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Magnetic response of FeRh to static and dynamic disorder

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Atomic scale defects generated using focused ion as well as laser beams can activate ferromagnetism in initially non-ferromagnetic B2 ordered alloy thin film templates. Such defects can be induced locally, confining the ferromagnetic objects within well-defined nanoscale regions. The characterization of these atomic scale defects is challenging, and the mechanism for the emergence of ferromagnetism due to sensitive lattice disordering is unclear. Here we directly probe a variety of microscopic defects in systematically disordered B2 FeRh thin films that are initially antiferromagnetic and undergo a thermally-driven isostructural phase transition to a volatile ferromagnetic state. We show that the presence of static disorder *i.e.*, the slight deviations of atoms from their equilibrium sites is sufficient to induce a non-volatile ferromagnetic state at room temperature. A static mean square relative displacement of $9 \times 10^{-4} \ \text{Å}^{-2}$ is associated with the occurrence of non-volatile ferromagnetism and replicates a snapshot of the dynamic disorder observed in the thermally-driven ferromagnetic state. The equivalence of static and dynamic disorder with respect to the ferromagnetic behavior can provide insights into the emergence of ferromagnetic coupling as well as achieving tunable magnetic properties through defect manipulations in alloys.

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1 Introduction

Equiatomic FeRh is well-known for its unique properties, including a first-order metamagnetic isostructural transition from a low temperature antiferromagnetic (AFM) to a high temperature ferromagnetic (FM) phase, at the transition temperature $T_{\rm tr}$ of approximately 370 K. Potential applications include heat-assisted magnetic recording (HAMR), magnetotransport, antiferromagnetic spintronics and magnetic refrigeration. For this purpose, efforts are made to engineer the hysteresis, for example by growing epitaxial thin films on different substrates, varying the strain affected volume by modifying the film-thickness to doping the system to shift

Apart from the isostructural phase transition, B2-FeRh also possesses a disorder-induced phase transition, which can be driven, for example, by ion or laser irradiation. 18 This process has been known for FeRh and was initially shown by Iwase et al.,19 where irradiating a bulk FeRh sample with Ni, Kr, Xe or Au ions, leads to a finite orbital polarization measured by X-ray magnetic circular dichroism (XMCD) at the Fe K edge below room temperature. Systematic disordering is achieved via irradiation with light noble gas ions, such as He⁺ or Ne⁺ with sufficient energy to cause displacements of the Fe and Rh atoms from their ordered sites without artificially doping the system with materials possessing free electrons. Recently, similar investigations have been performed for FeRh thin films irradiated with He⁺ (ref. 20) and Ne⁺ (ref. 21 and 22) showing, for low irradiation fluence, an increase of the magnetization at low temperature. For bulk FeRh alloys similar investigations have been performed, where the magnetization depends strongly on the ion species.23-25 Previously, only microscopic investigations of the disorder-induced ferromagnetic phase in FeRh were performed with measurement techniques, which integrate all magnetic contributions,

the phase transition towards lower or higher temperatures. ^{13,14} During this metamagnetic phase transition of equiatomic FeRh the local Fe and Rh moments increase from $\pm 3~\mu_{\rm B}$ and 0 $\mu_{\rm B}$ in the AFM phase to 3.3 $\mu_{\rm B}$ and 1.0 $\mu_{\rm B}$, respectively, in the FM phase, accompanied by a volume increase of 1%. ^{15–17}

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making it dificult to separate contributions from the different crystallographic sites or phases in metallic systems.

In comparison, a similar effect occurs in $Fe_{60}Al_{40}$, where the recombination of vacancies in ion irradiated B2-ordered $Fe_{60}Al_{40}$ thin films leads to the formation of a disordered bcc structure (A2 structure) with ferromagnetic ordering at room temperature. Extended X-ray absorption fine structure spectroscopy (EXAFS) measurements at the Fe K edge reveal the formation of Fe and Al-rich regions with increasing irradiation fluence, accompanied by an expansion of the lattice. Example 128

Additional investigations of FeRh showed the existence of a new monoclinic ground state, 29-31 due to a lattice instability. As evident from the Fe-specific vibrational (phonon) density of states (VDOS, g(E)) the low energy phonon modes of the low temperature AFM phase have a higher g(E) compared to those of the FM phase.³¹ This means that (at the same temperature) the lattice of the AFM phase is softer with respect to phonons than the lattice of the FM phase.³¹ This is also revealed by the Lamb–Mössbauer factor (f-factor) and by the average atomic force constant, which both are lower for the AFM phase than for the FM phase.31 The lattice softening was also revealed in a temperature-dependent EXAFS study performed by Wakisaka et al. 32 by observing a discontinuity of the mean square relative displacement along the phase transition. Recently, FeRh gained increased interest due to the possibility to tailor the metamagnetic phase transition by inducing external strain. This can be achieved by growing FeRh thin films on a ferroelectric substrate (for example on PMN-PT or BaTiO3).33-38 In a recent work of Keavney et al., it could be shown by a combination of XMCDphotoemission electron microscopy (PEEM) and nano-XRD measurements, that the magnetostructural phase transition exhibits a defect-driven domain nucleation behaviour.39 Similar effects of an inhomogeneous phase transition have been observed in a transmission electron microscopy (TEM) study of Gatel et al., 40 where the film-surface and the film-substrate interface have a lower transition temperature than the centre of the film. Saidl et al.41 observed that the optical properties of different microscopic regions possess different transition temperatures leading to a distribution of transition temperatures $T_{\rm tr}$. Furthermore, these results can be used to explain a stable FM phase located at the surface, which has been shown by Pressacco et al.42

In this work, we investigate the effect of static disorder compared to dynamic disorder on the metamagnetic phase transition of FeRh. Dynamic disorder is defined as the motion of nuclei for example by means of zero-point vibrations at low temperatures or at higher temperatures by lattice vibrations (phonons), leading to an oscillating atomic displacement. This kind of disorder is strongly dependent on temperature. In contrast, static disorder is temperature independent and is created, for example, at the time of the crystallization process during sample preparation, effectively minimizing the formation energy. Static disorder can, for example, occur in the form of mono-vacancies, vacancy cluster, anti-site contributions (nuclei on a different crystallographic site) or a grain boundary. These kinds of defects can lead to a change of the microscopic physical properties, for example, an anti-site contribution or a vacancy effectively change the exchange interaction. This can result in the formation of ferromagnetism in an otherwise non

ferromagnetic system.⁴³ On the other hand, a grain boundary or void can generate a distortion of the lattice, effectively varying the nearest neighbour distance. In a time-averaged microscopic picture, these static variations of the nearest neighbour distance have the same effect as lattice vibrations leading to a blurred distribution of bond lengths.

For a detailed investigation of the difference or similarities of dynamic and static disorder, it is necessary to investigate the system on a microscopic scale by considering the electronic structure, local structure and the defect structure. We combine magnetometry measurements with conversion electron Mössbauer spectroscopy (CEMS) in order to relate changes in macroscopic magnetization to the local magnetic properties and the electronic structure of the system. With this approach, we can separate changes of the electronic structure on the microscopic scale and correlate these with changes of the macroscopic scale. Also, changes of the local structure by element-specific extended X-ray absorption spectroscopy at the Fe K edge will be presented, while an interlink between defects and the disordering process will be highlighted by positron annihilation spectroscopy (PAS). We show that for an ion irradiation fluence below 0.4 Ne⁺ per nm² an equivalence of the AFM-FM transition occurs compared to a temperature-induced phase transition. By freezing in the ferromagnetic state, the mechanism for the emergence of the ferromagnetism can be explored in greater detail.

2 Results

2.1 Macroscopic magnetic properties

Field dependent measurements performed at 300 K (Fig. 1a) show, for a MBE grown 40 nm FeRh thin film, with a residual A1 phase, a small saturation magnetization of 25 emu cm⁻³ consistent with an AFM-ordered system with a small fraction of non-compensated Fe-spins particulary at the surface. 42,44 For the irradiated samples, a hysteresis divided into two parts is observed. In small applied magnetic fields a hysteresis occurs with a coercive field below 50 mT, while for higher magnetic fields a second loop occurs which closes in the case of applying a field of 9 T. This loop can also be observed in the ordered samples at temperatures below the phase transition by applying a large magnetic field (e.g. $H \approx 11 \text{ T for } T \approx 300 \text{ K})^{5,45}$ and can be interpreted as the field induced isostructural AFM-FM phase transition.46,47 Temperature-dependent magnetization measurements show, that for the initial B2-ordered sample the first-order phase transition occurs at 370 K with a symmetric thermal hysteresis width of 10 K (see Fig. 1b). The increase of the magnetization at low temperatures originates from defects and impurities48 in the MgO substrate. With increasing ion irradiation fluence, the initial sharp transition occurs at lower temperature and the hysteresis width increases, while additionally, the magnetization at low temperatures increases.

2.2 Microscopic magnetic properties

Mössbauer spectroscopy probes slight deviations in the energy levels of the ⁵⁷Fe-nuclei due to the presence of hyperfine

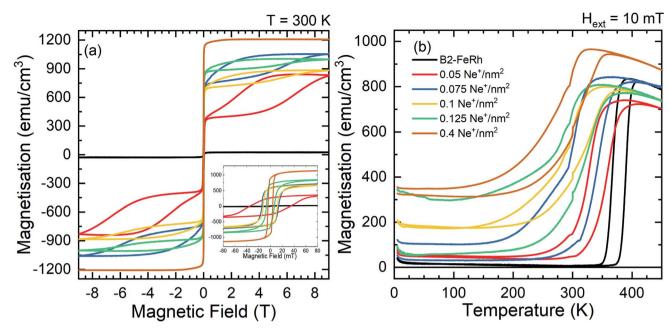


Fig. 1 Macroscopic magnetization as a function of magnetic field (a) and temperature (b) for different irradiation fluences. The field dependent measurements were performed at 300 K, while for the temperature dependent measurements an external magnetic field of 10 mT was applied. The inset of figure (a) shows the hysteresis in a field range between ±80 mT. The same color code is valid for (a) and (b).

interactions, and measures the valence state of iron and the orientation of the Fe-spin relative to the incident γ -ray. Since the hyperfine field may be roughly proportional to the magnetic moment⁴⁹ changes of the microscopic Fe moment can be probed. Room temperature zero-field measurements show two distinct states in the B2-FeRh film (see Fig. 2i). The majority phase can be described by a magnetic split sextet state with peaks of the lines 1 and 6 at -4.2 mm s⁻¹ and +4.1 mm s⁻¹ respectively, corresponding to a hyperfine field $B_{\rm hf}=25.4$ T. This is in good agreement with different Mössbauer investigations of AFM B2-ordered FeRh.^{15,50} The intensity ratio of lines 2 (5) and 3 (4), also referred to as $A_{2,3}$ -ratio describes the average angle θ between Fe-spin and incident γ -ray, by the formula.

$$A_{2,3} = \frac{I_2}{I_3} = \frac{4\sin^2(\theta)}{1 + \cos^2(\theta)}.$$
 (1)

Therefore, the $A_{2,3}$ -ratio exhibits values between 0 ($\Theta=0^\circ$ with spin orientation out of plane) and 4 ($\Theta=90^\circ$ with spin orientation in-plane). From the performed measurements, we determine an $A_{2,3}$ -ratio of 3.9, corresponding to an almost inplane spin orientation. The second contribution, (a single peak at about $-0.1~\rm mm~s^{-1}$) can be attributed to A1–FeRh, ^{15,51,52} which exhibits paramagnetism at RT. Both spectral contributions show a small negative isomer shift $\delta_{\rm iso}$ of $-0.01~\rm mm~s^{-1}$, close to that of bulk bcc-Fe, which represents the metallic character of the sample and no oxide contribution ($\delta_{\rm iso}$ (oxide) > 0.3 mm s⁻¹) is present. Upon rising temperatures (Fig. 2(ii)), the hyperfine splitting of the sextet decreases and close to the transition temperature at 380 K a third contribution appears, which indicates the isostructural AFM–FM transition. As is seen for temperatures below 380 K a decrease of the hyperfine field

occurs, expected for an AFM-system approaching its Néel temperature $T_{\rm N}$, and at 375 K the third phase occurs, leading to an increase of the average hyperfine field by 1.4 T. The third phase with the increased hyperfine field is assigned to the FM phase of B2-FeRh.¹⁵ The magnetic splitting of this third magnetic state also decreases upon heating. By using a Brillouin-function to describe the temperature dependence of the average $B_{\rm hf}$, one can determine an extrapolated Néel temperature $T_{\rm N}=615\pm17$ K for the first phase and a Curie temperature $T_{\rm C}=662\pm13$ K for the third phase, the latter being in reasonable agreement with the Curie temperature obtained by magnetometry on thin films ($T_{\rm C}=670$ K).⁵³ and bulk materials ($T_{\rm C}=675$ K).⁵⁴

In the chemically disordered system after irradiation with 25 keV Ne⁺ with a small ion fluence (Fig. 2(iii)), changes in the magnetically ordered state are observed. From the initially ordered state, it is seen that an additional spectrum arises leading to a broadening of lines 2 and 5 combined with an additional fine structure at lines 1 and 6 corresponding to a hyperfine field of 27.4 T. With increasing irradiation fluence the relative spectral area of this phase increases, which leads to an average hyperfine field of 27.4 T for the maximum irradiated sample. Hence, anti-site Fe (Fe on an initial Rh site with $B_{\rm hf}$ (Fe_{II} = 38 T)) is not created, as one can observe for a Fe-rich B2-FeRh sample, and also the formation of the A2 phase¹⁵ (B_{hf} (A2) = 35 T) does not occur. As discussed for the Mössbauer results, one can see that the samples have different amounts of A1-FeRh (blue central singlet), showing an inhomogeneous distribution of this impurity phase,52 while for the present low irradiation fluences a formation of additional A1-FeRh does not occur. 20-22

All of the measured magnetically split spectra were described by a hyperfine field distribution, which is presented for the

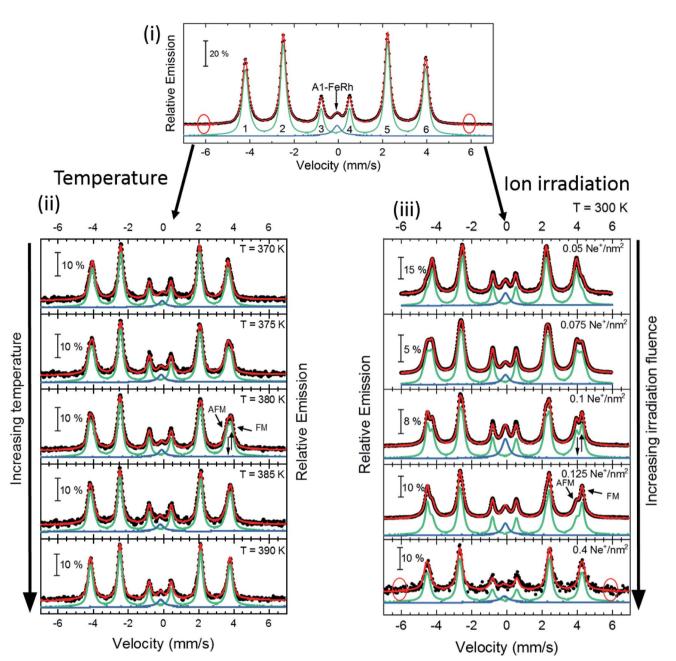


Fig. 2 Zero-field Conversion Electron Mössbauer Spectroscopy (CEMS) results for 40 nm thick FeRh thin film. (i) Room temperature Mössbauer spectrum and corresponding least-squares fit for the B2-FeRh thin film using a hyperfine-field distribution $p(B_{hf})$ for the sextet (green) and a Lorentzian single line for the central weak singlet (blue). The corresponding nomenclature of the different sextet lines is shown. (ii) Spectra for different temperatures across the phase transition in the AFM-FM coexistence region. The corresponding measurement temperature is presented in each panel. (iii) Spectra for samples irradiated with different ion fluences varying from 0.05 up to 0.4 Ne⁺ per nm² with an ion energy of 25 keV. In all graphs, the blue subspectra describe a paramagnetic secondary phase, while the green subspectra illustrates the contribution of hyperfine fields. The obtained hyperfine field distribution $p(B_{hf})$ for the different measurements can been seen in Fig. 3. The expected positions of sextets line 1 and 6 caused by anti-site Fe^{15,16} is highlighted by red circles in (i). Details of the fitting procedure are given in the text.

temperature-driven phase transition and irradiation induced transition in Fig. 3. By defining the macroscopic remanent magnetization as an order parameter of the individual phase transition, one can compare the changes of the microscopic ⁵⁷Fe hyperfine field for a system with a thermally driven phase transition (Fig. 3a) to a systematically structural disordered system (Fig. 3c). The plots for the dependence of the

microscopic hyperfine field as a function of the macroscopic magnetisation are shown in Fig. 3b and d. From this comparison we find that by a systematic increase of the structural disorder, a FM-phase with a hyperfine field of 27.4 T is induced (Fig. 2(iii)), which corresponds to the hyperfine field found at room temperature for ferromagnetic B2 ordered $Fe_{51}Rh_{49}$. ¹⁵⁻¹⁷ These measurements demonstrate, that the metamagnetic

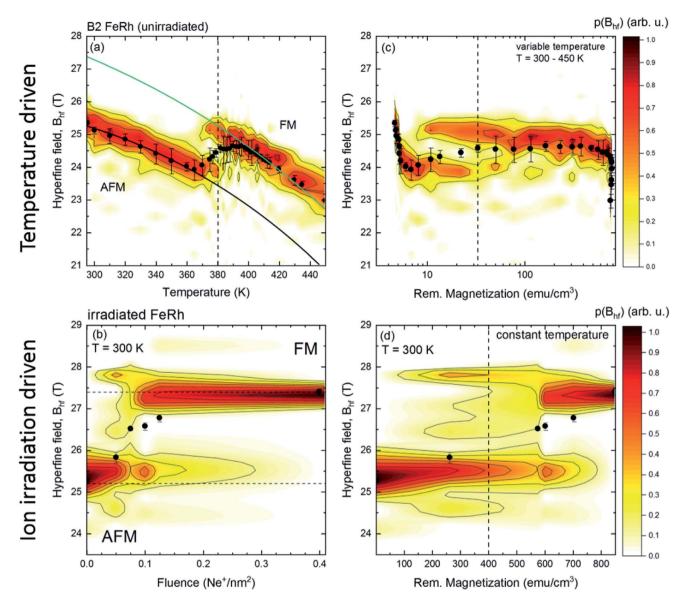


Fig. 3 Hyperfine field distribution $p(B_{hf})$ (color code) obtained from zero-field conversion electron Mössbauer spectroscopy for a 40 nm FeRh thin film. Subfigure (a) shows the changes of the hyperfine field distribution across the magnetostructural phase transition and subfigure (b) illustrates the hyperfine field distribution at 300 K for different disordered states obtained by ion irradiation with 25 keV Ne⁺ with different fluences. Subfigures (c) and (d) present the $p(B_{hf})$ distribution as a function of the macroscopic (remanent) magnetization obtained from temperature dependent (c) or field dependent measurements (d) shown in Fig. 1. The value of the average hyperfine field $\langle B_{hf} \rangle$ for each measurement is indicated with a black dot.

isostructural phase transition can be driven by ion irradiation with low fluences, as the changes of the microscopic moment as a function of the macroscopic remanent magnetisation show a similar trend compared to a temperature-driven system (Fig. 3).

2.3 Microscopic local structure

EXAFS measurements have been performed at the Fe K edge at low temperatures (T=5 K) to identify changes of the microscopic local structure. For the analysis of the measured spectra and to resolve the fine structure $\chi(k)$ the DEMETER package tool⁵⁵ has been used. For the Fourier transformation of the

signal a Kaiser-Bessel window function (Fig. 4a) has been used starting at $k_{\rm min} = 2.3 \, {\rm \AA}^{-1}$ and ending at $k_{\rm max} = 13.3 \, {\rm \AA}^{-1} \, (\Delta k = 11 \, {\rm \AA}^{-1})$ with a width of $dk = 0.1 \, {\rm \AA}^{-1}$. The Fig. 4a shows a small decrease of the amplitude in the fine structure, while no clear change of the oscillations can be discovered by comparing an as-grown film with a film irradiated with 0.4 Ne⁺ per nm².

In comparison, a similar $\chi(k)$ has been observed for FeRh in the work of Wakisaka *et al.*³² by temperature-dependent EXAFS measurements at Fe and Rh K edge. The amplitude of the Fourier Transform is illustrated in Fig. 4b for the two different states. The profiles are very similar, with an overall slight decrease in the intensity of the peaks. The first peak between 1.5–3 Å originates from back-scattering from the nearest

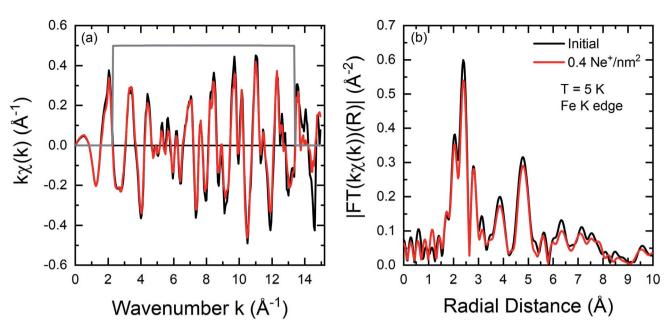


Fig. 4 (a) Fe K edge k weighted EXAFS oscillations $k\chi(k)$ for an initial FeRh (black) thin film and the sample irradiated with 0.4 Ne⁺ per nm² (red). (b) Corresponding Fourier transforms $|FT(k\chi(k))|$. Details concerning the Fourier transformation are given in the text. Measurements have been performed at T=5 K.

neighbour Rh shell. The dip at 2 Å (ref. 56 and 57) is due to the Ramsauer–Townsend effect, visible in the $\chi(k)$ as a pronounced minimum in the amplitude near 5 Å⁻¹.

2.4 Characterisation of open volume defect concentration

Doppler broadening variable energy positron annihilation spectroscopy (DB-VEPAS) probes the open volume defects in a solid, where one detects changes of width and intensity of the 511 keV positron annihilation line. The S-parameter is the fraction of positrons annihilating with low momentum valence electrons. It represents vacancy type defects and their concentration. Plotting the calculated S parameter as a function of positron implantation energy, S(E), provides depth dependent information on the defect concentration.58 For the analysis of positron diffusion length, L_{+} , which is inversely proportional to defect concentration, the VEPFit code⁵⁹ has been utilised, which permits to fit $S(E_p)$ curves for multilayered systems and to acquire thickness, L_+ , and the specific S-parameters for each layer within a stack. L_+ has been calculated as 19.7(1), 7.27(4), and 5.68(4) nm for the as-grown, irradiated with 0.1 Ne⁺ per nm², and 0.125 Ne⁺ per nm² films, respectively. The thickness of the film was fixed to 42.8 nm for all three samples, utilizing a material density of $\rho_{\rm FeRh} = 9.76 \ {\rm g \ cm^{-3}}$ for FeRh and $\rho_{\rm MeO} =$ 3.6 g cm⁻³ for MgO respectively. L_+ for MgO was fixed to 35 nm for all the samples (the fitted values: 33-37 nm). The as-grown sample, because of a large L_+ , has a relatively low defect concentration nearly as low as the MgO crystal. Ion irradiation produces damage to the film structure introducing vacancy like defects. Most likely, the size of defects remains the same and only the defect concentration increases (by a factor of 4 for the largest fluence). DB-VEPAS clearly shows an increase in the defect concentration, Fig. 5. This implies that the fraction of the

open volumes, the empty spaces in the lattice increase with increasing fluence. However, the defect type, whether purely static disorder or vacancy like defects, cannot be ascribed from the Doppler Broadening results alone. Nevertheless, the increase of the open volumes is consistent with the increased static disordering observed in the ion-irradiated films, as determined from the EXAFS measurements, discussed in the next section.

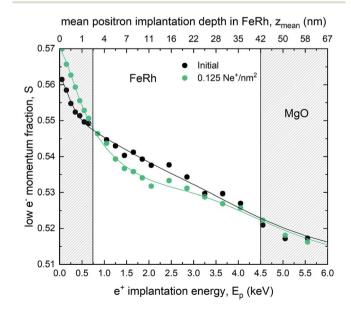


Fig. 5 Line shape parameter S of the annihilation as a function of the incident positron energy obtained by DB-VEPAS. Theoretical fits of the S(E) spectrum are presented for the as-grown and irradiated samples with a fluence of 0.125 Ne⁺ per nm².

3 Discussion & conclusion

From the performed EXAFS measurements it is evident that a change in the chemical composition of the nearest neighbour shell upon ion irradiation is not detected. A variation of the chemical composition that can give rise to the onset of Fe-rich regions due to intermixing and would lead to changes in the relative intensity of specific features in the Fourier transform, as it is the case for example in ion irradiated Fe₆₀Al₄₀ thin films does not occur in FeRh.28 This is in contrast to XRD measurements,22 where intermixing has been suggested due to an observed decrease of the long-range order parameter S with rising ion irradiation fluence. In fact, the spectra of the disordered sample can be simulated by analyzing the effect of a static mean square relative displacement (MSRD) $\sigma_{\rm stat}^2$ of 9 \times 10⁻⁴ \mathring{A}^{-2} on the spectra of the ordered (as-grown) sample, while changes of the dynamic contributions can be neglected due to the low measurement temperature (T = 5 K). This shows that the Ne⁺-irradiation causes an increase of the MSRD. This can be due to the increased structural disorder and lattice distortions, for example, by trapped Ne ions inside the lattice²⁰ or a decreased grain size, increasing the static disorder. DB-VEPAS reveals such an increase of the defect concentration leading to an increase of open volume.

On the other hand, in temperature-dependent magnetisation measurements, a ferromagnetic ordering at low temperatures is present for the ion irradiated samples, while this is accompanied by a broadening of the hysteresis and a decrease of $T_{\rm tr}$. From the field and temperature-dependent measurements, it is seen that a coexistence of two different magnetically ordered states occurs. As shown in Fig. 1, the first magnetic phase is a soft ferromagnetic phase and can be attributed to the disorder-induced phase, while the second phase can be described to the initial hard magnetic B2 phase with an AFM ordering, where an increased field breaks the anti-parallel spin alignment and induces the formation of FM ordering. A similar increase of the magnetisation at low temperatures has been observed previously, where, for higher irradiation fluences, 21,22,60 a suppression of the AFM-FM transition and even a suppression of the ferromagnetic ordering was observed, while forming the paramagnetic A1 phase (fcc). The deviation in the increase of the high field magnetisation as a function of the ion fluence is due to the fact, that the two samples exhibit a different amount of a secondary A1-FeRh phase (as discussed before in Section 2.2). The secondary phase has not been considered in the magnetisation normalisation due to the unknown composition of the secondary phase. 61 Defining the remanent macroscopic magnetisation M_r as an order parameter of the phase transition in the temperature-driven or ion-irradiation induced AFM-FM transition and comparing the dependence of $B_{\rm hf}$ as a function of the remanent magnetisation, a similarity between the two distinct phase transitions is present (shown in Fig. 3c and d). For the temperature-driven phase transition for small M_r the hyperfine field B_{hf} decreases, while a secondary magnetic contribution occurs at 10 emu cm⁻³

from the ferromagnetic phase with the coexistence of both $B_{\rm hf}$ contributions (AFM and FM) up to 100 emu cm⁻³. From the temperature dependence for elevated temperatures using a Brillouin function a hyperfine splitting $B_{\rm hf} = 27.4 \, \mathrm{T}$ at 300 K is obtained, which corresponds to the hyperfine field splitting of FM Fe₅₁Rh₄₉ at 300 K.¹⁵ In the ion irradiated samples, an additional magnetic contribution occurs at 27.4 T, whose spectral contribution increases with rising ion fluence and $M_{\rm r}$. The occurrence of this ferromagnetic phase can be explained, for example, by a change of the chemical composition and the formation of Fe-rich regions (Fe nucleus on a Rh-site). Such a change is not persuasively present in the Mössbauer spectra (maximum 0.6 Fe-at%), consistent with the EXAFS measurement. Therefore, the formation of the ferromagnetic ordering needs to be explained by a different process.

In the thermally induced phase transition a discontinuous increase of the short-range disorder (MSRD32 or Lamb-Mössbauer factor31) occurs, while in the ion irradiated sample an increase of the static disorder can be seen, indicated by the increased MSRD σ^2 (EXAFS). This is due to induced grain boundaries or lattice distortions owing to ion irradiation. This increase of the defect concentration was confirmed in the positron annihilation spectroscopy (decreasing L_+). Combining the observed changes of the hyperfine field splitting towards an identical splitting in the FM phase at 300 K and an increase of the static disorder in EXAFS, while changes of the chemical composition are absent - the effect can be explained in such a way that a structural defect breaks the local symmetry. Hence, a modification of the electronic structure takes place, effectively lowering the transition temperature of the surroundings. This concept of a defect-driven domain nucleation growth in B2 FeRh was previously suggested by Keavney et al.39

In summary, we found an increase of the static structural disorder in FeRh thin films irradiated with low ion fluences, while no substantial intermixing of Fe and Rh atoms can be observed on the local scale by microscopic probes such as CEMS or EXAFS. Besides, PAS-measurements show an increase of open volume defect concentration, while the size of the defects does not change. 57Fe-CEMS measurements reveal a second magnetic phase with an increased relative spectral area with rising irradiation fluence. The hyperfine field splitting of this second magnetic phase is identical to that of ferromagnetic B2-FeRh. By comparing the thermally-driven and the structural disorder-driven phase transition a jump-like behaviour of the remanent magnetization dependence of the hyperfine field can be observed. Thus, in B2 Fe₅₀Rh₅₀, slight deviations of the Fe and Rh atoms from equilibrium lattice positions are sufficient to induce a ferromagnetic onset. These lattice deviations can be dynamic, as realized through thermal excitations above the metamagnetic transition. The ferromagnetic onset can also be realized through irradiation-induced static disorder, which is a snap-shot equivalent to the thermally driven dynamic disorder. Further investigations, for example by positron annihilation lifetime spectroscopy, may reveal the defect type and

provide further understanding of the formation of irradiation-induced ferromagnetism in B2-FeRh.

4 Experimental

FeRh thin films were grown by molecular-beam epitaxy (MBE) by co-deposition of ⁵⁷Fe-metal (95% enriched in the isotope ⁵⁷Fe) and Rh in ultrahigh vacuum ($p_{\text{growth}} = 4 \times 10^{-9} \text{ mbar}$) on a MgO(001) substrate. Before the deposition of the film, the MgO(001) substrate was cleaned using isopropanol and was heated at 300 °C for 60 min in a pressure of 1×10^{-9} mbar to remove contaminants from the surface structure. During the deposition, the temperature of the substrate was 300 °C, while the deposition rates of ⁵⁷Fe and Rh were measured and controlled by independent quartz-crystal oscillators. After deposition the film was in situ annealed at $700~^{\circ}\text{C}$ for 90 min to ensure the formation of the B2 structure. The thickness of the sample was confirmed to be 42.8 nm by X-ray reflectivity. It is worthwhile to mention, that due to slight deviations of the composition it is possible to stabilize the FM phase below room temperature (for example in an Fe-rich sample consisting of Fe₅₁Rh₄₉) a stable FM phase is present even at low temperatures. Therefore, it is necessary to have an optimal control of the deposition rates of the individual constituents. Furthermore, the application of a capping layer to prevent oxidation has been avoided based on the observations made in different works, 20,62-64 where the capping layer influenced the magnetic properties of the B2-ordered system in such a way that a ferromagnetic phase was observed at the interface between the film and capping layer. Based on the performed CEMS and PAS measurements, we can neglect the formation of an oxide layer. In Mössbauer spectroscopy, an Fe-oxide (for example Fe₃O₄) would be present with a hyperfine splitting B_{hf} close to 50 T and an isomer shift δ_{iso} around 0.3 mm s⁻¹ (Fe³⁺) or 1.0 mm s⁻¹ (Fe²⁺) at room temperature.65 At the same time, FeOx (Wustite) is characterized by a paramagnetic asymmetric feature with an isomer shift of 1.0 mm s⁻¹.66 This contribution is not detected in our Mössbauer spectra. Furthermore, from the positron annihilation spectroscopy, an additional oxide layer would result in a different dependence of the S parameter at positron energies E_p below 1 keV, e.g. in the form of a plateau, a minimum, or a maximum.⁶⁷ Summarizing, all these spectroscopic features, which would hint towards an Fe-oxide layer, are not present in the studied samples.

The as-grown sample was cut into three pieces, while the first piece was used to perform magnetometry and temperature-dependent ⁵⁷Fe-CEMS measurements, the second and third sample pieces were used for an initial irradiation with 0.05 Ne⁺ per nm² and 0.075 Ne⁺ per nm² respectively. Both irradiated samples were then further irradiated with 0.05 Ne⁺ per nm² to achieve a total irradiation of 0.1 and 0.125 Ne⁺ per nm² respectively. In addition, a sample with an irradiation dose of 0.4 Ne⁺ per nm² was used for EXAFS measurements. For the different irradiation steps an ion energy of 25 keV has been chosen based on SRIM⁶⁸ simulations to fully penetrate the film volume while minimizing defects in the substrate.

Magnetic characterization was performed using the vibrating sample magnetometer (VSM) option of a Quantum Design PPMS DynaCool, providing magnetic fields up to ± 9 T

applied parallel to the film surface in a temperature range between 4.3 K and 400 K. Temperature-dependent magnetization measurements were performed in an external field of 10 mT using the ZFC-FC protocol. To achieve a temperature of 450 K a ceramic sample holder and the VSM oven option (temperature range between 300 and 1000 K) was used, resulting in an offset at 300 K due to different sensitivity ranges.

 57 Mössbauer spectroscopy at perpendicular incidence of the γ -rays onto the film surface was performed by detection of conversion electrons. For the detection of the electrons, the sample was installed in a proportional gas counter, *i.e.* housing with a continuous He gas flow mixed with 4% CH₄ to avoid ionization processes. For the measurement, a constant acceleration Mössbauer driving unit was used with a 57 Co source embedded in an Rh matrix, while the velocity of the spectrometer was calibrated with a α -Fe foil reference sample at room temperature. The experimental spectra were evaluated by a least-squares fitting routine using the Pi program package. 69

Element-specific EXAFS measurements have been performed at the XAS beamline BM23 at the ESRF. ⁷⁰ Spectra have been recorded at the Fe K absorption edge in the total fluorescence yield detection mode at 45° incident geometry using an energy dispersive detector to detect the signal originating from the Fe K_{α} -radiation.

Doppler broadening variable energy positron annihilation spectroscopy (DB-VEPAS) measurements have been conducted using the apparatus for in situ defect analysis^{67,71} of the slow positron beamline⁷² located at the Helmholtz-Zentrum Dresden-Rossendorf. Positrons were extracted from a radioactive 22Na source, moderated down to several eV and magnetically guided to the accelerator unit, where they were subsequently accelerated in discrete voltage values in the range of $E_p = 0.04-35$ keV. This positron energy allows depth profiling of the films from the surface down to about 2 µm for FeRh, while a mean positron implantation depth can be approximated by a simple material density-dependent formula: $z_{\text{mean}} =$ $3.69E_{\rm p}^{1.62}$, where $z_{\rm mean}$ is expressed in the units of nm. The broadening of the 511 keV annihilation line has been measured with a high purity Ge detector, having energy resolution of 1.09 \pm 0.01 keV at 511 keV. Implanted into a solid, positrons lose their kinetic energy due to thermalisation and after short diffusion time, annihilate in delocalized lattice sites or localise in vacancy like defects and interfaces usually emitting two anticollinear 511 keV gamma photons once they interact with electrons. Since at the annihilation site thermalised positrons have minimal momentum compared to the electrons a broadening of the 511 keV annihilation line is observed mostly due to the momentum of the electrons. The broadening of the positron annihilation line is characterised by two distinct parameters *S*, and W defined as a fraction of the annihilation line in the middle (511 \pm 0.93 keV) and outer regions (508.56 \pm 0.35 keV and 513.44 \pm 0.35 keV), respectively.

Conflicts of interest

There are no conflicts to declare.

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