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The surface passivation of Ge(100) and Ge(111) anodes in Ge–air batteries with different doping types and concentrations†

Yingjian Yu,^{id}*^{abc} Danshuo Chen,^a Shaoshuai Gao,^a Jian Huang,^a Sujuan Hu,^d Hai Yang^{ab} and Guojun Jin^{ab}

The surface passivation of Ge(100) and Ge(111) anodes in Ge–air batteries with different doping types and concentrations is analyzed by density function theory (DFT) calculations. Compared with Ge(111) anodes, the surface passivation is restrained on Ge(100) anodes as they have larger binding energies with GeO₂ layers. Meanwhile, doping would hinder the formation of a GeO₂ layer on Ge anodes, especially for p-type doping, like B. The dissimilarities of the electrostatic potential differences and projected local density of states between the p-type Ge(100)/GeO₂ and Ge(111)/GeO₂ also reveal the origins of their distinct performances in Ge–air batteries. Furthermore, the *I*–*V* curves show that the Ge(100)/GeO₂/Ge(100) device has a higher current than the Ge(111)/GeO₂/Ge(111) device. This work would help to fundamentally comprehend the different electrochemical properties of Ge–air batteries with different orientations and doping and provide guidelines for the design of Ge anodes in Ge–air batteries.

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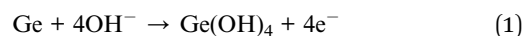
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Introduction

In recent decades, the energy revolution has moved to the top of the agenda around the world due to the shortage of fossil fuels and severe climate change. Nowadays, green energy systems, *e.g.* lithium ion batteries,¹ fuel cells,² and solar cells,³ are playing a critical role in human life. Among them, air batteries, with high energy/power densities and widely distributed raw materials, can be potentially applied to automotive vehicles, traffic signal systems, offshore power facilities and portable power supplies.^{4,5} What makes air batteries distinctive is their negligible cathode volumes since the oxidant (oxygen) can be directly obtained from the air. Metal–air batteries have been extensively studied, such as Li–air batteries,⁶ Al–air batteries⁷ and Zn–air batteries;⁸ however, challenges like dendrite formation still exist.⁹ Germanium has been introduced as the anode material in semiconductor air batteries, and exhibits high capacities and ideal safety.^{10–12} During the discharge process, the germanium oxidation reaction and the oxygen reduction reaction (ORR) occur in the anode and cathode. Meanwhile, the germanium

hydroxide dehydrates to its oxide, which would passivate the Ge anode surface and prevent further discharging. Eventually, the Ge/GeO₂ interface forms.^{10–12}

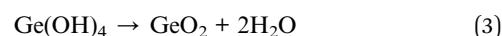
Anode discharge:



ORR:



Surface passivation:



Experiments have shown that the performances of Ge–air batteries are significantly affected by the doping and crystal orientations of Ge anodes.^{11,12} In general, p-type Ge anodes with the (100) crystal indices show better discharge properties. To further improve the fundamental understanding of the physics and chemistry of the Ge–air batteries, theoretical investigations on the surface passivation and properties of the Ge/GeO₂ interface in the cell become the urgent demands, which may provide guidelines to design the Ge anode.

In this work, atomic model structures of the Ge/GeO₂ interfaces with different Ge crystal orientations, doping types and concentrations were constructed and density functional theory (DFT) calculations were conducted. It was found that the GeO₂ layer prefer to form on the Ge(111) rather than Ge(100), and p-doped Ge may resist the surface passivation more obviously. The electrostatic difference potentials and projected local

^aCollege of Physics Science and Technology, Kunming University, Kunming, Yunnan, 650214, China. E-mail: yuyingjiankmu@163.com

^bNational Laboratory of Solid State Microstructures, Nanjing University, Nanjing, 210093, China

^cFujian Province Key Laboratory of Semiconductor Materials and Application, Xiamen University, Xiamen, Fujian, 361005, China

^dDepartment of Chemistry, Kunming University, Kunming, Yunnan, 650214, China

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density of states of the Ge(100)/GeO₂ and Ge(111)/GeO₂ interfaces were also calculated. Moreover, the *I*-*V* curves show that the Ge(100)/GeO₂/Ge(100) device has a higher current than the Ge(111)/GeO₂/Ge(111) device. This work would help to understand the different electrochemical properties of Ge-air batteries with different orientations and doping fundamentally.

Method

DFT calculations^{13,14} within the generalized gradient approximation (GGA) were performed using the Atomistix ToolKit (ATK) code from QuantumWise.¹⁵ The exchange–correlation functional of Perdew–Burke–Ernzerhof (PBE) was used for the GGA calculations.^{16,17} In the calculations of the models of Ge/GeO₂ interfaces, a 4 × 4 × 1 *k*-point mesh was used. The presented models were structurally relaxed within the force tolerance of 0.01 eV Å⁻¹. The thickness of the vacuum layer is 10 Å. The convergence tests of the *k*-point mesh and the thickness of the vacuum layer are shown in Fig. S1 and S2 in the ESI.† The methodology on the electrostatic potential difference, projected local density of states (PLDOS), transmission spectra and *IV* curves are detailed in ESI.†

Results and discussion

Atomic configurations of Ge(100)/GeO₂ and Ge(111)/GeO₂ models are shown in Fig. 1a and b. In the Ge(100)/GeO₂ model, the 3-fold bonded Ge and 3-fold O can be visualized at the interface, with the average Ge–O bond length of ~2.02 Å and average Ge–O–Ge bond angle of ~116.84°. For comparison, in the Ge(111)/GeO₂ model, the Ge slabs and GeO₂ layer are linked by the 2-fold O. The average Ge–O bond length is ~1.97 Å and average Ge–O–Ge bond angle is ~110.27°, which are both smaller than those in the Ge(100)/GeO₂ model, indicating the stronger coalescent of the Ge(111)/GeO₂ interface. To describe it quantitatively, the binding energy of Ge/GeO₂ interfaces is calculated by the definition of

$$E_{\text{b,Ge/GeO}_2} = (E_{\text{Ge/GeO}_2} - E_{\text{Ge}} - E_{\text{GeO}_2})/n, \quad (4)$$

where $E_{\text{Ge/GeO}_2}$ represents the total energy of the model of Ge/GeO₂ interface, E_{Ge} and E_{GeO_2} denote the total energies of the Ge slabs and GeO₂ layer in the corresponding model, and *n* stands for the number of GeO₂ units in the GeO₂ slab, respectively. The binding energies of various interfaces are summarized in Table 1. Apparently, the binding energy of the Ge(111)/GeO₂ interface is 0.53 eV, which is smaller than that of the Ge(100)/GeO₂ interface (1.61 eV), evidencing that the GeO₂ units prefer to form on the Ge(111) surface. During the discharge processes in Ge-air batteries, more GeO₂ units would accumulate on the Ge(111) surface and the discharge may be inhibited sooner by the passivation, which will decrease the lower power density of Ge-air batteries based on Ge(111).¹² Furthermore, the binding energies of Ge(100)/GeO₂ interfaces with different GeO₂ units have been investigated as shown in Fig. S3,† and an O vacancy has also been taken into consideration.¹⁸ In Fig. S3a,† there are 8 units of GeO₂ on the Ge(100) surface, and the calculated

binding energy is 2.12 eV. After taking an O vacancy into consideration (Fig. S3b†), the binding energy increases to 2.74 eV. The incorporation of an O vacancy causes the changes of bonds in the Ge/GeO₂ interface such as the newly formed Ge–Ge bonds, which may enhance the binding energy. When the unit of GeO₂ increases to 12 (Fig. S3c and d†), the binding energy without/with an O vacancy is 1.84/2.48 eV. In the previous experimental works, the GeO₂ layer accumulates on the Ge anodes during the discharge process in Ge-air battery.^{10–12} It can be concluded that the binding energy decreases when the unit of GeO₂ increases, as the effect of the Ge(100) substrate becomes less significant. The introduction of an O vacancy would cause a larger binding energy, indicating the instability of oxygen vacancy defective GeO₂ on the Ge(100).

In experiments, Ge anodes in Ge-air batteries are usually doped, thus the effects of the doping types on the binding energies are also explored in the Ge(100)/GeO₂ and Ge(111)/GeO₂ models. As exhibited in Fig. 1c and d, one Ge atom in the first and second slab is substituted by one B atom, respectively. In the Ge(100)–B/GeO₂ model in Fig. 1c, the B atom in the first slab forms two B–O bonds with lengths of 1.38 and 1.31 Å and one B–Ge bond with the length of 2.14 Å. The binding energy increases to 5.82 eV dramatically compared with that of Ge(100)/GeO₂ model without doping, suggesting that the B-doped Ge(100) anode has a positive effect to avoid the surface passivation.¹¹ In the case of the substitution in the second slab, the fourfold coordinated B atom has four bonds with Ge with an average length of 2.13 Å. The binding energy also increases to 5.63 eV, evidencing the conclusion above. Moreover, it can be concluded that the binding energy is more sensitive to the doping closer to the Ge(100)/GeO₂ interface with a larger binding energy. Similar phenomena can be found in the case of Ge(111)/GeO₂ interface as shown in Fig. 1d. The B atom in the first slab forms two B–Ge bonds with lengths of 2.09 and 2.16 Å and one B–O bond with the length of 1.31 Å. For B doped in the second slab, the fourfold coordinated B atom can be visualized which has four bonds with Ge with an average length of 2.16 Å. In both cases of Ge(111)–B/GeO₂, the binding energies increase apparently compared with those of Ge(111)/GeO₂ without doping, suggesting that the B-doped Ge(111) anode is also beneficial to prevent the severe passivation on the surface of anode. It is deserved to mention that the binding energies in the Ge(100)–B/GeO₂ interfaces are both larger than those in the corresponding Ge(111)–B/GeO₂, which conform to the comparison between Ge(100)/GeO₂ and Ge(111)/GeO₂ models, theoretically illustrating the better experimental electrochemical properties of Ge(100) anodes.

Besides doping by the B atom, various kinds of doping by the N atom are also analyzed in the Ge(100)/GeO₂ and Ge(111)/GeO₂ models as exhibited in Fig. 1e and f. In Fig. 1e, the N atom in the first slab forms one N–O bond (1.24 Å) and two N–Ge bonds with lengths of 2.07 and 2.12 Å after relaxation; the N atom in the second slab has three N–Ge bonds with an average length of 1.98 Å. In Fig. 1f, the N atom in the first slab forms two N–Ge bonds (1.84 Å and 1.83 Å); the fourfold coordinated N atom in the second slab has four N–Ge bonds with an average length of 2.10 Å.



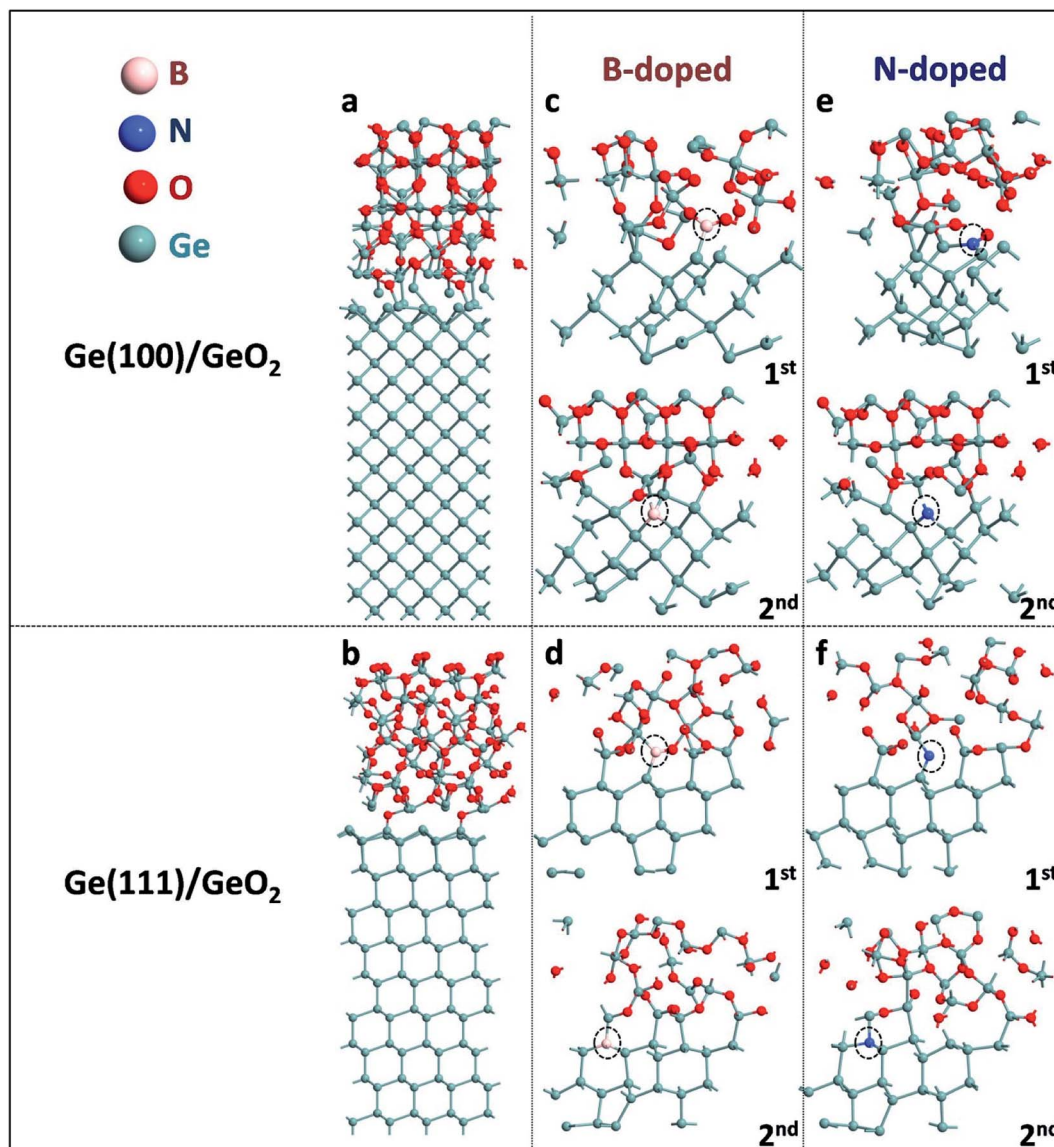


Fig. 1 Atomic configurations of (a) Ge(100)/GeO₂ and (b) Ge(111)/GeO₂ interfaces; the interfaces of B-doped (c) Ge(100)/GeO₂ and (d) Ge(111)/GeO₂ by substituting one Ge atom in the 1st and 2nd slab with one B atom, respectively; the interfaces of N-doped (e) Ge(100)/GeO₂ and (f) Ge(111)/GeO₂ by substituting one Ge atom in the 1st and 2nd slab with one N atom, respectively.

Table 1 The binding energies (eV) of Ge(100)/GeO₂ and Ge(111)/GeO₂ interfaces with different kinds of doping

| | Ge(100)/GeO ₂ | | Ge(111)/GeO ₂ | |
|-----------------|--------------------------|------|--------------------------|------|
| None | 1.61 | | 0.53 | |
| Doped | B | N | B | N |
| 1 st | 5.82 | 5.39 | 5.39 | 5.38 |
| 2 nd | 5.63 | 5.38 | 5.32 | 5.11 |

According to the corresponding binding energies of those models in Table 1, reasonable conclusions can be concluded: (i) doping by the N atom also helps to alleviate the passivation on the Ge(100) and (111) surfaces; (ii) the binding energies are more sensitive to the N/B atom closer to the Ge/GeO₂ interface;

(iii) the B-doped Ge anode is a better candidate for Ge-air batteries than the N-doped Ge anode. Furthermore, all the Ge(100) substrates exhibit larger binding energies than corresponding Ge(111) substrates, theoretically revealing that Ge(100) anodes would show better electrochemical properties than Ge(111) anodes. That phenomenon has already been found in experiments by Ocon.¹²

The bonds formed by heteroatoms in the first slab are analyzed by charge density difference as shown in Fig. 2. Both in the Ge(100)/GeO₂ and Ge(111)/GeO₂ models, there are charge transfer of $\sim 0.2 \text{ e}\text{\AA}^{-3}$ to form the B-Ge bonds and N-Ge bonds. The charge transfer between the N and O atom is more distinct ($\sim 0.3 \text{ e}\text{\AA}^{-3}$), indicating the stronger binding of the interface induced by the N doping. It can be found that the dopants like B and N near the Ge/GeO₂ interface would affect the configuration



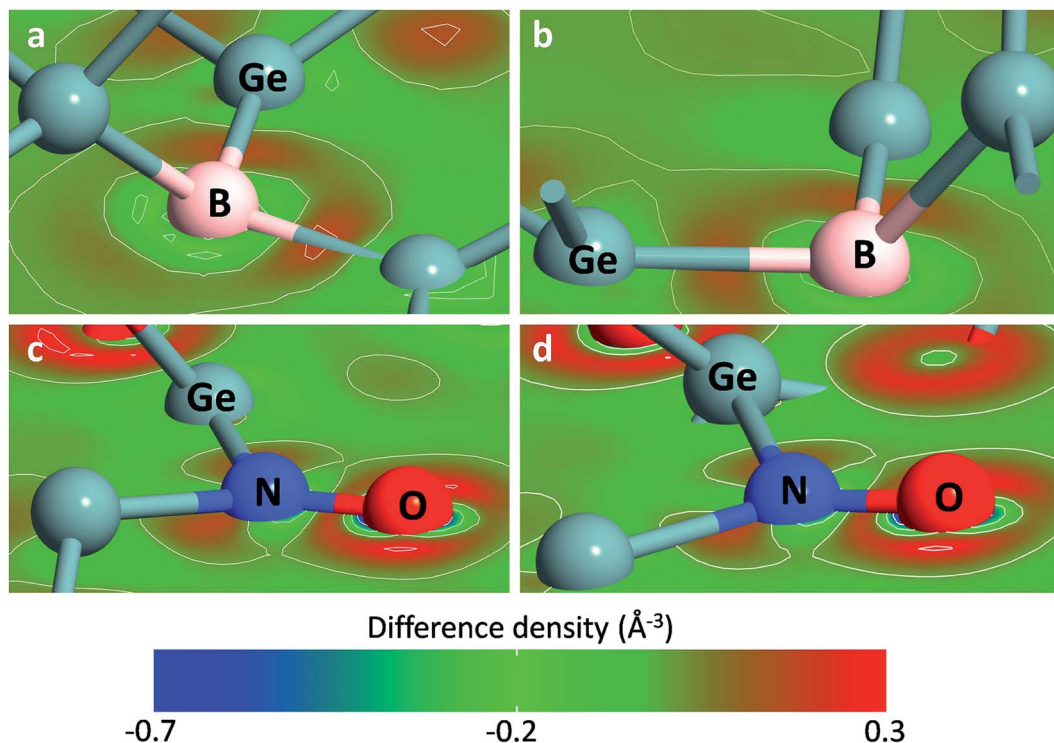


Fig. 2 The charge density difference of B-doped (a) Ge(100)/GeO₂ and (b) Ge(111)/GeO₂ interfaces and N-doped in the (c) Ge(100)/GeO₂ and (d) Ge(111)/GeO₂ interfaces.

of the interface obviously by forming the B–O, B–Ge, N–O and N–Ge bonds. Also, the charge transfer would be affected by the introducing of dopants. As a result, the binding energy would be significantly impacted by the dopant in the first or second slab for both Ge(100) and Ge(111) orientations.

Since doping by B leads to better performances, for simplicity, the binding energies of p-type Ge(100)/GeO₂ and p-type Ge(111)/GeO₂ models with various doping concentrations are calculated to strength the viewpoint, as shown in Fig. 3. In experiments, the Ge wafers with doping concentrations of 10¹⁴,

10¹⁶ and 10¹⁸ are usually considered to be slightly, medium and heavily doped; so the doping concentrations larger than 10¹⁴ are investigated. Using the ATK code, different doping concentrations can be modeled by doping charge to the selected Ge atoms without explicitly introducing dopant atoms (detailed in Fig. S4†). In the full range of 10¹⁴ to 10²¹, the p-type Ge(100)/GeO₂ models have larger binding energies than those of p-type Ge(111)/GeO₂ models and Ge(100)/GeO₂ models without doping, which verify the conclusion above. It cannot be neglected that the binding energies decrease markedly when the Ge substrates are doped with the concentration of 10²¹. Those relaxed models have the elongation of ~2% along the *c* axis than the models with the doping concentration of 10¹⁶. Meanwhile, the p-type Ge(111) with the doping concentration of 10²¹ are linked with GeO₂ layer by only twofold O atoms; however, both twofold and threefold O atoms can be seen across the interface in Fig. 4b (10¹⁶). Those differences between the models with doping concentrations of 10¹⁶ and 10²¹ may lead to the variations of the binding energies.

Besides the binding energies, the electrostatic difference potentials are analyzed to disclose the differences between the p-type Ge(100)/GeO₂ and p-type Ge(111)/GeO₂ interfaces as shown in Fig. 4. Similar offsets of 3–4 V can be found across the p-type Ge/GeO₂ interfaces in Fig. 4a and b, which result from the differences in electronegativities between Ge and O.¹⁹ It is worth mentioning that the electrostatic difference potentials rise apparently across the GeO₂/vacuum in Fig. 4a; however, the rising in Fig. 4b is not that obvious. The differences in the electrostatic difference potentials imply that it would be

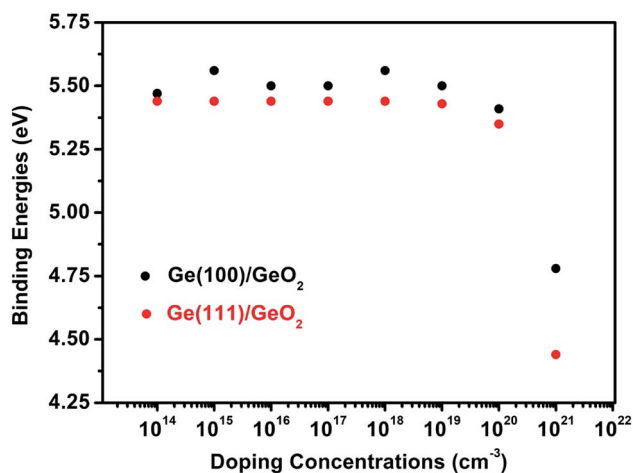


Fig. 3 The binding energies of p-type Ge(100)/GeO₂ and p-type Ge(111)/GeO₂ with various doping concentrations.



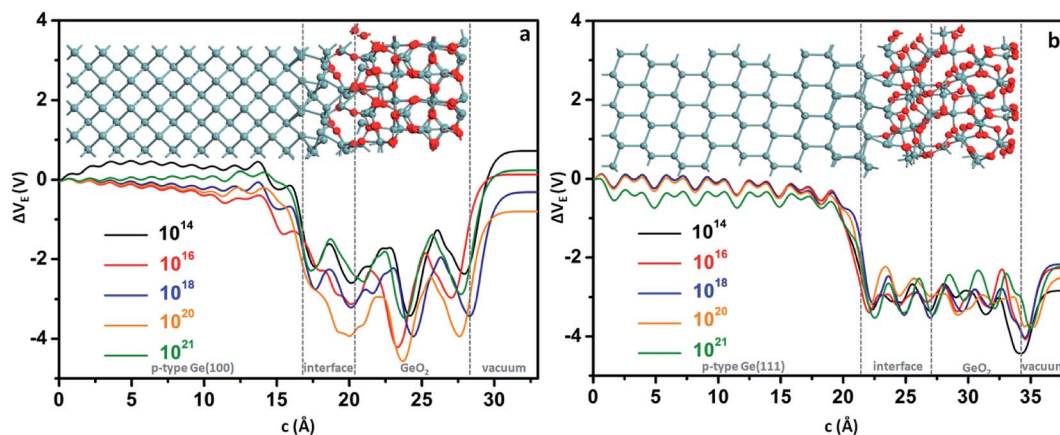


Fig. 4 The electrostatic potential difference near the interfaces: (a) p-type Ge(100)/GeO₂ and (b) p-type Ge(111)/GeO₂ interfaces with different doping concentrations. The models shown in the figure have a medium doping concentration of 10¹⁶.

favourable for the electrons to transfer from the Ge(100) anode to the air cathode *via* the GeO₂ passivation layer in discharge processes.

The projected local density of states (PLDOS) of the p-type Ge(100)/GeO₂ and p-type Ge(111)/GeO₂ with the doping concentration of 10¹⁶ are displayed in Fig. 5a and b. The PLDOS offers a highly useful visualization of the band diagram of the interface. It nicely shows the electronic structure across the full length of the interface and the band gaps of the left and right side of the Ge/GeO₂ interface can be visualized clearly. The similar band gap of ~0.55 eV can be found in the regions of Ge(100) and Ge(111) substrate; however, a more distinct valence band demarcation can be visualized in the Ge(111)/GeO₂ model with a larger band gap of ~2.58 eV in the region of GeO₂ layer than that of ~2.40 eV in the Ge(100)/GeO₂ model. The larger band gap would probably hinder the electron transfer and result in a higher resistivity.¹² The band gap of Ge measured at 300 K is 0.66 eV (ref. 20) and that of GeO₂ is 4.68 eV.²¹ Our values are smaller than the experimental data due to the well-known underestimation of conduction band state energies in DFT calculations. The PBE has been widely used in the theoretical investigation of the Ge/GeO₂ interface.^{17,22,23} In this work, the calculated band gap of Ge is only 0.11 eV smaller than the experimental value, and this band gap is larger than that in the

previous work (0.4 eV).¹⁷ Given the well-known underestimation of the band gap with PBE, the calculated value in this work is acceptable and reasonable.

To investigate the transmission spectra and *I-V* characteristics of the Ge(100)/GeO₂ and Ge(111)/GeO₂ interfaces, the devices of Ge(100)/GeO₂/Ge(100) and Ge(111)/GeO₂/Ge(111) are constructed as shown in Fig. 6a. Smaller models are used here because the calculations of the transmission spectra and *I-V* curves need much more time than the preceding DFT analysis. The energy gaps of the two models are ~2.0 eV as exhibited in Fig. 6b. Generally, the transmission of the Ge(100)/GeO₂ interface is higher than that of the Ge(111)/GeO₂. For the Ge(100)/GeO₂ interface, the transmission is higher than 2 mainly at the energy ranges of approximately -4.3 to -2.0 eV and 2.2–4.6 eV. For the Ge(111)/GeO₂ interface, the corresponding energy range is about -4.2 to -2.2 eV. Furthermore, the *I-V* curves are calculated as exhibited in Fig. 7. Since the operating voltages of Ge(100) and Ge(111) anodes were 0.92 and 0.87 V in a previous work,¹² the voltage bias of 0–1 V was calculated. The current is relatively low when the voltage bias is smaller than 0.3 V, which is corresponded to the half of the band gap of Ge. When the voltage bias comes to 1 V, the current of Ge(100)/GeO₂/Ge(100) device reaches to 245 nA, which is much higher than that of Ge(111)/GeO₂/Ge(111) device (170 nA), evidencing that the flow

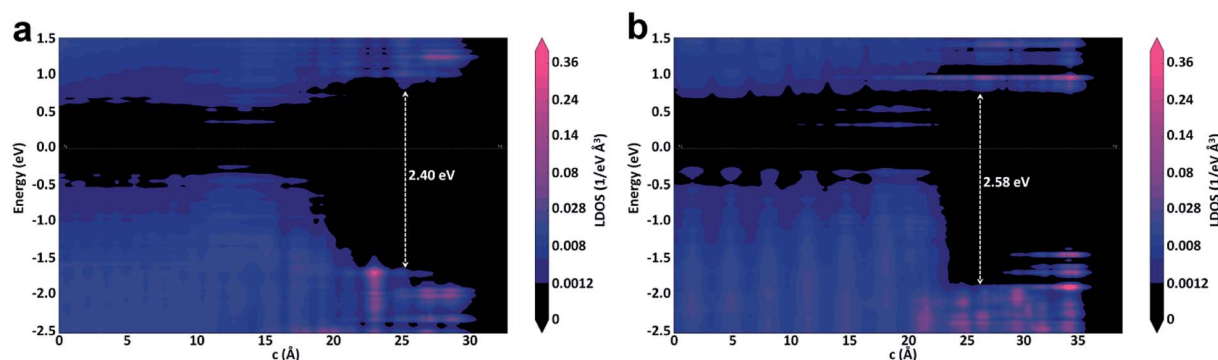


Fig. 5 The projected local density of states of the (a) p-type Ge(100)/GeO₂ and (b) p-type Ge(111)/GeO₂ with the doping concentration of 10¹⁶.



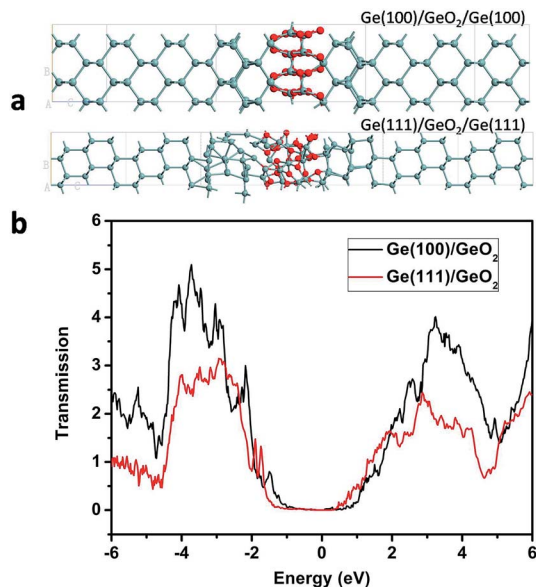


Fig. 6 (a) Atomic configurations of the Ge(100)/GeO₂/Ge(100) and Ge(111)/GeO₂/Ge(111) devices; (b) the k -point averaged transmission spectra of Ge(100)/GeO₂ and Ge(111)/GeO₂ interfaces as function of energy.

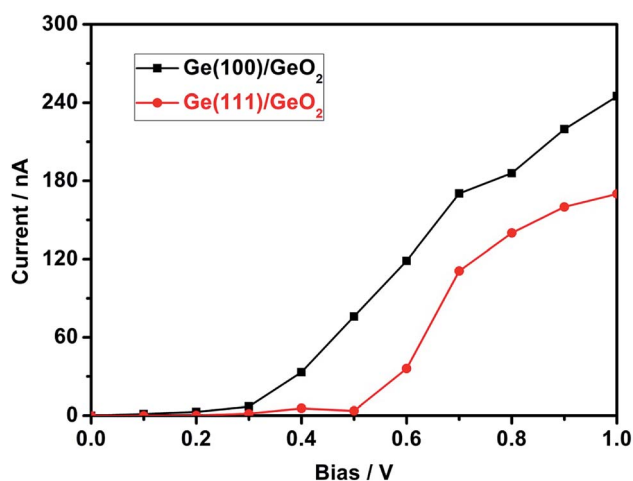


Fig. 7 The I - V curves of Ge(100)/GeO₂ and Ge(111)/GeO₂ interfaces.

of electrons is affected by the crystal structure of the anode.¹² Furthermore, the configurations, transmission and I - V curves of Ge(100)/GeO₂ with oxygen vacancies are shown in Fig. S5.† As shown in Fig. S5b,† the transmission spectrum is similar to that of the Ge(100)/GeO₂ model without O vacancies. In Fig. S5c,† the current is 211 nA at the voltage bias of 1 V, which is a little smaller than that of the Ge(100)/GeO₂ interface.

Conclusions

In conclusion, the Ge(100)/GeO₂ and Ge(111)/GeO₂ models are constructed to analyze the properties of the anodes interfaces in Ge-air batteries. By calculating the binding energies with the

density function theory, Ge(100) anodes are found to be better candidates for Ge-air batteries than Ge(111) anodes. Meanwhile, doping, especially the p-type doping like B, would result in larger binding energies and relieve the surface passivation caused by the formation of GeO₂ layers on Ge surfaces. Moreover, the band gap of GeO₂ in the p-type Ge(100)/GeO₂ model is smaller than that in the p-type Ge(111)/GeO₂ model, which would improve the electron transfer from anodes to cathodes in discharge processes. Finally, the Ge(100)/GeO₂/Ge(100) device exhibits a higher current than the Ge(111)/GeO₂/Ge(111) device. This work would help to explore the origins of the different electrochemical properties of Ge-air batteries with different orientations and doping fundamentally and provide guidelines for the design of Ge anodes in Ge-air batteries.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

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