



## Magnetic ordering in a frustrated bow-tie lattice†

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We report a systematic X-ray and powder neutron diffraction study of the geometrically frustrated material,  $\text{Ca}_2\text{Mn}_3\text{O}_8$ .  $\text{Ca}_2\text{Mn}_3\text{O}_8$  exhibits a 'bow-tie' like connectivity of  $\text{Mn}^{4+}$  with  $\text{Ca}^{2+}$  occupying octahedral sites between  $\text{MnO}_6$  layers. Magnetic refinements of neutron powder diffraction data indicate that the spins order with a canted four sub-lattice-like ( $\uparrow\uparrow\downarrow\downarrow$ ) arrangement below  $\sim 50$  K. In addition, short range magnetic correlations can be seen to persist until  $\sim 130$  K.

## Introduction

Geometric frustration arises when interactions between magnetic degrees of freedom are incompatible with the underlying crystal geometry.<sup>1</sup> In materials which exhibit triangular (e.g. delafossite<sup>2</sup> and kagomé<sup>3</sup>), tetrahedral (e.g. pyrochlore<sup>4</sup>), honeycomb (e.g.  $\text{Bi}_3\text{Mn}_4\text{O}_{12}\text{NO}_3$ <sup>5</sup>) and 'bow-tie' connectivity between magnetic species each spin cannot satisfy all pairwise interactions leading to ground state degeneracy and the realization of unconventional magnetic properties.<sup>6</sup> In systems with Jahn–Teller (JT) active species the magnetic spin alignment can also result in an ordered arrangement of the JT distorted  $\text{MO}_6$  octahedral bond arrangement resulting in the emergence of weak ferroelectric character.

Layered transition metal oxides are emerging as an important class of frustrated materials due to their compositional flexibility and wide range of applications. In these materials frustration can be (partially) lifted through either the propagation of a  $120^\circ$  spin spiral or incommensurate spin order through lattice distortions leading to a wide range of exotic magnetic states.<sup>2,7–10</sup> For example,  $\text{CuFeO}_2$  has been shown to exhibit two magnetic phase transitions the first at  $\sim 14$  K and a

second at  $\sim 11$  K. At 14 K the material exhibits a collinear spin density wave with an incommensurate modulation which turns into collinear commensurate four sub-lattice ( $4\text{SL}$ ,  $\uparrow\uparrow\downarrow\downarrow$ ) ordering at  $T_N$  (11 K).<sup>2</sup> In contrast, incorporation of Jahn–Teller active  $\text{Mn}^{3+}$  ions into  $\text{CuMnO}_2$  results in complex nearest neighbour,  $J_1$  and diagonal nearest neighbour,  $J_2$  interactions which lead to a frustrated square lattice due to an anisotropy of the triangular lattice.<sup>10</sup> This results in magnetic spins which are antiferromagnetically (AFM) aligned along the  $[1\bar{1}0]$  direction and ferromagnetically aligned along the  $[110]$  direction corresponding to a collinear AFM order.<sup>10</sup>

The layered transition metal oxide,  $\text{Ca}_2\text{Mn}_3\text{O}_8$ , is beginning to attract attention within the literature. This material can be thought of as comprising of a series of  $\text{MnO}_6$  layers separated, by  $\text{Ca}^{2+}$  ions. However, in contrast with the triangular layered transition metal oxides, both the A-cation and B-cation layers can be thought of as incomplete (nominal formula  $\text{Ca}_{0.5}\text{Mn}_{0.75}\text{O}_2$ ) resulting in an ordered vacancy within the layers similar to that seen in kagomé lattices. However, in contrast with kagomé lattices, where the vacancy is ordered in a staggered diagonal fashion, the vacancy in  $\text{Ca}_2\text{Mn}_3\text{O}_8$  is ordered in a striped arrangement realizing a 'bow-tie' connectivity of the Mn sub-lattice and a potentially frustrated geometry (Fig. 1). The location of this vacancy alternates between subsequent  $\text{MnO}_6$  layers giving rise to ABAB stacking with the  $\text{Ca}^{2+}$  occupying octahedral co-ordination within the layers. Research into  $\text{Ca}_2\text{Mn}_3\text{O}_8$  has been primarily focused on its catalytic and electrochemical characteristics with the magnetic properties largely ignored since the first structural reports in the 1980's.<sup>11–16</sup> Recently we investigated the effects of morphology on the magnetic properties of  $\text{Ca}_2\text{Mn}_3\text{O}_8$  based on the synthetic methods reported in the literature.<sup>17</sup> We demonstrated that it could be expected that  $\text{Ca}_2\text{Mn}_3\text{O}_8$  materials would exhibit more complex antiferromagnetic spin order than a simple  $\uparrow\downarrow$  spin arrangement.<sup>17</sup> We also noted that the

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**Fig. 1** (a) Schematic representation of  $\text{Ca}_2\text{Mn}_3\text{O}_8$  showing the ABAB layered structure, ordered vacancy in the  $bc$  plane and 'bow-tie' connectivity of the  $\text{Mn}^{4+}$  cations. The pink and purple spheres and squares represent the  $\text{Mn}^{4+}$  ions and  $\text{MnO}_6$  octahedra on the Mn1 and Mn2 crystallographic sites respectively. The teal spheres represent the  $\text{Ca}^{2+}$  ions and the red spheres the oxygen ions, rietveld refinement of (b) X-ray and (c) neutron diffraction data collected for  $\text{Ca}_2\text{Mn}_3\text{O}_8$  at 300 K. Where the black circles represent the observed data, the red line is the calculated model and the blue line is the difference curve.

quality of materials produced by these methods limited any detailed magnetic studies.<sup>17</sup> The magnetic behaviour of the isostructural material,  $\text{Mn}_2\text{Mn}_3\text{O}_8$  ( $\text{Mn}_5\text{O}_8$ ) has also recently been reported by Kishore *et al.*<sup>18</sup> They proposed four different magnetic spin arrangements and generated simulated patterns which they then compared to powder neutron diffraction data collected at 9 K.<sup>18</sup> Subsequently, they differentiate between their assumed models using *ab initio* total energy calculations which suggested a model where both the  $\text{MnO}_6$  layers and  $\text{Mn}^{2+}$  interlayer ions are coupled antiferromagnetically with all the spins located around the manganese 'bow-tie' coupled ferromagnetically to be the lowest energy.<sup>18</sup> We note, however, that these materials were synthesised using a wet chemical route (similar to our previous studies on  $\text{Ca}_2\text{Mn}_3\text{O}_8$ <sup>17</sup>) with the resulting materials poorly crystalline potentially leading to difficulties fully identifying the magnetic structure experimentally.<sup>18</sup>

In this paper we report the first synthesis of high quality bulk  $\text{Ca}_2\text{Mn}_3\text{O}_8$ , allowing us to perform a systematic structural and magnetic study of a material with a 'bow-tie' lattice. A 4SL-like ( $\uparrow\downarrow\uparrow\downarrow$ ) ordering is clearly indexed from the magnetic Bragg structure with short range magnetic correlations persisting above  $T_N$ .

## Experimental

Single phase polycrystalline  $\text{Ca}_2\text{Mn}_3\text{O}_8$  was prepared using molten salt synthesis methods similar to those reported previously for Hollandite materials.<sup>19</sup> Stoichiometric ratios of  $\text{CaCO}_3$  and  $\text{MnCO}_3$

(both Sigma Aldrich,  $\geq 99.0\%$ ) were mixed with a 350% (w/w) eutectic mixture of  $\text{KCl}/\text{NaCl}$  and reacted at 700 °C (ramp rate 10 °C  $\text{min}^{-1}$ ) for 48 hours after which the sample was quenched to room temperature. The material was then washed and dried at ambient temperature. An additional 350% (w/w) eutectic mixture of  $\text{KCl}/\text{NaCl}$  was added and the mixture further heated at 700 °C (ramp rate 10 °C  $\text{min}^{-1}$ ) for an additional 24 hours and quenched to room temperature.

Phase purity was initially determined using a Bruker D8 Advance powder diffractometer over a  $2\theta$  range of 10° to 70° (40 kV and 40 mA, with  $\lambda = 1.54413$  Å). Subsequent high quality and variable temperature data was collected between 12 K and 300 K using a Rigaku SmartLab rotating Anode  $\theta/2\theta$  instrument over a  $2\theta$  range of 10° to 70° (45 kV and 200 mA, with  $\lambda = 1.54413$  Å). Neutron Powder Diffraction (NPD) data were collected using the BT-1 32 detector neutron powder diffractometer at the NIST Center for Neutron Research (NCNR). The sample was loaded into a vanadium can of length 50 mm and diameter 10.8 mm. Data were collected at several temperatures between 4 K and 300 K. A Ge(311) monochromator with a 75° take-off angle,  $\lambda = 2.0787(2)$  Å, and in-pile collimation of 60' were used. Data were collected over the range of 1.3°–166.3°  $2\theta$  with a step size of 0.05°. Inelastic neutron diffraction data was collected between 4 K and 150 K using the Disc Chopper Spectrometer (DCS) at the NCNR. Data were collected with a chopper speed of 20 000 rpm and a graphite filter at wavelengths of 1.8 Å and 2.5 Å using the same sample environment (vanadium can) as for the BT-1 experiments.

Magnetic susceptibility data were collected at the Materials Characterisation Laboratory at the ISIS Neutron and Muon



facility using a Magnetic Property Measurement System (MPMS) XL-7 instrument. Zero-field cooled/field cooled data were collected in a temperature range of 2 K to 300 K with an applied magnetic field ( $H$ ) of 0.1 T. Field dependence hysteresis measurements were performed at 2 K, 25 K and 300 K between  $\pm 7$  T. AC susceptibility measurements were performed using the Quantum design PPMS-9 Physical Property Measurements System. Data were collected as a function of frequency between 100 Hz and 2700 Hz over a temperature range of 2 K to 100 K.

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## Results and discussion

Room temperature diffraction data clearly demonstrated the formation of single phase  $\text{Ca}_2\text{Mn}_3\text{O}_8$  with no indication of either  $\text{Mn}_2\text{O}_3$  or  $\text{CaMnO}_3$  impurities. Refinements performed using the GSAS suite of programs<sup>20,21</sup> indicated excellent agreement to the monoclinic,  $C2/m$ , model proposed by Ansell *et al.*<sup>11</sup> The Rietveld refinement profile for both room temperature powder neutron and X-ray diffraction data are shown in Fig. 1 with parameter details given in Table 1. All refinement details are given in the ESI.† Bond-valence analysis was performed on the neutron diffraction data collected at 300 K using the Valist program in order to probe the oxidation state of the manganese.<sup>22</sup> This gives bond valences of 4.0(1) and 3.9(2) on

the Mn1 and Mn2 crystallographic sites respectively consistent with the expected Mn oxidation state of 4+.

DC magnetic susceptibility data indicates a broad peak with a maximum at approximately 80 K consistent with low dimensional/frustrated antiferromagnetic ordering (Fig. 2).<sup>23</sup> The derivative  $d\chi T/dT$  clearly demonstrates that  $T_N = 58$  K (Fig. 2 and ESI†). Examination of the Curie–Weiss behaviour indicates a deviation from linearity at approximately 130 K ( $T^*$ ) (Fig. 2). These deviations are common in frustrated systems and suggest that whilst magnetic correlations are building up as the material is cooled, frustration acts to hinder the formation of a three dimensional (Néel) ordered state.<sup>24</sup> An effective magnetic moment,  $\mu_{\text{eff}}$ , was calculated at 300 K to be  $6.47 \mu_B$  per formula unit consistent with that expected for  $\text{Mn}^{4+}$  ( $\mu_{\text{calc}} = 6.7 \mu_B$  per formula unit) in  $\text{Ca}_2\text{Mn}_3\text{O}_8$  consistent with our previous study.<sup>17</sup> The Weiss constant,  $\theta_{\text{CW}}$ , was determined to have a value of  $-150.5$  K. The level of frustration in the material can be determined using the frustration index,  $f$ , as given by;<sup>25,26</sup>

$$f = \frac{-\theta_{\text{CW}}}{T_N}$$

This gives a frustration index of approximately 2.6 confirming some level of frustration in this material; a frustration index value of 1 would normally be expected for non-frustrated spin order.<sup>27</sup> To put this into context, in related layered triangular lattices frustration indexes as low as 1.3 and as high as 13 have been reported.<sup>19,28,29</sup> It should be noted, however, that care needs to be taken when making direct comparisons of  $f$  or using it explicitly as evidence of frustration since it is greatly influenced by nearest neighbour interactions and dimensionality.<sup>24</sup> Slight deviations between the zero field cooled and field cooled data are evident below  $T_N$  suggesting the possibility of weak ferromagnetic interactions or spin glass-like behaviour. However, as with our previous study, there is no evidence of either appreciable field or frequency dependence of the susceptibility as a function of temperature as shown in Fig. S7 and S8 in the ESI† which would seem to rule out these possibilities (ESI†).<sup>17</sup>

Variable temperature X-ray (XRD) and neutron diffraction studies were performed in order to further understand the temperature dependence and magnetic ordering in this material. Refinement of these data demonstrated the material could be satisfactorily indexed to the  $C2/m$  model with no obvious change in symmetry over the whole temperature range studied (12–300 K). Rietveld refinement details and profiles are shown in the ESI.†

The temperature dependence of the cell volume shows thermal expansion above approximately 50 K as expected for layered metal oxide materials. However, this expansion clearly demonstrates two distinct regions with different slopes which intersect at approximately 130 K (Fig. 3). The temperature dependence of the lattice parameters is even less straight forward. The  $a$  and  $c$  parameters exhibit linear thermal expansion above 50 K as shown in Fig. 4. In contrast both the  $b$  parameter and the  $\beta$  angle exhibit invariant behaviour up to approximately 130 K (Fig. 4) giving rise to the behaviour observed in the cell volume.

**Table 1** Rietveld refinement parameters for X-ray and neutron diffraction data collected at 300 K for  $\text{Ca}_2\text{Mn}_3\text{O}_8$ , refined using the space group  $C2/m$  and the model proposed by Ansell *et al.*<sup>11</sup> Values in parentheses indicate one standard deviation in the parameter

Parameter	X-ray	Neutron
$\chi^2$	0.9383	0.9822
$wR_p$ (%)	4.98	4.52
$R_p$ (%)	3.90	3.69
$a$ (Å)	11.0131(1)	11.023(2)
$b$ (Å)	5.84160(9)	5.84629(8)
$c$ (Å)	4.93926(8)	4.94346(7)
$\beta$ (°)	109.78(1)	109.771(1)
Cell vol. (Å <sup>3</sup> )	299.016(5)	299.785(6)
Ca ( $x, 0, y$ )	0.7244(3)	0.7248(3)
	0.6656(1)	0.6661(5)
	1.00	0.4(1)
Ca $U_{(\text{iso})}/U_{(\text{e})} \times 100$ (Å <sup>2</sup> )	1.00	—
Mn1 ( $0, 0, \frac{1}{2}$ )	—	—
Mn1 $U_{(\text{iso})}/U_{(\text{e})} \times 100$ (Å <sup>2</sup> )	1.00	1.3(2)
Mn2 ( $0, y, 0$ )	0.2575(1)	0.2577(6)
Mn2 $U_{(\text{iso})}/U_{(\text{e})} \times 100$ (Å <sup>2</sup> )	1.00	0.7(1)
O1 ( $x, y, z$ )	0.1004(2)	0.1005(2)
	0.2296(2)	0.2228(3)
	0.3982(2)	0.3919(3)
O1 $U_{(\text{iso})}/U_{(\text{e})} \times 100$ (Å <sup>2</sup> )	1.00	0.66(7)
O2 ( $x, \frac{1}{2}, z$ )	0.5913(2)	0.5967(2)
	0.8886(1)	0.9011(4)
O2 $U_{(\text{iso})}/U_{(\text{e})} \times 100$ (Å <sup>2</sup> )	1.00	0.52(9)
O3 ( $x, 0, z$ )	0.5984(2)	0.6041(3)
	0.9609(3)	0.9605(4)
O3 $U_{(\text{iso})}/U_{(\text{e})} \times 100$ (Å <sup>2</sup> )	1.00	1.0(1)



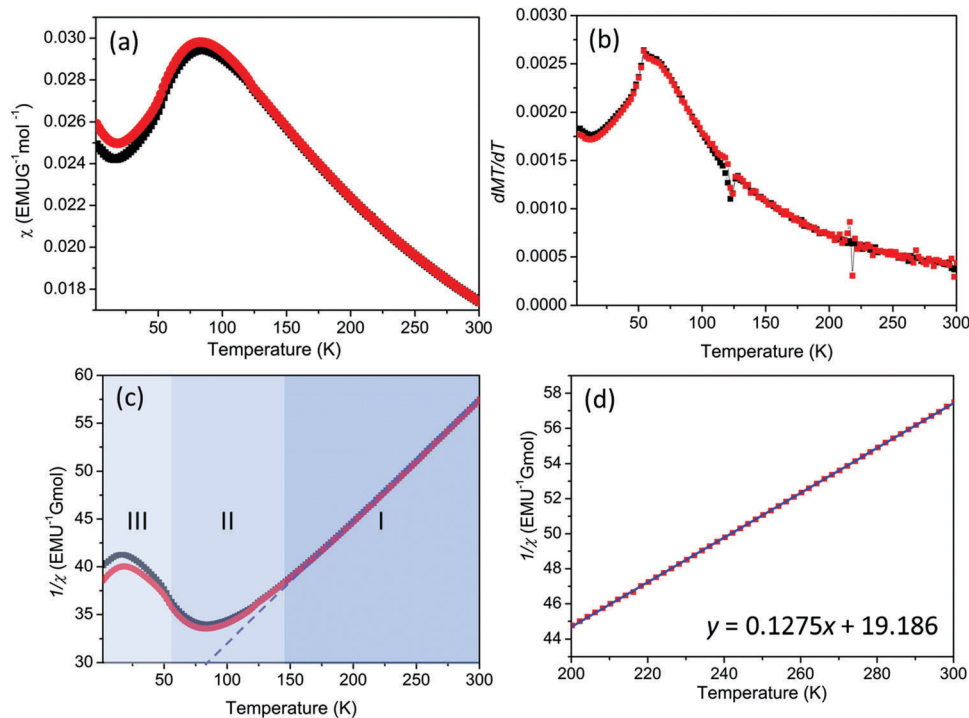


Fig. 2 SQUID magnetometry field cooled (red) and zero field cooled (black) data collected as a function of temperature for  $\text{Ca}_2\text{Mn}_2\text{O}_8$  showing (a)  $\chi$  vs.  $T$  behaviour (b) derivative,  $dMT/dT$  vs.  $T$ , (c)  $\chi^{-1}$  vs.  $T$ , indicating a deviation from the Curie–Weiss law as highlighted by a dashed line and is further divided into three regions, where region I represents the paramagnetic region, region II indicates a region of weak magnetic correlations and region III represents the 3-dimensional antiferromagnetically ordered state respectively. (d) Shows a linear fit to the paramagnetic region, within a range of  $200 \text{ K} \leq T \leq 300 \text{ K}$ .

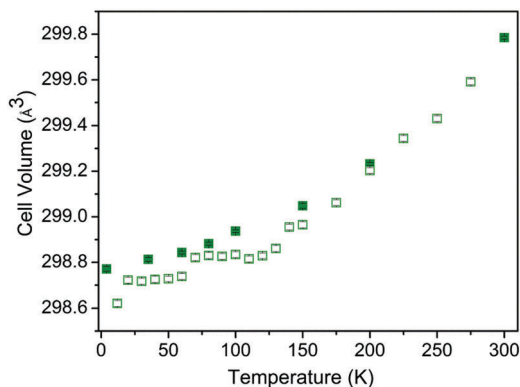


Fig. 3 Cell volume as a function of temperature showing a change in lattice expansion at approximately 130 K. Open and closed squares are the XRD and neutron data respectively. Note: error bars indicate 1 standard deviation and are smaller than the symbol size.

This temperature is consistent with the deviation from Curie–Weiss behaviour at  $T^*$  and may suggest the possibility of low dimensional spin ordering or correlations in the lattice  $b$  direction which do not result in the formation of 3-dimensionally ordered Néel state between  $T_N$  and  $T^*$ .

Close inspection of the powder neutron diffraction data clearly indicates the presence of magnetic Bragg peaks in the 35 K and 4 K data consistent with long range magnetic order below  $T_N$ . The magnetic structure was determined using

SARAH<sup>30,31</sup> and the Fullprof<sup>32,33</sup> suite and programs. The magnetic Bragg peaks, evident below  $T_N$ , can be indexed with a commensurate propagation vector  $k = \frac{1}{2}a^* + \frac{1}{2}b^*$  or  $(\frac{1}{2}, \frac{1}{2}, 0)$  using the  $k$ -search routine in Fullprof. Essentially, this vector doubles the chemical unit cell in the  $a$ - and  $b$ -directions to make the magnetic unit cell. From the parent space group  $C2/m$  and propagation vector  $k$ , we found the little group  $G_k$ , which contains only two symmetry elements—the identity operation and inversion centre. Within  $G_k$ , there are two irreducible representations,  $\Gamma_1$  and  $\Gamma_2$ , which are one-dimensional. Table S6 (ESI<sup>†</sup>) lists the basis vectors for both  $\Gamma_1$  and  $\Gamma_2$  with respect to both the Mn1 and Mn2 crystallographically distinct sites. Essentially,  $\Gamma_1$  is the totally symmetric representation that couples all the equivalent positions within the Mn1 and Mn2 sites ferromagnetically. For the Mn2 site,  $\Gamma_2$  couples the atoms at  $x, y, z$  and  $-x, -y, -z$  antiferromagnetically. We found the best solution to be one where  $\Gamma_1$  describes the Mn1 and  $\Gamma_2$  describes Mn2 sites respectively with the two sites anticoupled to each other. After fitting the magnetic Bragg peaks with this model, we obtained goodness-of-fit parameters  $\chi^2 = 1.21$ ,  $R_p = 11.1\%$ ,  $R_{wp} = 11.7$  and magnetic  $R$  factor = 12.99% as shown in Fig. 5. Furthermore, the magnetic structure can be described as belonging to the magnetic space group  $P_5\bar{1}$ . Goodness-of-fit parameters for 35 K are detailed in Table S5 (ESI<sup>†</sup>) with the refinement profile given in Fig. S5 (ESI<sup>†</sup>). The components of the moments were observed to be  $2.5(2) \mu_B$  and  $2.0(2) \mu_B$  on the Mn1 and Mn2 sites respectively at 4 K.





Fig. 4 Lattice parameters (a)  $a$ , (b)  $b$ , (c)  $c$ , and (d)  $\beta$  angle as a function of temperature showing an invariant effect in the lattice  $b$ -direction and  $\beta$  angle which persists up to a temperature of approximately 130 K. Open and closed symbols are XRD and neutron diffraction data respectively. Note: error bars indicate 1 standard deviation and in some data are smaller than the symbol size.



Fig. 5 (a) Rietveld refinement of neutron diffraction data collected for  $\text{Ca}_2\text{Mn}_3\text{O}_8$  at 4 K. Where the black circles are the observed data, the red line is the calculated model and the blue line is the difference curve. The bottom tick marks are the  $C2/m$  phase and the top tick marks represent the magnetic Bragg reflections. (b) Shows a zoomed in region at high  $d$ -spacing (as shown in the box in figure (a)) showing the magnetic Bragg peaks more clearly.

However, whilst the moments on the Mn1 site lie exclusively along the crystallographic  $a$  direction, the spins on the Mn2 crystallographic site exhibit an additional cant in the  $c$ -direction with moments of  $2.1(2) \mu_B$  and  $0.57(5) \mu_B$  in the  $a$ - and  $c$ -directions respectively. Attempts to refine the moments of the Mn1 site in the  $c$ -direction resulted in unstable refinements whilst refining both the Mn1 and Mn2 moments in the  $b$ -direction resulted in values of zero within reported errors. We also note that whilst the Mn1 crystallographic site is reasonably close to the  $3 \mu_B$  expected for  $S = 1.5$ , the observed moment on the Mn2 crystallographic site is lower than expected suggesting that full static order of the moments is not achieved at 4 K.

The full magnetic spin structure is shown in Fig. 6. The spin structure can be described by staggered single ferromagnetic stripes that run parallel to the  $c$ -direction. This results in a canted 4SL-like  $\uparrow\uparrow\downarrow\downarrow$  spin arrangement along the base of the 'bow-ties' in the  $b$ -direction with these spins canted in the  $c$ -direction. The centre of the 'bow-ties' are coupled antiferromagnetically in the  $c$ -direction and act like pinning centres such that the moment lies solely in the  $a$ -direction. Between the  $\text{MnO}_6$  layers the spins are coupled antiferromagnetically in the  $a$ -direction and ferromagnetically in the (110) plane. This is in contrast with the structure reported for  $\text{Mn}_2\text{Mn}_3\text{O}_8$  whereby the spin order within the  $\text{MnO}_6$  layers (and thus around the 'bow-tie')



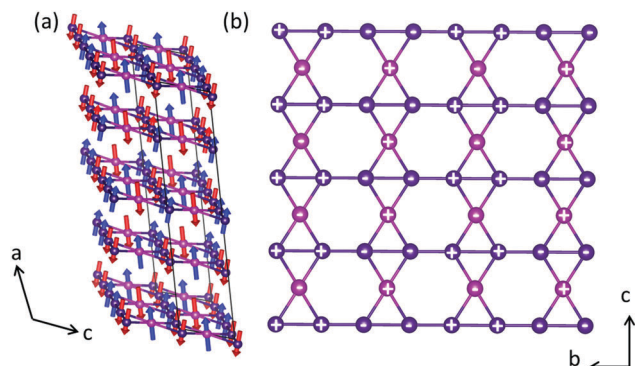


Fig. 6 (a) Magnetic structure of  $\text{Ca}_2\text{Mn}_3\text{O}_8$  refined at 4 K showing the spin orientation between the  $\text{MnO}_6$  layers in the  $a$ -direction (red is spin-up, blue is spin-down) and (b) the  $\uparrow\uparrow\downarrow\downarrow$  spin arrangement on the Mn2 crystallographic site (purple) in the  $bc$  plane.

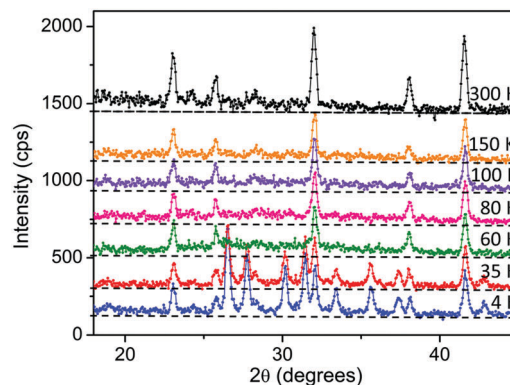


Fig. 7 Neutron diffraction data collected for  $\text{Ca}_2\text{Mn}_3\text{O}_8$  showing the temperature dependence of the deviations/Warren-like behaviour of the background. Note the dotted line is a guide for the eye.

is ferromagnetic but the coupling between layers is antiferromagnetic.<sup>18</sup> Refinement of the data collected at 35 K further confirms the proposed magnetic structure with no obvious changes in magnetic symmetry as a function of temperature. Considering the alternative model, whereby the magnetic spins are now angled in the  $bc$  plane, provides a significantly worse magnetic  $R$  factor (magnetic  $R$  factor = 192.5%) and clearly fails to model the observed magnetic Bragg peaks as shown in Fig. S6 in the ESI† further confirming the robustness of the  $\Gamma_1$ ,  $\Gamma_2$  solution proposed above (†).

Previously Warren demonstrated that low dimensional order could be characterised by diffuse anisotropic reflections which exhibit a sharp rise at low  $Q$  with a slow fall off at higher  $Q$  ( $Q = 2\pi/d$ ).<sup>34</sup> In related layered materials, such as  $\alpha\text{-NaMnO}_2$ , the presence of Warren peaks has been used to describe two-dimensional short range spin order within the metal oxide layers above  $T_N$  and below  $T^*$ .<sup>23,24</sup> However, we find no evidence of strong Warren peaks within our data suggesting that 2D ordering of the spins within the  $\text{MnO}_6$  layers above  $T_N$  and below  $T^*$  does not occur. Alternatively if we consider the possibility of the formation of spin-ordered 1D chains in the crystallographic  $b$  direction, consistent with the observed invariant effect, a sharper step-like feature in the background would be expected to be observed.<sup>23,35</sup> We note that above  $T_N$  we see a broad anisotropic deviation in the background which propagates over a  $2\theta$  range of approximately  $20^\circ$ – $40^\circ$  rather than the sharper features expected from 1D ordering (Fig. 7). This behaviour shows a clear temperature dependence which indicates that it is most likely magnetic in origin. With decreasing temperature below  $T^*$  this deviation increases in intensity up to  $\sim 60$  K before abruptly disappearing at  $T_N$  with the onset of the magnetically ordered state, with only a weak deviation in the background remaining. This behaviour may suggest a transition from a magnetically correlated to a fully ordered state at  $T_N$ . However, given the energy range that the diffraction data is integrated over it is difficult to determine if this behaviour arises as a result of 2D or 1D static interactions in the elastic channel or dynamic correlations in the inelastic channel.

Preliminary inelastic scattering (INS) experiments were performed using the Disc Chopper Spectrometer (DCS) at the NIST centre for neutron research to further investigate the spin dynamics of  $\text{Ca}_2\text{Mn}_3\text{O}_8$  to understand if the missing magnetic moment is dynamic and thus only in the inelastic channel. In order to investigate the anomalous background behaviour observed in the diffraction data we took an energy cut ( $-1$  to  $1$  meV) across the whole  $Q$ -range. This allows purely for the analysis of the elastic range of the spectrum. There is no evidence of anisotropic Warren-like and/or 1D step-like behaviour across all temperatures studied (ESI,† Fig. S10). Since these contributions are elastic in nature this confirms that deviations in the background observed in the diffraction data arise as a result of inelastic interactions as opposed to low-dimensional ordering of static-correlations as have been reported for  $\alpha\text{-NaMnO}_2$ <sup>6,23</sup> and  $\text{AgCrS}_2$ <sup>28</sup> materials. The spectra collected at  $\lambda = 2.5$  Å show a clear temperature dependence with inelastic scattering observed in a  $Q$  range of approximately  $1.4$  Å to  $2.0$  Å consistent with the  $Q$  range of the observed magnetic Bragg peaks in the elastic channel (Fig. 8). At 4 K this scattering is fairly weak in nature consistent with the formation of a three-dimensional ordered Néel state. As the temperature approaches  $T_N$  these features of the spectrum become more intense consistent with the loss of magnetic order and increased dynamic motion of the spins. Above  $T_N$  there is a clear band of intensity which extends to approximately 3 meV. This band of intensity becomes more diffuse and less well defined with increasing temperature before collapsing completely between 100 K and 150 K consistent with  $T^*$ . These data suggest that even below  $T_N$  the spins still retain some dynamic motion, particularly those on the crystallographic Mn2 site as evidenced by the lower than expected magnetic moment associated with this site in the crystallographic data and the observed spin canting of the Mn2 site. This may act to relieve frustration in the lattice and we are currently in the process of collecting additional INS data and modelling/fitting these data further which will be reported in a subsequent manuscript.





Fig. 8 Inelastic spectra collected at  $\lambda = 2.5 \text{ \AA}$  for  $\text{Ca}_2\text{Mn}_3\text{O}_8$  at variable temperatures.

## Conclusions

In summary the magnetic behaviour of  $\text{Ca}_2\text{Mn}_3\text{O}_8$  is clearly complex. Two transitions,  $T_N$  and  $T^*$ , occur at approximately 58 K and 130 K respectively. Below  $T^*$  short range spin correlations are observed. These are clearly linked to the crystallographic  $b$ -direction but fully ordered 1D chains are not realized. At  $T_N$  a three-dimensional ordered Néel state is observed. Frustration results in quasi-static behaviour of the spins on the Mn2 site such that frustration is partially relieved through the adoption of a dynamic spin state. However, the pinning centres provided by the Mn1 site act to stabilize the material and prevent the formation of wholly dynamic (spin-liquid) state. Clearly the 'bow-tie' lattice offers an exciting platform for complex magnetic order and further investigations are necessary to fully understand these phenomena.

## Conflicts of interest

We report no conflicts of interests.

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