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# Mo<sub>2</sub>B, an MBene member with high electrical and thermal conductivities, and satisfactory performances in lithium ion batteries†

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Owing to their high specific area, good flexibility and many other unique properties, two-dimensional (2D) materials have attracted extensive attention in the recent two decades. As an analogy to the well-studied MXenes, MBenes also emerged. In this work, Mo<sub>2</sub>B, an MBene member, is predicted both in H- and T-type configurations from first-principles calculations. Structural, mechanical, electronic, and thermal properties, and performances in lithium ion batteries (LIBs) for both configurations are investigated. The H-type Mo<sub>2</sub>B is found to be the stable structure, which can be transformed into the T-type by applying strains. The elastic constants  $c_{11}$  in the H- and T-type Mo<sub>2</sub>B are respectively calculated to be 187.5 and 157.6 N m<sup>-1</sup>, which are higher than that in the previously reported Mo<sub>2</sub>C. The electronic thermal conductivity and electrical conductivity are investigated based on the semiclassical Boltzmann transport theory. The electrical conductivities for both structures are of the order of 10<sup>6</sup> Ω<sup>-1</sup> m<sup>-1</sup>. Because of the large phonon contributions, the thermal conductivities in the H- and T-type Mo<sub>2</sub>B are much higher than that of the synthesized Mo<sub>2</sub>C. Based on a 5 μm flake length, the phonon thermal conductivities at room temperature are calculated to be 146 and 141 W m<sup>-1</sup> K<sup>-1</sup> respectively for the H- and T-type configurations. The T-type Mo<sub>2</sub>B shows promising performances in LIBs. The theoretical volumetric capacity is as high as 2424 mA h cm<sup>-3</sup>, and the migration energy barrier is as low as 0.0372 eV. These data imply that Mo<sub>2</sub>B has widespread applications, such as in conductive films and anode materials.

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## Introduction

Since the discovery of graphene,<sup>1</sup> two-dimensional (2D) materials have attracted extensive attention.<sup>2,3</sup> Especially, the high specific surface area and great flexibility of the 2D configuration meet the increasing technological demands for paper displays and wearable electronics.<sup>4,5</sup> To date, a large number of 2D configurations have been predicted and synthesized,<sup>6,7</sup> such as the high-profile molybdenum disulfide<sup>8</sup> and phosphorene.<sup>9</sup> Since 2011, MXenes have generally stood out owing to their abundant configurations and adjustable properties.<sup>10–12</sup> Different from graphene, MXenes are a large family, which were initially synthesized by the selective etching of M<sub>n+1</sub>AX<sub>n</sub> phases (or abbreviated to MAX phases). Here, M denotes an early transition metal, A is an A-group element (mostly in the IIIA or

IVA group), X is carbon and/or nitrogen,<sup>13</sup> and *n* is a number normally ranging from one to three. Since M–A bonds are generally weaker than M–X bonds in the MAX phases, the A atomic layer is normally etched out in adequate etchants. Therefore, the synthesized MXene generally has the formula M<sub>n+1</sub>X<sub>n</sub>T<sub>x</sub>, where T<sub>x</sub> denotes surface groups.<sup>12</sup> Later, non-MAX layered carbides, such as Zr<sub>3</sub>Al<sub>3</sub>C<sub>5</sub> and Hf<sub>3</sub>(Al,Si)<sub>4</sub>C<sub>6</sub>, were also employed as precursors for Zr<sub>3</sub>C<sub>2</sub>T<sub>x</sub><sup>14</sup> and Hf<sub>3</sub>C<sub>2</sub>T<sub>x</sub> MXenes.<sup>15</sup> Moreover, non-stoichiometric Mo<sub>1.33</sub>CT<sub>x</sub> (ref. 16) and W<sub>1.33</sub>CT<sub>x</sub> (ref. 17) were also developed through selective etching of (Mo<sub>2/3</sub>Sc<sub>1/3</sub>)<sub>2</sub>AlC and (W<sub>2/3</sub>M<sub>1/3</sub>)<sub>2</sub>AlC (M = Sc, Y), respectively. Until now, approximately thirty MXene members have been synthesized,<sup>18</sup> which have been demonstrated to show widespread applications, such as energy storage,<sup>19–21</sup> electromagnetic shielding,<sup>22</sup> sewage treatment,<sup>23</sup> nuclide adsorption,<sup>24</sup> photothermal therapy,<sup>25</sup> multicolor cellular imaging,<sup>26</sup> electrocatalysts,<sup>27,28</sup> etc.

MBene, by replacing the X element of MXene with the neighboring B, naturally aroused increasing attention in the recent three years.<sup>29–33</sup> Moreover, most boron-containing compounds are high-temperature refractory materials.<sup>34,35</sup> With respect to the formula M<sub>n+1</sub>X<sub>n</sub>T<sub>x</sub> for MXenes, MBenes have more adjustable space. For instance, M<sub>2</sub>B<sub>2</sub>T<sub>x</sub> with two boron atomic layers intercalated in the transition metals are reported based

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on existing bulk precursors MAB, such as MoAlB.<sup>32</sup> Theoretically, Guo *et al.* found that Mo<sub>2</sub>B<sub>2</sub> and Fe<sub>2</sub>B<sub>2</sub> show good electrical conductivities, small migration energy barriers, and high storage capacities for lithium ion batteries (LIBs). Moreover, Fe<sub>2</sub>B<sub>2</sub> was determined to be a potential catalyst for hydrogen evolution.<sup>31</sup> Furthermore, Bo *et al.* reported a new type of M<sub>2</sub>B<sub>2</sub> MBenes with two boron atoms forming a planar honeycomb sandwiched by two M atomic planes. Six M<sub>2</sub>B<sub>2</sub> (M = Sc, Ti, V, Cr, Y, Zr, Mo) members were determined to be the global minimum structures. Ti<sub>2</sub>B<sub>2</sub> was determined to be a candidate anode material for LIBs and SIBs.<sup>29</sup> Using a high-throughput structural search, Jiang *et al.* determined twelve metastable MBenes, MnB, HfB, ZrB, Au<sub>2</sub>B, Mo<sub>2</sub>B, Nb<sub>3</sub>B<sub>2</sub>, Nb<sub>3</sub>B<sub>4</sub>, Ta<sub>3</sub>B<sub>4</sub>, V<sub>3</sub>B<sub>4</sub>, OsB<sub>2</sub>, FeB<sub>2</sub>, and RuB<sub>2</sub>, and they found that bare or functionalized MnB compounds are ferromagnets with high Curie temperatures.<sup>30</sup> Although H-type Mo<sub>2</sub>B has been predicted,<sup>30</sup> this structure was not discussed in detail. In their experiment, Alameda *et al.* used MoAlB as the precursor to synthesize MBene, but they obtained MoAlB slabs of nanoscale thickness in their first attempt.<sup>32</sup> Furthermore, they performed etching of MoAlB in two steps, and they identified isolated MoB layers inside the etched cavities.<sup>33</sup> Based on the discussions above, MBenes have potential applications, which have been shown to be feasible in experiments. Thus, an in-depth investigation on MBene is justified.

Previously, Xu *et al.* synthesized the bare Mo<sub>2</sub>C configuration by chemical vapor deposition (CVD), which was proven to show superconductivity<sup>36</sup> and oscillatory magnetoresistance.<sup>37</sup> Theoretically, the synthesized Mo<sub>2</sub>C was also found to show high storage capacities and low migration energy barriers for Li, Na and K ions. Specifically, the storage capacity was determined to be 263 mA h g<sup>-1</sup>, and the migration barrier is calculated to be as low as 0.043 eV for Li ion.<sup>38</sup> In addition, Mo<sub>2</sub>C is determined to be robust under varying temperatures and strains since it possesses relatively low thermal expansion coefficient and high mechanical strength.<sup>39</sup> In analogy to Mo<sub>2</sub>C, Mo<sub>2</sub>B, both in the H- and T-type configurations, is predicted in this work. The structural, mechanical and thermal properties, and the performances in LIBs are studied. Compared with Mo<sub>2</sub>C, both the H- and T-type Mo<sub>2</sub>B are found to show comparable electrical conductivities, and much higher thermal conductivities. In addition to a relatively low migration energy barrier and a high storage capacity, the T-type Mo<sub>2</sub>B is a potential candidate anode material for LIBs.

## Methods

The first-principles calculations are implemented in the plane-wave VASP code<sup>40</sup> in this work. Based on the projected augmented wave (PAW) pseudopotential, the generalized gradient approximation (GGA) by Perdew–Burke–Ernzerhof (PBE)<sup>41</sup> is employed for description of the exchange and correlation functional. A plane-wave cutoff energy of 500 eV is adopted for describing the ion–electron interaction, in which the Mo 4p<sup>6</sup>, 5s<sup>1</sup>, 4d<sup>5</sup> and B 2s<sup>2</sup>, 2p<sup>1</sup> electrons are considered as valence electrons. All the structures are relaxed until the force on each atom is less than 1.0 × 10<sup>-3</sup> eV Å<sup>-1</sup>, and the criterion for energy convergence is set as 1.0 × 10<sup>-6</sup> eV per cell. A *T*-

centered sampling of 12 × 12 × 1 *k*-point mesh is adopted for the Brillouin zone (BZ) of the Mo<sub>2</sub>B unit cell. In order to eliminate the layer interaction, a vacuum layer larger than 23 Å is employed parallel to the Mo<sub>2</sub>B surface. In order to test the stable configuration for Mo<sub>2</sub>B, the local particle swarm optimization for 2D structures is performed combined with the CALYPSO package<sup>42</sup> and the VASP code. All the structures are visualized in the VESTA3 code.<sup>43</sup> In order to investigate the elastic constants, the stress–strain relationship<sup>44</sup> is employed as implemented in the VASP code. Spin-polarization is considered in the calculation. To investigate the electrical conductivity and electronic thermal conductivity, the semiclassical Boltzmann transport calculations are performed based on constant relaxation time approximation, which are undertaken in the BoltzTraP code.<sup>45</sup> The electronic structure for transport properties is calculated based on a very fine *k*-point mesh of 42 × 42 × 1, and the mesh is interpolated to a dense one of 20 times in the BoltzTraP calculation. The obtained transport parameters from BoltzTraP are rescaled using *h/d*, where *h* denotes the lattice parameter in the *c*-axis, and *d* represents the layer thickness, which is equal to the monomer thickness in its multilayer configuration.<sup>39,46</sup>

Regarding the thermal properties, the specific heat, thermal expansion coefficient, and phonon thermal conductivity are calculated. The phonon dispersions are calculated based on density functional perturbation theory (DFPT),<sup>47</sup> which is implemented by a combination of the VASP and Phonopy<sup>48</sup> softwares. For calculating the dynamical matrix, a 4 × 4 × 1 supercell with a 6 × 6 × 1 *T*-centered *k*-point mesh is employed. The phonon dispersions are plotted using a 120 *k*-point grid for various directions and the entire BZ. The specific heat and thermal expansion coefficient are calculated based on the Grüneisen approximation.<sup>39,49–51</sup> The phonon thermal conductivity is calculated according to the Klemens theory.<sup>39,52–55</sup> The details are presented in eqn (S1)–(S3) in the ESI.†

Regarding the Mo<sub>2</sub>B performance in LIBs, 4 × 4 × 1 supercells for both H- and T-type Mo<sub>2</sub>B are optimized. Diffusion energy barriers for Li atom on the supercells are calculated according to the climbing-image nudged elastic-band (CI-NEB) method.<sup>56</sup> The binding energies of Li atoms on the 4 × 4 × 1 supercells are calculated according to the following equation:

$$E_{\text{binding}} = (E_{\text{Mo}_2\text{B}} + xE_{\text{Li}} - E_{\text{Mo}_2\text{BLi}_x})/x \quad (1)$$

where  $E_{\text{Mo}_2\text{B}}$ ,  $E_{\text{Li}}$ , and  $E_{\text{Mo}_2\text{BLi}_x}$  denote the total energies of the Mo<sub>2</sub>B supercell, of a Li atom in its stable bulk state and of Li-adsorbed Mo<sub>2</sub>B, respectively.  $x$  represents the number of adsorbed Li atoms. The VDW-D3 correction<sup>57</sup> is employed for describing the interaction between Mo<sub>2</sub>B and adsorbed Li atoms. Additionally, the open-circuit voltage is approximated according to the following equation:<sup>38</sup>

$$V \approx \frac{E_{\text{Mo}_2\text{BLi}_{x_1}} - E_{\text{Mo}_2\text{BLi}_{x_2}} + (x_2 - x_1)E_{\text{Li}}}{(x_2 - x_1)e} \quad (2)$$

where  $x_1$  and  $x_2$  represent different concentrations of Li and  $e$  denotes the electron charge. To be more precise, the difference between  $x_1$  and  $x_2$  is taken as one in our work. The theoretical storage capacity is calculated according to the voltage.



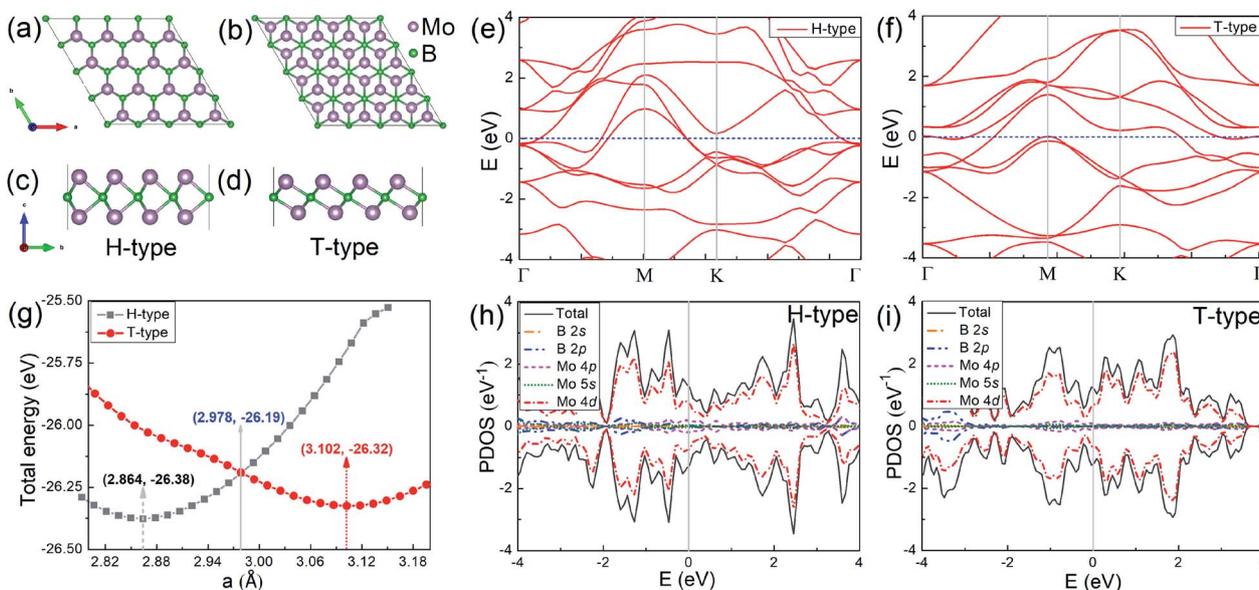
## Results and discussion

In order to investigate the physical properties of the H- and T-type Mo<sub>2</sub>B, their structures are investigated firstly. Fig. 1(a) and (c) show the top- and side-view of H-type Mo<sub>2</sub>B, whose structure is similar to that of the well-studied MoS<sub>2</sub>.<sup>58</sup> A boron atomic layer is sandwiched by two Mo layers, and the Mo atoms in the top-layer are on the top-sites of those in the bottom layer. The corresponding space group is 187. Fig. 1(b) and (d) present the top- and side-view of the T-type Mo<sub>2</sub>B. This configuration is similar to that of Mo<sub>2</sub>C reported previously,<sup>38,39</sup> with a space group of 164. The difference is that the carbon in Mo<sub>2</sub>C is replaced by boron in the T-type Mo<sub>2</sub>B. In addition, other possible metastable configurations for the chemical formula Mo<sub>2</sub>B are also studied from the local particle swarm optimization, and some structures and corresponding relative total energies are provided in Fig. S1 and Table S1 in the ESI.† Evidently, the H-type Mo<sub>2</sub>B is determined to be the most stable structure in this chemical formula, and the T-type is the second most stable one. The relationships between the total energy and lattice parameter for both H- and T-type Mo<sub>2</sub>B are presented in Fig. 1(g). The total energy of the H-type Mo<sub>2</sub>B is 0.06 eV lower than that of the T-type configuration based on their unit cells after relaxation. However, the H-type can be transformed to the T-type by applying tensile strains. According to this figure, the optimal lattice parameters for the H- and T-type Mo<sub>2</sub>B in the basal plane are determined to be 2.864 and 3.102 Å, respectively. The T-type configuration becomes more stable since the lattice parameter increases to 2.978 Å. The lattice parameters, bond lengths, layer thicknesses, and the elastic constants for these two configurations are provided in Table 1. From the table, the T-type configuration shows a smaller layer thickness compared

to that in the H-type configuration. Both the T- and H-type Mo<sub>2</sub>B show higher  $c_{11}$  values compared to that of the synthesized Mo<sub>2</sub>C (143.8 N m<sup>-1</sup>).<sup>39</sup> In addition, the H-type also presents a large  $c_{12}$  value of 124.1 N m<sup>-1</sup>. The discrepant mechanical strengths in the H- and T-type Mo<sub>2</sub>B could be ascribed to their structural differences. In the H-type configuration, a tensile strain needs to overcome the interatomic attraction between the neighbouring Mo and B atoms, and the atomic repulsion between the counter Mo atoms. In the T-type structure, the interatomic attraction between the neighbouring Mo and B atoms could be the main resistance to the tensile strain. Based on the two independent elastic constants  $c_{11}$  and  $c_{12}$ , the Young's moduli for both the H- and T-type Mo<sub>2</sub>B are further calculated according to  $Y_{2D} = (c_{11}^2 - c_{12}^2)/c_{11}$ ,<sup>59</sup> the corresponding values are also provided in Table 1. These high elastic constants imply that both configurations are robust under strains. Fig. 1(e) and (f) present the electronic energy bands of the H- and T-type Mo<sub>2</sub>B, respectively. Fig. 1(h) and (i) show the corresponding projected density of states (PDOS). Both structures are nonmagnetic metals with large DOS in the vicinity of their Fermi levels. The DOS around Fermi levels are mainly contributed by the electrons in the Mo 4d orbitals. The electronic energy bands and PDOS imply that both the H- and T-type Mo<sub>2</sub>B could possess favorable electrical conductivities.

**Table 1** The lattice parameters, bond lengths, layer thickness (in Å), elastic constants  $c_{11}$ ,  $c_{12}$  and Young's moduli (in N m<sup>-1</sup>) of both the H- and T-type Mo<sub>2</sub>B

| Mo <sub>2</sub> B | $a$   | $h$   | $d$   | Mo–B  | Mo–Mo | $c_{11}$ | $c_{12}$ | $Y_{2D}$ |
|-------------------|-------|-------|-------|-------|-------|----------|----------|----------|
| H-type            | 2.864 | 33.04 | 5.443 | 2.176 | 2.830 | 187.5    | 124.1    | 105.4    |
| T-type            | 3.102 | 28.16 | 4.713 | 2.115 | 2.876 | 157.6    | 28.95    | 152.3    |



**Fig. 1** (a) and (b) Top-views of the H- and T-type Mo<sub>2</sub>B, respectively; (c) and (d) corresponding side-views for the configurations displayed above. (e) and (f) Electronic energy bands, respectively for the H- and T-type Mo<sub>2</sub>B. (g) Relationships between the total energy and the lattice parameter in the basal plane, for both the H- and T-type structures. (h) and (i) Projected density of states (PDOS), respectively for the H- and T-type Mo<sub>2</sub>B.



Regarding the transport properties of the H- and T-type  $\text{Mo}_2\text{B}$ , the electrical conductivities and the electronic thermal conductivities are further investigated based on constant relaxation time approximation. It is found that these transport coefficients are isotropic in the basal plane regardless of temperatures and chemical potentials. Therefore,  $\sigma_{xx}/\tau$  and  $\kappa_{xx}/\tau$  for both configurations are adopted to present the transport properties, as provided in Fig. 2. Here  $\sigma_{xx}$  and  $\kappa_{xx}$  respectively denote the electrical conductivity and electronic thermal conductivity along the  $x$ -axis direction,  $\tau$  represents the electron relaxation time. According to this figure, temperature has a relatively weak influence on the electrical conductivity. In contrast, the electronic thermal conductivity is proportional to the increasing temperatures, and the shape of the relationship between the values of the electrical conductivity and electronic thermal conductivity meets the Wiedemann–Franz law.<sup>60</sup> For the H-type  $\text{Mo}_2\text{B}$ ,  $\sigma_{xx}/\tau$  is determined to be  $12.78 \times 10^{20} \Omega^{-1} \text{m}^{-1} \text{s}^{-1}$  at room temperature at  $\mu = 0.0$  eV, where the transport coefficient slightly decreases with increasing chemical potential. This behavior could be explained by the similar trend of PDOS with increasing energy presented in Fig. 1(h), since the electrical conductivity is approximately proportional to the PDOS. In the chemical potential range presented, the largest  $\sigma_{xx}/\tau$  at room temperature is calculated to be  $14.30 \times 10^{20} \Omega^{-1} \text{m}^{-1} \text{s}^{-1}$  at  $\mu = -0.473$  eV. From Fig. 2(b),  $\kappa_{xx}/\tau$  of zero chemical potential is calculated to be  $93.35 \times 10^{14} \text{W}^{-1} \text{m}^{-1} \text{K}^{-1} \text{s}^{-1}$  at room temperature, which is increased to  $155.7 \times 10^{14} \text{W}^{-1} \text{m}^{-1} \text{K}^{-1} \text{s}^{-1}$  at 500 K. For the T-type configuration,  $\sigma_{xx}/\tau$  and  $\kappa_{xx}/\tau$  generally show minimum values at the zero chemical potential, which imply that one can enhance these transport coefficients by employing both n- and p-doping. At room temperature,  $\sigma_{xx}/\tau$  and  $\kappa_{xx}/\tau$  are respectively determined to be  $4.121 \times 10^{20} \Omega^{-1} \text{m}^{-1} \text{s}^{-1}$  and  $30.87 \times 10^{14} \text{W}^{-1} \text{m}^{-1} \text{K}^{-1} \text{s}^{-1}$  when  $\mu = 0.0$  eV. To be more intuitive, the electrical conductivity and electronic thermal conductivity calculated are compared with those of  $\text{Mo}_2\text{C}$ , based on the same electron relaxation time ( $\tau = 5.52 \times 10^{-15} \text{s}$ ) determined in experiments for  $\text{Mo}_2\text{C}$ .<sup>36</sup> At zero chemical

potential and at room temperature, the electrical conductivity and electronic thermal conductivity of  $\text{Mo}_2\text{C}$  have been previously calculated to be  $3.590 \times 10^6 \Omega^{-1} \text{m}^{-1}$  and  $26.4 \text{W}^{-1} \text{m}^{-1} \text{K}^{-1} \text{s}^{-1}$ .<sup>39</sup> Under the same conditions, the electrical conductivity and electronic thermal conductivity of the H-type  $\text{Mo}_2\text{B}$  are determined to be  $7.546 \times 10^6 \Omega^{-1} \text{m}^{-1}$  and  $51.53 \text{W}^{-1} \text{m}^{-1} \text{K}^{-1}$ , respectively. Regarding the T-type  $\text{Mo}_2\text{B}$ , the corresponding values are determined to be  $2.275 \times 10^6 \Omega^{-1} \text{m}^{-1}$  and  $17.07 \text{W}^{-1} \text{m}^{-1} \text{K}^{-1}$ . Moreover, the electron relaxation time ranging from  $1.00 \times 10^{-15} \text{s}$  to  $1.00 \times 10^{-14} \text{s}$  is also considered for  $\text{Mo}_2\text{B}$ . Based on  $\tau = 1.00 \times 10^{-15} \text{s}$ ,  $\sigma_{xx}$  and  $\kappa_{xx}$  in the H-type  $\text{Mo}_2\text{B}$  at room temperature are calculated to be  $1.278 \times 10^6 \Omega^{-1} \text{m}^{-1}$  and  $9.335 \text{W}^{-1} \text{m}^{-1} \text{K}^{-1}$  at zero chemical potential. With  $\tau = 1.00 \times 10^{-14} \text{s}$ , the corresponding  $\sigma_{xx}$  and  $\kappa_{xx}$  are an order of magnitude larger. Obviously, both H-type and T-type  $\text{Mo}_2\text{B}$  are promising electrical conductors.

Since the thermal conductivity comprises electron and phonon contributions, the phonon thermal conductivity is further investigated. The phonon dispersions for both the H- and T-type  $\text{Mo}_2\text{B}$  are provided in Fig. S1 in the ESI,<sup>†</sup> where ZA, TA and LA respectively denote the out-of-plane, transversal and longitudinal acoustic modes. The phonon dispersions are predicted without an imaginary frequency, which implies that both structures are dynamically stable. According to the method described in the Methods section,<sup>39,54,55</sup> the phonon thermal conductivities along the  $IM$  and  $IK$  directions are calculated, where the high-symmetry directions  $IM$  and  $IK$  in BZs respectively correspond to the armchair and zigzag directions in the real spaces of both H- and T-type  $\text{Mo}_2\text{B}$ , as shown in Fig. S2 in the ESI.<sup>†</sup> The calculated values with increasing temperatures based on various flake lengths are provided in Fig. 3. Since the size of the synthesized  $\text{Mo}_2\text{C}$  is approximately  $100 \mu\text{m}$ ,<sup>36</sup> the flake lengths of  $\text{Mo}_2\text{B}$  ranging from 1 to  $100 \mu\text{m}$  are studied here. Apparently, the phonon thermal conductivity increases with a larger flake length when the flake length is smaller than  $100 \mu\text{m}$ , and decreases with increasing temperature in the range from 100 to 500 K. Fig. 3(a) shows the phonon thermal conductivity along the armchair direction in the H-type  $\text{Mo}_2\text{B}$ . Based on the different flake lengths of 1, 2, 5, 50 and  $100 \mu\text{m}$ , the phonon thermal conductivities are respectively determined to be 108.7, 125.0, 146.4, 200.2 and  $216.4 \text{W}^{-1} \text{m}^{-1} \text{K}^{-1}$  at room temperature. Regarding the increasing temperatures, the values based on the  $5 \mu\text{m}$  flake length are calculated to be 362.1, 205.4, 146.4, 114.8 and  $95.00 \text{W}^{-1} \text{m}^{-1} \text{K}^{-1}$ , respectively at 100, 200, 300, 400 and 500 K. Fig. 3(b) shows the corresponding phonon thermal conductivity along the zigzag direction. Obviously, the phonon thermal conductivity is anisotropic, with much lower values in the zigzag direction. At room temperature, the phonon thermal conductivity with the flake length of  $5 \mu\text{m}$  is determined to be  $72.78 \text{W}^{-1} \text{m}^{-1} \text{K}^{-1}$ . Fig. 3(c) and (d) respectively present the phonon thermal conductivities along the armchair and zigzag directions in the T-type configuration, whose values are generally similar to those in the H-type  $\text{Mo}_2\text{B}$ . Based on the  $5 \mu\text{m}$  flake length, the phonon thermal conductivities along the armchair and zigzag directions at room temperature are 141.3 and  $67.14 \text{W}^{-1} \text{m}^{-1} \text{K}^{-1}$ . In a word, both the H- and T-type  $\text{Mo}_2\text{B}$  possess high phonon thermal conductivities, especially along

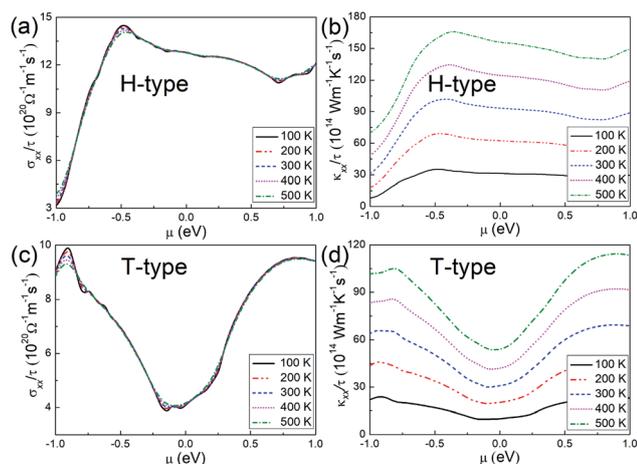


Fig. 2 (a) and (b) Transport coefficients  $\sigma_{xx}/\tau$  and  $\kappa_{xx}/\tau$ , respectively, for the H-type  $\text{Mo}_2\text{B}$ . (c) and (d) Corresponding transport coefficients  $\sigma_{xx}/\tau$  and  $\kappa_{xx}/\tau$  for the T-type  $\text{Mo}_2\text{B}$ .



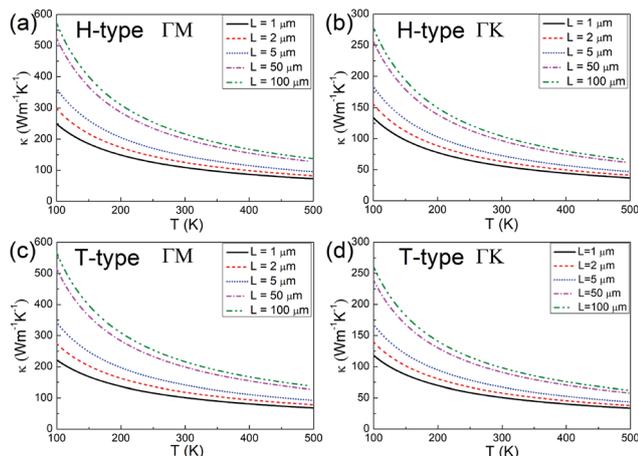


Fig. 3 (a) and (b) Phonon thermal conductivity along the armchair ( $\Gamma M$ ) and zigzag ( $\Gamma K$ ) directions of the H-type  $\text{Mo}_2\text{B}$ . (c) and (d) Corresponding values along the armchair and zigzag directions of the T-type  $\text{Mo}_2\text{B}$ , respectively.

their armchair direction. These calculated values are much higher than those of many well-known metals,<sup>61</sup> and those in the reported  $\text{Mo}_2\text{C}$ .<sup>39</sup>

In order to understand the high phonon thermal conductivities, each acoustic mode contribution is calculated and provided in Fig. S3 in the ESI.† According to this figure, each acoustic mode presents evident contribution to its phonon thermal conductivity in the H-type  $\text{Mo}_2\text{B}$ , although the ZA mode contribution is relatively smaller in the armchair direction. Regarding the T-type configuration, the phonon thermal conductivity is mainly dominated by the LA mode. The ZA mode presents little contribution in both directions. This behaviour could be explained from their phonon dispersions, where the frequency magnitude of the ZA mode is much smaller in the T-type configuration. Based on the low phonon frequency, the phonon velocity is smaller, which induces the small phonon thermal conductivity contribution. Compared with the reported  $\text{Mo}_2\text{C}$ , the larger phonon thermal conductivity of  $\text{Mo}_2\text{B}$  is mainly caused by its larger phonon group velocities and lower Grüneisen parameters (GPs). Since the T-type  $\text{Mo}_2\text{B}$  and  $\text{Mo}_2\text{C}$  possess the same space group, and their phonon thermal conductivities are both mainly dominated by the LA modes, the phonon thermal conductivities in the armchair directions of these two configurations are compared. In  $\text{Mo}_2\text{B}$ , the phonon group velocity and the square of the GP of the LA mode are respectively determined to be  $2.967 \times 10^3 \text{ m s}^{-1}$  and 1.454, while the corresponding values in  $\text{Mo}_2\text{C}$  are determined to be  $2.167 \times 10^3 \text{ m s}^{-1}$  and 53.88, respectively. According to eqn (S2) in the ESI,† the thermal conductivity of  $\text{Mo}_2\text{B}$  is naturally much higher than that in  $\text{Mo}_2\text{C}$ .

Combined with the electron and phonon contributions, both the H- and T-type  $\text{Mo}_2\text{B}$  could have outstanding thermal conductivities in a wide temperature range, since the electron part increases and the phonon part decreases with increasing temperature. Based on the  $5 \mu\text{m}$  flake length and the constant electron relaxation time  $\tau = 5.52 \times 10^{-15} \text{ s}$ , the thermal

conductivities in the armchair direction in the H-type  $\text{Mo}_2\text{B}$  are determined to be 379.3, 239.8, 197.9, 183.5 and  $180.9 \text{ W m}^{-1} \text{ K}^{-1}$ , respectively at 100, 200, 300, 400 and 500 K. Correspondingly, the values in the armchair direction of the T-type  $\text{Mo}_2\text{B}$  are 347.4, 208.0, 158.3, 134.6 and  $122.3 \text{ W m}^{-1} \text{ K}^{-1}$ . These high thermal conductivities enable both the H- and T-type  $\text{Mo}_2\text{B}$  applications in thermal conductive materials. In addition, the specific heat and thermal expansion coefficients (TECs) of these two configurations are studied, and corresponding results are provided in Fig. 4. From Fig. 4(a), the specific heats of the H- and T-type  $\text{Mo}_2\text{B}$  are generally equivalent in the entire range of temperature investigated. The room temperature values are calculated to be 289.4 and  $281.8 \text{ J kg}^{-1} \text{ K}^{-1}$ , respectively. Regarding the thermal expansion behaviors as shown in Fig. 4(b), the TEC of the H-type  $\text{Mo}_2\text{B}$  increases with increasing temperature. The value at room temperature is calculated to be  $4.780 \times 10^{-6} \text{ K}^{-1}$ , which increases to  $5.498 \times 10^{-6} \text{ K}^{-1}$  at 1000 K. For the T-type configuration, its TEC is much smaller than that in the H-type, and the corresponding value at room temperature is determined to be  $2.148 \times 10^{-6} \text{ K}^{-1}$ . Interestingly, the TEC of the T-type configuration is negative under 50 K, and the negative TEC with the largest absolute value is determined to be  $-1.153 \times 10^{-6} \text{ K}^{-1}$  at 14 K. In order to understand the different thermal expansion behaviors between the H- and T-type  $\text{Mo}_2\text{B}$ , the GPs of the acoustic modes in the BZs of both configurations are calculated and provided in Fig. 4(c) and (d). From these figures, the GPs of the TA and LA are positive in the entire BZs for both H- and T-type configurations, which imply that both the TA and LA modes contribute to thermal expansion.<sup>50,51,62</sup> The GP of the ZA mode in the H-type  $\text{Mo}_2\text{B}$  is generally positive, although it shows small negative values around the high symmetry K point. Consequently, the TEC of the H-type  $\text{Mo}_2\text{B}$  increases with increasing temperature. In the T-type configuration, the ZA mode shows large negative GPs, especially around its BZ center. The large negative value implies that the amplitude of ZA mode is significant, which contributes to the thermal contraction. As a result, this

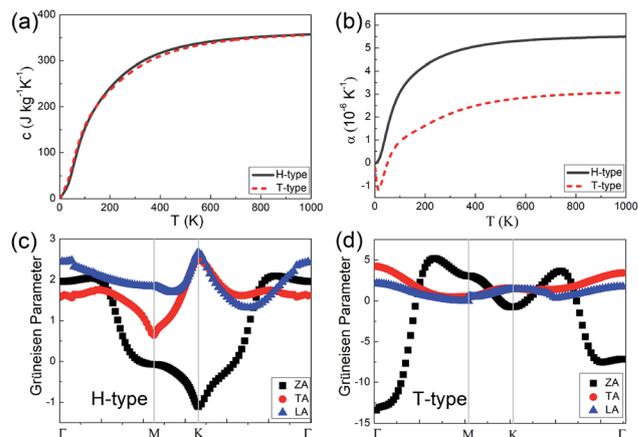


Fig. 4 (a) The specific heats with increasing temperature. (b) The thermal expansion coefficients (TECs) with increasing temperature for both the H- and T-type  $\text{Mo}_2\text{B}$ . (c) and (d) Grüneisen parameters (GPs) in the Brillouin zones (BZs) of the H- and T-type  $\text{Mo}_2\text{B}$ , respectively.



structure shows negative TEC in the low temperature range. For in-depth understanding, the different behaviors of the ZA modes in the H- and T-type  $\text{Mo}_2\text{B}$  are ascribed to the different layer thickness and mechanical strength of these two configurations.<sup>51</sup> The configuration with a thinner layer thickness and weaker mechanical strength could be more flexible, and the amplitude of the ZA mode is more significant. In addition, the GP values in Fig. 4(c) and (d) could also explain the magnitude of the phonon thermal conductivity. For instance, the ZA mode in the T-type  $\text{Mo}_2\text{B}$  makes little contribution to its thermal conductivity, ascribed to the large absolute value of GP, since the phonon thermal conductivity is inversely proportional to the square of GPs.<sup>54,55,63</sup> Based on the different thermal expansion behaviors of the H- and T-type  $\text{Mo}_2\text{B}$ , it is possible to obtain a zero TEC intuitively by combining these two phases, since two competitive phases can be obtained concurrently by applying strains or other techniques.<sup>64</sup> This could be an interesting topic for future work.

Based on the high mechanical strength, promising electrical and thermal conductivities, and low TECs calculated above, both the H- and T-type  $\text{Mo}_2\text{B}$  could have widespread applications. In the following, the performances in LIBs of both configurations are further investigated. The key parameters, *i.e.*, theoretical storage capacity and migration energy barrier are studied. Based on  $4 \times 4$  supercells, the stable adsorption sites for the Li ion on both H- and T-type  $\text{Mo}_2\text{B}$  are investigated firstly. According to Fig. S4 and S5,<sup>†</sup> three possible locations for each configuration are considered, and corresponding relative total energies are provided in Table S2 in the ESI.<sup>†</sup> From the table, the Li atom is stabilized on the top-site of the hexagonal centre of the H-type  $\text{Mo}_2\text{B}$ , as shown in Fig. S4(c) and (f).<sup>†</sup> The distance between the Li atom and the MXene surface is calculated to be 2.416 Å. The corresponding total energy is 0.0263 eV lower than that of the structure with Li on the top-site of Mo atom. In the T-type  $\text{Mo}_2\text{B}$ , the Li atom is found to stabilize on the top-site of the bottom Mo atom, and its location is 2.311 Å higher than that of the MXene surface. The top- and side-views for the stable location are presented in Fig. S5(c) and (f),<sup>†</sup> respectively. The corresponding total energy is 0.0125 eV lower than that of the configuration with Li on the top-site of the middle B atom.

Since the migration energy barrier is a key parameter in determining the rates of charging and discharging, it is studied after the stable location of Li is determined. The migration barrier profiles for Li on the H- and T-type  $\text{Mo}_2\text{B}$  are respectively shown in Fig. 5(a) and (b), respectively. For each configuration, three possible migration pathways are studied. In the H-type  $\text{Mo}_2\text{B}$ , PATH I denotes the diffusion of the Li atom directly from the top-site of the hexagonal centre to the neighbouring top-site of the hexagonal centre. PATH II represents the diffusion of the Li atom from the top-site of the hexagonal centre to the top-site of neighbouring boron, and then moves to the neighbouring top-site of the neighbouring hexagonal centre. PATH III shows the diffusion path from the top-site of the hexagonal centre to the top-site of neighbouring molybdenum, and then moves to the top-site of the neighbouring hexagonal centre. The energy barriers for PATH I, PATH II and PATH III are determined to be

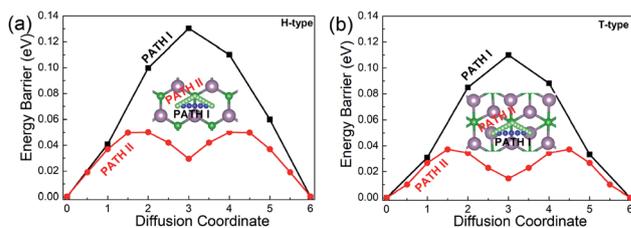


Fig. 5 Diffusion barrier profiles for Li on (a) the H-type  $\text{Mo}_2\text{B}$  and (b) the T-type  $\text{Mo}_2\text{B}$ . The insets show the two migration pathways with low energy barriers on each configuration.

0.130, 0.050 and 0.188 eV, respectively. To give a clear view, only the two lower energy barriers are provided in Fig. 5(a). Based on the different stable locations for Li atom on the T-type configuration, PATH I shows the diffusion route directly from the top-site of the bottom Mo atom to the top-site of a neighbouring bottom Mo atom. PATH II shows that the Li diffuses from the top-site of the bottom Mo atom to the top-site of the middle boron atom, and then moves to the stable top-site of the neighbouring bottom Mo atom. PATH III is the route from the top-site of the bottom molybdenum to the neighbouring top-site of top molybdenum, and then diffuses to the top-site of bottom molybdenum. The corresponding energy barriers for PATH I, PATH II and PATH III are calculated to be 0.110, 0.037 and 0.152 eV, respectively. The energy barriers for PATH I and II are given in Fig. 5(b). Evidently, the diffusion energy barrier of PATH II is generally lower than those for PATH I and PATH III in both H- and T-type  $\text{Mo}_2\text{B}$ . The energy barriers of PATH II in both configurations are comparable to that in  $\text{Mo}_2\text{C}$  (0.043 eV).<sup>38</sup> Moreover, these values are much smaller than that (0.35–0.65 eV) in the commercially used anode material  $\text{TiO}_2$ .<sup>65</sup> Based on the relatively low diffusion energy barriers, both the H- and T-type  $\text{Mo}_2\text{B}$  could show rapid charge and discharge rate when applied as anode materials for LIBs.<sup>38</sup>

After the diffusion energy barrier is calculated, the binding energy and open-circuit-voltage for LIBs are further studied. Based on the  $4 \times 4 \times 1$  supercells, increasing number of Li atoms from one to sixty-four are studied. From the previous discussion, the Li atom could prefer the top-site of the hexagonal centre in the H-type  $\text{Mo}_2\text{B}$  until its number reaches thirty-two, with both sides of  $\text{Mo}_2\text{B}$  adsorbing one atomic layer of Li atoms. If more Li atoms are adsorbed, an additional Li atomic layer will be formed based on the  $4 \times 4 \times 1$  supercells, and thus the stable location for the additional atomic layer must be investigated. As shown in Fig. S6,<sup>†</sup> three possible locations for the thirty-three Li atoms on the H-type  $\text{Mo}_2\text{B}$  are studied, and their relative total energies are provided in Table S3.<sup>†</sup> From the table, the second Li atomic layer is stabilized on the top-site of the Mo atomic layer. The top- and side-views for the stable location are provided in Fig. S6(a) and (d),<sup>†</sup> respectively. With a similar procedure, the second Li atomic layer is found to locate on the top-site of the neighbouring Mo atomic layer in the T-type  $\text{Mo}_2\text{B}$ , and the corresponding structures are provided in Fig. S7(a) and (d).<sup>†</sup> After all the structures with increasing Li atoms are optimized, the binding energies and open-circuit



voltages for the adsorbed Li atoms are calculated according to eqn (1) and (2) in the Methods section. To facilitate elaboration,  $\text{Mo}_2\text{BLi}_x$  is adopted to denote the Li-adsorbed  $\text{Mo}_2\text{B}$ . Since sixty-four Li atoms are studied based on the  $4 \times 4 \times 1$  supercells, the  $x$  value ranges from zero to four. The corresponding binding energies and voltage profiles for Li atoms on both H- and T-type  $\text{Mo}_2\text{B}$  are provided in Fig. 6. From Fig. 6(a), the binding energies of Li on both H- and T-type  $\text{Mo}_2\text{B}$  are positive in the entire range of concentration  $x$  investigated, which imply that both configurations could adsorb at least four Li atomic layers on their surfaces. The binding energy for Li on the T-type  $\text{Mo}_2\text{B}$  is generally large than that on the H-type  $\text{Mo}_2\text{B}$ , which could be ascribed to the larger specific area of the T-type configuration. The three large binding energies around the Li concentration  $x = 2.0$  on the H-type  $\text{Mo}_2\text{B}$  are due to structural distortion. It is noteworthy that, although the binding energies calculated are positive, it is better to estimate the theoretical storage capacity by inspecting the open voltage.<sup>38,66</sup> Fig. 6(b) presents the corresponding voltage profiles. Obviously, the voltage varies significantly with the increasing concentration of Li atoms. Moreover, the first negative value appears at  $x = 0.625$  (the number of Li atoms is 10) on the H-type  $\text{Mo}_2\text{B}$ , and  $x = 2.062$  (the number of Li atoms is 33) on the T-type configuration. Based on the binding energies and open voltages calculated, the theoretical storage capacities for the H- and T-type  $\text{Mo}_2\text{B}$  are calculated to be 74.18 and 264.0  $\text{mA h g}^{-1}$ , respectively (corresponding  $x$  values are 0.562 and 2.00, respectively). Based on the volumes of the bare H- and T-type  $\text{Mo}_2\text{B}$ , corresponding volumetric capacities are respectively calculated to be 647.8 and 2424  $\text{mA h cm}^{-3}$ . Obviously, the volumetric capacity in the T-type configuration is much higher than those in commercial carbon-based electrodes.<sup>67</sup> Therefore,  $\text{Mo}_2\text{B}$  could be a candidate anode material, especially for applications where size matters. Regarding the volume changes of the lithium adopted configurations, the volumes of the H-type  $\text{Mo}_2\text{BLi}_{0.562}$  and T-type  $\text{Mo}_2\text{BLi}_2$  are respectively 1.408 and 1.845 times of those for the bare H- and T-type  $\text{Mo}_2\text{B}$ . The averaged voltage in the range of  $0 \leq x \leq 0.562$  is calculated to be 0.386 V in the H-type  $\text{Mo}_2\text{B}$ . Similarly, in the T-type configuration, the averaged voltage averaged over  $0 \leq x \leq 2.00$  is calculated to be 0.628 V. As reported previously, the potential voltage range for an anode material is from 0.1 to 1.0 V.<sup>38</sup> Both the average voltages for the H- and T-type  $\text{Mo}_2\text{B}$  fall in this potential range, which imply that both configurations are favourable anode materials.

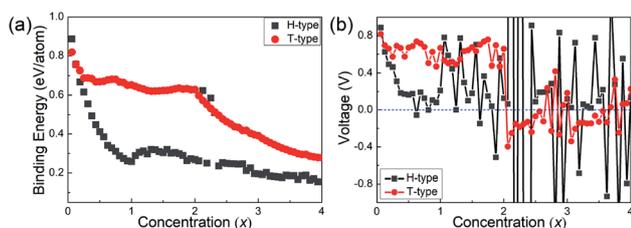


Fig. 6 (a) Binding energies of Li atoms as a function of concentration  $x$  on both H- and T-type  $\text{Mo}_2\text{B}$ , respectively. (b) Voltage profiles as a function of Li concentration  $x$  on both H- and T-type  $\text{Mo}_2\text{B}$ , respectively.

## Conclusions

In summary, we have investigated an MBene member  $\text{Mo}_2\text{B}$  in both H- and T-type configurations in this work. Compared with the synthesized  $\text{Mo}_2\text{C}$ ,  $\text{Mo}_2\text{B}$  shows higher mechanical strength and comparable electrical conductivities. More importantly, both the H- and T-type configurations show relatively higher thermal conductivities. Based on a 5  $\mu\text{m}$  flake length, the thermal conductivities along the armchair direction of the H- and T-type  $\text{Mo}_2\text{B}$  are respectively determined to be 197.9 and 158.3  $\text{W m}^{-1} \text{K}^{-1}$  at room temperature. In addition, the specific heat and thermal expansion behavior are studied. Low TECs are determined, and thermal contraction is determined in the T-type configuration. Based on the high mechanical strength, favorable electrical and thermal conductivities, and low TECs, both the H- and T-type  $\text{Mo}_2\text{B}$  could be promising conductive materials in 2D electronic devices. Moreover, the performances in LIBs are studied. The storage capacity in the T-type configuration is comparable with that in the synthesized  $\text{Mo}_2\text{C}$ , and the migration energy barrier is even lower. Based on the data calculated,  $\text{Mo}_2\text{B}$  could be a candidate anode material in LIBs. We look forward to the synthesis of this MBene in the near future.

## Conflicts of interest

There are no conflicts to declare.

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