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## Apex hydrogen bonds in dendron assemblies modulate close-packed mesocrystal structures†

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The close-packed mesocrystal structures from soft-matter assemblies have recently received attention due to their structural similarity to atomic crystals, displaying various sphere-packing Frank–Kasper (FK) and quasicrystal structures. Herein, diverse mesocrystal structures are explored in second-generation dendrons (G2-X) designed with identical wedges, in which the terminal functionalities X = CONH<sub>2</sub> and CH<sub>2</sub>NH<sub>2</sub> represent two levels of the strong and weak hydrogen-bonding apices, respectively. The cohesive interactions at the core apex, referred to as the core interactions, are effectively modulated by forming heterogeneous hydrogen bonds between these two functional units. For the dendron assemblies compositionally close to each pure component of G2-CONH<sub>2</sub> and G2-CH<sub>2</sub>NH<sub>2</sub>, their own FK A15 and C14 phases dominate other phases, respectively. We show the existence of the wide-range FK  $\sigma$  including the dodecagonal quasicrystal (DDQC) phases from the dendron mixtures between G2-CONH<sub>2</sub> and G2-CH<sub>2</sub>NH<sub>2</sub>, providing an experimental phase sequence of A15– $\sigma$ –DDQC–C14 as the core interactions are alleviated. Intriguingly, the temperature dependence of particle sizes shows that the high plateau values of particle sizes are maintained equivalently until each threshold temperature ( $T_{th}$ ), followed by a prompt decrease above the  $T_{th}$ . A decrease in  $T_{th}$  by alleviating the core interactions and its composition dependence suggest that the more size-dispersed particles, the more susceptibility to chain exchange with increasing temperature. Our results on the formation of supramolecular dendron assemblies provide a guide to understand the core-interaction-dependent mesocrystal structures toward the fundamental principle underlying the temperature dependence of their particle sizes.

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### Introduction

Most of the metallic elements usually pack together into simple high-symmetry structures, such as body-centred cubic (BCC), face-centred cubic, and hexagonal close-packed phases,<sup>1–3</sup> except for a few complex structures of manganese and uranium.<sup>4–6</sup> In contrast, the soft-matter spheres obtained from single-component molecular assemblies have recently emerged as synthetic building units prone to transform into complex close-packed mesocrystal structures, where the spherical particles with different sizes and shapes pack into low-symmetry structures.<sup>7–9</sup> These point-like particle assemblies are analogous

to those of metal alloys in terms of three-dimensional (3D) packing characteristics such as the coordination number (CN), particle size and shape dispersity.<sup>10,11</sup> The low-symmetry phases observed in soft-matter assemblies include Frank–Kasper (FK) structures<sup>12–15</sup> as well as 10- and 12-fold quasiperiodic lattices.<sup>16–19</sup> To date, these sophisticated mesocrystal structures have been identified in the molecular self-assemblies of dendritic molecules,<sup>12,20–22</sup> surfactants,<sup>9,15</sup> block copolymers,<sup>14,23</sup> amphiphiles,<sup>24,25</sup> and other soft matters.<sup>26–28</sup> Some of these unconventional structures have been found to possess unique properties applicable for photonic and electronic devices.<sup>29,30</sup>

In order to infer the assembling principle of molecules into thermodynamically stable structures, it is essential to understand the formation of complex phases and their packing mechanism. Thermotropic and lyotropic liquid crystals (LCs) are found beneficial for addressing such challenges because their modular features can afford to provoke the packing diversity arising from the delicate thermodynamic balance in such systems.<sup>31</sup> In particular, a dendron assembly is a simple and versatile platform that has provided a rich series of 2D columnar and 3D sphere-packing structures,<sup>32,33</sup> in which the cohesive interactions at the core apex, referred to as the core inter-

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actions, are the attractive force acting radially towards the body and peripheral chains.<sup>21,25,34–36</sup> Their supramolecular assemblies associated with unique architectures have enabled earlier access to well-defined mesocrystal structures such as the FK and quasicrystal phases.<sup>12,20,22,37</sup>

The pioneering studies by Percec, Ungar, and co-workers well demonstrated the FK A15 and  $\sigma$  phases and the dodecagonal quasicrystal (DDQC) phase was demonstrated by adjusting the structural combination and generation number of dendrons.<sup>12,20–22,34,38</sup> By presenting the radial distribution of volume functions ( $dV/dr$ ) for the sphere-packing structures, they suggested that the dendritic wedges determine the geometry of particle assemblies.<sup>12,13,39</sup> In this concept of topologically close-packed structures, the body-periphery composition in dendron architectures influences the mesoscale packing structures of dendritic assemblies.<sup>35,40–42</sup> Furthermore, it has been believed that the cohesive interactions from the apex functional units also play an important role in guiding specific packing structures. Our previous study highlighted that the discrete increase in the core interactions in single-component dendron assemblies resulted in a remarkable increase in the dendron's interfacial tension ( $\gamma_o$ ) between alkyl chains (corona) and benzyl ether bodies (core).<sup>43</sup> The thermotropic and lyotropic approaches to form apex-dependent second-generation (G2) dendrons led to the observation of columnar and various mesocrystal structures. This finding triggered an interesting question as to how delicate control of the core interactions can affect diverse supramolecular assemblies, transitions, and the temperature dependence of particle sizes.

To answer this question, we explored core-interaction-dependent mesocrystal structures with two types of G2 dendrons, G2-CONH<sub>2</sub> and G2-CH<sub>2</sub>NH<sub>2</sub>, which represent two levels of the strong and weak hydrogen-bonding apexes, respectively. The core interactions were effectively modulated by forming heterogeneous hydrogen bonds between these two apex units. In the dendron assemblies compositionally close to each pure component of G2-CONH<sub>2</sub> and G2-CH<sub>2</sub>NH<sub>2</sub>, their own FK A15 and C14 phases dominated other phases, respectively. However, the FK  $\sigma$  phase including the DDQC phase widely existed over the composition of the dendron mixtures, providing an experimental phase sequence of A15– $\sigma$ –DDQC–C14 by alleviating the core interactions. From the temperature dependence of particle sizes, we generalized that the high plateau values of particle sizes are maintained equivalently until each threshold temperature ( $T_{th}$ ), followed by a prompt decrease above the  $T_{th}$ . Our concept of a master curve for the  $T_{th}$  pointed out the size dispersity effect induced by the core-interaction-dependent mesocrystal structures.

## Experimental

### Synthesis and chemical characterisation

All reagent-grade chemicals were purchased from Sigma-Aldrich, TCI, Alfa Aesar, Duksan, or Fluka. The commercial products dichloromethane (CH<sub>2</sub>Cl<sub>2</sub>), *n*-hexane, tetrahydrofuran

(THF), and methanol (CH<sub>3</sub>OH) were freshly distilled before each use, and all other chemicals were used as received without further purification. To characterise the molecular structures, <sup>1</sup>H and <sup>13</sup>C NMR spectra were measured using a DPX 400 (Bruker) at room temperature in deuterated CH<sub>2</sub>Cl<sub>2</sub> (CD<sub>2</sub>Cl<sub>2</sub>) and chloroform solutions, respectively. Matrix-assisted laser desorption ionisation time-of-flight mass spectrometry (MALDI-TOF-MS) was performed using an LRF20 (Bruker) using dithranol (1,8,9-trihydroxyanthracene) as a matrix. Detailed information on the synthetic processes has been described in the previous study.<sup>43</sup> The bulk densities of the dendrons were evaluated using a solution mixture of water and ethanol once the sample species were constantly suspended in the solution for 30 min. The thermal properties of all samples were characterised using a PerkinElmer Diamond differential scanning calorimetry (DSC) instrument with loading amounts of approximately 10 mg under a nitrogen flow. The temperature and heat flow scales were calibrated using indium as the standard material.

### Small-angle X-ray scattering (SAXS) measurements

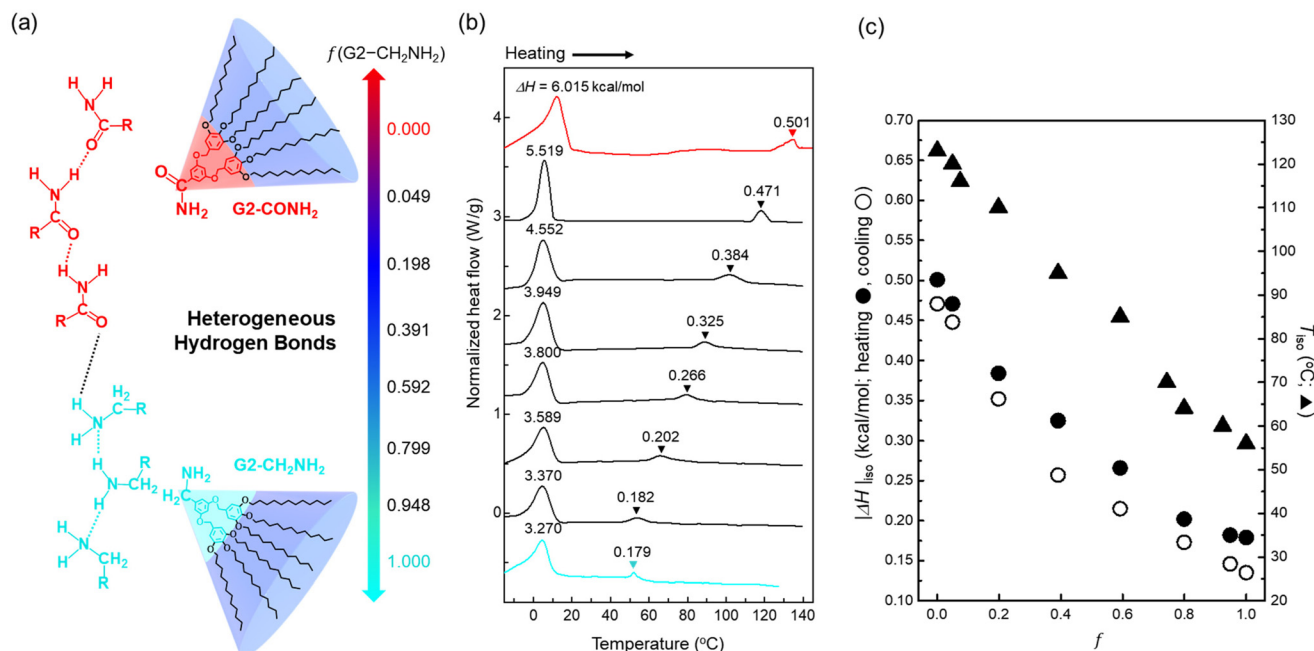
SAXS experiments were performed at the 4C and 9A beamlines of the Pohang Accelerator Laboratory, Korea, or the 12-ID-B beamline of Advanced Photon Source, USA. The operating conditions for the 4C and 9A beamlines were set at a wavelength of  $\lambda = 0.633$  Å, a sample-to-detector distance (SDD) of 1 m, and an exposure time of 1–15 s; these were similarly set at the 12-ID-B beamline with  $\lambda = 0.954$  Å, SDD = 2 m, and an exposure time of 1–10 s. The scattered intensities were collected using 2D detectors (Rayonix SX165 and Pilatus2M) at the target temperatures. The system temperature was selected as the mean value during heating at a rate of 1.0 °C min<sup>-1</sup> under a nitrogen flow.

### Electron density (ED) map reconstructions

The SAXS intensity profiles of all dendron assemblies were recorded to obtain the ED maps of each characteristic sphere-packing phase. Using MATLAB, the structure-factor intensities and positions for each peak over  $q = 0.1$ –5.0 nm<sup>-1</sup> were assigned according to each space-group symmetry and lattice parameter,<sup>44,45</sup> and then recorded as the input values for SUPERFLIP.<sup>46</sup> Random phases were initially generated through a charge-flipping algorithm of SUPERFLIP, and the densities at each pixel in a unit cell were examined. If the calculated density is below zero (indicating an unphysical result), it is multiplied by  $-1$  to make it positive. A discrete Fourier transform of the resulting density maps was employed to regenerate new structural factors, which were again subjected to other iterations. The converged results were averaged and visualised using MATLAB software (in 90% contour levels) to construct Voronoi cells for the experimental polyhedra.

## Results and discussion

Fig. 1a illustrates the chemical structures of (3,4,5-3,5)12G2-X dendrons with two different terminal units, X = CONH<sub>2</sub> and



**Fig. 1** (a) Chemical structures of G2 dendrons (3,4,5-3,5)12G2-X with two different terminal units, X = CONH<sub>2</sub> and CH<sub>2</sub>NH<sub>2</sub>, at the same body and peripheral chains, in which the two functionalities represent the strong and weak hydrogen-bonding apexes, respectively. (b) DSC thermograms of the dendron assemblies, measured at a heating rate of 10 °C min<sup>-1</sup> from -30 to 150 °C. The large endotherms at lower temperatures upon heating imply that the peripheral alkyl chains melt below room temperature, and the second endotherms represent each clearing temperature of LC phases into an isotropic state ( $T_{\text{iso}}$ ). (c)  $|\Delta H|_{\text{iso}}$  (open and closed circles) and  $T_{\text{iso}}$  (closed triangle) as a function of  $f$ .

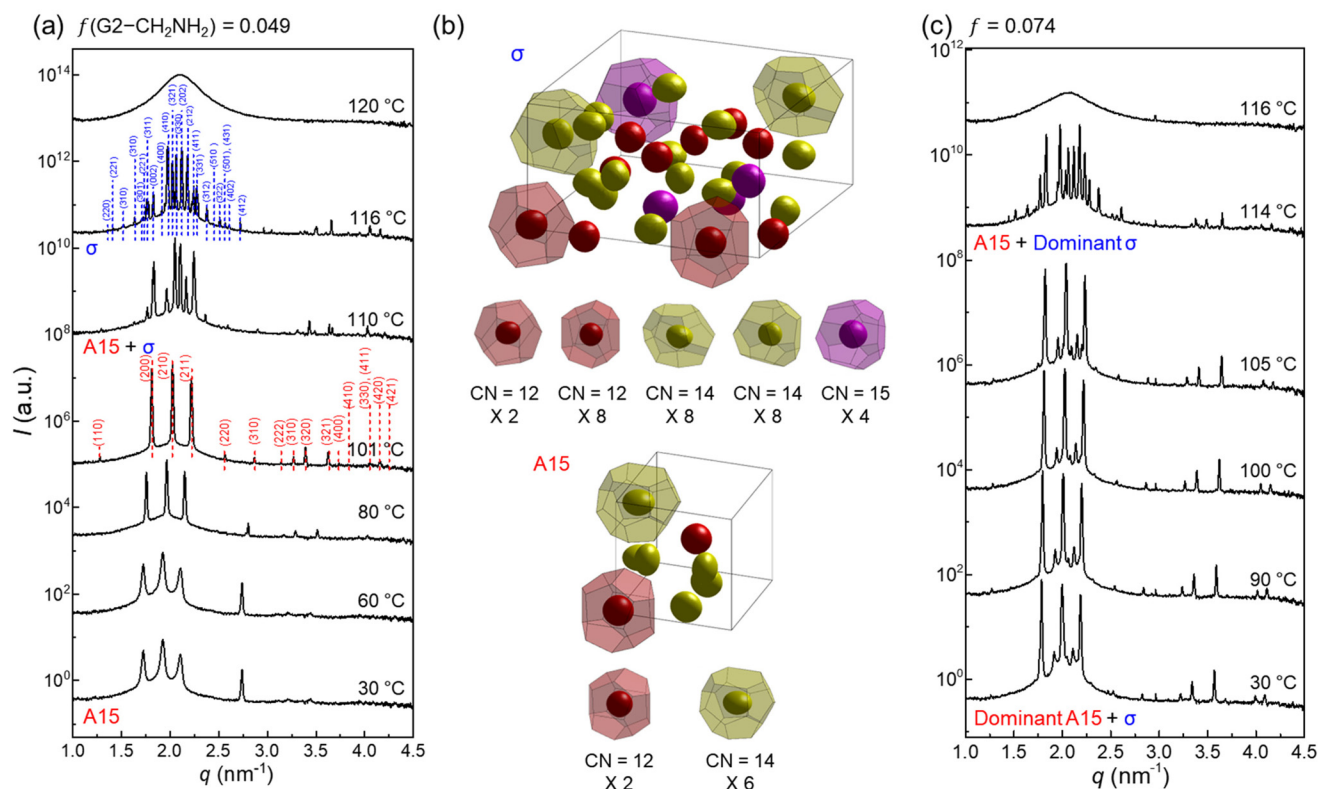
CH<sub>2</sub>NH<sub>2</sub>, at the same body and peripheral chains, where the two functionalities represent the strong and weak hydrogen-bonding apexes, respectively.<sup>43</sup> If the G2 dendron analogues possessing identical wedges are miscible, a heterogeneous hydrogen bond can be formed between these two apex units. As an easy way of controlling the supramolecular sphere-packing structures, this chemical compatibility is essentially required for modulating the core interactions that attract the wedges.

The dendron mixtures between G2-CONH<sub>2</sub> and G2-CH<sub>2</sub>NH<sub>2</sub> were prepared by a solvent casting method from a co-solvent of chloroform and subsequently dried under vacuum before thermal treatments. DSC measurements were conducted at heating/cooling rates of  $\pm 10$  °C min<sup>-1</sup> between -30 and 150 °C to trace the phase behaviours of the dendron assemblies (Fig. 1b and Fig. S1†). The large endotherms and exotherms at lower temperatures upon heating and cooling, respectively, imply that the peripheral alkyl chains melt below room temperature, and the second endotherms (or exotherms upon cooling) at higher temperatures represent each clearing temperature of LC phases into an isotropic state ( $T_{\text{iso}}$ ).

As the mass fraction ( $f$ ) of G2-CH<sub>2</sub>NH<sub>2</sub> increases, the magnitude of the enthalpy change ( $|\Delta H|_{\text{iso}}$ ) at isotropisation and the  $T_{\text{iso}}$  decrease (Fig. 1c). Above all, there are no indications of macrophase separation that would generate two separate transitions in the immiscible binary mixtures. In this framework of dendron assemblies arising from the heterogeneous hydrogen bonds between two apex units attached to identical

wedges,  $|\Delta H|_{\text{iso}}$  can be an indicator of the dendron's overall interfacial tension ( $\gamma_o$ ) that signifies the core interactions. Thus, we speculate that the consistent decreases in  $|\Delta H|_{\text{iso}}$  and  $T_{\text{iso}}$  upon compositionally increasing  $f$  are attributed to weakening of the core interactions in the dendron assemblies. Even the values of  $|\Delta H|$  at lower temperatures are found to show the same decreasing trend as  $|\Delta H|_{\text{iso}}$ , indicating that the alkyl chain melting is also affected by a gradual reduction of the core interactions.

The SAXS intensity profiles of all dendron assemblies were recorded for structural analysis at the target temperatures, at which a constant interval of 5 min was applied to all samples during a stepwise heating process because of the relatively rapid kinetics in forming the mesocrystal structures. The scattering vector  $q = (4\pi/\lambda) \sin \theta$ , where  $2\theta$  and  $\lambda$  are the scattering angle and wavelength of the X-ray beam, respectively. To erase the previous thermal histories, the sample aggregates were first heated to 130 °C and cooled to room temperature at a rate of -10 °C min<sup>-1</sup>. All samples were then annealed at 30 °C under vacuum, which is still higher than the crystallisation temperatures (5–12 °C) of the peripheral alkyl chains. Note that pure G2-CONH<sub>2</sub> exhibited hexagonal columnar (Col<sub>h</sub>), A15, and BCC phases with increasing temperature.<sup>43</sup> At a small fraction of  $f = 0.049$  (Fig. 2a), the SAXS profile measured at 30 °C shows a pattern corresponding to a cubic A15 phase, which becomes increasingly distinctive up to 101 °C, representing that a small amount of G2-CH<sub>2</sub>NH<sub>2</sub> is sufficient to modify the packing structures manifested in pure G2-CONH<sub>2</sub>. This cubic structure first



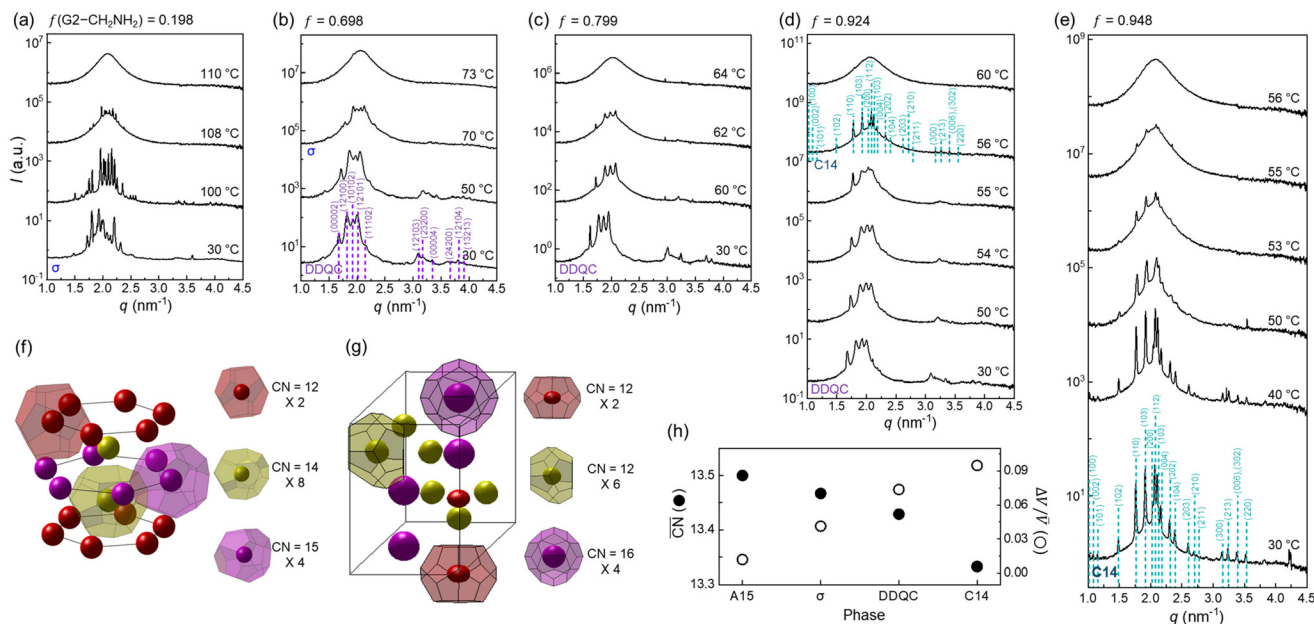
**Fig. 2** (a) SAXS intensity profiles of a dendron assembly with  $f = 0.049$ . A cubic A15 phase measured at 30 °C became increasingly distinctive up to 101 °C, and reorganised to a tetragonal  $\sigma$  phase, and then to an isotropic phase above 120 °C. (b) ED maps reconstructed from the X-ray scattering data, where the dendron cores are displayed at 90% contour levels (isosurfaces) and colour-coded with a sequence of red-yellow-magenta-cyan-blue according to each particle type for clarity. (c) SAXS intensity profiles of a dendron assembly with  $f = 0.074$ . The A15 and  $\sigma$  phases coexist at temperatures lower than 116 °C.

reorganises to a tetragonal  $\sigma$  phase in a narrow temperature window of 110 to 116 °C, and then to an isotropic phase above 120 °C. The A15– $\sigma$  transition is accessed by a small alleviation of the core interactions; this type of transition was reported in a G3 dendron with a terminal COOH apex.<sup>12</sup>

Electron density (ED) maps were reconstructed from the X-ray scattering data using a SUPERFLIP software program.<sup>44–46</sup> The dendron cores are displayed at 90% contour levels (isosurfaces) and colour-coded with a sequence of red-yellow-magenta-cyan-blue according to each particle type for clarity, displaying that the larger the particles (with higher CN) are, the more rounded are the cores. An A15 phase has two polyhedra with CN = 14 and 12, whereas a  $\sigma$  phase has five different types of polyhedra with CN = 15, 14, 14, 12, and 12 (Fig. 2b); these are analyzed with the number of Voronoi cells, surface area, volume, and isoperimetric quotient (IQ), as listed in Table S1.† At  $f = 0.074$  (Fig. 2c), the A15 and  $\sigma$  phases coexist at temperatures lower than 116 °C. However, the  $\sigma$  phase continues to grow at the expense of the A15 phase as the temperature increases, as observed similarly at  $f = 0.103$  (Fig. S2†). In principle, this phenomenon indicates that an increase in temperature in the system is consistent with a reduction of the hydrogen-bonding strength at the core apexes to produce more diverse particle species.

When increasing  $f$  to 0.198 (Fig. 3a), the A15 phase completely disappears and only the  $\sigma$  phase appears during the heating process before it becomes an isotropic phase at 110 °C. The  $\sigma$  phase window extends to  $f = 0.592$  (Fig. S3†), although the characteristic intensities of the  $\sigma$  phase diminish with increasing  $f$ . At  $f = 0.698$  (Fig. 3b), interestingly, the DDQC phase appears at 30 °C and retains the same structure up to 50 °C, which has three different types of polyhedra with CN = 15, 14, and 12 (Fig. 3f). It further transforms into the  $\sigma$  phase at 70 °C. The weak intensity of the  $\sigma$  phase is presumably attributable to smaller grain sizes prior to becoming an isotropic phase. The same trend continues up to  $f = 0.743$  (Fig. S4†), although the DDQC– $\sigma$  transition and isotropisation occur at slightly lower temperatures than those of  $f = 0.698$ . This type of DDQC– $\sigma$  transition was also often observed in G3 dendrons with a terminal CH<sub>2</sub>OH apex,<sup>22</sup> oligomeric G1 dendrons,<sup>47</sup> and AB<sub>*n*</sub> dendron-like giant molecules.<sup>48</sup>

The slow-cooling (–1 °C min<sup>–1</sup>) phase from an isotropic state was not the DDQC but the  $\sigma$  phase within the experimental time scale of 1 day. However, the DDQC phase at  $f = 0.698$  was fully recovered when the sample was reannealed at 30 °C for a long period of 2 months, as shown by the 2D diffraction pattern and intensity profile of the DDQC phase (Fig. S5†). This evidence supports that the DDQC phase



**Fig. 3** SAXS intensity profiles of dendron assemblies with (a)  $f = 0.198$  (only  $\sigma$  phase), (b)  $f = 0.698$  (DDQC– $\sigma$  transition), (c)  $f = 0.799$  (only DDQC phase), (d)  $f = 0.924$  (DDQC–C14 transition), and (e)  $f = 0.948$  (only C14 phase). ED maps of (f) DDQC and (g) C14 phases obtained from dendron assemblies with  $f = 0.799$  (c) and  $f = 0.948$  (e) at 30 °C, respectively. For the ED map of the DDQC phase, Voronoi cells were retrieved from its ideal fractional coordinates and the unit cell size determined from the X-ray data (Fig. S7†). (h)  $\overline{CN}$  and  $\Delta V/\overline{V}$  for the sphere-packing structures. Our experimental phase sequence of A15– $\sigma$ –DDQC–C14 with increasing  $f$  follows an increase in  $\Delta V/\overline{V}$  and a decrease in  $\overline{CN}$  as the core interactions are alleviated.

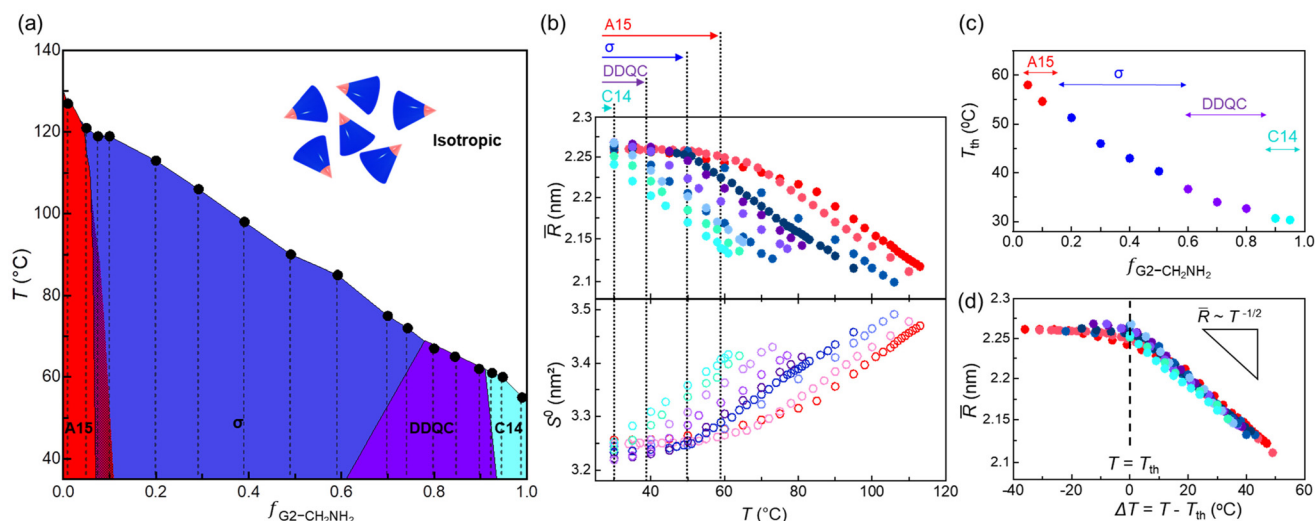
obtained from our dendron assemblies is an equilibrium state requiring long-time annealing, and not a metastable state. For  $f = 0.799$  (Fig. 3c), only the DDQC phase forms at 30 °C and becomes an isotropic phase at 64 °C, similar to that observed up to  $f = 0.897$  (Fig. S6†).

When the  $f$  approaches 0.924 (Fig. 3d), the DDQC phase formed at 30 °C undergoes a transition to the hexagonal C14 phase at 56 °C, which has three different types of polyhedra with CN = 16, 12, and 12 (Fig. 3g), before becoming an isotropic phase at 60 °C. Notably, this unique DDQC–C14 transition is elicited by further alleviating the core interactions, which has never been reported to date. However, the dendron assembly at  $f = 0.948$  (Fig. 3e) begins with a C14 phase at 30 °C and retains the same structure up to 55 °C prior to becoming an isotropic phase; this  $T_{\text{iso}}$  is slightly higher than that (50 °C) measured in pure G2-CH<sub>2</sub>NH<sub>2</sub>. In addition, the advent of the C14 phase only above  $f = 0.924$  indicates that the delicate tuning of the core interactions from the dendron mixtures meets the demanding conditions for the rare C14 phase and its transition. It should be pointed out that the  $T_{\text{iso}}$  follows a decreasing tendency from 120 to 60 °C with increasing  $f$  because of the gradual reduction of the hydrogen-bonding strength at the core apex. Furthermore, all the LC transitions such as A15– $\sigma$ , DDQC– $\sigma$ , and DDQC–C14 were reproducible upon heating when the isotropic samples were annealed at 30 °C for a short period of 10 min.

Based on the four experimental phases of A15,  $\sigma$ , DDQC, and C14 (Table S1†) obtained at the specified temperatures, the dendron assemblies are treated as Voronoi cells composed

of polyhedra. The average particle volume is set to  $\overline{V} = 4\pi\overline{R}^3/3 = n^{-1} \sum_{i=1}^n V_i$ , where  $\overline{R}$  and  $V_i$  are the average spherical sizes of the polyhedra and the  $i^{\text{th}}$  polyhedron volume of  $n$  particles, respectively. We analyzed the average coordination number ( $\overline{CN}$ ) and particle size dispersity ( $\Delta V/\overline{V}$ ) depending on the sphere-packing structures (Fig. 3h). In principle, the more coordinated with the others, the less size-dispersed the sphere-packing particles are, and *vice versa*.<sup>49</sup> Our experimental phase sequence of A15– $\sigma$ –DDQC–C14 with increasing  $f$  follows an increase in  $\Delta V/\overline{V}$  and a decrease in  $\overline{CN}$  as the core interactions are alleviated. This suggests that the weak hydrogen-bonding dendrons are prone to generate larger and smaller particles, whereas the strong hydrogen-bond dendrons favour more uniform-sized particles rather than larger and smaller ones, which is consistent with a theoretical consideration from the previous study.<sup>43</sup>

Fig. 4a shows the overall phase diagram of temperature *versus*  $f$ , and the red, blue, purple, and cyan phase regions represent the A15,  $\sigma$ , DDQC, and C14 phases, respectively. It displays the composition-dependent phases of A15– $\sigma$ –DDQC–C14 along with a linear decrease in  $T_{\text{iso}}$ . The  $\sigma$  and DDQC phases occupy 87.5% with respect to the entire range of  $f$ , representing that they accommodate a moderate and broad range of hydrogen-bonding strengths at the core apex. For more details, we examined the temperature dependence of  $\overline{R}$  and the interfacial area per chain ( $S^0 = 4\pi\overline{R}^2/N_{\text{agg}}$ ), where  $N_{\text{agg}}$  denotes the aggregation number of average particles by  $\overline{N}_{\text{agg}} = 4\pi\overline{R}^3 N_{\text{AP}}/3M$ .



**Fig. 4** (a) The phase diagram of temperature *versus* *f*, where the red, blue, purple, and cyan phase regions represent the A15,  $\sigma$ , DDQC, and C14 phases, respectively. The dashed lines denote the experimental traces, and the overlapped region between the A15 and  $\sigma$  phases represents a mixed phase between the two phases. (b)  $\bar{R}$  and  $S^0$  curves as a function of temperature. The symbols coloured in red, blue, purple, and cyan with increasing *f* denote the A15,  $\sigma$ , DDQC, and C14 phases, respectively. The dotted lines denote each  $T_{th}$ , which is the maximum temperature for maintaining a consistent  $\bar{R}$ . (c)  $T_{th}$  as a function of *f*, which suggests that the more size-dispersed particles, the more susceptibility to chain exchange with increasing temperature. (d) The master curve for  $\bar{R}$  as a function of temperature, in which all the  $\bar{R}$  curves are shifted and superimposed along the temperature axis onto a designated *f* = 0.950 with no  $T_{th}$ .

Here,  $N_A$ ,  $\rho$ , and  $M$  are the Avogadro's number, density, and the molecular weight of each dendron depending on *f*, respectively. Since the  $N_{agg}$  is proportional to the average particle volume  $\bar{R}^3$ ,  $S^0$  is in turn inversely proportional to  $\bar{R}$ .

Fig. 4b shows the  $\bar{R}$  and  $S^0$  curves as a function of temperature. The symbols coloured in red, blue, purple, and cyan with increasing *f* denote the A15,  $\sigma$ , DDQC, and C14 phases, respectively. At lower temperatures, all the values remain relatively constant in each range of  $2.24 < \bar{R} < 2.27$  nm and  $3.22 < S^0 < 3.26$  nm<sup>2</sup>. From the A15 to DDQC phases (the red to purple colours indicated at the top of Fig. 4b), the plateau  $\bar{R}$  and  $S^0$  values were maintained equivalently until each threshold temperature ( $T_{th}$ ), which is the maximum temperature for maintaining a consistent  $\bar{R}$ . When temperatures further increase above the  $T_{th}$ , the  $\bar{R}$  promptly decreases ( $S^0$  increases) with the same slopes. Unlike the plateau  $\bar{R}$  for the lower-*f* dendron assemblies close to the A15 phase, the  $\bar{R}$  for the higher-*f* dendron assemblies close to the C14 phase immediately decreases (the  $S^0$  increases) as soon as the temperature increases.

A decrease in the  $T_{th}$  by alleviating the core interactions and its composition dependence (Fig. 4c) suggest that the more size-dispersed particles, along with the phase sequence of A15- $\sigma$ -DDQC-C14, the more susceptibility to chain exchange with increasing temperature. Considering  $\Delta T = T - T_{th}$ , we constructed a master curve for  $\bar{R}$  (Fig. 4d) as a function of temperature, where all the  $\bar{R}$  curves were shifted and superimposed along the temperature axis onto a designated *f* = 0.950 with no  $T_{th}$ . Above each  $T_{th}$  of the sphere-packing structures, the  $\bar{R}$  values follow a scaling relationship of  $\bar{R} \sim T^{-1/2}$ , indicating that the average particle sizes decrease with increasing temperature and the core-corona interfaces per chain become

broader. As a consequence, our results on the temperature dependence of particle sizes establish an opportunity to associate the core-interaction-dependent phases with their particle size dispersities.

As another aspect of the particle analysis, one can adopt the average radial distribution functions of volume ( $dV/dr$ ) to explain dendritic particles as a function of radial distance (*r*) from the centre.<sup>12,13,39</sup> The  $dV/dr$  function with increasing temperature requires a higher  $dV/dr$  peak due to the lateral thermal expansion of peripheral chains and a shorter  $dV/dr$  tail due to the longitudinal contraction of the chains. This effect may bring about the less size-dispersed phase at higher temperatures towards uniform-sized structures such as a BCC phase; this concept can be applied to the DDQC- $\sigma$  transition measured in our study. However, the A15- $\sigma$  and DDQC-C14 transitions, as observed in our study, indicate that the particle size dispersity increases with increasing temperature; this is against the general explanation from the  $dV/dr$  for temperature-dependent particles.

## Conclusion

We have demonstrated that the core-interaction-dependent phases could be readily achieved by two homologous dendrons of G2-CONH<sub>2</sub> and G2-CH<sub>2</sub>NH<sub>2</sub> possessing different apices but identical wedges. As the amount of weak hydrogen-bonding G2-CH<sub>2</sub>NH<sub>2</sub> increases, the  $|\Delta H|_{iso}$  and  $T_{iso}$  of the dendron assemblies gradually decrease, indicating that the heterogeneous hydrogen bonds between the two apex units successfully tune the core interactions. In the dendron assemblies

compositionally close to each pure component of G2-CONH<sub>2</sub> and G2-CH<sub>2</sub>NH<sub>2</sub>, their own FK A15 and C14 phases dominate other phases, respectively. We show the existence of the wide-range FK  $\sigma$  phase, including the DDQC phase from the dendron mixtures, providing an experimental phase sequence of A15- $\sigma$ -DDQC-C14 by alleviating the core interactions. Particularly, the DDQC-C14 transition elicited at  $f = 0.924$  has never been accessed in soft-matter assemblies to date. This phase sequence also corresponds to the increase in the particle size dispersity (or volume asymmetry).

The temperature dependence of  $\bar{R}$  (and  $S^0$ ) reveals that all the  $\bar{R}$  curves are shifted and superimposed along the temperature axis onto a master curve for  $\bar{R}$  with temperature, of which the  $T_{th}$  for maintaining a consistent  $\bar{R}$  decreases as the core interactions are alleviated. The stronger hydrogen-bonding dendrons with higher  $T_{th}$  favour more uniform-sized sphere-packing structures, whereas for the weaker hydrogen-bonding dendrons with lower or no  $T_{th}$ , the size-dispersed particles are more susceptible to chain exchange with increasing temperature, following the same phase sequence of A15- $\sigma$ -DDQC-C14. Our thermotropic approach for supramolecular dendron assemblies offers valuable insight into the size dispersity effect induced by the core-interaction-dependent mesocrystal structures. Moreover, our systematic concept based on controlling the hydrogen-bonding or cohesive interaction can be a simple strategy applicable for exploring the formation of a predictable, unidentified structure in supramolecular assemblies.

## Author contributions

T. J. performed SAXS measurements and analyzed the properties of each Voronoi cell obtained from the reconstructed ED maps (under the instructions of D. Y. R. and B. L.). H. P. synthesised and characterised the dendron samples using NMR spectroscopy and MALDI-TOF mass spectrometry (under the instructions of W.-D. J.). S. J. assisted and reviewed the experimental results. H. A. assisted with the SAXS measurements and provided advice for data analysis. D. Y. R., W.-D. J., and B. L. discussed the results and wrote the manuscript. D. Y. R. and B. L. co-directed all aspects of the project.

## Conflicts of interest

There are no conflicts of interest to declare.

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