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## Mechanism of amorphous phase stabilization in ultrathin films of monoatomic phase change material†

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Elemental antimony has been recently proposed as a promising material for phase change memories with improved performances with respect to the most used ternary chalcogenide alloys. The compositional simplification prevents reliability problems due to demixing of the alloy during memory operation. This is made possible by the dramatic stabilization of the amorphous phase once Sb is confined in an ultrathin film 3–5 nm thick. In this work, we shed light on the microscopic origin of this effect by means of large scale molecular dynamics simulations based on an interatomic potential generated with a machine learning technique. The simulations suggest that the dramatic reduction of the crystal growth velocity in the film with respect to the bulk is due to the effect of nanoconfinement on the fast  $\beta$  relaxation dynamics while the slow  $\alpha$  relaxation is essentially unaffected.

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### 1. Introduction

Chalcogenide phase change materials are attracting an increasing interest for several technological applications ranging from electronic non-volatile memories<sup>1–3</sup> and neuro-inspired computing<sup>4–6</sup> to photonic devices.<sup>7</sup> The prototypical materials for these applications are ternary GeSbTe alloys, mostly on the pseudobinary GeTe–Sb<sub>2</sub>Te<sub>3</sub> tie-line.<sup>1</sup> The devices exploit a fast and reversible switching between the crystalline and amorphous phases induced by heating either by electrical current pulses or by laser irradiation in electronic or optical devices. Amorphization of the material is obtained upon heating the crystal above the melting temperature, with subsequent rapid quenching, while recrystallization of the amorphous phase takes place at temperatures in between the glass transition and melting.

The high electric fields and high temperature gradients that are present during device operations are responsible for atomic diffusion which, beside incongruent melting, can lead to demixing of the chalcogenide alloy with device failure.<sup>8,9</sup> Moreover, scaling of the devices can exacerbate the cell-to-cell

variability due to compositional variations which are unavoidable in multielement alloys.

Recently, it has been proposed that these reliability problems could be overcome by using pure antimony as a monoatomic phase change material.<sup>10</sup> Although amorphous Sb crystallizes very rapidly or even explosively at normal conditions in the bulk,<sup>11</sup> crystallization is hindered in ultrathin films 10–3 nm thick encapsulated by capping layers (a silica substrate plus a (ZnS)<sub>8</sub>–(SiO<sub>2</sub>)<sub>2</sub> capping). Stabilization of the amorphous phase at 286 K for up to tens of hours has been shown indeed for the thinnest film of 3 nm.<sup>10</sup> Confinement of antimony at the nanoscale also leads to a dramatic reduction of the structural relaxations responsible for the aging and the drift in time of the electrical conductivity in the amorphous phase<sup>10</sup> which could be further exploited for precise neuromorphic computing.<sup>12</sup> Switchable antimony films with thickness below 15 nm have also been proposed very recently for photonic applications.<sup>13</sup>

Molecular dynamics (MD) simulations based on Density Functional Theory (DFT) revealed that the protocol used to generate the amorphous phase has strong effects on the crystallization kinetics of Sb.<sup>10</sup> An abrupt quenching from the melt to 300 K yielded indeed an amorphous model that did not crystallize by homogeneous nucleation over 0.8 ns, while a supercritical nucleus appeared within 100 ps at 300 K in a model quenched from 900 to 300 K in about 60 ps.<sup>10</sup> It is, however, unclear whether the spatial confinement in the thin film in the experimental device of ref. 10 could also imply a sufficiently fast quenching.

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Different other factors, either dynamical or thermodynamical, could in principle concur to raise the crystallization temperature  $T_x$  by decreasing thickness in thin films as reviewed for phase change materials in ref. 14. For instance, a higher interfacial energy with the capping layer for the crystal than for the amorphous phase could also raise  $T_x$ . A thickness dependence stress introduced by the interface could affect either the thermodynamics of the crystallization process or most probably the atomic mobility in the film. The presence themselves of thermally stable capping layers is also expected to affect the atomic mobility close to the interface and deeper in the film.<sup>15</sup> In the presence of cooperative atomic motions, a change in mobility might also arise once the size of Cooperative Rearranging Region (CRR) in the supercooled liquid phase becomes comparable with the film thickness.<sup>15</sup> The formation of strong bonds with the unpassivated surface of the capping layer has also been shown to hinder crystallization in a three-layers  $\text{Sb}_2\text{Te}_3$  ultrathin film capped by amorphous silica.<sup>16</sup>

In this paper, we report on large scale MD simulations of antimony in nanoconfined geometries aiming at uncovering the mechanisms of stabilization of the amorphous phase in ultrathin films. To this end, we made use of an interatomic potential generated by fitting a large database of DFT energies and forces with the machine learning method based on a Neural Network (NN) scheme proposed in ref. 17 and 18. The same framework was exploited previously to generate an interatomic potential for the phase change compound  $\text{GeTe}$ <sup>19</sup> which allowed us to address several properties ranging from dynamical heterogeneity<sup>20</sup> and fast crystallization<sup>21–23</sup> in the supercooled liquid to structural relaxations and thermal transport in the amorphous phase in the bulk<sup>24–26</sup> and in nanowires.<sup>27,28</sup>

## 2. Computational details

Molecular dynamics simulations have been performed with an interatomic potential generated with NN scheme of ref. 17 and 18, implemented in the code RuNNer<sup>29</sup> which is interfaced with the MD driver LAMMPS.<sup>30</sup> We used a feed-forward neural network featuring 2 hidden layers, 20 nodes per layer, and hyperbolic tangent as activation functions. The input layer consists of a set of 11 radial plus 16 angular symmetry functions with hyper-parameters<sup>17,18</sup> which are used to discriminate among inequivalent atomic environments within a distance cutoff of 6.5 Å which is sufficient to include the third coordination shell. In particular, the radial functions are constructed analytically as the sum of Gaussians (both shifted and unshifted), while the angular terms are constructed for all triplets of atoms by summing the cosine values of the bonding angles  $\theta_{ijk} = R_{ik} \cdot R_{ij} / (R_{ij} R_{ik})$  centered at atom  $i$ , where  $R_{ij} = R_i - R_j$  is the vector distance between atoms  $i$  and  $j$ . The parameters of the symmetry functions are chosen as to effectively and uniformly span the region of the parameters space which is most relevant for representing the local atomic environments of the crystalline, amorphous and liquid states that we monitored

from the pair correlation and bond angles distribution functions. The network contains about 1000 synaptic weights which are optimized over a large database of DFT total energies and forces of about 23 000 configurations of crystalline, liquid and amorphous models containing from 54 to 144 atoms at different temperatures and densities. These configurations were generated by DFT molecular dynamics employing the Perdew–Burke–Ernzerhof (PBE) approximation to the exchange and correlation energy functional,<sup>31</sup> norm conserving pseudopotentials and the CP2k code.<sup>32</sup> Kohn–Sham orbitals were expanded in Triple-Zeta-Valence plus Polarization (TZVP) Gaussian-type basis and the charge density was expanded in a plane-wave basis set with a cutoff of 100 Ry to efficiently solve the Poisson equation within the Quickstep scheme.<sup>32</sup> Brillouin Zone (BZ) integration was restricted to the supercell  $\Gamma$  point.

The total energies and forces of configurations used to train the NN were then computed with the Quantum-Espresso code<sup>33</sup> using the PBE functional, norm-conserving pseudopotentials and plane-waves expansion of Kohn–Sham orbitals up to an energy cutoff of 40 Ry. The BZ integration was performed over a uniform mesh by keeping approximately the same  $k$ -point linear spacing of 0.13 Å<sup>-1</sup> for all models. Mean square errors in the energy and forces for the training and test sets are given in Fig. S1 in the ESI† The NN potential was validated by computing the structural properties of the crystalline, liquid and amorphous phases as shown in Fig. S2–S7 and in Table S1 in ESI† There is evidence in literature that the inclusion of van der Waals (vdW) interactions is important to properly describe the structural properties of phase change materials such as  $\text{GeTe}$  and  $\text{Ge}_2\text{Sb}_2\text{Te}_5$ .<sup>34,35</sup> The NN potential was then used in MD simulations supplemented by the Grimme semiempirical vdW interaction potential D2.<sup>36</sup> The NN + D2 potential is able to well reproduce the A7 crystalline structure of  $\text{Sb}$ <sup>37</sup> with the alternation of short and long bonds (Table S1 in ESI†). The time step in MD simulations was set of 2 fs. A Nosé–Hoover thermostat (with 3 chains thermostats) was used as implemented in LAMMPS. The DFT benchmark calculations on liquid and amorphous  $\text{Sb}$  reported in ESI† were performed with the QE program, a 144-atom cubic supercell at the experimental density of the liquid at  $T_m$  and by restricting BZ integration to the supercell  $\Gamma$  point.

We estimated the theoretical NN + D2 melting temperature by means of a phase coexistence approach in constant pressure simulations. We prepared an orthorhombic 11 664-atom cell elongated in one direction containing a single crystal slab and a liquid slab previously equilibrated at 850 K, which is our first estimate for the melting point. The single crystal slab was generated in turn from the recrystallization of a melt-quenched amorphous model. The supercell edges were free to adjust in order to maintain a zero hydrostatic pressure. For temperatures below  $T_m$  the crystalline slab grows, while for higher temperatures the crystalline slab shrinks. Therefore, by analyzing the movement of the crystal/liquid interface we estimated  $T_m = 845$  K to be compared with the experimental value of  $T_m = 903$  K.<sup>38</sup> At 845 K the theoretical equilibrium density of the



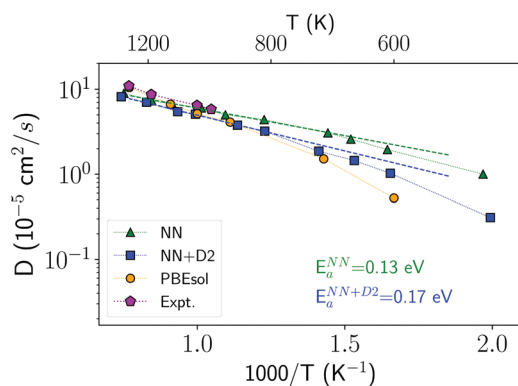
liquid of  $\rho = 0.0319 \text{ atom } \text{\AA}^{-3}$  is in very good agreement with the experimental value at melting of  $\rho = 0.0320 \text{ atom } \text{\AA}^{-3}$ .<sup>39</sup>

### 3. Results and discussion

In order to investigate the crystallization process, we first studied the atomic mobility by computing the diffusion coefficient  $D(T)$  in the bulk as a function of temperature  $T$ . The results reported in Fig. 1 are fitted by an Arrhenius function  $D = D_0 \exp(-E_a/k_B T)$  with an activation energy  $E_a = 0.17 \text{ eV}$  and a prefactor  $D_0 = 34.4 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$  which are close to the experimental values of  $E_a = 0.18 \text{ eV}$  and  $D_0 = 54.6 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$  from ref. 40.

To investigate confinement effects in the stabilization of the amorphous phase, we first considered the crystallization process in the bulk. Antimony is a growth dominated material in which crystallization mostly proceeds from the crystalline/liquid or crystalline/amorphous interface rather than from the homogeneous nucleation of crystallites, at least at the temperatures of maximal crystal growth. DFT molecular dynamics simulations have shown indeed that Sb crystallizes very fast in the presence of a crystalline Sb boundary with growth velocity of about  $36 \text{ m s}^{-1}$  at 600 K while no sign of crystal nucleation was detected on the time scale of half a ns at the same temperature.<sup>41</sup> In fact, crystal nucleation does occur on the time span of a DFT-MD run, but only in the temperature range 300–500 K as reported in ref. 42 and 43.

In agreement with previous DFT results,<sup>41–44</sup> homogeneous crystal nucleation in the supercooled liquid was not observed in NN-MD simulation on a ns time scale above 600 K. Supercritical nuclei appear instead on the time scale of 1–15 ns in the temperature range 300–450 K, but not below 300 K, as we discuss in more details later on. Therefore, in order to explore the crystallization speed in a wide temperature range,

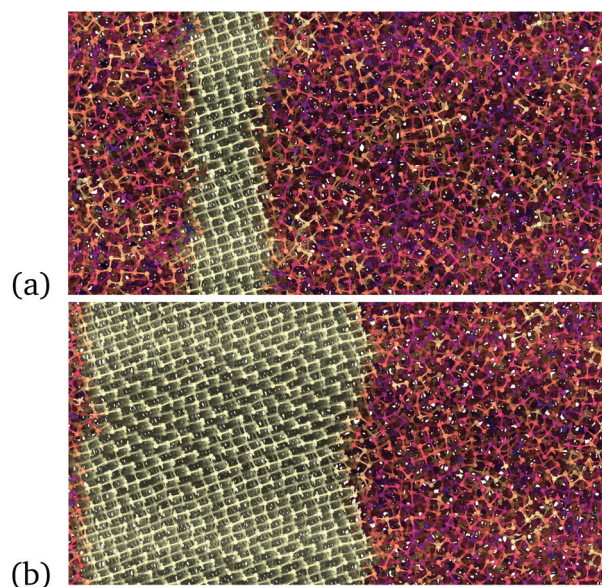


**Fig. 1** Diffusion coefficient of liquid antimony computed with the NN and NN + D2 potentials compared with the DFT-PBEsol results from ref. 41 and from experiments.<sup>40</sup> Simulations are performed at the experimental density of the liquid at the melting point ( $0.0320 \text{ atom } \text{\AA}^{-3}$ ).<sup>39</sup> The diffusion coefficient is obtained from the atomic mean square displacement over a simulation time of 100 ps at constant energy (NVE ensemble).

we consistently studied the crystal growth at a preformed crystal/amorphous interface which is also believed to be close to the experimental situation realized in the device of ref. 10. To this aim, we built an amorphous model by quenching a liquid model from 1000 K to 300 K in 80 ps with the density fixed at the experimental value for the liquid at the melting point ( $0.0320 \text{ atom } \text{\AA}^{-3}$ ).<sup>39</sup> The model contains 11 664 atoms in a supercell with edges  $14.871 \text{ nm} \times 4.957 \text{ nm} \times 4.957 \text{ nm}$  and 3D periodic boundary conditions (PBC).

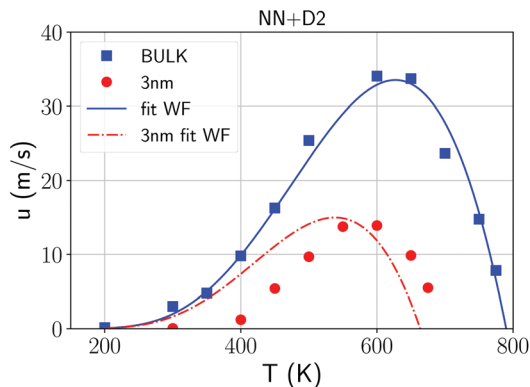
Then a slice of the simulation cell was annealed at 400 K to promote the formation of a crystalline seed, while all the other atoms in the cell were kept frozen. At these conditions, we observed the formation of a crystalline nucleus that grows fast giving rise to a uniform single-crystal region that spans the entire slice with free atoms, as shown in Fig. 2. The model was then equilibrated at different temperatures in the range 200–800 K at which constant temperature simulations were performed with all atoms free to move. Snapshots of the growth on the crystalline front in the bulk at 300 K is given in Fig. 2. The number of crystalline atoms is obtained in turn by labeling an atom as crystalline or not depending on the value of the order parameter  $\bar{Q}_4$  defined in ref. 45 and in ESI (see Fig. S8†).

The evolution of the crystal/amorphous interface was then monitored to extract the crystal growth velocities  $u$  reported in Fig. 3. The crystal growth velocity is obtained by the time derivative of the effective thickness of the crystalline slab  $L_{\text{cr}}(t) = N_{\text{cr}}(t)/2A\rho$  where  $N_{\text{cr}}(t)$  is the number of crystalline atoms,  $\rho$  is the atomic density and  $A$  is the cross section of the simulation cell which corresponds to the area of the growing



**Fig. 2** (a) Initial and (b) final configurations of the constant temperature simulation of crystal growth from a crystal/amorphous interface in the bulk at 300 K. The time lag between the initial and final snapshots is 1 ns. The color map reflects the value taken by the  $\bar{Q}_4$  parameter for crystallinity (see text, yellow for  $\bar{Q}_4 = 1$ , dark violet for  $\bar{Q}_4 \leq 0$ ).





**Fig. 3** Crystal growth velocities from NN + D2 simulations in the bulk (blue squares) and in the 3 nm film (red dots) with the Wilson–Frenkel (WF) fitting using the Arrhenius-like diffusion coefficient obtained at high temperature for the bulk (blue line, see Fig. 1) and for the film (red curve, see Fig. 5). The crystal growth velocity in the film at 300 K is  $0.06 \text{ m s}^{-1}$ .

surface. This definition is justified by the linear growth with time observed for  $L_{\text{cr}}(t)$  (Fig. S9 in ESI†) and by the nearly uniform crystal growth over the whole cross section. The factor  $1/2$  accounts for the fact that two crystal fronts are growing simultaneously from the two sides of the crystalline slab. The crystal growth velocity at 600 K in Fig. 3 is comparable with the value of  $36 \text{ m s}^{-1}$  obtained by DFT-MD with the PBEsol functional in ref. 41. We remark that the crystal growth velocities should be weakly dependent on the orientation of the crystal/liquid interface. In fact, we observed a nearly isotropic growth of crystallites nucleated homogeneously as shown in Fig. S10 in ESI.†

We remark that the alternation of short and long bonds typical of the A7 crystalline phase survives in the amorphous phase although in a disordered manner. On the other hand, the recrystallized amorphous phase also features several defective sites as shown by the angular-limited bond correlation function (ALTBC)<sup>46</sup> shown in Fig. S11 in the ESI.†

We attempted to fit the data on the crystal growth velocity with the Wilson–Frenkel (WF) expression as  $u = u_{\text{kin}}(1 - \exp(-\Delta\mu/k_{\text{B}}T))$ , where  $\Delta\mu$  is the difference in free energy between the crystalline and supercooled liquid phase which was computed according to Thomson and Spaepen<sup>47</sup> as  $\Delta\mu(T) = \frac{\Delta H(T_{\text{m}} - T)}{T_{\text{m}}} \frac{2T}{(T_{\text{m}} + T)}$ . The latent heat of fusion  $\Delta H = 0.148 \text{ eV}$  per atom was calculated at the theoretical (NN + D2) melting point  $T_{\text{m}} = 845 \text{ K}$ , estimated from the phase-coexistence method (see section 2). The theoretical value is close to the experimental value of  $\Delta H = 0.2 \text{ eV}$  per atom.<sup>48</sup> A better fit of the data on the crystal growth velocity is obtained, however, by setting  $T_{\text{m}} = 790 \text{ K}$  in the Spaepen–Thomson formula (which actually corresponds to the fitting curve in Fig. 3) possibly because the simulations of crystallization are performed at constant volume while the theoretical  $T_{\text{m}}$  is correctly obtained from constant pressure simulations which account for variations on the volume per atom upon structural transition. In

the approach used here, we consider that the free energy of the overheated amorphous phase is equal to the free energy of the supercooled liquid at the same temperature. In the original Wilson–Frenkel model, the kinetic prefactor  $u_{\text{kin}}$  is expressed as  $6D(T)/\lambda$  where  $D(T)$  is the temperature dependent diffusion coefficient and  $\lambda$  is a fitting parameter which should be of the order of the jump distance of the elementary diffusion process. The diffusion coefficient entering in  $u_{\text{kin}}$  should, however, be read as an effective atomic mobility because the diffusion coefficient  $D(T)$  is obtained from long range and long time atomic displacements while only local atomic motions actually seem to control the crystal growth of Sb as well as of Sb-rich In AgSbTe alloys (AIST) as shown by DFT-MD simulations in ref. 41 and 49. Nevertheless, a very good fitting of the data in the whole temperature range 200–800 K is obtained by using the Arrhenius function for  $D(T)$  resulting in turn from the fitting of the diffusion coefficient at high temperatures (from Fig. 1). The fitting yields a value of  $\lambda = 1.2 \text{ \AA}$  which is close to the value of  $1.7 \text{ \AA}$  obtained from the fitting with the Wilson–Frenkel formula of the DFT-MD data on the crystallization of AIST down to 455 K.<sup>50</sup> Note, however, that in the fitting for AIST the crystal growth velocity from WF is 20 % higher than the value obtained from DFT-MD at 585 K while it is a factor two lower at 455 K.<sup>50</sup>

Although the good fitting with the WF formula seems reassuring on the validity of the simple classical nucleation and growth theory, we must notice that at 350 K and below a plateau appears in the mean square displacement (MSD) as a function of time, as shown in Fig. S12 in ESI.† This behavior is typical of a two steps relaxation dynamics with a faster  $\beta$  relaxation and a slower  $\alpha$  relaxation that controls the long range atomic diffusivity after the plateau.<sup>51</sup> The system at 300 K behaves as a supercooled liquid close to the glass transition. In fact, antimony in the bulk crystallizes explosively at 300 K. The glass transition is difficult to be measured experimentally in phase change materials because crystallization obscures the exothermic peak in differential scanning calorimetry expected by heating above  $T_{\text{g}}$ . Therefore,  $T_{\text{g}}$  is often identified with the crystallization temperature. Estimates of  $T_{\text{g}}$  are given in literature for Ge doped Sb, with  $T_{\text{g}} = 382 \text{ K}$  for  $\text{Ge}_8\text{Sb}_{92}$  and  $T_{\text{g}} = 466 \text{ K}$  for  $\text{Ge}_{12}\text{Sb}_{88}$ .<sup>52</sup> There is a strong suppression of the crystallization and a raise in  $T_{\text{g}}$  due to Ge doping. Therefore, one can expect to have  $T_{\text{g}}$  close or below 300 K in pure Sb. The MSD in Fig. S12 in ESI† is obtained from constant temperature simulations (NVT) for a better control of temperature; at high temperatures we checked that NVE and NVT simulations with our settings gave the same results for  $D(T)$ . At 300 K the plateau at about a fraction of  $\text{\AA}^2$  extends up to 1 ns (Fig. S12 in ESI†) while at the same temperature the crystalline front grows by as much as  $30 \text{ \AA}$  on a 1 ns time scale. This would suggest that the crystallization kinetics at low temperature should be controlled by the  $\beta$  relaxation dynamics and not by the diffusion coefficient defined by the  $\alpha$  relaxation dynamics at longer times after the plateau in the MSD.

At high temperatures in the supercooled liquid, far from the glass transition in glass former materials, the  $\alpha$  and  $\beta$



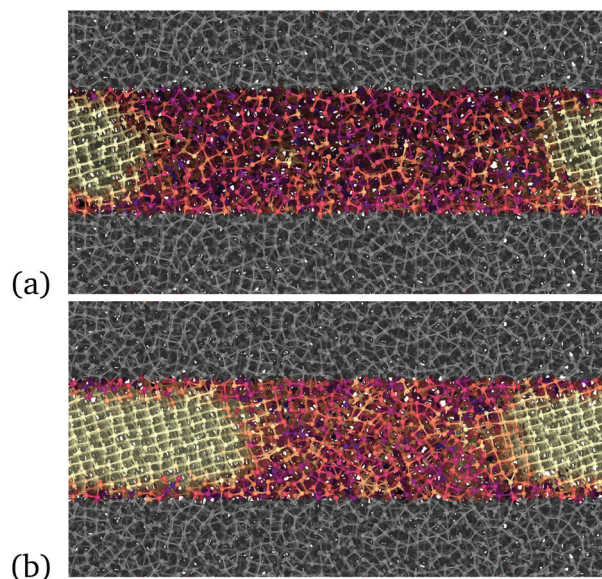
relaxations actually coincide.<sup>51</sup> Still, the good fitting with the WF formula over the whole temperature range with a single activation energy for the atomic diffusivity (see Fig. 3) suggests that the activation energy at high temperatures captures the elemental process of the local atomic motion that also controls the kinetics of crystallization at low temperature.

Actually, the processes responsible for the  $\beta$  relaxation have been proposed to accelerate the crystallization kinetics in metallic glasses<sup>53</sup> and more recently in phase change chalcogenide alloys as well.<sup>54</sup> The presence of a  $\beta$  relaxation process in phase change materials has been recently identified from the so called  $\beta$ -wing in the temperature dependence of the loss modulus measured by dynamical mechanical spectroscopy (DMS).<sup>54</sup>

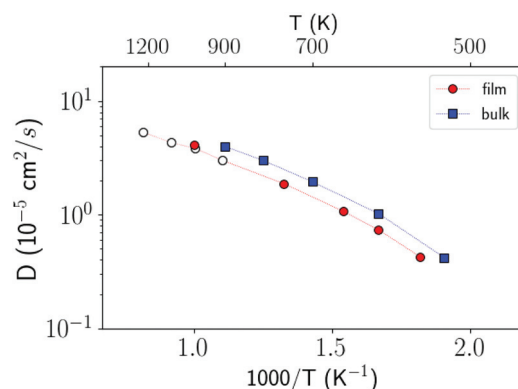
On these premises on the crystallization process in the bulk, we moved to study the crystallization in ultrathin films. We considered the thinnest film of 3 nm studied experimentally in ref. 10. To mimic confinement by the silica capping layers employed experimentally, we proceeded as described below. We considered a supercell with edges 14.871 nm  $\times$  4.957 nm  $\times$  4.957 nm and PBC in three dimensions. The simulation cell is divided in two regions which are stacked along the  $z$  direction and correspond respectively to the encapsulating layer and the active film. The encapsulating layer is approximately 2 nm thick and contains frozen 5340 Sb atoms whose configuration is extracted from a NVT run at 1500 K at a density 15% higher than the equilibrium density at  $T_m$  to mimic the higher atomic density of amorphous silica used as capping layers in ref. 10 (although the density of amorphous silica is about a factor 2.2 higher than that of liquid Sb). The active region, 3 nm thick, contains 7066 atoms free to move at the experimental density of the liquid at the melting point (see Fig. 4). The diffusion coefficient in the film turns out to be very similar to that of the bulk as shown in Fig. 5. The fitting of  $D(T)$  in the film with an Arrhenius function yields an activation energy of 0.17 eV and a prefactor of  $28.3 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$  which are close to those given above for the bulk. At low temperatures a two steps relaxation in the mean square displacement is present for the film as well.

We then proceeded as we did for the simulation of the crystallization in the bulk. We first generated a uniform amorphous region in the 3 nm thick film by quenching from the melt, and we then crystallized a small slice of the film. We then equilibrated the system at different temperatures with all atoms free to move but those in the capping layer. Note that in Fig. 4 we changed visualisation with respect to the bulk in Fig. 2 in such a way that half of the crystalline slab is on the left and half on the right of the figure in the case of the film. This allows highlighting the shrinking with time of the amorphous region to parallel what we expect to see in the linear device with the two crystalline sides at the electrodes that grow at the expense of a central amorphous region.

Constant temperature simulations were then performed to compute the crystal growth velocity as a function of temperature from the evolution of the crystal-amorphous interface. The evolution of the crystalline front as a function of time in



**Fig. 4** Snapshots of the model of the thin film, 3 nm thick, during crystallization at 300 K and at the experimental density of the liquid at melting. The film is confined on both sides by a region of Sb atoms (gray area) generated from the liquid at a higher density, approximately +15% of the density of the liquid at melting, to mimic a capping layer at high density. The atoms of the capping layers are frozen in a configuration extracted from the MD run at 1500 K. The color code for atoms in the film is the same as in Fig. 2; the crystal grows from the two sides of the figures.



**Fig. 5** Diffusion coefficient of the bulk (filled blue squares) and of the 3 nm film (filled red dots) calculated in NVT simulations. The diffusion coefficient in the film is obtained by multiplying by 3/2 the mean square displacements in the  $xy$  planes,  $z$  being the direction of the 3 nm thickness, i.e.  $\langle r^2 \rangle = 6Dt$ , with  $\langle r^2 \rangle = 3/2(\langle x^2 \rangle + \langle y^2 \rangle)$ . The empty dots refer to data from NVE simulations in the film at high temperatures.

the film at different temperatures is shown in Fig. S13 in ESI.† The same protocols discussed for the simulation of the crystallization in bulk is used here to extract the crystal growth velocity for the film. The results (red dots) are collected and compared in Fig. 3 with the corresponding data for the bulk. The maximum in the crystal growth velocity is much lower in the film than in the bulk and it is located at a lower temperature



than in the bulk. A similar comparison was found in the crystallization kinetics in bulk and nanowires of the GeTe phase change compound<sup>27</sup> where the lower crystallization speed of the nanowire was ascribed to a lower melting temperature in the nanowire than in the bulk. To investigate this effect, we again used the WF expression  $u = 6D(T)/\lambda(1 - e^{-\frac{u}{6D(T)}})$  by using the Arrhenius fit of  $D(T)$  at high temperature. The interfacial free energy was included in the calculation of  $\Delta\mu$  (see below) entering in the Thomson–Spaepen formula with a melting temperature initially set to the value of  $T_m = 790$  K used for the bulk. The fitting yields  $\lambda = 0.8$  Å which is slightly lower than the value of 1.2 Å obtained for the bulk. The fitting is decent at high temperatures but not at low temperatures for the reasons outlined below.

The large difference in the temperature at which the crystal growth velocity vanishes in the film with respect to the bulk is just due to the interfacial free energy (see Fig. 3). We estimated the difference in the interfacial free energy  $\Delta\gamma$  between the amorphous and crystalline phases in contact with our model of the capping layer as follows  $\Delta\gamma = (U^a - U^c - N(u_a - u_c))/2S$  where  $N$  is the total number of active atoms in the 3 nm thick film (7066),  $U^a$  and  $U^c$  are the time-averaged energies of the thin film model (including the capping layers) in the amorphous and fully crystallized phase at 300 K,  $u_a$  and  $u_c$  are the energy per atom in the bulk of the amorphous and crystalline (crystallized) phases at the same temperature, and  $S$  is the interfacial area. The calculation yields  $\Delta\gamma = -0.011$  eV Å<sup>-2</sup> which means that the interfacial energy is lower for the amorphous phase than for the crystal as expected by the higher flexibility of the amorphous phase to adapt to the change in density of the capping layer. This value, corresponding to an energy cost  $\sigma = -0.0233$  eV per atom in the 3 nm film, is used to correct the difference in free energy between the two phases obtained from the Thomson–Spaepen formula for the bulk once applied to the thin film.

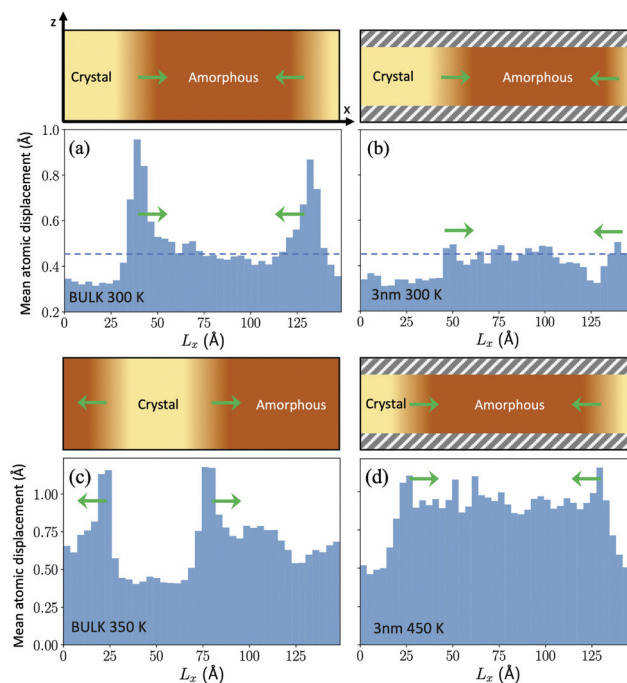
We actually used a temperature independent interfacial free energy which might overamplify the change in the  $u(T)$  at high temperatures, in fact the same interfacial free energy which disfavors the crystal with respect to the amorphous phase is expected to reduce the melting temperature in the film as well. The difference in the crystal growth velocities between the bulk and the film at high temperature might thus be ascribed mostly to thermodynamical effects related to the interfacial free energy. This is not the case at low temperatures, where a more interesting behavior emerges related to the strong stabilization of the amorphous phase found experimentally.<sup>10</sup>

As opposed to the bulk, it turns out that the crystal growth velocity for the thin film at low temperatures is much lower than the prediction of the Wilson–Frenkel formula with the diffusion coefficient  $D(T)$  extracted at high temperature (red line in Fig. 3). That amounts to say that the  $\beta$  relaxation, that should control the crystallization at low temperatures is strongly suppressed in the thin film.

The  $\beta$  relaxation, although faster than the  $\alpha$  relaxation, has also been shown to feature cooperative effects in simulations of model systems.<sup>55–57</sup> In particular, it was shown that ran-

domly pinning only a small fraction of atoms (about 2%) can strongly suppress the  $\beta$  relaxation (and then the  $\beta$ -wing in DMS)<sup>58</sup> in a Lennard-Jones glass model.<sup>56</sup> We therefore ascribe the stabilization of the amorphous phase towards crystallization in ultrathin antimony film to a reduction of the  $\beta$  relaxation due to confinement effects which is supposed to appear once the size of the CRR involved in the  $\beta$  process approaches the thickness of the film. This conclusion suggests that the experimental measurement of the  $\beta$ -wing by DSM could provide crucial insights on the change in crystallization kinetics of phase change materials in confined geometries.

The  $\beta$  relaxation is supposed to control the short range dynamics and not long range diffusional processes. In the respect, we have observed an enhancement in the atomic mobility at the crystalline/amorphous interface at low temperature (300 K) in the bulk as shown in Fig. 6a. This mobility is



**Fig. 6** The figure shows the average displacement of atoms over a 20 ps time lag within slices approximately 3.5 Å thick along the growth direction of the crystalline front ( $L_x$ ) for the bulk (panels (a) and (c)) and for the film (panels (b) and (d)). A sketch of the geometry of the system with an indication of the crystalline and amorphous regions is given in the upper part of each panel. There, the direction of the crystal growth is indicated by green arrows. The  $z$  direction is instead the direction of the thickness of the film capped by the two confining layers. The capping layers are indicated by shaded gray regions in the upper part of panels (b) and (d). The dashed horizontal line in panels (a) and (b) indicates the average mean square displacement in the homogeneous amorphous bulk at 300 K. Panels (a) and (c) refer to the crystal growth in the bulk at 300 and 350 K. Panels (b) and (d) refer to the crystal growth in the film at 300 and 450 K. The behaviour of the bulk and of the film are compared at the same temperature (300 K) in panels (a) and (b) and at different temperatures in panels (c) and (d) at which the crystal growth velocities in the film (at 450 K) and in the bulk (at 350 K) are equal (see Fig. 3). The enhancement of the atomic displacement at the growing surface is present in the bulk but not in the film (see text).



measured as the mean square displacement over a 20 ps time lag averaged over slices 3.5 Å thick along the direction of crystal growth. This enhancement is not due to a local increase in temperature due to the heat released in the crystallization process. In fact, the thermostat acting on the ions is able to remove the heat and to keep the temperature nearly constant and uniform during growth. On the other hand, this enhancement is absent at the crystal/amorphous interface in the thin film at the same temperature (see Fig. 6b). One might read the lack of an enhanced mobility at the interface in the thin film as the result of the low crystal growth speed and not as its cause. However, an additional piece of information comes for Fig. 6c and d where we compare the mean square displacement at the crystal/amorphous interface in the bulk and in the thin film at the two temperatures at which the crystal growth velocity is the same in the bulk and in the film, namely 350 K for the bulk and 450 K in the film (see Fig. 3). Again, we see an enhancement of the atomic mobility at the interface in the bulk and not in the film. This can be a coincidence due to the fact that the MSD at the interface necessary to sustain the measured crystal growth velocities coincide with the MSD far from the interface at the same temperature in the film. However, these results might be suggestive of an even more local dynamics controlling the crystal growth than the  $\beta$  dynamics of the amorphous/supercooled liquid in quasi equilibrium.

As a final remark, we comment on the effect of confinement and of the density on crystal nucleation. The effect on density on crystal nucleation in the bulk was highlighted by the DFT simulations reported in ref. 10. We actually investigated the effect of the density on the crystal nucleation by estimating the incubation time defined operatively as the time elapsed until a markedly change in slope is observed in the number of the crystalline atoms as a function of time which would signal the appearance of a fast growing supercritical nucleus. The results are collected for the bulk (simulation cell with 3888 atoms) at different temperatures and at different densities in the range +2/−5% of the experimental density of the liquid at  $T_m$ . A single simulation was performed for each temperature/density condition; due to the stochasticity of the nucleation process the data should therefore be read as qualitative and not quantitative. The missing data points in Fig. 7 correspond to conditions at which the incubation time is longer than 20 ns which is the maximum length we set for our simulations. Models at lower densities clearly show longer incubation times in agreement with the outcomes of DFT molecular dynamics with smaller simulation cells and shorter simulation times.<sup>10</sup> We also analyzed crystal nucleation in the model of the capped 3 nm film that contains 7066 atoms. Crystal nucleation was studied by heating at 380 K the amorphous model generated with the protocol discussed previously. The estimated incubation time in the film, 3 nm thick at the experimental density of the liquid, is 3.3 ns which is close to that of the bulk at the same temperature (4.0 ns). Analogously the incubation time of the film with a density 2 % lower than the equilibrium density of the liquid is about 11.3 ns which is

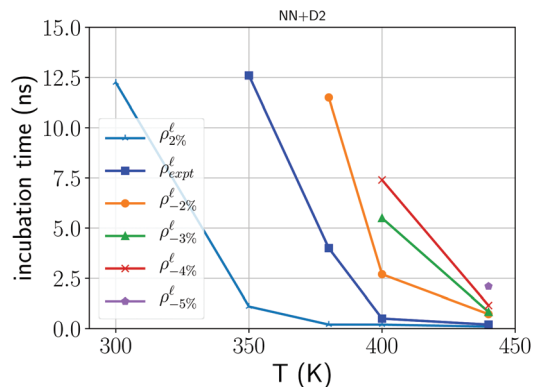


Fig. 7 Estimated incubation time for crystal nucleation (see text) in the bulk at different temperatures and at different densities with changes expressed in percentage with respect to the experimental density of the liquid.

again close to the value of 12.0 ns obtained for the bulk at the same conditions. However, since the number of atoms in the bulk models is a factor 1.8 less than the number of atoms in the models of the film, at fixed nucleation rate, the incubation time for the film should be 1.8 factor less than in the bulk. These results suggest, albeit with the large uncertainties due to our very rough estimate of the incubation time from a single simulation, that the confinement can reduce the nucleation rate with respect to the bulk, although not by the same large factor that it was found for the crystal growth velocities.

## 4. Conclusions

In conclusions, we have performed large scale molecular dynamics simulations of the crystallization kinetics of the monoatomic phase change material Sb in confined geometry. The simulations confirm the higher stability of the amorphous phase in a 3 nm film, discovered experimentally by Salinga *et al.*,<sup>10</sup> and shed light on the microscopic origin of the increase in the crystallization temperature. As discussed in ref. 10 the higher  $T_x$  in confined geometry makes Sb suitable for applications in memories with improved performances because the compositional simplification eliminates reliability problems due to alloy demixing and it mitigates the drift in the electrical resistance due to aging of the amorphous phase which affect the most used GeSbTe phase change alloys. The simulations reveal that at high temperatures in the bulk, crystallization is well described by the Wilson–Frenkel formula for crystal growth with the self diffusion coefficient as kinetic prefactor. Crystallization at low temperatures in the bulk is controlled by atomic motion on a shorter length and time scales typical of the  $\beta$  relaxation dynamics as opposed to the longer length and time scales of the  $\alpha$  relaxation responsible for the self-diffusion coefficient. It is this  $\beta$  relaxation dynamics which seems to be strongly affected by the confinement of amorphous Sb in 3 nm thin films. As a matter of fact, we found a dramatic reduction in the crystal growth velocity in the film



with respect to the bulk at temperatures equal and lower than 300 K, despite the diffusion coefficient in the film and in the bulk are essentially the same at high temperatures. This outcome suggests that the key for understanding the effect of nanostructuring/confinement on the crystallization kinetics is the analysis of the  $\beta$  relaxation dynamics which just started very recently to be investigated experimentally in bulk phase change materials.<sup>54</sup>

## Conflicts of interest

There are no conflicts of interest to declare.

## Author contributions

D. D. and M. B. conceptualized the work. J. B. contributed to the development of the interatomic potential. The simulations were performed by D. D. M. B. and D. D. analyzed the data and wrote the paper. All authors approved the final version of the paper.

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