

Cite this: *RSC Adv.*, 2019, 9, 10345

Influence of surface tension-driven network parameters on backflow strength†

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Surface tension-driven flow is widely used, owing to its spontaneous motion, in microfluidic devices with single channel structures. However, when multiple channels are used, unwanted backflow often occurs. This prevents precise and sophisticated solution flow, but has been rarely characterized. We hypothesize that, with an analytical model, the parameters that influence backflow can be systematically characterized to minimize the backflow. In a microfluidic network, inlet menisci and channels are modeled as variable pressure sources and fluidic conductors, respectively. Through the model and experiment, the influence of each network element on the backflow strength is studied. Backflow strength is affected by the interplay of multiple inlet-channel elements. With the decrease (increase) of the fluidic channel conductance (inlet size), the backflow pressure of the corresponding inlet decreases. On the other hand, backflow volume reaches its peak value during the radius change of the corresponding inlet. In networks consisting of five inlet-channel elements, backflow pressure decreases with increasing step number. Our results provide the foundations for microfluidic networks driven by the Laplace pressure of inlet menisci.

Received 27th November 2018

Accepted 26th March 2019

DOI: 10.1039/c8ra09756a

rsc.li/rsc-advances

1. Introduction

Surface tension-driven flows are increasingly used in microfluidics, because they generate spontaneous solution flow and eliminate the need for external pumping systems. To date, studies have focused on the dynamics of surface tension-driven flows in a simple single channel.^{1–7} Such studies helped in characterizing the basic traits of the flow^{8–10} and developing surface tension-driven devices.^{11–15} Then, due to the recent demands for sequential and parallel assays, surface tension-driven devices have had increased numbers of channels and input solutions.^{16–18} Compared to flow behavior in the single channel, behavior in the multiple channels is more complex and is hard to orchestrate. However, flow characteristics in the network have been rarely studied with an analytical model.

One problem observed in a surface tension-driven microfluidic network is the backflow of liquids. Backflow can occur in the surface tension-driven devices including polymer and even paper microfluidic devices, if the devices have at least three channels with a junction and Laplace pressure difference in their inlets. For the surface tension-driven flow, inlet menisci

generate inlet pressures (*i.e.*, the Laplace pressure). Importantly, this pressure significantly affects the motion of the flow. When multiple channels are prefilled with solutions and a solution is injected to an inlet, the inlet of the solution has high Laplace pressure and pushes other solutions to their corresponding inlets. The ideal case is that the initial flow direction in each channel is maintained until the flow stops. However, the flow direction in several channels can often reverse unexpectedly, resulting in backflows. Even when the filling of channels occurs by capillary action, backflow occurs. For example, when liquid fronts of two solutions merge at Y-junction and move to the junction downstream, one solution from an inlet unexpectedly moves back to the other inlet through the Y-junction.^{19–22} Such unwanted motion occurs by the imbalance of the Laplace pressure of inlets. To date, such unwanted backflows have been reported in the process of immunoassay,^{18,19} micromixing,²⁰ blood typing,²¹ and cell-based assay.²² In the case of unexpected backflows in a surface tension-driven bioassay chip, the designed sequence of fluidic motion is changed unintentionally, and the detection of targets will fail. Thus, reducing backflow in network channels is a crucial challenge that must be overcome for such applications. Our recent study showed that backflow results from the difference between the time constant ratios of a network's inlet-channel elements.²³ However, the contributions of network elements including channel fluidic conductance, inlet radius, and pressure to backflow strength were not analyzed in detail.

In this paper, we study the effect of each element of a surface tension-driven network on backflow strength. We model inlet

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† Electronic supplementary information (ESI) available: Modeling pressures of inlet meniscus and channel junction. Modeling the relation between meniscus height and inlet pressure. Change of meniscus height and volume of inlet by inlet radius. Change of volume ratio and inlet pressures by radius of inlet 2. See DOI: 10.1039/c8ra09756a

menisci as variable pressure sources, and channels as fluidic conductors. Using the model, we characterize how the fluidic conductance of channels, and the radius and initial pressures of inlets, influence backflow strength. This analysis systematically explains the complex relations between network elements that affect backflow. Our model is first applied to characterize backflow in a surface tension-driven network with three inlets, and then extended to a network with five inlets.

2. Working process and theoretical modeling

In this section, we explain the process of capillary filling and backflow generation, and then discuss the corresponding theoretical model. Backflow can occur in a channel network consisting of multiple channels, Y-junctions, and multiple branched junctions. During the merging process of the solutions at the junctions, backflows occur by the pressure difference of inlets. To describe the basic process of backflow generation, we used a network with three inlets and three channels. This is the minimum element condition that can describe the backflow in a channel network. Three steps are

used to fill the network and generate the backflow. Fig. 1a depicts the fluidic motion in the network in the last step; the motion is driven by the Laplace pressure of the inlet menisci. Fig. 1b presents each step. In step 1, solution 1 (green) injected at inlet 1 stops at a capillary valve²⁴ of channel 1. In step 2, solution 2 (red) injected at inlet 2 moves through channel 2 to channel 1. The fluidic motion continues until the two inlet pressures equilibrate. Backflow does not occur because only two inlet pressures are involved for fluidic motion. Step 3 consists of two parts (steps 3a and 3b). In step 3a, solution 3 (clear) injected at inlet 3 moves into channels 1 and 2. Then in step 3b, the flow direction in either channel 1 or 2 is reversed and backflow may occur. The right panels of Fig. 1b present two cases with different backflow strengths. In case 1, solution 2 exits inlet 2 and moves back from channel 2 to channel 1, resulting in the strong backflow of solution 2. If channel 1 is the target channel that each solution needs to move into sequentially, then the sequence is disrupted in step 3 by the backflow. In case 2, although the backflow of solution 2 occurs, the flow stops in channel 2 without entering channel 1, and the backflow strength is weak. Thus, the three solutions were successfully injected into channel 1 in a sequential manner.

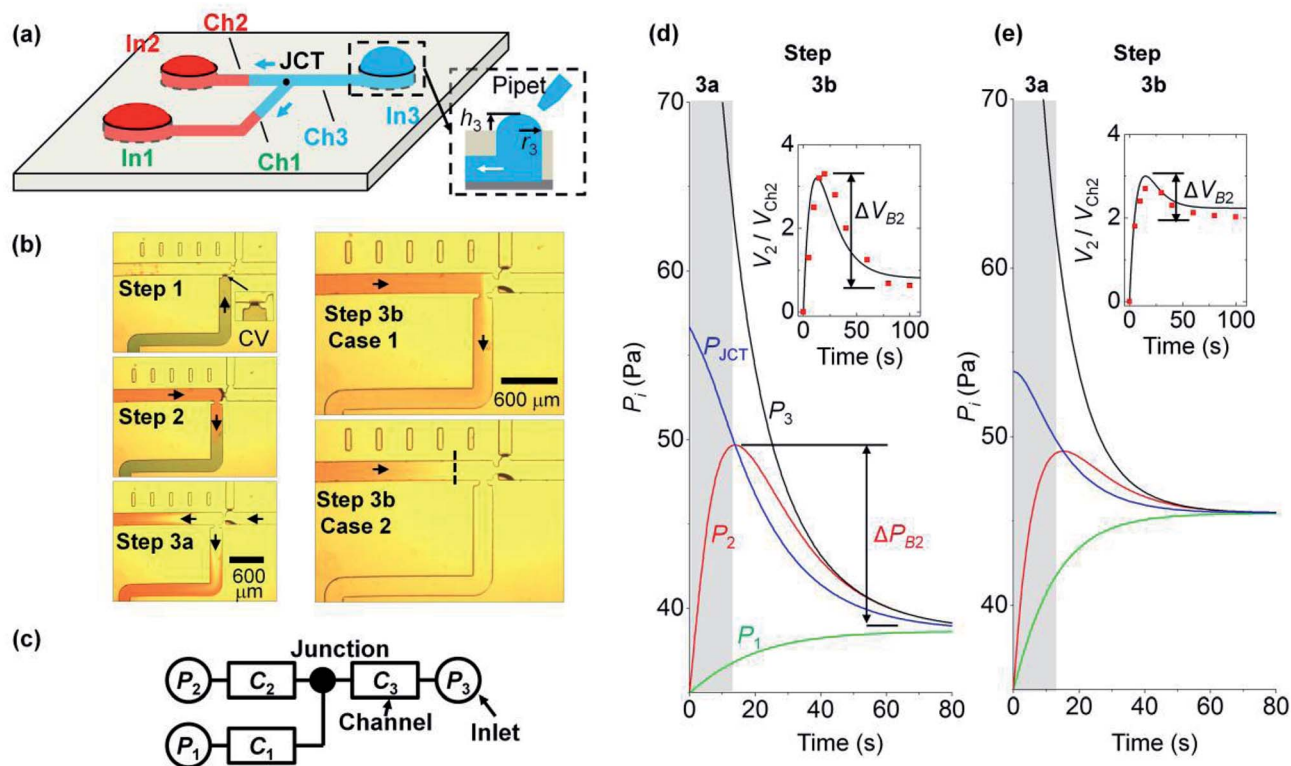


Fig. 1 Surface tension-driven network showing backflow. (a) Generation of fluidic motion by the pressure difference of inlet menisci. Inlets (In i , $i = 1$ to 3) are connected to each other through channels (Ch i) and the junction (JCT). The inset shows the cross-section of inlet 3 with inlet radius r_3 and meniscus height h_3 . (b) Photographs showing backflow generation process. The process consists of three steps, and backflow occurs in step 3b. Cases 1 and 2 show strong and weak backflows, respectively. In step 3, the initial pressures of inlet i (P_{i0}) were the same for both cases with $P_{i0} = 35, 35$, and 100 Pa ($i = 1$ to 3). (c) Circuit diagram of the capillary network. P_i is the pressure of inlet i with radius r_i , and C_i is fluidic conductance of channel i . (d and e) Temporal change in inlet pressures in step 3. Lines and points are the theoretical and experimental values, respectively. Inlet i has pressure P_i in step 3. ΔP_{B2} is the backflow pressure of inlet 2, and ΔV_{B2} is the normalized backflow volume. In (d), $r_i = 2, 1$, and 1 mm ($i = 1$ to 3), and $C_i = 9, 9$, and $9 (\times 10^{-12}) \text{ m}^5 \text{ N}^{-1} \text{ s}^{-1}$. In (e), $r_i = 1.5, 1$, and 1 mm, and $C_i = 12, 9$, and $9 (\times 10^{-12}) \text{ m}^5 \text{ N}^{-1} \text{ s}^{-1}$.



We modeled the process of backflow generation in a surface tension-driven network (Fig. 1c). The inlet menisci were modeled as variable pressure sources because the volume of each meniscus changes in each step, which temporally varies inlet pressures. The channels were modeled as fluidic conductors. The detailed derivation process is explained in Sections 1 and 2 of ESI.† The pressure (P_i) of inlet i is obtained by

$$P_i = \frac{4\sigma h_i}{h_i^2 + r_i^2} \quad (1)$$

where σ is the surface tension of a solution injected into inlet i , h_i is the height of the convex meniscus of the solution at inlet i , and r_i is the radius of inlet i (see inset of Fig. 1a). For eqn (1), the shape of inlet meniscus is assumed to be a spherical cap. This is because gravitational forces on the inlet meniscus are negligible with the small Bond number, $Bo = \rho g L^2 / \sigma < 0.02$. Here, L is the characteristic length and we used the meniscus height. Also, each inlet meniscus is assumed to be pinned to the rim of the inlet. We experimentally confirmed the meniscus pinning at the inlet rim under the condition of height-to-radius ratio $h_i/r_i < 0.5$ and solution contact angle $> 49^\circ$ (Section 3 of ESI†). We note that the condition $h_i/r_i < 0.5$ is satisfied in normal surface tension-driven devices. Also, the condition of solution contact angle $> 49^\circ$ is normally met, because the inlets of surface tension-driven devices typically use hydrophobic or moderately hydrophilic surfaces to confine the solution menisci to the rims of their inlets. Thus, our condition for meniscus pinning at the inlet rim can be considered as valid in most cases.

The pressure (P_{JCT}) at the junction of the channels is obtained by the analogy of Kirchhoff's current law and is given by

$$P_{JCT} = \frac{\sum_{i=1}^j C_i P_i}{\sum_{i=1}^j C_i} \quad (2)$$

where C_i is the fluidic conductance of channel i , which is the inverse of channel fluidic resistance. The change rate of h_i is given by

$$\frac{dh_i(t)}{dt} = \frac{2C_i(P_{JCT} - P_i)}{\pi(r_i^2 + (h_i(t))^2)} \quad (3)$$

Eqn (3) is obtained by the condition where change rate of inlet volume is the same with the flow rate in the channel that connects the corresponding inlet and the junction. In addition, for eqn (2) and (3) we use Poiseuille's law, which neglects the contribution of flow inertia in the relation between pressure and flow rate. This is because the Reynolds number is small ($Re < 0.5$) in our system. In eqn (3), the number of h_i increases with increasing step number. For example, in step 2, h_1 and h_2 are used; and in step 3, h_1 , h_2 , and h_3 are used. The corresponding numbers of P_i , r_i , and C_i also increase with increasing step number. To solve the simultaneous differential form of eqn (3), we measured the initial values of h_i in each step, and used them as the initial condition of each step. The equations were numerically solved with MATLAB.

3. Experimental

We fabricated devices using soft lithography technique.²⁵ The devices have two layers. The top layer was produced from hydrophobic polydimethylsiloxane (PDMS) with channel features, while the bottom layer was comprised of hydrophilic slide glass. The hydrophilicity of the slide glass was increased by an air plasma machine (Femto Science) so that the solutions injected at the inlets can spontaneously fill the channels and meet at the junction. The dimensions of inlets and channels were measured to calculate the fluidic conductance of each channel. The channel dimensions were in the range 60–100 μm (h) \times 180–400 μm (w) \times 1.4–50 mm (l), with inlet radii ranging from 1 to 2.5 mm. The channel dimensions varied C_i in the range of 7×10^{-14} to $9 \times 10^{-12} \text{ m}^5 \text{ N}^{-1} \text{ s}^{-1}$. We used a stereo microscope (Olympus) and digital microscope (Dino-lite) to measure the meniscus height of each inlet. We used de-ionized water for the working solution and food dyes were added for flow visualization.

4. Results and discussion

4.1. Backflow formation process

We analyze backflow formation with our model. Fig. 1d and e show the theoretical change in pressures that correspond to cases 1 (strong backflow) and 2 (weak backflow) in Fig. 1b, respectively. The solutions move from high to low pressure positions. In step 3a (gray region in Fig. 1d and e), the pressure condition is $P_3 > P_{JCT} > P_2$ ($P_{12} = P_{11}$). Thus, solution 3 at inlet 3 moves through the junction to inlets 1 and 2. Owing to the fluidic motions, P_3 decreased and P_1 and P_2 increased. In step 3b (white region), P_2 becomes greater than P_{JCT} , which reverses the flow direction of solution 2 from inlet 2 to the junction. Thus, because $P_2 > P_{JCT} > P_1$, solution 2 moves through the junction toward channel 1 and inlet 1. We note that the backflow volume of solution 2 is different for the two cases. The insets of Fig. 1d and e present the volume ratio (V_2/V_{Ch2}) of the inlet meniscus volume (V_2) and channel 2 volume (V_{Ch2}). V_{Ch2} was fixed at 30 nL, and the initial value of V_2 was expressed as 0 by subtracting its initial volume from V_2 . During backflow, V_2/V_{Ch2} decreases because solution 2 is released from inlet 2. To quantify the backflow volume at inlet 2, we define normalized backflow volume (ΔV_{B2} , see the insets) at inlet 2 as $\Delta V_{B2} = (V_{2P} - V_{2E})/V_{Ch2}$, where V_{2P} and V_{2E} are the volumes of inlet 2 meniscus at the peak and equilibrium states of P_2 , respectively. The corresponding backflow pressure at inlet 2 (ΔP_{B2}) is defined in Fig. 1d. If $\Delta V_{B2} > 1$ (i.e., $V_{2P} - V_{2E} > V_{Ch2}$), then the volume that goes out of inlet 2 is greater than the channel 2 volume, so the backflow of solution 2 moves through channel 2 to another channel. This case is shown in the inset of Fig. 1d, where $\Delta V_{B2} = 2.8 > 1$ (case 1 in Fig. 1b). In contrast, in the inset of Fig. 1e, $\Delta V_{B2} = 0.6 < 1$, so solution 2 does not go out of channel 2 even for its backflow (case 2 in Fig. 1b). We analyzed how P_{1i} , r_i , and C_i influence the backflow strength at inlet 2.

We note that the backflow shown in this system does not result from inertia of fluids. This is because the Reynolds number (Re), which is the ratio of inertia to viscous force, was



$Re < 0.5$ in our system. For the inertia effect to be dominant, Re needs to be high. Indeed, the studies that reported backflows even in single channel systems had $Re > 10$, owing to large channel size and high inlet pressure driven by repeated injection of small drops.^{26–29} In addition, we used a solution containing food dye with the same concentration (3.6% by weight). Thus, there was no flow induced by concentration gradient.

4.2. Effect of fluidic conductance and channel size on the backflow

We study the effect of the fluidic conductance of channel i (C_i , $i = 1$ to 3) on the backflow. When one fluidic conductance was changed, the others were fixed at $7 \times 10^{-12} \text{ m}^5 \text{ N}^{-1} \text{ s}^{-1}$. In step 3, inlet 3 releases solution 3 to the other inlets, inlet 2 is the place where backflow occurs, and inlet 1 takes the backflow solution. We analyze the backflow of inlet 2 under the change of C_i . Fig. 2a shows that high C_1 decreases ΔP_{B2} and ΔV_{B2} . This behavior is explained by the fast rise of P_1 and its resultant small difference between P_1 and P_2 . When C_1 increases, solution 3 injected from inlet 3 can easily move to inlet 1 rather than inlet 2. This is because comparatively high fluidic conductance of channel 1 allows rapid fluidic transport through channel 1 to inlet 1. As a result, P_1 rapidly increases, according to the comparison P_1 in the gray region of Fig. 1e and d. When P_1 becomes high, the difference between P_2 and P_1 decreases (step 3b in Fig. 1d and e). Thus, the backflow that moves from inlet 2 toward inlet 1 decreases. Compared to C_1 , high C_2 increases ΔP_{B2} and ΔV_{B2} (Fig. 2b). This is because, with high C_2 , solution 3 can easily move through channel 2 to inlet 2, thereby causing a more rapid increase in P_2 in step 3a. Similar to C_2 , C_3 increases ΔP_{B2} and ΔV_{B2} (Fig. 2c). With high C_3 , inlet 3 releases solution 3 more rapidly to the other channels through channel 3. This significantly increases P_2 in step 3a and leads to high ΔP_{B2} and ΔV_{B2} in step 3b. In addition, when the size of channel 2 increases under constant condition of C_2 , ΔV_{B2} decreases. This result is analyzed in Section 4 of ESI.†

The backflow of inlet 2 by the change of C_i can be collectively explained. High C_2 and C_3 increase backflow of inlet 2. This is because, at step 3a, solution 3 moves more rapidly to inlet 2 through channels 2 and 3 owing to high C_2 and C_3 . On the other hand, high C_1 decreases the backflow of inlet 2. This is because

solution 3 moves more to inlet 1 rather than inlet 2 by the high fluidic conductance of channel 1 in step 3a and finally reduces the backflow of inlet 2 by the small pressure difference between inlets 1 and 2.

4.3. Influence of inlet radius and inlet pressure on the backflow

Here, we analyze the effect of inlet radius on the backflow of inlet 2. Fig. 3a shows how the three inlets influence ΔP_{B2} . First, the left panel of Fig. 3a shows that high r_1 increases ΔP_{B2} . This is because high r_1 makes the change of P_1 gradual (eqn (1)), leading to larger difference between P_1 and P_2 at the end of step 3a (Fig. 1d). As a result, ΔP_{B2} increases in step 3b. For the two cases of C_i (7, 7, and 7; and 5, 9, and 10 ($\times 10^{-12} \text{ m}^5 \text{ N}^{-1} \text{ s}^{-1}$)), this trend is maintained. Second, the middle panel of Fig. 3a shows that high r_2 decreases ΔP_{B2} . This is because increasing r_2 reduces the change rate of P_2 (eqn (1)), and P_2 gradually increases in step 3a (Fig. 1d). Thus, difference between P_1 and P_2

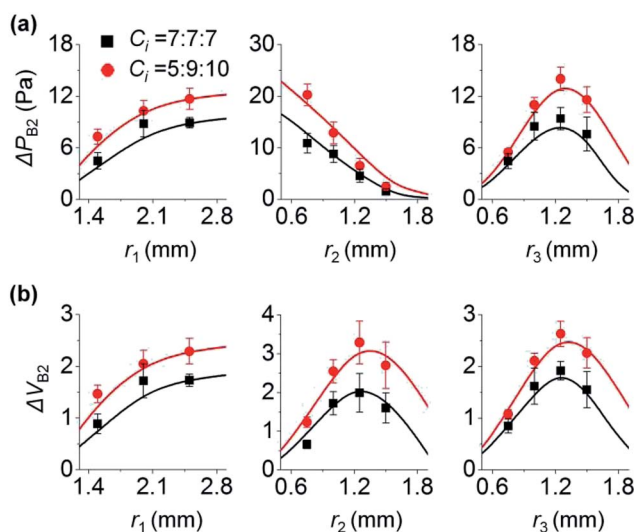


Fig. 3 Influence of inlet radius r_i on the backflow of inlet 2. Unless otherwise noted, $r_1 = 2 \text{ mm}$, and $r_2 = r_3 = 1 \text{ mm}$. In step 3, $P_{i1} = 35, 35$, and 75 Pa ($i = 1$ to 3). ΔP_{B2} and ΔV_{B2} are shown in (a) and (b), respectively. Lines and points are the theoretical and experimental ($n = 3$) values, respectively.

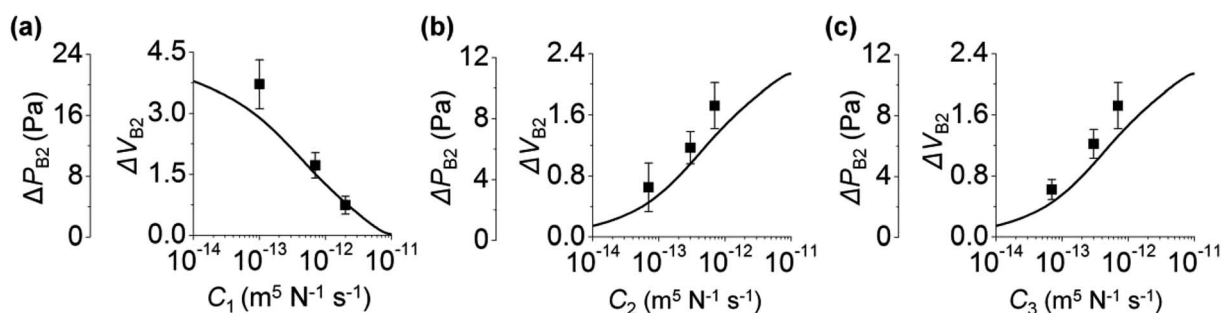


Fig. 2 Influence of C_i on the backflow of inlet 2. When one fluidic conductance was changed, the others were fixed at $7 \times 10^{-12} \text{ m}^5 \text{ N}^{-1} \text{ s}^{-1}$. Here, $r_i = 2, 1$, and 1 mm ($i = 1$ to 3). In step 3, $P_{i1} = 35, 35$, and 75 Pa . Variations of ΔP_{B2} and ΔV_{B2} by C_1 are shown in (a), by C_2 in (b), and by C_3 in (c). Lines and points are the theoretical and experimental ($n = 3$) values, respectively.



at the end of step 3a in Fig. 1d becomes small, thereby reducing ΔP_{B2} . Third, unlike the cases of r_1 and r_2 , increasing r_3 does not monotonously vary ΔP_{B2} (right panel of Fig. 3a). When r_3 increases from 0.6 to 1.2 mm, ΔP_{B2} increases. Herein, the initial pressure of inlet 3 was kept at $P_{13} = 75$ Pa regardless of r_3 . To meet the constant P_{13} condition even for increasing r_3 , the initial meniscus volume of inlet 3 increases (Section 5 of ESI†). Consequently, a larger amount of solution 3 goes from inlet 3 to inlet 2, thereby increasing ΔP_{B2} . On the other hand, when r_3 becomes greater than 1.2 mm, ΔP_{B2} decreases. We explain this result by using the difference between P_2 and P_{JCT} that influences the flow from inlet 2 to the junction. Backflow occurs in step 3b only when $P_2 > P_{JCT}$ (Fig. 1d). Importantly, backflow decreases if $P_2 - P_{JCT}$ is small in step 3b; compare Fig. 1d and e. High r_3 let P_{JCT} stay at a high value through P_3 in step 3b (Fig. 1d). This is because P_{JCT} is considered as the weighted average of inlet pressures including P_3 (eqn (2)) and slow decrease of P_3 by high r_3 let P_{JCT} remain at a high value. Accordingly, pressure difference between P_{JCT} and P_2 decreases in step 3b, decreasing ΔP_{B2} .

Collectively, when inlet 1 receives backflow from inlet 2, high r_1 decreases the difference between P_1 and P_2 at step 3a, leading to lower ΔP_{B2} at step 3b. Oppositely, high r_2 increases the difference between P_1 and P_2 , thus increasing ΔP_{B2} at step 3b. Increasing r_3 rises ΔP_{B2} at first because of large volume of inlet 3 meniscus, and then reduces decreases ΔP_{B2} because of the low difference between P_2 and P_{JCT} at step 3b.

The change in ΔV_{B2} follows the trend of ΔP_{B2} when r_1 and r_3 vary (left and right panels of Fig. 3). As shown in Fig. 2, with C_i variation, ΔV_{B2} and ΔP_{B2} changed in the same manner. On the other hand, ΔV_{B2} varied differently with ΔP_{B2} with the change in r_2 (middle panels of Fig. 3). ΔV_{B2} increases when r_2 increases from 0.6 to 1.2 mm, and then decreases when $r_2 > 1.2$ mm. The increasing r_2 lets inlet 2 take more fluids from inlet 3 in step 3a (Section 6 of ESI†). This allows inlet 2 to release a greater amount of backflow volume in step 3b for $0.6 < r_2 < 1.2$ mm. However, with increasing r_2 , the reduction of P_2 becomes more gradual in step 3b while P_{JCT} insignificantly changes by r_2 . This leads to the reduced difference between P_{JCT} and P_2 , thus decreasing ΔV_{B2} for $r_2 > 1.2$ mm in step 3b.

To study the effect of the initial inlet pressures (P_{1i}) in step 3 on the backflow, P_{1i} values were varied and the backflow at inlet 2 was measured. Here, P_{13} was 75 Pa for different values of P_{12} , with $P_{12} = P_{11}$. We used three sets of C_{ij} as shown in Fig. 4. Under this condition, ΔP_{B2} and ΔV_{B2} unanimously increased with the increasing $P_{13} - P_{12}$. This is because at higher $P_{13} - P_{12}$, a comparatively larger amount of inlet meniscus volume is used for inlet 3, which results in higher ΔP_{B2} and ΔV_{B2} .

4.4. The effect of increasing step on reducing the backflow

So far, we have studied the backflow in surface tension-driven networks with three inlets and three channels. Now, we expand our understanding to surface tension-driven networks with five inlets and five channels with one junction. Fig. 5a shows the circuit diagram of the surface tension-driven network. Solution i was injected at inlet i in step i , and the

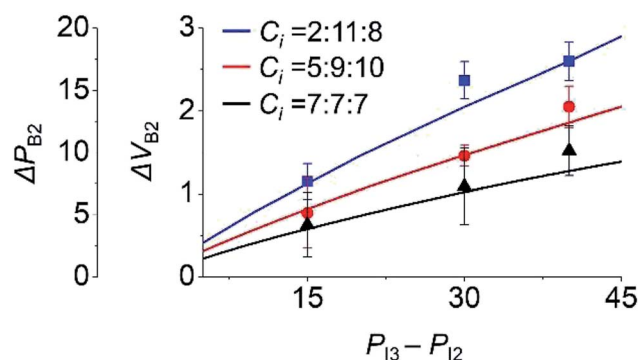


Fig. 4 Effect of initial pressure (P_{1i}) of inlet i in step 3 on the backflow of inlet 2. Lines and points are the theoretical and experimental ($n = 3$) values, respectively.

initial pressures of inlet i in step i were 35, 35, 75, 75, and 75 Pa, respectively. The left to right panels of Fig. 5b show the change in ΔP_{Bi} and ΔV_{Bi} at inlet i ($i = 1$ to 3). For example, inlet 4 (right panel) shows the changes in ΔP_{B4} and ΔV_{B4} only in step 5 without steps 3 and 4. This is because the injection to inlet 4 occurs in step 4, and inlet 4 is empty before step 4. Similarly,

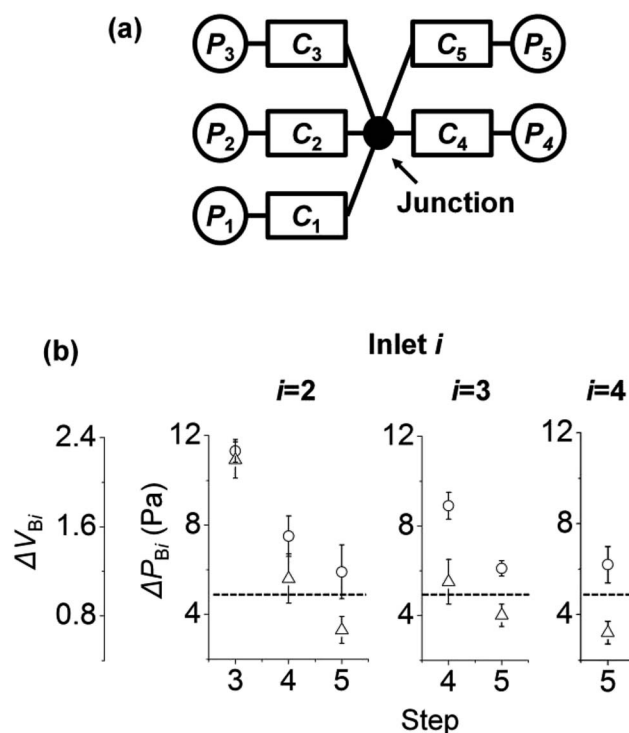


Fig. 5 Backflow in surface tension-driven networks with five inlets and five channels. (a) Circuit diagram of the surface tension-driven network. (b) Change of ΔP_{Bi} and ΔV_{Bi} at inlet i ($i = 2$ to 4). Symbols designate subsets: circles for case 1; triangles for case 2. In case 1, $C_j = 5, 10, 9, 13$, and $13 (\times 10^{-12}) \text{ m}^5 \text{ N}^{-1} \text{ s}^{-1}$ ($j = 1$ to 5). In case 2, $C_j = 5, 10, 9, 5, 4 (\times 10^{-12}) \text{ m}^5 \text{ N}^{-1} \text{ s}^{-1}$. For both cases, $r_j = 2, 1, 1, 1$, and 1 mm. For $\Delta V_{Bi} < 1$ (under the dashed line), the backflow of inlet i stays in channel i and does not go into other channels. The error bars were obtained from five experiments.



inlet 3 (middle panel) shows the variations in ΔP_{B3} and ΔV_{B3} only in steps 4 and 5, without step 3.

For inlets 2 and 3, ΔP_{Bi} and ΔV_{Bi} decrease as the step number increases. The initial pressures of inlets increase with increasing step number. This is because by adding solutions to inlets, the volumes of inlet menisci increase as the step number increases. On the other hand, we set the initial pressure of inlet i in step i ($i = 3$ to 5) as constant at 75 Pa. As a result, the initial pressure difference between inlet i and the other inlets in step i decreased. In Fig. 4, we explained that the backflow pressure at inlet 2 decreases if the pressure difference between P_{13} and P_{12} is reduced in step 3. Thus, similar to the case in Fig. 4, ΔP_{Bi} and ΔV_{Bi} decrease with increasing step number. In addition, if ΔV_{Bi} is under the dashed lines ($\Delta V_{Bi} < 1$) in Fig. 5b, then the backflow of inlet i stays in channel i and does not go into other channels.

In addition, our model is broadly applicable to analyze the backflow of the paper microfluidic devices as well as polymer devices. This is because, even for a paper device with porous layer, its inlet pressure can be modeled as variable pressure source by Laplace pressure and its channels can be modeled as fluidic conductor. Specifically, although paper channels follow Darcy's law and polymer channels obey Poiseuille's law, in the two laws flow rate (Q) is commonly proportional to pressure difference (ΔP). That is, $Q = C\Delta P$, where C is fluidic conductance of a channel. C is $Ak/(\mu L)$ in a paper channel and is $\pi r^4/(8\mu L)$ in a polymer channel with circular cross section. Here, A is cross sectional area of channel, μ is viscosity, L is filled channel length, k is permeability, r is channel radius. Thus, because of the similarity between the two channel types, our model is applicable to paper microfluidic devices.

5. Conclusion

Our main contributions for a surface tension-driven network, where the pressure difference of the inlet menisci drives fluidic motions, are as follows: (i) developing a detailed model that describes the backflow strength of the surface tension-driven network; (ii) analyzing the contributions of network parameters (e.g., fluidic conductance of channels, inlet radius, and initial pressure of inlets) to the backflow strength; (iii) characterizing the nonlinear relation between backflow volume and backflow pressure by the change of inlet radius; and (iv) presenting the change in backflow pressure with increasing step numbers.

We showed that each network element, including channel and inlet, has distinct characteristics that affect the change in inlet pressure. A large inlet size makes the change in the corresponding inlet pressure slow. Low fluidic conductance of a channel also makes the pressure change of the inlet directly connected to the channel slow. These two characteristics result in the complex behaviors of inlet pressures when the network elements constitute a surface tension-driven network. Backflow pressure decreases with the decrease (increase) in the corresponding fluidic channel conductance (inlet size). On the other hand, backflow volume reaches its peak value in the middle of the radius change of the corresponding inlet. This is because the inlet pressure was strongly affected by the radius change,

but other inlet pressures were insignificantly influenced. In addition, we showed that backflow strength decreases when the initial pressure difference between the inlets decreases. Finally, we showed that in networks consisting of five inlet-channel elements, backflow pressure decreases as the step number increases because the pressure difference between the inlet where the solution is injected and the other inlets decreases. Findings in this study provide useful guidelines for controlling backflow in surface tension driven networks. Further studies could be performed to analyze and prevent backflows in more complex microfluidic networks with multiple junctions.

Conflicts of interest

There are no conflicts of interest to declare.

Acknowledgements

This study was supported by Konkuk University in 2016.

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