spallation of the protective alumina scales from Ni and Fe substrates.<sup>5–8</sup> The so-called “sulfur effect” has long been of both fundamental and technological interest to the materials research society.<sup>7–12</sup> Our previous studies have suggested<sup>13,14</sup> that S also strongly segregates to Cu/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> interface, degrading the adhesion and further reducing the size stability of Al<sub>2</sub>O<sub>3</sub> dispersoids in Cu. To improve the performance and reliability of ADSC alloys, it is natural to consider the alloy design strategy, *i.e.* designing appropriate alloying elements to directly enhance the oxide interface binding, and/or to prevent S segregation to the interfaces.<sup>10–12,15,16</sup> Ag, with the same superior electrical/thermal conductance as Cu, can be considered as a good candidate for such alloying elements. However, there was only one single report that alloying with Ag increases the macroscopic hardness of ADSC alloys.<sup>17</sup> This, as a hypothesis, has been ascribed to Ag segregation to internal oxide interfaces (Cu/Al<sub>2</sub>O<sub>3</sub>) which presumably enhanced the interface adhesion. Direct evidence from microscopic characterizations still lacked, leaving this hypothesis with many uncertainties. Meanwhile, a recent experimental characterization on a Cu bicrystal with only the well-defined  $\Sigma 5(310)$  grain boundary (GB)<sup>18,19</sup> suggested that Ag has a noticeably strong segregation tendency to this GB, as compared to many other high-angle GBs in polycrystalline Cu. Thus, there appears to be a competition between GB segregation and oxide-interface segregation (if possible) for Ag in Cu. In other words, in the

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case of strong GB segregation, the potential impact of segregation to oxide interfaces would be greatly limited, and *vice versa*.

First principles calculations provide a useful tool to test all aspects of interface segregation at an electronic–atomic scale. One successful example is on the thermally-grown coating interface of Ni/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub>.<sup>11–13,15,16,20–23</sup> Encouraged by these efforts, we apply the similar first-principles strategy to evaluate the potential impact of Ag segregation on the oxide interface of Cu/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub>, and Cu grain boundaries as well. In this work, we first constructed a series of oxide interfaces with different interfacial stoichiometries and coordinations, along with a series of low- $\Sigma$  symmetric tilted grain boundaries (STGBs) using the structural-unit (SU) model. The following calculations and analyses were further performed. (1) The heats of segregation ( $\Delta G_{\text{seg}}$ ) for Ag and S from inner Cu matrix to the most relevant interfaces, and correspondingly, the most possible segregation paths. (2) The work of separation ( $W_{\text{sep}}$ ), as a measurement of adhesion strength, for both the clean and S/Ag-contaminated interfaces.

## 2. Computational methods

To construct a heterogeneous metal/oxide interface model, we choose the Cu(111) and the  $\alpha$ -Al<sub>2</sub>O<sub>3</sub>(0001) surfaces, each with the lowest surface energy in its bulk, to yield an interface orientation of Cu(111) ( $\sqrt{3} \times \sqrt{3}$ )/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub>(0001) ( $1 \times 1$ ). This orientation was employed for it has the lowest strains to commensuration: the Cu(111) lattice was stretched and the Al<sub>2</sub>O<sub>3</sub>(0001) was compressed by the same amount, only 3.8%. It is also consistent with the high resolution transmission electron microscopy (HRTEM) observations for Cu/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub>.<sup>24</sup> Stacking such an Al<sub>2</sub>O<sub>3</sub> and two Cu blocks together with a sufficient vacuum thickness, one obtains a Cu/Al<sub>2</sub>O<sub>3</sub>/Cu sandwich hexagonal supercell, with  $a = 4.62$  Å and  $c = 51.08$  Å, that can be regarded as a more appropriate atomistic model of the Cu(111)/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub>(0001) interface. Nevertheless, TEM and HRTEM cannot provide all detailed information that is needed for an atomistic modeling of the interface. Ascertaining interfacial stoichiometry and atomic coordination must be resorted to energetic calculations. Upon the local chemical activity of Al or O, the interface structure can be stoichiometric, Al-rich, or O-rich. Under each stoichiometry, interfacial Cu atoms may sit at Al-top, O-top, or hollow sites of Al<sub>2</sub>O<sub>3</sub>. Among different stoichiometry or coordination types, the associated formation energy and adhesion strength could vary by several folds.<sup>12</sup> In our previous studies,<sup>13,14</sup> we have evaluated the thermodynamic equilibrium interface structures and energies of Cu/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> as a function of both  $a_{\text{Al}}$  and  $p_{\text{O}_2}$ . The results have been used to construct the interface phase diagram. According to the phase diagram, at  $T = 1000$  K, the equilibrium interface structure of practical interest still resides in the Al-rich phase regime, but is near the transition between the Al-rich and the stoichiometric phases, especially when considering the prediction uncertainty of Al activity. Therefore, it is practically possible for both types of interfaces to coexist. All the ensuing interface calculations were hence carried out for both the Al-rich and the stoichiometric phases.

The GB structure models are rather diverse, being mostly the coincident-site-lattice (CSL) model<sup>25</sup> and the structural-unit (SU) model.<sup>26,27</sup> The CSL model is constructed by rotating one grain lattice against the other about a rotation axis by a certain angle, so as to achieve a number of coincident lattice sites. The degree of fit ( $\Sigma$ ) of a GB is measured as the reciprocal of the ratio of coincidence sites to the total number of sites. A lower  $\Sigma$  boundary corresponds to a higher density of coincident sites, and thus generally a more stable GB structure. While in the SU model, a GB is constructed using a serial of “favored” structural units (SUs). Each SU typically has a low  $\Sigma$  value, and thus can be seen as a favored symmetric tilt grain boundary (STGB). In this sense, a GB with a long period can be treated as a combination of SUs comprising one or several neighboring favored boundaries with shorter periods.<sup>28</sup> In our previous work,<sup>23,29</sup> the SU model has been suggested to be more appropriate for describing low- $\Sigma$  GBs of Fe and Cu, and thus was employed in the ensuing calculations of GBs in this work. All SU-modeled GBs were calculated using “sandwich” supercells with periodic boundary conditions. Each supercell hosts two identical GB interfaces which are separated by a sufficient thickness of one grain lattice to preclude any possible spatial interaction. This sandwich model avoids the necessity of vacuum and two extra free surfaces, enabling a good balance between computational efficiency and accuracy (as long as a full relaxation can be carefully performed both on supercell shape and volume).

All the ensuing structural relaxation and energetic calculations were performed using the density functional theory (DFT) code-VASP (Vienna *Ab initio* Simulation Package, version 5.3)<sup>30,31</sup> with plane-wave basis sets. The electron–core interaction was described by the Blöchl projector augmented wave method (PAW) within the frozen-core approximation<sup>32</sup> as implemented in VASP. The plane-wave basis sets were generated with valence configurations of Cu-3p<sup>6</sup>3d<sup>10</sup>4p<sup>1</sup>, Al-3s<sup>2</sup>3p<sup>1</sup>, and O-2s<sup>2</sup>2p<sup>4</sup>. The validation of the exchange–correlation (XC) functional was performed by fitting the energy–volume data of crystalline Cu and Al<sub>2</sub>O<sub>3</sub> to the universal equation of state<sup>33</sup> and comparing the predicted bulk properties with experiments.<sup>34,35</sup> The PAW-PW91 functional was finally chose for all subsequent calculations, for it yielded the best predictions for bulk Cu and Al<sub>2</sub>O<sub>3</sub>.<sup>13</sup> The interface calculations were performed using a Cu/Al<sub>2</sub>O<sub>3</sub>/Cu sandwich configuration with a vacuum thickness of at least 12 Å and a  $3 \times 3 \times 1$  M–P  $k$ -mesh. In the sandwich model, each Cu block consists of seven atomic layers (with a total of twenty-one Cu atoms), and the alumina consists of four O-layers and eight Al-layers (with a total of twelve O and eight Al atoms for the stoichiometric case). All ground-state configurations were optimized using a high energy cutoff of 550 eV for the plane-wave basis set, until the total energy was a minimum and the total force on each ion converged to within 0.02 eV Å<sup>−1</sup>.

## 3. Results and discussion

### 3.1. Interface segregation and adhesion

In our previous studies,<sup>13,14</sup> we have shown the strong dependence of interface energy on interface structure, both of which are dictated by local thermodynamic conditions ( $T$  and  $a_{\text{Al}}$ ). For



a given interface structure, we further computed and compared the heat of segregation  $\Delta G_{\text{seg}}$  of Ag from inside the (unstrained) matrix to various interfacial sites.

The heat of segregation ( $\Delta G_{\text{seg}}$ ) is defined as the energy difference associated with a solute atom segregating from the ground-state, unstrained bulk Cu to a possible interstitial or substitutional sites in the interface. For Ag segregation,

$$\Delta G_{\text{seg}} = G_{\text{intf}} + G_{\text{Cu}}^{\text{Ag}} - (G_{\text{intf}}^{\text{Ag}} + G_{\text{Cu}}), \quad (1)$$

where  $G_{\text{intf}}$  and  $G_{\text{intf}}^{\text{Ag}}$  represent the total energy of the clean interface supercell and of the interface supercell containing one segregated Ag, respectively.  $G_{\text{Cu}}$  and  $G_{\text{Cu}}^{\text{Ag}}$  are the total energy of

the perfect  $3 \times 3 \times 3$  Cu supercell and of the same-size Cu supercell containing one substitutional Ag. The heat of segregation must be exothermic to enable segregation. For a segregated interface, we then assessed the adhesion strength in term of the work of separation ( $W_{\text{sep}}$ ) which is defined as the cleavage energy needed to separate an interface rigidly into two halves.

$$W_{\text{sep}} = \frac{G_{\text{intf}} - G_{\text{A}} - G_{\text{B}}}{2A}, \quad (2)$$

where  $E_{\text{intf}}$  is the total energy of the bonded interface,  $G_{\text{A}}$  and  $G_{\text{B}}$  represent the total energy of each separated half,  $A$  is the area of the interface. The calculated energies and corresponding structures are summarized in Fig. 1.

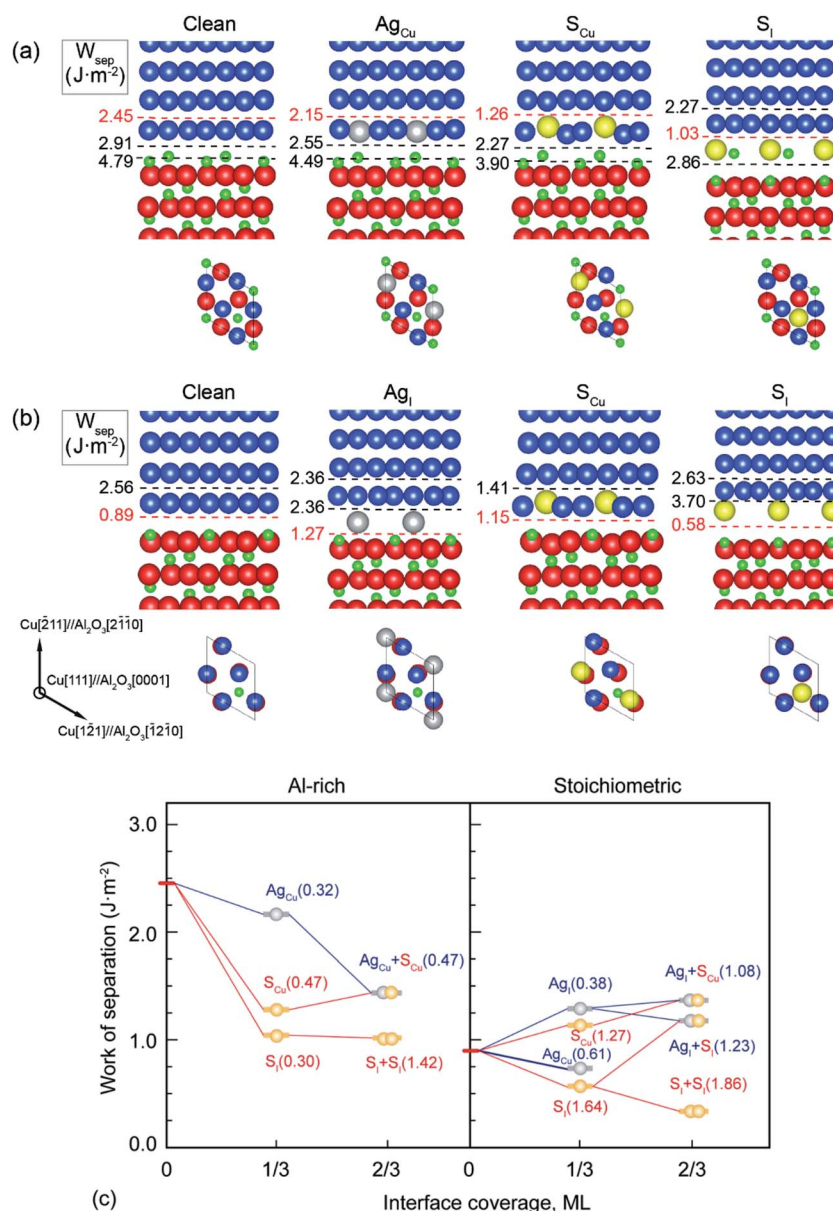


Fig. 1 Segregation structures and  $W_{\text{sep}}$  for Ag and S on (a) the Al-rich and (b) the stoichiometric interfaces. Here Cu, Al, O, S, and Ag are represented in blue, green, red, yellow, and gray, respectively. The dashed lines denote the places where the interfaces separate. (c) The work of separation  $W_{\text{sep}}$  as a function of interface coverage for both interfaces. Here, the full monolayer (ML) coverage is defined as 3 Cu atoms per interfacial layer in unit cell. The lines are to guide the eyes.



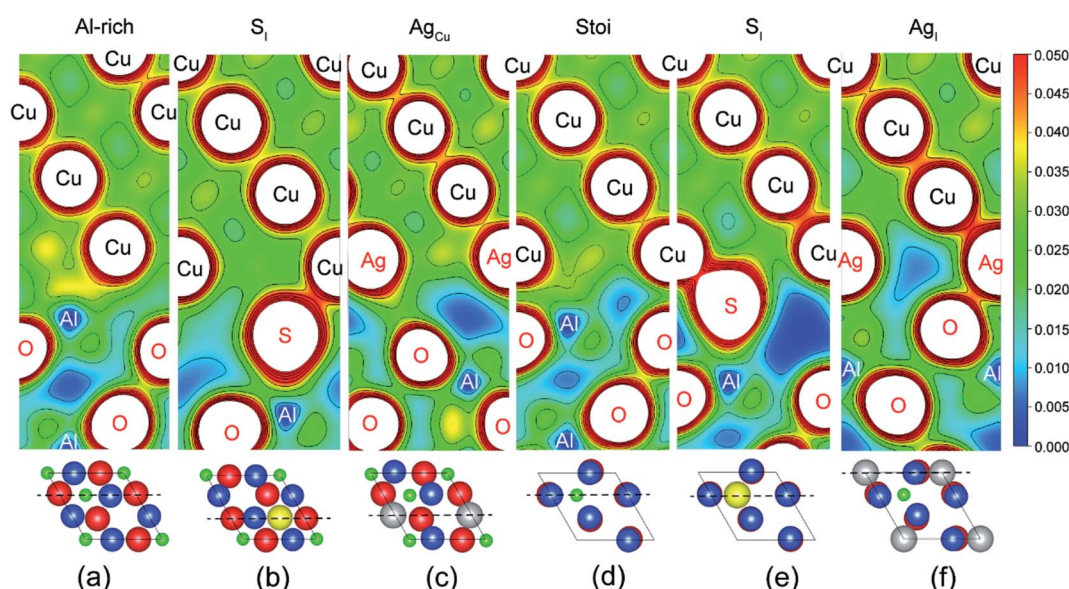


It is shown in Fig. 1a and b that the clean Al-rich interface has a significantly higher adhesion strength ( $2.45 \text{ J m}^{-2}$ ), about three times that of the stoichiometric counterpart ( $0.89 \text{ J m}^{-2}$ ). Segregated elements strongly affect the interface adhesion. Fig. 1c reveals the segregation trends and sites of Ag and S, as well as their impacts on adhesion. Please note that values in parentheses represent the heats of segregation associated with each segregation step (in units of eV per atom). It is clear that segregated Ag and S have a site competition at both interfaces. For the strong Al-rich interface, the segregation of Ag and S are rather weak and closely comparable. Ag only segregates to Cu substitutional ( $\text{Ag}_{\text{Cu}}$ ) sites with  $\Delta G_{\text{seg}} = 0.32 \text{ eV}$  per atom. When impurity S presents, it can segregate to interstitial ( $\text{S}_{\text{i}}$ ) and Cu substitutional ( $\text{S}_{\text{Cu}}$ ) sites, lowering the energy of the system by  $\Delta G_{\text{seg}} = 0.30$  and  $0.47 \text{ eV}$  per atom, respectively. Co-segregation of Ag and S can hardly occur due to the low energy driving force, 0 or  $0.15 \text{ eV}$  per atom when refers to single  $\text{S}_{\text{Cu}}$  or  $\text{Ag}_{\text{Cu}}$ . For the weak stoichiometric interface, Ag segregates to interfacial interstitial ( $\text{Ag}_{\text{i}}$ ) and Cu substitutional ( $\text{Ag}_{\text{Cu}}$ ) sites, with  $\Delta G_{\text{seg}} = 0.38$  and  $0.61 \text{ eV}$  per atom, respectively. These heat of segregation values are way below those of S, *i.e.*  $\Delta G_{\text{seg}} = 1.64 \text{ eV}$  per atom for interstitial ( $\text{S}_{\text{i}}$ ) and  $1.27 \text{ eV}$  per atom for Cu substitutional ( $\text{S}_{\text{Cu}}$ ) sites. Similarly as seen for the Al-rich interface, co-segregation of Ag with S can hardly occur, due to the strong segregation of single S.

Fig. 2 provides electron density contours for these interfaces. The Al-rich interface results are found in Fig. 2a–c, while the stoichiometric interface results are in Fig. 2d–f. For the strong Al-rich interface, Fig. 2a reveals strong metallic character in the bonding between Cu and the extra Al on the Al-rich  $\text{Al}_2\text{O}_3$

surface, corresponding to a high  $W_{\text{sep}}$  of  $2.45 \text{ J m}^{-2}$ . Good electrical conductance can be also expected at this interface. Segregated S and Ag both reduce the interfacial electron density. Fig. 2b reveals a directed partially-ionic, partially-covalent bond between Cu and S atoms across the Al-rich interface, which significantly decreases  $W_{\text{sep}}$  from  $2.45 \text{ J m}^{-2}$  down to  $1.03 \text{ J m}^{-2}$ . Fig. 2c reveals a slightly weaker metallic bonding between the substitutional Ag and Cu than that between Cu and Cu. Correspondingly, the adhesion is slightly reduced by  $\sim 12\%$ , down to  $2.15 \text{ J m}^{-2}$ . For the weak stoichiometric interface, S segregation to interstitial sites is strong and decreases  $W_{\text{sep}}$  from  $0.89$  to  $0.58 \text{ J m}^{-2}$  (Fig. 2e). This happens because the interfacial covalent-ionic Cu–O bonds (Fig. 2d) tend to be replaced with much weaker ionic S–Al bonds (Fig. 2e). Compared to Al-rich interface, there are certain benefits of Ag on the stoichiometric. When at an interstitial site ( $\text{Ag}_{\text{i}}$ ), the valence electron density between the Ag and the surface O in Fig. 2f is obviously higher than that between the Cu and the O in Fig. 2d, knitting Cu and  $\alpha\text{-Al}_2\text{O}_3$  together and increasing  $W_{\text{sep}}$  by  $\sim 40\%$ , up to  $1.27 \text{ J m}^{-2}$ .

When co-segregation of Ag and S occurs,  $W_{\text{sep}}$  may further decrease to  $1.29 \text{ J m}^{-2}$  ( $\text{Ag}_{\text{Cu}} + \text{S}_{\text{Cu}}$ ) on the Al-rich interface and to  $1.21 \text{ J m}^{-2}$  ( $\text{Ag}_{\text{i}} + \text{S}_{\text{i}}$ ) on the stoichiometric interface (Fig. 1c), making the two interfaces are comparable in adhesion. Nevertheless, the lowest value is still above that for a clean stoichiometric interface ( $0.89 \text{ J m}^{-2}$ ) and well in excess of that with  $2/3$  monolayer (ML) of S ( $0.32 \text{ J m}^{-2}$ ). Evidently, when any unpinned S reach the interface, Ag counteracts the deleterious effects of S at the interface and hence the seriously reduced  $W_{\text{sep}}$  by a higher coverage of S can be modestly negated.



**Fig. 2** Valence electron density contours (in unit of  $\text{e} \text{ \AA}^{-3}$ ). (a) The clean Al-rich interface showing the metallic bonding between the Cu and the extra Al. (b) The Al-rich interface containing segregated S ( $\text{S}_{\text{i}}$ ) at  $1/3$  ML coverage. (c) The Al-rich interface containing segregated Ag ( $\text{Ag}_{\text{Cu}}$ ) at  $1/3$  ML coverage. (d) The clean stoichiometric interface showing the Cu–O bonds with each Cu atop each O. (e) The stoichiometric interface containing segregated S ( $\text{S}_{\text{i}}$ ) at  $1/3$  ML coverage. Note the S pushes the Cu and O apart, weakening those bonds, and a relatively weak S–Al/S–O bond is created. (f) The stoichiometric interface containing segregated Ag ( $\text{Ag}_{\text{i}}$ ) at  $1/3$  ML coverage. The dash-dotted lines at the bottom correspond to the positions of the contour planes in top views.



### 3.2. GB segregations

Extensive calculations were further performed to evaluate Ag and S segregation to various interfacial sites, including both substitutional and interstitial sites, of a group of low- $\Sigma$  STGBs ( $\Sigma \leq 11$ ) within the  $\langle 100 \rangle$  and  $\langle 110 \rangle$  tilt systems. Fig. 3 plots the most energy-favored structures of those GBs after segregation. The resulting works of separation are labeled on the side. The corresponding segregation energies are compared in Table 1.

It is seen that, except for the  $\Sigma 9(221)$  GB, Ag segregation is generally weak and has undesired effects on GB adhesion. For the  $\Sigma 3(112)$ ,  $\Sigma 5(210)$ ,  $\Sigma 5(310)$ , or  $\Sigma 11(113)$ , Ag only weakly segregates to Cu substitutional ( $\text{Ag}_{\text{Cu}}$ ) sites on the GB interface layer (with  $\Delta G_{\text{seg}} = 0.23\text{--}0.69$  eV per atom), slightly reducing  $W_{\text{sep}}$  by 2–5% only. While for the  $\Sigma 9(221)$  GB, Ag can strongly segregate to Cu substitutional ( $\text{Ag}_{\text{Cu}}$ ) sites on the first sub-interface layer ( $\Delta G_{\text{seg}} = 1.12$  eV per atom) and increase  $W_{\text{sep}}$  from 2.39 to 2.57  $\text{J m}^{-2}$ . Meantime, Ag may also weakly

segregate to interfacial interstitial ( $\text{Ag}_{\text{i}}$ ) sites ( $\Delta G_{\text{seg}} = 0.54$  eV per atom) and slightly decrease  $W_{\text{sep}}$  to 2.30  $\text{J m}^{-2}$ .

S segregation always reduces GB adhesion. S weakly segregates to Cu substitutional ( $\text{S}_{\text{Cu}}$ ) sites in the first sub-interface layers of  $\Sigma 3(112)$ ,  $\Sigma 5(310)$ , and  $\Sigma 11(113)$ , with  $\Delta G_{\text{seg}} = 0.3\text{--}0.7$  eV per atom. Besides  $\text{S}_{\text{Cu}}$  sites, S may also segregate to interfacial interstitial ( $\text{S}_{\text{i}}$ ) at the  $\Sigma 5(210)$  and  $\Sigma 9(221)$ , and in particular, S segregation to the  $\Sigma 9(221)$  is fairly strong, with  $\Delta G_{\text{seg}} = 1.57$  eV per atom.

Fig. 4 shows the calculated valence charge density distributions for the clean and segregated  $\Sigma 9(221)$  GBs. The charge density distributions in the (0–10) plane of  $\Sigma 9(221)$  GB are found in Fig. 4a–c, while the (010) plane results are in Fig. 4d–f. As seen from the (0–10) plane contour of the GB, the strong segregation of Ag to a Cu substitutional ( $\text{Ag}_{\text{Cu}}$ ) site ( $\Delta G_{\text{seg}} = 1.12$  eV per atom) increases the interfacial charge density in Fig. 4b. This is consistent with an increase of  $W_{\text{sep}}$  from the initial value of 2.39 to 2.57  $\text{J m}^{-2}$  (Table 1 and Fig. 3a). In

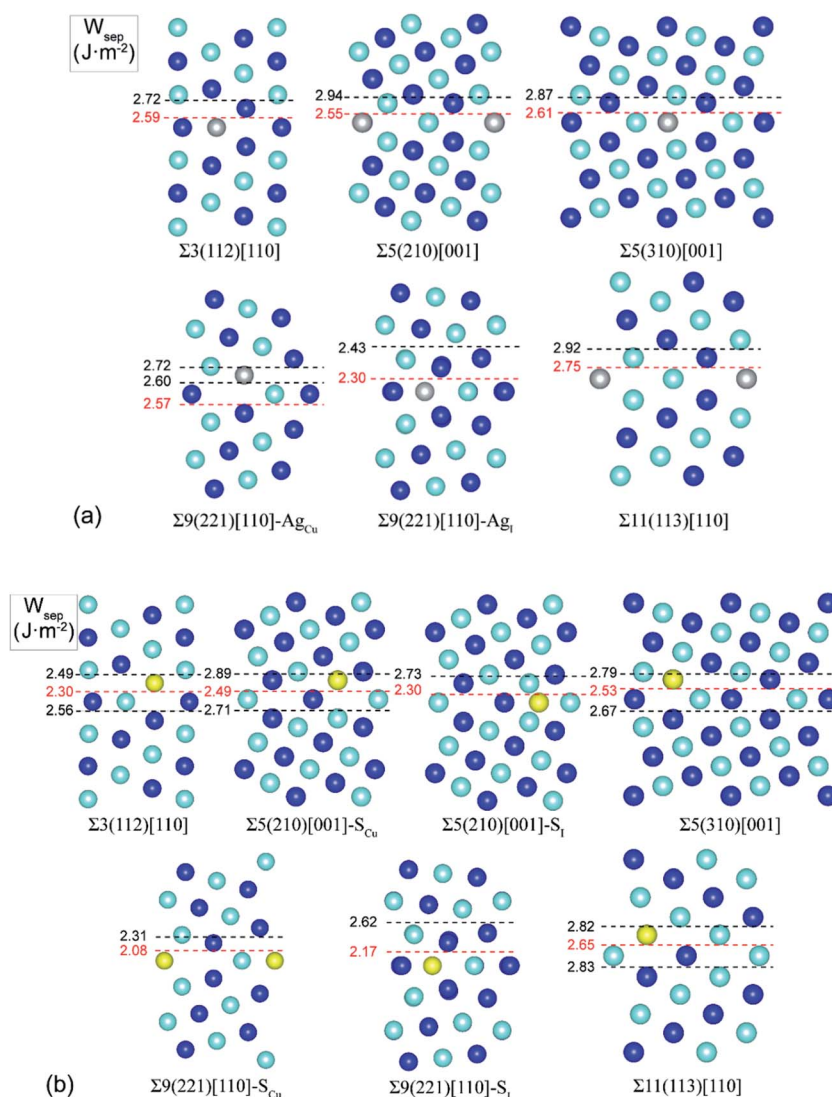
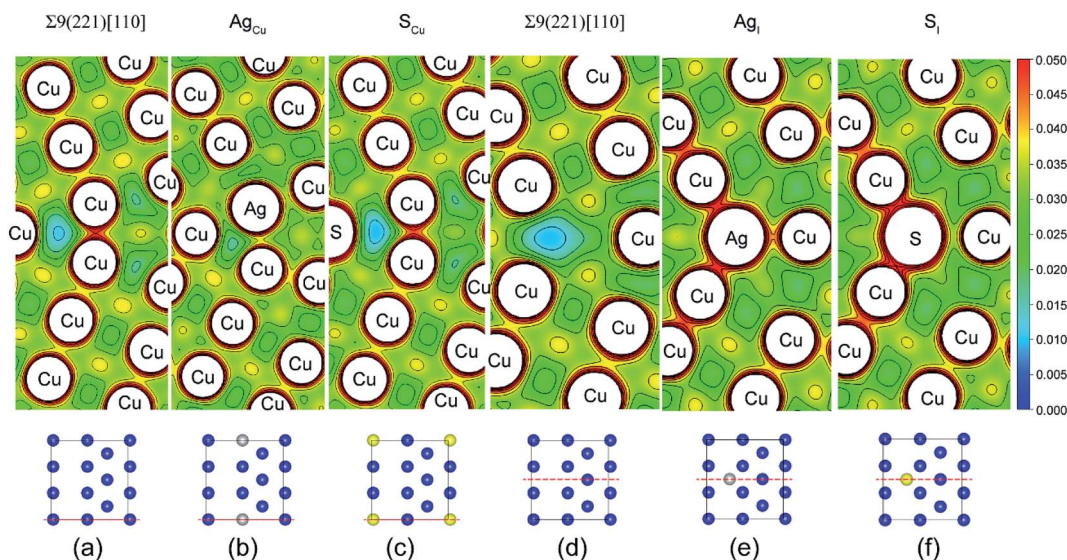


Fig. 3 Segregation structures and  $W_{\text{sep}}$  for Ag (a) and S (b) on low- $\Sigma$  STGBs ( $\Sigma \leq 11$ ) of Cu. Blue and cambridge blue spheres denote atoms on different  $\langle 110 \rangle$  planes for the  $\langle 110 \rangle$  tilt GBs and  $\langle 100 \rangle$  planes for the  $\langle 100 \rangle$  tilt GBs.



**Table 1** Calculation segregation energies and works of separation for all the low- $\Sigma$  STGBs ( $\Sigma \leq 11$ ) of Cu

Grain boundary	$\theta$ (deg)	$N$	$W_{\text{sep}}$ (J m <sup>-2</sup> )	Ag segregation		S segregation	
				$\Delta G_{\text{seg}}$ (eV per atom)	$W_{\text{sep}}$ (J m <sup>-2</sup> )	$\Delta G_{\text{seg}}$ (eV per atom)	$W_{\text{sep}}$ (J m <sup>-2</sup> )
$\Sigma 3(111)[110]$	190.47	96	2.53	-0.04	—	-0.03	—
$\Sigma 3(112)[110]$	70.53	102	2.71	0.30	2.59	0.44	2.30
$\Sigma 5(210)[100]$	53.13	160	2.67	0.54	2.55	0.73(S <sub>Cu</sub> ), 0.41(S <sub>I</sub> )	2.49, 2.30
$\Sigma 5(310)[100]$	36.87	152	2.66	0.69	2.61	0.68	2.53
$\Sigma 9(221)[110]$	141.06	102	2.39	1.12(Ag <sub>Cu</sub> ), 0.54(Ag <sub>I</sub> )	2.57, 2.30	0.44(S <sub>Cu</sub> ), 1.57(S <sub>I</sub> )	2.08, 2.17
$\Sigma 11(113)[110]$	50.48	132	2.86	0.23	2.75	0.30	2.65

**Fig. 4** Valence electron density contours of  $\Sigma 9(221)[110]$  GBs (in unit of  $e \text{ \AA}^{-3}$ ): (a) and (d) the clean GB, (b) substitutional Ag (Ag<sub>Cu</sub>), (c) substitutional S (S<sub>Cu</sub>), (e) interstitial Ag (Ag<sub>I</sub>), (f) interstitial S (S<sub>I</sub>).

contrast, the weak segregation of S to a Cu substitutional (S<sub>Cu</sub>) site ( $\Delta G_{\text{seg}} = 0.44$  eV per atom) induces almost no changes in the interfacial charge density in Fig. 4c, but an obvious reduction of  $\sim 13\%$  in  $W_{\text{sep}}$  (from 2.39 to 2.08 J m<sup>-2</sup>). Similarly, the segregated Ag or S at the interstitial sites corresponds to a high interfacial charge density (Fig. 4e and f), as compared to the clean interface, and  $W_{\text{sep}}$  is also reduced slightly to 2.30 (Ag<sub>I</sub>) and 2.17 J m<sup>-2</sup> (S<sub>I</sub>). The reduction in  $W_{\text{sep}}$  for S<sub>Cu</sub>, S<sub>I</sub>, and Ag<sub>I</sub>, shall refer to the even stronger adsorption of S or Ag on Cu surface after interface separation (Fig. 5).

Given a temperature, the interfacial occupancy of a segregant not only depends on segregation energy, but also on the initial bulk concentration. Ag, as an alloying element, far outnumbers impurity S in the matrix, normally by  $\sim 2$  orders of magnitude. Based on McLean's equation,<sup>36</sup> the interfacial occupation of Ag and S under the thermodynamic equilibrium can be estimated by

$$C_{\text{intr}} = \frac{C_{\text{bulk}} \exp(\Delta G_{\text{seg}}/kT)}{1 + C_{\text{bulk}} \exp(\Delta G_{\text{seg}}/kT)} \quad (3)$$

here,  $\Delta G_{\text{seg}}$  is segregation energy.  $T$  is the temperature.

To assess the potential of Ag pinning S, we further evaluated the pair affinity of Ag-S in Cu as

$$\Delta G_{\text{g}}(\text{Ag-S}) = (G_{\text{perf}} + G_{\text{Ag-S}}) - (G_{\text{Ag}} + G_{\text{S}}), \quad (4)$$

where  $G_{\text{perf}}$ ,  $G_{\text{Ag-S}}$ ,  $G_{\text{Ag}}$ , or  $G_{\text{S}}$  is the total free energy of a  $3 \times 3 \times 3$  Cu supercell with a perfect lattice, with a Ag-S pair in the first nearest-neighbor (NN) distance ( $\sim 2.5 \text{ \AA}$ ), with a single substitutional Ag atom, or with a single substitutional S atom, respectively. Thus  $(G_{\text{Ag}} + G_{\text{S}})$  represents the reference state of the two atoms being sufficiently separated and thus essentially non-interacting in Cu. Clearly, negative  $\Delta G_{\text{g}}$  indicates an attractive interaction. We calculated the pair affinity of  $\Delta G_{\text{g}}(\text{Ag-S})$  was to be 0.03 eV per pair only, suggesting that Ag has essentially no affinity to S in Cu and thus cannot pin S effectively in Cu. This is somewhat frustrating, but seems to be consistent with the basic fact that copper forms a wide range of mixed-valence sulfides in nature while silver does not.

Based on the knowledge gained in this work, a joint design strategy can be suggested for achieving high quality ADSC alloys: (1) alloying with Ag, for its segregation can directly enhance the weak stoichiometric oxide interfaces, and has only





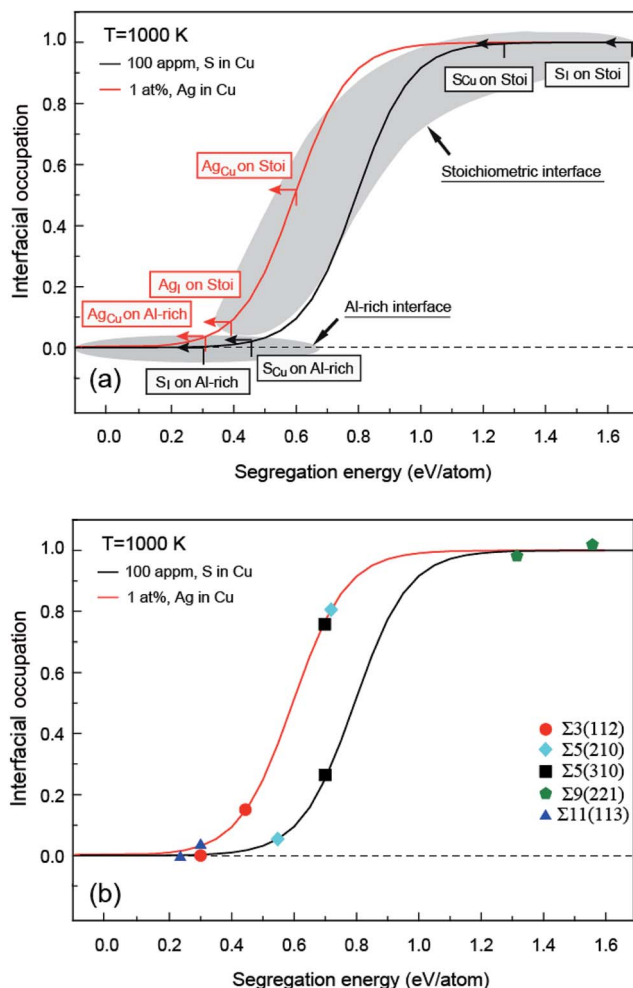


Fig. 5 Interfacial site occupation versus segregation energy for Ag and S. (a) interface (b) grain boundary as calculated from Mclean's equation for bulk concentrations of  $C_{\text{Ag}} = 1 \text{ at\%}$  and  $C_{\text{S}} = 100 \text{ appm}$ , under  $T = 1000 \text{ K}$ .

minimal influence on the strong Al-rich oxide interfaces and most GBs (except to enhance the  $\Sigma 9$ ) (2) introducing certain desulfurization processes during fabrication, such as hydrogen-based annealing, to substantially reduce S content in Cu matrix, for Ag cannot pin S effectively in Cu, and (3) alloying with other reactive elements, to effectively bind S in the matrix. In one our earlier study, rare-earth elements Ce, Y, and Hf have been predicted effective in pinning S in Ni alloys.<sup>16</sup> Their effectiveness in Cu alloys awaits our further studies.

## 4. Conclusions

The structure and adhesion of the Cu/ $\alpha$ - $\text{Al}_2\text{O}_3$  interfaces in Cu and Cu grain boundaries, along with the potential impact of alloying with Ag, have been thoroughly studied using DFT calculations. The Al-rich Cu/ $\alpha$ - $\text{Al}_2\text{O}_3$  interface has a significantly larger  $W_{\text{sep}}$  than its stoichiometric counterpart. Segregation of S to the interfaces degrades adhesion by up to 64%. Ag itself segregates to the interfaces, can slightly weaken the strong Al-

rich interface, but greatly enhance the weak stoichiometric interface. Ag cannot pin S in Cu matrix, thus cannot prevent S segregation to the interfaces. Co-segregation of Ag with S at both interfaces only modestly negates the detrimental influence of any S that reaches the interfaces, but can still hardly occur. As for the GBs, Ag has a weak segregation tendency to most GBs and reduces the adhesion slightly. The only one exception is on the  $\Sigma 9$  GB. Ag can strongly segregate to the  $\Sigma 9(221)$  GB and directly enhance the adhesion. Based on the gained insights, we proposed that Ag alloying has limited benefits but can be still encouraged, especially when the impurity S in Cu can be effectively eliminated.

## Conflicts of interest

There are no conflicts to declare.

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