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# Molecular mechanism of secreted amyloid- $\beta$ precursor protein in binding and modulating GABA<sub>B</sub>R1a†

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A recent phenomenal study discovered that the extension domain of secreted amyloid- $\beta$  precursor protein (sAPP) can bind to the intrinsically disordered sushi 1 domain of the  $\gamma$ -aminobutyric acid type B receptor subunit 1a (GABA<sub>B</sub>R1a) and modulate its synaptic transmission. The work provided an important structural foundation for the modulation of GABA<sub>B</sub>R1a; however, the detailed molecular interaction mechanism, crucial for future drug design, remains elusive. Here, we further investigated the dynamical interactions between sAPP peptides and the natively unstructured sushi 1 domain using all-atom molecular dynamics simulations, for both the 17-residue sAPP peptide (APP 17-mer) and its minimally active 9 residue segment (APP 9-mer). We then explored mutations of the APP 9-mer with rigorous free energy perturbation (FEP) calculations. Our *in silico* mutagenesis studies revealed key residues (D4, W6, and W7) responsible for the binding with the sushi 1 domain. More importantly, one double mutation based on different vertebrate APP sequences from evolution exhibited a stronger binding ( $\Delta\Delta G = -1.91 \pm 0.66$  kcal mol<sup>-1</sup>), indicating a potentially enhanced GABA<sub>B</sub>R1a modulator. These large-scale simulations may provide new insights into the binding mechanism between sAPP and the sushi 1 domain, which could open new avenues in the development of future GABA<sub>B</sub>R1a-specific therapeutics.

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## Introduction

Amyloid- $\beta$  peptide is the main component of senile plaques found in the brains of patients with Alzheimer's disease (AD) and is derived from normal proteolytic cleavage of the amyloid- $\beta$  precursor protein (APP).<sup>2</sup> APP is a single-pass type I membrane protein with a large amino-terminal ectodomain and a short carboxyl-terminal cytoplasmic domain.<sup>3</sup> Mature APP goes through ectodomain shedding *via*  $\alpha$ -,  $\beta$ -, or  $\eta$ -secretase to release secreted APP (sAPP $\alpha$ , sAPP $\beta$ , or sAPP $\eta$ , respectively).<sup>4,5</sup> The synaptic function of APP<sup>6–12</sup> is performed by sAPP<sup>13,14</sup> and is mediated by cell-surface receptors.<sup>14–16</sup> Unraveling these sAPP functions and their binding partners has not been trivial, because APP undergoes complex processing, and this results in

numerous fragments, which have different and sometimes opposing functional properties. Interestingly, a very recent phenomenal study by De Wit and coworkers has shown that the  $\gamma$ -aminobutyric acid type B receptor subunit 1a (GABA<sub>B</sub>R1a) is also a synaptic receptor for sAPP1, which might open new avenues to treat AD – not only through targeting A $\beta$  but also by strengthening alternate routes of cleaving APP and utilizing nonamylogenic pathways.

GABA<sub>B</sub>R is a metabotropic receptor of the central inhibitory neurotransmitter  $\gamma$ -aminobutyric acid (GABA). It is composed of two subunits: GABA<sub>B</sub>R1 and GABA<sub>B</sub>R2, which supply the GABA binding site and allow the heterotrimeric G protein activation. The isoform of GABA<sub>B</sub>R1, GABA<sub>B</sub>R1a, has potential therapeutic significance to a number of neurological disorders which implicate GABA<sub>B</sub>R signaling.<sup>17</sup> GABA<sub>B</sub>R1a contains two protein interaction motifs known as sushi domains in the amino-terminal extracellular region.<sup>18–22</sup> The sushi 1 domain of GABA<sub>B</sub>R1a is natively unstructured, and it interacts with the flexible, partially structured extension domain (ExD) in the linker region of sAPP. This interaction induces a conformational change in the sushi 1 domain, which leads to increased short-term facilitation in mouse hippocampal synapses and decreased neuronal activity *via* inhibition of neurotransmitter release. A short peptide within the sAPP ExD, the APP 17-mer, functionally mimics sAPP1. This work discovered a surprising role of the sushi 1 domain of GABA<sub>B</sub>R1a as a new binding

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partner for sAPP and also provided a preliminary complex structure involving these intrinsically disordered protein domains (NMR structure, more below); however, the detailed molecular interaction mechanism still remains elusive, which is crucial for future potential drug design on this important sushi-containing neurotransmitter receptor.

Here, we undertake extensive all-atom molecular dynamics (MD) simulations and free energy perturbation (FEP) calculations to characterize the effect of the APP 17-mer and its minimal 9-amino acid sequence, the APP 9-mer, in binding to the sushi 1 domain of GABA<sub>B</sub>R1a.<sup>1</sup> FEP calculations can supplement experiments in investigating the complicated binding between biomolecules such as protein–protein interaction, ligand–receptor binding, protein–DNA/RNA binding, as well as solvation free energy calculations.<sup>23–34</sup> A large number of FEP calculations have achieved excellent agreements with the difficult and expensive experimental measurements in antigen–antibody, protein–ligand, and protein–protein binding affinities.<sup>7,8,10,27,29,30,32,35,36</sup> In this study, we found that the APP 9-mer is sufficient to bind GABA<sub>B</sub>R1a and stabilize the sushi 1 domain, in agreement with the previous experimental investigation.<sup>1</sup> The stacking interaction between W6 in the APP 9-mer and T20 in the sushi 1 is crucial to preserve the strong binding. A single mutation of W6A can cause a decrease in binding affinity by  $\Delta\Delta G = 4.90 \pm 0.45$  kcal mol<sup>−1</sup>. Moreover, the hydrophobic interactions between W7 in the APP 9-mer and the hydrophobic pocket of the sushi 1 consisting of G16, G17, V43, C44, and R45 also contribute substantially to the APP 9-mer–sushi 1 association, as indicated by the significant loss of binding affinity ( $\Delta\Delta G = 3.45 \pm 0.60$  kcal mol<sup>−1</sup>) due to a single mutation of W7A. Meanwhile, D4A mutation results in a binding affinity loss of  $\Delta\Delta G = 2.19 \pm 0.25$  kcal mol<sup>−1</sup>, due to the loss of favorable electrostatic interactions, in particular the loss of a salt-bridge between D4 and R25 of sushi 1 domain. Most interestingly, we found that one double mutation based on different vertebrate APP sequences from evolution has a stronger binding ( $\Delta\Delta G = -1.91 \pm 0.66$  kcal mol<sup>−1</sup>), indicating a potentially enhanced GABA<sub>B</sub>R1a modulator. These findings not only reveal key interactions between the sushi 1 domain and the ExD of APP, but also provide insights for the future development of GABA<sub>B</sub>R1a therapeutics.

## Simulation methods

### Molecular dynamics simulations

We performed all-atom MD simulations on complexes of the APP 17-mer and 9-mer peptides<sup>4</sup> bound to the sushi 1 domain of GABA<sub>B</sub>R1a. The complexes were solvated in water boxes using the TIP3P<sup>37</sup> water model. Na<sup>+</sup> and Cl<sup>−</sup> were added to neutralize the systems and we set the ion concentration to be 0.15 M. Each system was energy minimized for 20 000 steps, equilibrated for 10 ns, followed by a 300 ns production run. All MD simulations were carried out with NAMD<sup>38</sup> using the CHARMM force field.<sup>39</sup> Long-range electrostatic interactions were calculated using the particle-mesh Ewald (PME) method,<sup>40,41</sup> and van der Waals (vdW) interactions were calculated using a cutoff distance of 12 Å. All production runs were performed with the NPT ensemble

at 1 atm pressure and 310 K temperature. The covalent bonds with hydrogen atoms were constrained at their equilibrium values by the LINCS algorithm,<sup>42</sup> which allows a time step of 2 fs.

### FEP protocol

The *in silico* mutagenesis studies were carried out with the FEP calculations.<sup>24,26,43–45</sup> The binding free energy change  $\Delta G$  caused by a mutation can be calculated as:

$$\Delta G_{\lambda} = -kT \ln \langle \exp(-\beta[V(\lambda + \Delta\lambda) - V(\lambda)]) \rangle_{\lambda}, \quad (1)$$

$$\Delta G = \sum_{\lambda} \Delta G_{\lambda}, \quad (2)$$

where  $V(\lambda) = (1 - \lambda)V_1 + \lambda V_2$ , with  $V_1$  representing the potential energy of the wild type and  $V_2$  representing the potential energy of the mutant. When the system changes from wild type to mutant, the FEP parameter  $\lambda$  changes from 0 to 1, and  $\langle \dots \rangle_{\lambda}$  represents average over the ensemble with potential  $V(\lambda)$ . The starting structures for the FEP calculations were randomly selected from the MD production run, and multiple independent FEP calculations were performed for each mutant. We employed a 20-window scheme with soft-core potential ( $\lambda = 0.00001, 0.0001, 0.001, 0.01, 0.05, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 0.95, 0.99, 0.999, 0.9999, 0.99999, 1$ ). Given the long timescale of the binding process between two interacting surfaces, like in the case of APP 9-mer and sushi 1 domain, it is difficult to directly calculate the absolute binding affinity. To overcome this problem, we calculated the relative binding free energy change  $\Delta\Delta G$  with a thermodynamic cycle, as shown in Fig. S1.† Then we could obtain the free-energy changes for the same mutation in both the bound state (sushi 1–APP 9-mer binding complex,  $\Delta G_1$ ) and the free state (APP 9-mer,  $\Delta G_2$ ), instead of calculating the difficult direct binding energies  $\Delta G_A$  and  $\Delta G_B$ . From this thermodynamic cycle, the total change in free energy should be zero, and the relative binding affinity for the mutation from A to B is:

$$\Delta\Delta G = \Delta G_B - \Delta G_A = \Delta G_1 - \Delta G_2 \quad (3)$$

We calculated the free energy changes for the same mutation(s) in both the bound state and the free state. In this case, for every mutation, five independent runs were started from different initial configurations randomly chosen from the MD simulations for improved sampling. The simulation time for each run was 6 ns, amounting to 60 ns (6 ns  $\times$  5 runs  $\times$  2 states) of FEP calculations for each mutation.

Following the protocols in our previous studies,<sup>46,47</sup> we also performed the decomposition of binding affinity into its van der Waals and electrostatic components, since it offers useful information about the contributions of various physical interactions involved in the sAPP peptides–sushi 1 domain binding. Of course, the free energy decomposition might be path-dependent (turning on van der Waals interactions first or electrostatic interactions first).<sup>48–51</sup> In this study, we use a straightforward decomposition in FEP by collecting van der Waals and electrostatic interaction contributions separately, *i.e.*,  $V(\lambda) =$



$V(\lambda)_{\text{elec}} + V(\lambda)_{\text{vdw}}$ , in the same ensemble with full interactions in eqn (1) (see above). Due to the nonlinearity of the FEP formulation, there might be a small coupling term in this approach as the total binding free energy  $\Delta\Delta G$  is not additive from the two components.<sup>51</sup>

## Results and analyses

### Key residues for sAPP-GABA<sub>B</sub>R1a binding

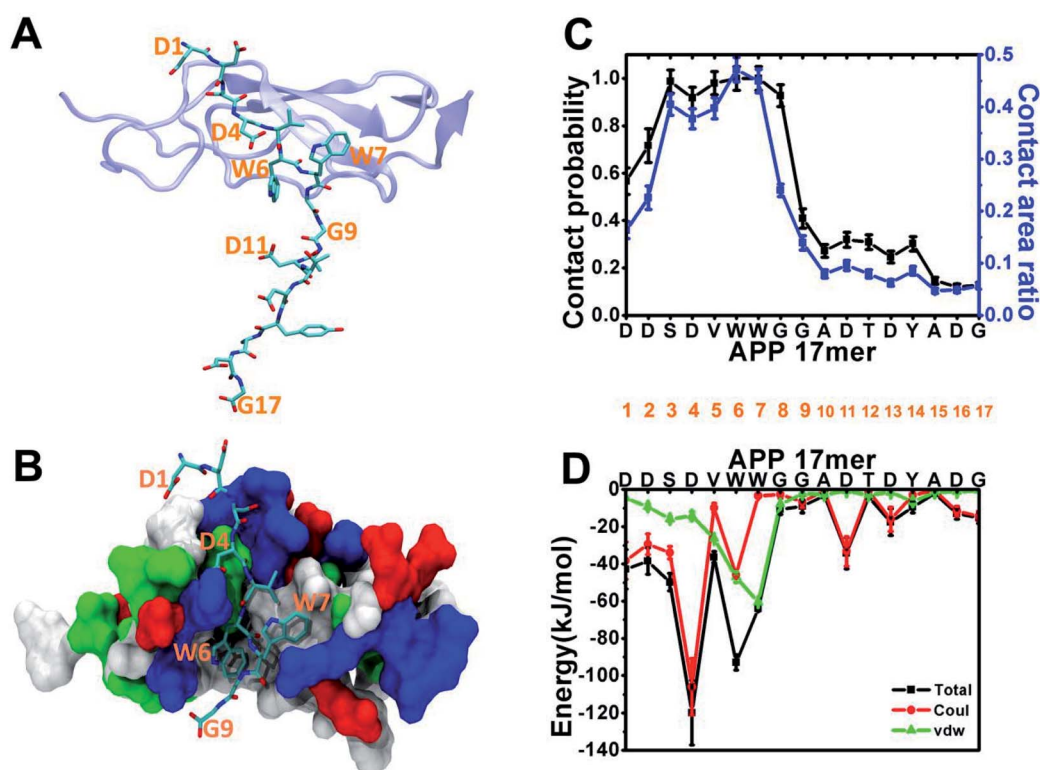
Following the experiment,<sup>1</sup> we began our analysis with the structure of the sushi 1 domain of GABA<sub>B</sub>R1a (PDB ID: 6HKC) bound to a short peptide from the ExD of sAPP in two forms: a 17-amino acid peptide (DDSDVWVGADTDYADG) and a truncated 9-amino acid peptide (DDSDVWVG). To characterize ExD peptide–sushi 1 binding, we perform 300 ns all-atom MD simulation for each bound complex (APP 17 mer–sushi 1 and APP 9 mer–sushi 1).

As illustrated in Fig. 1A and B, both the APP 17-mer and 9-mer bind to a shallow groove of the sushi 1 domain. The per-residue contact probabilities and contact area ratios between the APP 17-mer and the sushi 1 domain are shown in Fig. 1C. A residue of the APP 17-mer is considered to be in contact with sushi 1 domain if any heavy atom is within 4 Å from any heavy atom of sushi 1. The contact probability is calculated as the ratio of the residue contact time to the total 300 ns simulation

time. The contact area ratio is defined as the ratio between the residue surface area in contact with sushi 1 domain and the total solvent-accessible surface area (SASA) of that residue. The first nine residues of the 17-mer maintain high contact probabilities and high contact area ratios with the sushi 1 domain. Fig. 1D shows the average interaction energy between each residue of the APP 17-mer and the sushi 1 domain. Again, the interaction energy is dominated by contributions from the first nine amino acids (Fig. 1D).

Fig. 2 depicts structural fluctuations of the APP 9-mer and 17-mer during the 300 ns MD simulations. The APP 9-mer was relatively stable, as indicated by the root-mean-square deviations (RMSD) of the backbone atoms which saturates at around 0.21 nm. In contrast, the APP 17-mer is less stable, whose RMSD fluctuates between 0.22 nm and 0.89 nm (with an average of 0.53 nm), although the first nine of the 17 residues are as stable as the APP 9-mer.

To better characterize the conformation of APP 17-mer and APP 9-mer in complex with the sushi 1 domain, we calculated their end-to-end distance, the time-dependent distance between the C atoms of the terminal residues (D1 and G17 for APP 17-mer; D1 and G9 for APP 9-mer), in Fig. 2B. Our analysis illustrates that the end-to-end distance of APP 17-mer fluctuates drastically between 0.74 nm and 4.41 nm (averaged at 2.74 nm), while the first nine of the 17 residues were more stable with an



**Fig. 1** Sushi 1 domain of GABA<sub>B</sub>R1a binding with the APP 17-mer peptide (A) and APP 9-mer peptide (B). The APP 17-mer peptide and APP 9-mer peptide are represented by sticks, while the sushi 1 domain is shown in cartoon and surface representations. In (B), non-polar residues are colored white, polar uncharged residues green, positively charged residues blue, and negatively charged residues red. (C) APP 17-mer–sushi 1 domain average residue contact probabilities (black) and average contact area ratios (blue) extracted from the MD simulation. (D) Per-residue average interaction energy between the APP 17-mer peptide and the sushi 1 domain.





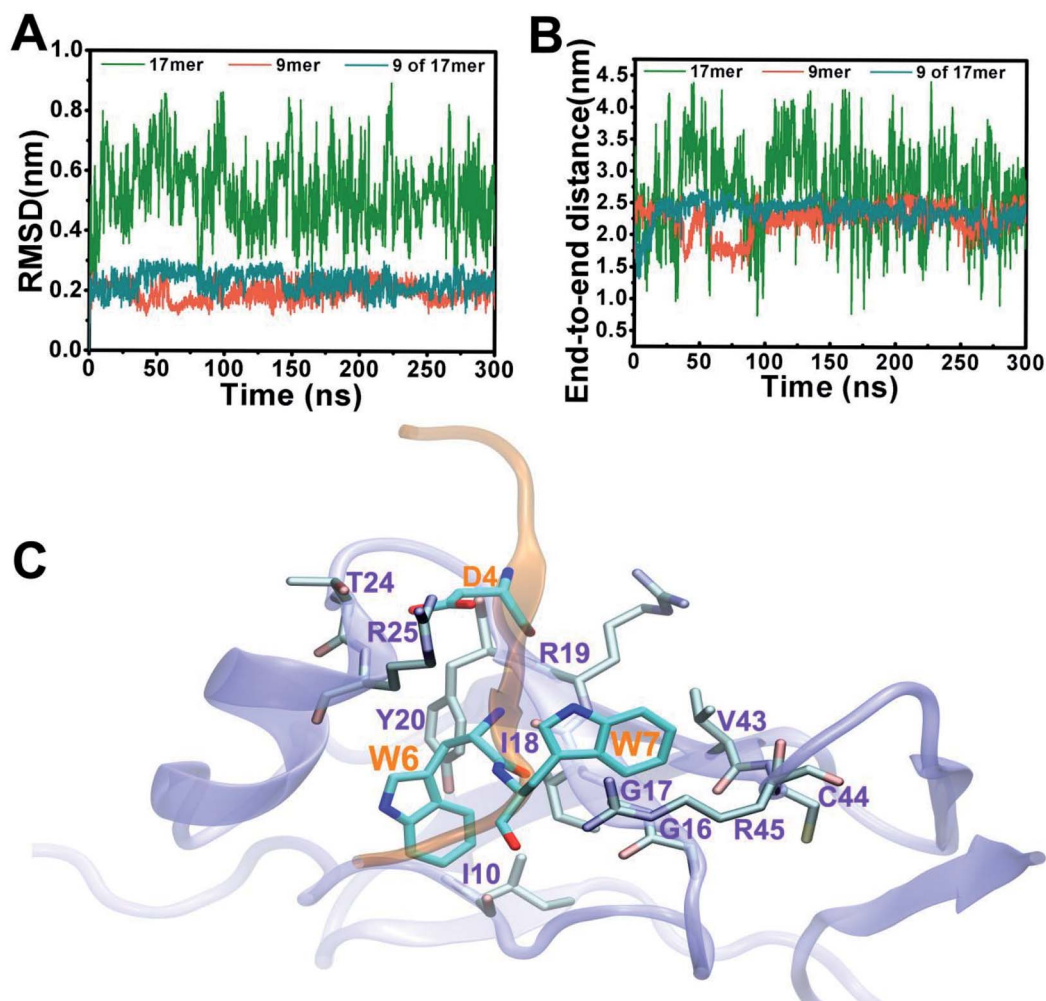


Fig. 2 Structural fluctuations and key binding residues for the sAPP-GABA<sub>B</sub>1a complexes. (A) RMSD of the backbone atoms of APP 17-mer (green), APP 9-mer (blue) and the first nine residues of APP 17-mer (red) with respect to the reference structure at  $t = 0$ . (B) Time-dependent end-to-end distances of the APP 17-mer, APP 9-mer, and the first nine residues of APP 17-mer peptide. (C) APP 9-mer-sushi 1 binding interface, APP 9-mer and sushi 1 domain are represented by orange and purple NewCartoon, respectively. The contact residues are highlighted as sticks.

average end-to-end distance around 2.36 nm, close to that of APP 9-mer (2.25 nm). This suggests that the conserved, minimal 9-amino acid sequence fits well into the shallow groove of the sushi 1 domain, while the remaining 8 residues extends into the solution and move freely in large. No stable contacts were observed between these remaining 8 residues and sushi 1 domain. Only temporary contacts were made occasionally by residues like Asp11 through “salt-bridge-like” short range electrostatic interactions with basic residues such as Arg25 and Lys29 on the sushi 1 domain (see Fig. S2 and descriptions in ESI†).

The binding interface between APP 9-mer and sushi 1 domain is presented in Fig. 2C, which reveals three key residues: (i) D4, which forms hydrogen bonds with R19 and Y20 of sushi 1, and the side chain of D4 forms electrostatic interactions with T24 and R25 of sushi 1 (salt-bridge between D4 and R25) (also shown in more details in Fig. 3A, left); (ii) W6, which stacks with the side chain of Y20, establishes hydrogen bonds with G17 and I18, and forms hydrophobic interactions with

G17, I18 and I10 (Fig. 3B, left); (iii) W7, making contacts with the hydrophobic pocket of sushi 1 consisting of G16, G17, V43, C44 and R45 (Fig. 3C, left).

### Structural analysis of the mutants

To further characterize the binding between APP 9-mer and sushi 1, we separately mutated several central sites on APP 9-mer and ran additional MD simulations. The three residues with the highest interaction energy were chosen for alanine scan mutations, including residues D4, W6, and W7. Fig. 4 presents the RMSD results for the WT and the three mutants. These RMSD profiles demonstrate that alanine scan mutations in APP 9-mer give rise to significant conformational changes in the sushi 1 domain—the average RMSD of the sushi 1 domain in the case of D4A (0.37 nm) and W6A (0.38 nm) was much higher than that of WT (0.27 nm). In comparison, we also analyzed the trajectories of a system containing the sushi 1 domain alone (Fig. S3†), whose RMSD saturates at around 0.38 nm (Fig. S3C†). The RMSD profiles reveal that binding by



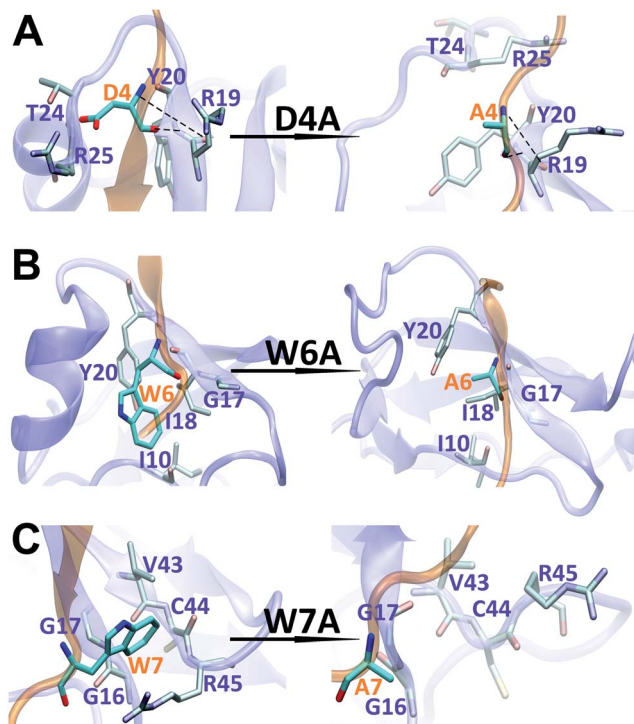


Fig. 3 Structural comparison of sushi 1 domain bound to WT APP 9-mer (left) and mutated APP 9-mer's (right) at the end of 300 ns of MD simulation: (A) for D4A mutation; (B) for W6A; (C) for W7A.

APP 9-mer stabilized the sushi 1 domain, while D4A and W6A mutations in APP 9-mer destabilized binding of APP 9-mer to sushi 1 domain and made the sushi 1 domain less stable. The structure of the binding complexes (Fig. 4E–H) further support the RMSD calculations, showing the shallow groove of sushi 1 (marked by the red circle) lost its native structure when interacting with mutant APP 9-mer's (especially for D4A and W6A mutations). The secondary structure analysis shows the same conclusion with D4A and W6A mutants lost most of the helices within residues 16–35 in the wild-type after a few nanoseconds

while the W7A mutant maintained a significant portion of the helical content during the simulation length (Fig. S4†).

The final binding site conformations for the mutant D4A, W6A, and W7A systems at the end of simulations are also shown in Fig. 3 (right part as compared the wild-type on the left). In the D4A system, despite A4 being still hydrogen-bonded with R19 and Y20, the electrostatic interactions with T24 and R25 were completely disrupted (Fig. 3A, right). For the W6A system (Fig. 3B), the stacking interaction with Y20 was sundered (Fig. 3B, right). In both cases, APP 9-mer can no longer bound to or stabilized the shallow groove of the sushi 1 domain (Fig. 4F and G). For the W7A system (Fig. 3C), since the mutant A7 lacks an aromatic ring, the binding interaction with the hydrophobic pocket (G16, G17, V43, C44 and R45) was mostly lost, and only weak hydrophobic interactions with residues G16 and G17 remain (Fig. 3C, right). Since V43, C44, and R45 are not in the binding groove, the mutation has little effect on APP 9-mer stabilizing the sushi 1 domain, and the conformational change of the sushi 1 domain is not significant (Fig. 4H).

### FEP *in silico* mutagenesis study

We further explored the effect of mutations in APP 9-mer through free energy perturbation (FEP) calculations.<sup>24,26,43–45</sup> As detailed in the Methods section, we calculated the free energy changes for the same mutation(s) in both the bound state and the free state. For every mutation, five independent runs were started from different initial configurations randomly chosen from the MD simulation trajectories for improved sampling. The results of a complete alanine scan mutation on the first nine residues are summarized in Table 1. Our rigorous FEP calculations reveal a dramatic decrease in the binding affinity for mutation W6A ( $\Delta\Delta G = 4.90 \pm 0.45$  kcal mol<sup>−1</sup>). The free energy decomposition shows that this decrease is mainly contributed by the vdW interaction ( $5.29 \pm 0.39$  kcal mol<sup>−1</sup>). There are also significant reductions in the binding affinity for the mutations D4A ( $\Delta\Delta G = 2.19 \pm 0.25$  kcal mol<sup>−1</sup>), with majority contribution from the electrostatic interaction ( $1.97 \pm 0.49$  kcal mol<sup>−1</sup>); V5A ( $\Delta\Delta G = 2.96 \pm 0.20$  kcal mol<sup>−1</sup>), with

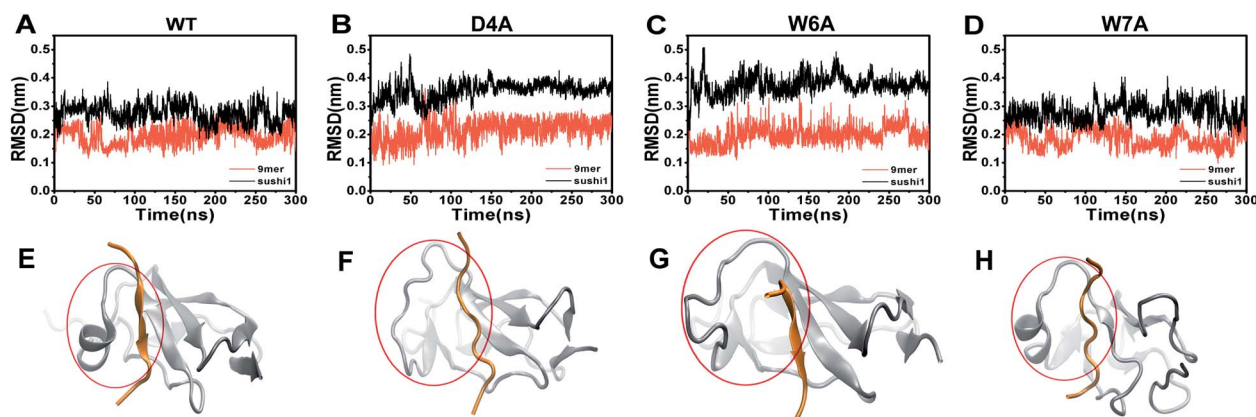


Fig. 4 RMSD of the backbone atoms of APP 9-mer (red) and sushi 1 domain (black) for WT APP 9-mer (A) and APP 9-mer's with mutations D4A (B), W6A (C), and W7A (D). Final structure of sushi 1 domain binding to WT and mutated APP 9-mer's (E–H). APP 9-mer is colored in orange and sushi 1 domain in gray. The shallow binding groove of sushi 1 is marked by the red circle.



**Table 1** FEP results for the APP 9-mer peptide–sushi 1 domain binding free energy change caused by the alanine scan mutations in the APP 9-mer

Mutation	$\Delta\Delta G$ (kcal mol <sup>-1</sup> )	$\Delta\Delta G_{\text{elec}}$ (kcal mol <sup>-1</sup> )	$\Delta\Delta G_{\text{vdw}}$ (kcal mol <sup>-1</sup> )	$\Delta\Delta G_{\text{coupling}}$ (kcal mol <sup>-1</sup> )
D1A	0.62 ± 0.63	0.33 ± 0.39	0.52 ± 0.38	−0.23 ± 0.05
D2A	0.04 ± 0.38	−0.05 ± 0.43	0.14 ± 0.43	−0.05 ± 0.10
S3A	1.14 ± 0.23	1.82 ± 0.59	−0.53 ± 0.49	−0.15 ± 0.05
D4A	2.19 ± 0.25	1.97 ± 0.49	0.67 ± 0.41	−0.44 ± 0.15
V5A	2.96 ± 0.20	0.007 ± 0.083	2.95 ± 0.20	0.006 ± 0.003
W6A	4.90 ± 0.45	−0.37 ± 0.17	5.29 ± 0.39	−0.02 ± 0.03
W7A	3.45 ± 0.60	−1.68 ± 0.14	5.25 ± 0.59	−0.12 ± 0.04
G8A	0.10 ± 0.14	0.07 ± 0.04	0.02 ± 0.14	0.006 ± 0.004
G9A	−0.03 ± 0.04	0.01 ± 0.01	−0.04 ± 0.04	−0.001 ± 0.001

majority contribution from the vdW interaction ( $2.95 \pm 0.20$  kcal mol<sup>-1</sup>); and W7A ( $\Delta\Delta G = 3.45 \pm 0.60$  kcal mol<sup>-1</sup>), with majority contribution from the vdW interaction ( $5.25 \pm 0.59$  kcal mol<sup>-1</sup>). The effect of mutations at the other five residues are relatively mild or neutral.

### Design novel peptides for enhanced binding

In order to better understand the binding mechanism between APP 9-mer and sushi 1 domain, we designed single or double mutations for possible stronger binding. As shown in Table 2, we first examined two single mutations D1E and D2E through our previous experiences.<sup>46,47</sup> However, this conservative mutation of similar size and charge had little influence on the binding affinity, with  $\Delta\Delta G = 1.12 \pm 0.74$  kcal mol<sup>-1</sup> (D1E) and  $\Delta\Delta G = 0.29 \pm 0.56$  kcal mol<sup>-1</sup> (D2E). We also observed slight reduction in the binding affinity by the single mutation S3M ( $\Delta\Delta G = 0.44 \pm 0.28$  kcal mol<sup>-1</sup>). The D4E mutation at the binding interface results in a somewhat modest reduction in binding affinity  $\Delta\Delta G = 2.79 \pm 0.90$  kcal mol<sup>-1</sup>, similar to D4A ( $\Delta\Delta G = 2.19 \pm 0.25$  kcal mol<sup>-1</sup>). For V5, we examined three different mutations: V5I ( $\Delta\Delta G = 0.12 \pm 0.28$  kcal mol<sup>-1</sup>), V5A ( $\Delta\Delta G = 2.96 \pm 0.20$  kcal mol<sup>-1</sup>), and V5D ( $\Delta\Delta G = 4.82 \pm 1.11$  kcal mol<sup>-1</sup>), which revealed the importance of hydrophobic interactions. For the target site W6, the conservative mutation W6F ( $\Delta\Delta G = 0.28 \pm 0.27$  kcal mol<sup>-1</sup>) had a much smaller effect than the mutation W6A ( $\Delta\Delta G = 4.90 \pm 0.45$  kcal mol<sup>-1</sup>), which

indicates the importance of the stacking interaction. The double mutation V5W + W6V resulted in a significant reduction in binding affinity,  $\Delta\Delta G = 9.72 \pm 3.11$  kcal mol<sup>-1</sup>. For the target site W7, two other different mutations were also tested: the conservative mutation W7F had little influence on the binding affinity ( $\Delta\Delta G = 0.70 \pm 0.73$  kcal mol<sup>-1</sup>), while W7I caused a more significant decrease ( $\Delta\Delta G = 3.09 \pm 0.85$  kcal mol<sup>-1</sup>), similar to W7A ( $\Delta\Delta G = 3.45 \pm 0.60$  kcal mol<sup>-1</sup>). These FEP calculations indicate that the APP-9 peptide is well conserved and optimized.

We then explored the APP sequences from other species trying to learn from the evolution. The first nine residues among different vertebrate APP sequences, APP\_human, APP\_pig, APP\_chicken, APP\_rat, APP\_mouse, APP\_frog, APPa\_fish, and APPb\_fish are highly conserved<sup>1</sup> (see Table 3). Only APP\_frog 9-mer (DDSDAWWGG) and APPb\_fish 9-mer (ANSDVWWGG) are different from the others (DDSDVWWGG). APP\_frog 9-mer can be regarded as single mutation V5A of APP\_human 9-mer, and APPb\_fish can be regarded as a double mutation D1A + D2N of APP\_human 9-mer. Our FEP calculations show that the double mutation D1A + D2N enhanced the binding affinity by  $\Delta\Delta G = -1.91 \pm 0.66$  kcal mol<sup>-1</sup> (see Table 3; also included in Table 2 for completeness), with majority of the contribution from electrostatic interactions ( $-1.43$  kcal mol<sup>-1</sup>), indicating the two consecutive acidic residues D1 and D2 in the APP 9-mer might not be optimal for binding in this case. As we

**Table 2** FEP results for the APP 9-mer peptide–sushi 1 domain binding free energy change due to designed mutations in the APP 9-mer

Mutation	$\Delta\Delta G$ (kcal mol <sup>-1</sup> )	$\Delta\Delta G_{\text{elec}}$ (kcal mol <sup>-1</sup> )	$\Delta\Delta G_{\text{vdw}}$ (kcal mol <sup>-1</sup> )	$\Delta\Delta G_{\text{coupling}}$ (kcal mol <sup>-1</sup> )
D1E	1.12 ± 0.74	0.51 ± 0.49	0.54 ± 0.75	0.07 ± 0.36
D2E	0.29 ± 0.56	−0.46 ± 0.46	0.94 ± 0.52	−0.19 ± 0.23
D2N	−1.14 ± 0.51	−0.85 ± 0.64	−0.12 ± 0.71	−0.17 ± 0.17
S3M	0.44 ± 0.28	0.11 ± 0.72	0.66 ± 0.72	−0.33 ± 0.12
D4E	2.79 ± 0.90	1.41 ± 0.76	1.09 ± 0.55	0.30 ± 0.26
V5I	0.12 ± 0.28	−0.08 ± 0.03	0.22 ± 0.28	−0.01 ± 0.01
V5D	4.82 ± 1.11	4.33 ± 1.00	0.66 ± 0.67	−0.17 ± 0.12
V5A	2.96 ± 0.20	0.007 ± 0.083	2.95 ± 0.20	0.006 ± 0.003
W6F	0.28 ± 0.27	−0.31 ± 0.08	0.48 ± 0.26	0.12 ± 0.03
W7F	0.70 ± 0.73	−1.10 ± 0.10	1.92 ± 0.76	−0.12 ± 0.03
W7I	3.09 ± 0.85	−1.06 ± 0.32	4.30 ± 0.72	−0.15 ± 0.03
V5W + W6V	9.72 ± 3.11	0.29 ± 0.40	9.24 ± 2.84	0.19 ± 0.13
D1A + D2N	−1.91 ± 0.66	−1.43 ± 1.61	−0.03 ± 1.42	−0.45 ± 0.89





**Table 3** FEP results of APP 9-mer peptide–sushi 1 domain binding free energy change for mutations to other species' corresponding APP 9-mer sequences

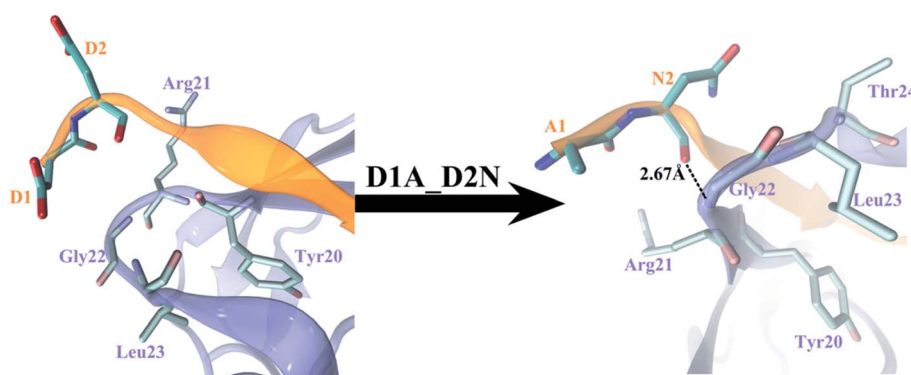
Species	9-mer sequence	$\Delta\Delta G$ (kcal mol <sup>−1</sup> )
APP_human	DDSDVWVG	—
APP_pig	DDSDVWVG	0
APP_chicken	DDSDVWVG	0
APP_rat	DDSDVWVG	0
APP_mouse	DDSDVWVG	0
APP_frog	DDSDAVWVG	2.96 ± 0.20
APPa_fish	DDSDVWVG	0
APPb_fish	ANSDVWVG	−1.91 ± 0.66

already learned from above that the single mutation D1A is not favorable ( $\Delta\Delta G = 0.62 \pm 0.63$  kcal mol<sup>−1</sup>), we further investigated the single mutation D2N (also included in Table 2 for completeness), which turned out to enhance the binding affinity by  $\Delta\Delta G = -1.14 \pm 0.51$  kcal mol<sup>−1</sup>, with majority of the contribution also from electrostatic interactions (−0.85 kcal mol<sup>−1</sup>). A closer look indicates that there exists about −1.39 kcal mol<sup>−1</sup> “synergy” in the double D1A + D2N mutation as compared to the sum of the two single mutations (−1.91 − 0.62 − (−1.14) = −1.39 kcal mol<sup>−1</sup>), and the free energy decomposition shows the synergy consists of contributions of −0.91 kcal mol<sup>−1</sup> in electrostatic and (a meaningful) −0.43 kcal mol<sup>−1</sup> in van der Waals interactions, with the remaining in coupling terms. Fig. 5 further illustrates the structural changes due to the double mutation, which clearly shows the strong repulsion between D1 and D2 in the wild-type peptide, with both D1 and D2's negatively charged sidechains sticking into solvent (Fig. 5, left), thus less binding to the sushi 1 domain. On the other hand, the double mutant A1N2 displays a backbone hydrogen bond between N2 and Gly22 in the sushi 1 domain, and meanwhile, both A1 and N2 residues are pushed closer to the sushi 1 domain, with 5 residues in close proximity (defined as within 6 Å from the first two APP residues) as compared to only 4 in the wild-type (Fig. 5, right), which

explains the meaningful synergy contributions from both electrostatic and van der Waals interactions (−0.91 and −0.43 kcal mol<sup>−1</sup>, respectively). Either D1A or D2N single mutation cannot generate strong enough hydrophobic force to push the first two APP 9-mer residues to be in “tight binding” with sushi 1 domain. All these analyses confirm our earlier suspicion that the two consecutive acidic residues D1 and D2 in the APP 9-mer might not be optimal for binding in this case. Even though the double mutant (APPb\_fish peptide) is not overwhelmingly stronger in terms of binding affinity (∼3*kT* at room temperature), we believe this new peptide learned from evolution can potentially serve as an enhanced GABA<sub>B</sub>R1a modulator. Further experimental validation on our *in silico* prediction is highly desired.

## Conclusion

In this work, we investigated the binding dynamics and underlying molecular mechanism of the App 17-mer (and its minimal 9-amino acid sequence) in binding with the sushi 1 domain of GABA<sub>B</sub>R1a. Our MD simulations revealed important structural binding patterns and major driving forces that sAPP peptides utilize to stabilize the natively unstructured sushi 1 domain. Contact and energy analyses identified three key binding residues in the APP 9-mer peptide (D4, W6, and W7), which were further examined through *in silico* mutagenesis studies. We found that the stacking interaction between W6 of the APP-9 mer and T20 of the sushi 1 domain is crucial to the strong binding between the two. Our FEP calculations suggest that W6A mutation will cause a significant decrease in binding affinity ( $\Delta\Delta G = 4.90 \pm 0.45$  kcal mol<sup>−1</sup>). In addition, the hydrophobic interaction between W7 (APP-9 mer) and the hydrophobic pocket (sushi 1) is also important, as evidenced by the significant loss of binding affinity ( $\Delta\Delta G = 3.45 \pm 0.60$  kcal mol<sup>−1</sup>) due to a single W7A mutation. Finally, we designed single and double mutations for potentially stronger binding and found that a double mutation (D1A + D2N) learned from evolution shows a stronger binding ( $\Delta\Delta G = -1.91 \pm$



**Fig. 5** The binding complex structural changes due to the double mutation D1AD2N of APP 9-mer. All the sushi 1 domain residues within 6 Å from the first two APP 9-mer residues are shown in sticks, with the rest shown in ribbon view. The figure clearly shows the strong repulsion between D1 and D2 in the wild-type, with both D1 and D2's negatively charged sidechains sticking into solvent (left). On the other hand, the double mutant A1N2 displays a backbone hydrogen bond between N2 and Gly22, and meanwhile, both A1 and N2 residues are pushed closer to the sushi 1 domain (right).



0.66 kcal mol<sup>-1</sup>), indicating a potentially enhanced GABA<sub>B</sub>R1a modulator. Our current work reveals novel insights into App 9-mer-sushi 1 domain binding, which might provide new targets for the development of GABA<sub>B</sub>R1a isotype-specific therapies that are associated with many neurological diseases involving GABA<sub>B</sub>R signaling.

## Author contributions

R. Z. conceived and designed the study. M. F. and S. H. C. performed the molecular dynamics simulations. Y. S. carried out the free energy perturbation calculations. M. F., Y. S. and Y. Z. performed computational analysis and wrote the manuscript with support from all authors.

## Conflicts of interest

There are no conflicts to declare.

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