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Stoichiometry matters: correlation between antisite defects, microstructure and magnetic behavior in the cathode material $Li_{1-z}Ni_{1+z}O_2$

Damian Goonetilleke, 🗅 ‡¶ª Björn Schwarz, ២ ^b Hang Li, ^b Francois Fauth, ២ ^c Emmanuelle Suard, ២ ^d Stefan Mangold, ^e Sylvio Indris, ២ ^b Torsten Brezesinski, 🕩 ^a Matteo Bianchini ம §^{af} and Daniel Weber 🕩 ¶*^b

As contemporary battery applications such as electric vehicles demand higher energy densities, layered LiNiO₂ (LNO) could contribute as the end-member of the LiNi_{1-x-v}Co_xMn_vO₂ (NCM) family with the highest extractable specific capacity in a practical voltage window. Achieving high capacities requires among other things a defect free crystal structure, which is not easily achieved due to the natural occurrence of Ni excess on the Li site (Ni1,) and/or antisite defects where Ni and Li switch crystallographic sites. Here, we present a study of the evolution of point defects in a series of LNO samples varying from underlithiated to fully lithiated stoichiometry in layered $Li_{1-z}Ni_{1+z}O_2$ with $-0.05 \leq$ $z \leq 0.35$. Using the high angular resolution of synchrotron X-ray diffraction complemented with the different elements contrast provided by neutron diffraction, we are able to identify two defect regimes. In the first regime, at the underlithiated end, both Ni_{1i} as well as Li on the Ni site (Li_{Ni}) defects are present. Inhibited crystal growth during synthesis is found to coincide with the presence of these Li_{Ni} defects for $z \ge 0.15$. Upon decreasing z values and the vanishing of Li_{Ni}, the primary particle size distribution as well as average refined crystallite size increases. Investigation of the local structure by nuclear magnetic resonance reveals the presence of a Li environment not detected by diffraction methods at low z, the Li-rich end of the sample series. Finally, magnetometry data suggest the onset of the ferrimagnetic-to-antiferromagnetic transition in LNO correlates with the elimination of Li_{Ni} defects in the structure. The present study thus not only highlights the correlation between defect chemistry and physical properties, but also shows the relationship to crystal growth, a field highly relevant for industrial battery cathode materials engineering

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Introduction

Layered oxide cathode materials of the NCM family having a high Ni content have been widely adopted in applications requiring energy storage with a high energy density. To further improve gravimetric energy density, Ni-rich compositions have been developed with Ni content as high as 95%,¹⁻³ effectively approaching the LiNiO₂ (LNO) end-member. Despite being the NCM cathode active material with the highest specific capacity ($\approx 245 \text{ mA h g}^{-1}$ at 4.3 V vs. Li⁺/Li at 25 °C), key issues remain, as LNO is challenging to synthesize, suffers from both structural and surface instabilities in the pristine and de-lithiated state, as well as crystallographic defects hindering full delithiation.⁴ LiNiO₂ has been the subject of numerous studies regarding its synthesis,⁵⁻⁹ crystallographic and electronic structures,¹⁰⁻¹⁴ and electrochemical behaviour,¹⁵⁻¹⁸ and the reader is directed to

^aBattery and Electrochemistry Laboratory, Institute of Nanotechnology, Karlsruhe Institute of Technology (KIT), Hermann-von-Helmholtz-Platz 1, 76344 Eggenstein-Leopoldshafen, Germany

^bInstitute for Applied Materials-Energy Storage Systems (IAM-ESS), Karlsruhe Institute of Technology (KIT), Hermann-von-Helmholtz-Platz 1, 76344 Eggenstein-Leopoldshafen, Germany. E-mail: daniel.weber3@kit.edu

CELLS-ALBA Synchrotron, 08290 Cerdanyola del Vallès, Barcelona, Spain

^dInstitut Laue-Langevin (ILL), BP 156, 71 Avenue des Martyrs, 38042 Grenoble, France

^eInstitute for Photon Science and Synchrotron Radiation, Karlsruhe Institute of Technology (KIT), Hermann-von-Helmholtz-Platz 1, 76344 Eggenstein-Leopoldshafen, Germany

^fBASF SE, Carl-Bosch-Strasse 38, 67056 Ludwigshafen, Germany

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[‡] Current Affiliation: Corporate Research and Development, Umicore, Watertorenstraat 33, 2250 Olen, Belgium.

[¶] Equal author contribution.

[§] Current affiliation: University of Bayreuth, Bavarian Center for Battery Technology (BayBatt), Universitätsstrasse 30, 95447 Bayreuth, Germany.



Fig. 1 (a) Illustration of the LiNiO₂ crystal structure projected along the [001] vector. The illustration highlights the types of defects which may be present in the structure. *S* and *I* represent the height of the slab and interlayer distances, respectively. (b) Ternary pseudo-phase diagram of NiO–NiO₂–Li₂NiO₂, as a snippet from the general Ni–O–Li phase space including formal Ni oxidation state; white dots indicate the layered Li_{1–z}-Ni_{1+z}O₂ compositions synthesised in this study.

a recent review for a more comprehensive overview of the material.¹⁹ While current efforts yielded recipes for LNO with 1–2% of Ni²⁺ on the Li site (Ni_{Li}),²⁰ the formation of defects, and thus possibility for their complete elimination, remains poorly understood in LNO.

In a recent study, the LNO formation mechanism from the mixture of the industrial relevant reactants LiOH·H2O + Ni(OH)2 was elucidated by in situ diffraction.5 There, three steps were identified: (I) dehydration towards NiO + LiOH, (II) partial lithiation/oxidation of the Ni-containing phase towards cubic $Ni_{1-x}Li_{x}O$ (space group $Fm\bar{3}m$) up to $x \approx 0.31$ and even up to x \approx 0.4 during the *in situ* lithiation, and (III) a final oxidation with a concomitant full lithiation towards stoichiometric LiNiO₂. In the cubic, rock salt type phase, Ni and Li share a crystallographic site as well as an oxide anion polyhedron of the same volume. Once sufficient amounts of Ni²⁺ (r = 0.69 Å) are oxidized to Ni³⁺ (r = 0.56 Å), the difference of the average ionic radius of the nickel ions vs. the radius of 0.76 Å for Li⁺ becomes too large, inducing a phase transition towards layered, rhombohedral $\text{Li}_{1-z}\text{Ni}_{1+z}\text{O}_2$ (space group $R\bar{3}m$). In ideal structure of LNO at z = 0, Ni³⁺, Li⁺ and O occupy the 3*a*, 3*b* and 6*c* site, as depicted in Fig. 1a. Hence, the oxygen ions remain in a cubic close packed (ccp) array similar to the rock salt phase, while Li and Ni separate into alternating layers along the c axis of the unit cell.

In real LNO materials though, nickel oxidation and thus separation of lithium and nickel into different crystallographic sites remains incomplete, leading to structural defects. The first such defect, excess of Ni on the Li site NiLi, is found in many studied materials and commonly referred to as "off-stoichiometry". The defect originates from facile lithium losses during synthesis, even in samples of nearly perfect stoichiometry, and leads to a reduced, divalent oxidation state of Ni²⁺ in the Li site. The additional charges in the Li layer are compensated by the formation of charge defects in the NiO₂⁻ layer, *i.e.* $[Li_{1-z}Ni_{z}^{2+}]_{3b}[Ni_{z}^{2+}Ni_{1-z}^{3+}]_{3a}[O_{2}]_{6c}$. As shown recently, with low temperature, ion exchange-based synthesis of LNO from NaNiO₂ at around 320 °C instead of 700 °C, Li loss can be avoided.²¹ The Ni_{Li} defect is easily identified even in lab X-ray powder diffractometry due to the large additional electron density of nickel vs. lithium and thus routinely quantified in LNO studies. Another important defect, in which Ni and Li



Dr Daniel Weber enjoys blending solid state, nano and molecular chemistry to create novel and often metastable inorganic layered materials for energy storage and conversion. After finishing his PhD in the group of Prof. Bettina Lotsch at the Max-Planck-Institute for Solid State Research, he visited the Goldberger group at the Ohio State University as a postdoctoral fellow of the German Science Foundation working on layered magnets. At the Institute of Applied Materials and Battery and Electrochemistry Laboratory (BELLA) of the Karlsruhe Institute of Technology, he currently investigates battery materials and will soon start his independent research group at Chalmers University of Technology as an assistant professor and WISE fellow.

switch their crystallographic sites, i.e. $[\text{Li}_{1-y}\text{Ni}_y^{3^+}]_{3b}[\text{Li}_y^+\text{Ni}_{1-y}^{3^+}]_{3a}[\text{O}_2]_{6c}$, matches the definition of an antisite defect. In general, occupancy of Li⁺ in NiO₂⁻ slabs is highly unusual due to the difference in ionic radii. However, high temperatures may lead to the formation of such antisite defects, as has been reported in highly disordered Li_{0.92}Ni_{1.08}O₂ $(Li_{0.74}Ni_{0.26})_{3a}[Ni_{0.82}Li_{0.18}]_{3b}O_2$ single crystals prepared at = 900 °C.22 Another option to incorporate Li in the Ni site is to have a Li/Ni ratio higher than 1 and increasing the oxygen chemical potential at a lower T of around 550 °C, hence generating oxidized compounds until reaching Li2NiO3 (corresponding to an extended z range from $-0.33 \le z \le 0.0$).²³ A recent combined synchrotron X-ray and neutron diffraction study in isostructural NCM materials by Yin et al.24 indicates that antisite defect concentrations increase with the volume of the transition metal oxide octahedron $Ni_{1-x-y}Co_xMn_yO_6$. There, the polyhedral volume is driven by the reduction of Ni³⁺ to Ni²⁺ in the presence of Mn⁴⁺ and thus strongly dependent on the stoichiometry. While a similar mechanism could be imagined in LNO due to the Ni²⁺ charge defect in the trivalent NiO₂ layer induced by the off-stoichiometry NiLi defect, a similar correlation is not known. Moreover, the limited concentration and nature of antisite defects makes them difficult to probe with conventional characterisation techniques, for example X-ray scattering has low sensitivity for Li, or the relatively high electronic conductivity of LiNiO₂ reduces its Raman scattering efficiency.25 Researchers have hence turned to more advanced methods, including neutron scattering,^{12,26} X-ray absorption spectroscopy,27 and solid-state nuclear magnetic resonance (NMR) spectroscopy^{28,29} to more precisely resolve the crystallographic, electronic, and magnetic structure of LiNiO₂. In tandem with experimental studies, several authors have also adopted computational modelling to predict possible structures of LiNiO2.30-33 Yet, to date in most of the literature models of either antisite defects or off-stoichiometry are often chosen without a precise reasoning behind the choice of the models.

Using a comprehensive suite of characterisation techniques, we aim to resolve the relationship between material stoichiometry and the presence of site defects over a wide range of compositions with nominal stoichiometry $\text{Li}_{1-z}\text{Ni}_{1+z}O_2$ where $-0.05 \le z \le 0.35$, and the resulting consequences for the physical properties of the materials. The site occupancy defects of Li and Ni in the structure are quantitatively determined using combined Rietveld analysis of structural models against X-ray and neutron diffraction data to characterise the bulk average structure. Complementary solid-state NMR spectroscopy provides more detailed insight into the local environments of Li in the defective structures. Finally, we correlate the observed defect chemistry to the magnetic properties and particle size, which yields insights into growth dynamics highly relevant for industrial crystal engineering.

Results & discussion

To better understand the consequences of Li : Ni stoichiometry for the micro- and crystal structure of LNO, a series of Li_{1-z^-} $\text{Ni}_{1+z}\text{O}_2$ samples with a nominal stoichiometry in the range of



Fig. 2 Violin plot of the samples' primary particles size distribution as obtained via SEM.

 $-0.05 \le z \le 0.35$ were prepared *via* solid-state synthesis from commercially relevant hydroxide precursors LiOH·H2O and $Ni(OH)_2$, see white dots in the ternary pseudo-phase diagram in Fig. 1b. Consistent with the studies mentioned above, a clear trend is seen in the evolution of the material's microstructure/ morphology with changing nominal stoichiometry z, as shown in Fig. 2 and S1.[†] All the samples inherit a spherical secondary particle morphology from the Ni hydroxide precursor. However, an obvious change in the size of primary particles can be noticed among the different samples. To more accurately quantify the morphological changes, a semiautomated machine learning algorithm was used to measure the particle size distribution (PSD) from analysis of the electron microscopy images (further details are found in the Experimental section). The results are summarized in Fig. 2, including the median D_{eq} , the 5th to 95th and 25th to 75th percentile of the PSD for each sample. The PSDs are multimodal and present some variation in their shape, which possibly originates from the counting statistics limited by the semiautomatic analysis workflow. Yet, an overall trend emerges: while the median D_{eq} stagnates between approximately 77 and 90 nm for samples with $z \ge 0.15$, the primary particle size steadily increases for samples with $z \leq$ 0.10 up to a median D_{eq} of 308 nm. This observation indicates that the Li: Ni ratio in the precursors mixture plays a crucial role in crystal growth, with a threshold between $0.10 \le z \le 0.15$.

In order to find possible atomistic explanations for this observation and to quantitatively model the evolution of the crystal structure as a function of the nominal stoichiometry, synchrotron X-ray diffraction (SXRD) and neutron diffraction (ND) patterns were collected from the samples. The combination of both SXRD and ND is particularly useful for LNO and other layered cathode materials, as the high intensity and angular resolution coupled with negligible peak profile contributions of the instrument used in SXRD provides precise

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structural parameters. Neutrons on the other hand offer significantly improved sensitivity for Li and O in the presence of heavier transition metal elements for complementary accuracy of atomic parameters.³⁴⁻³⁶ The high-quality SXRD patterns feature narrow peak shapes in the best crystallized samples, allowing for more reliable deconvolution of the contribution to peak broadening due to crystallite size. A single structural model was simultaneously refined against both synchrotron and neutron data where both diffraction data sets were available. This allows for a more meaningful determination of the cation (especially Li) distribution among the 3a and 3b sites in the layered structure. Fig. 3a and b show diffraction patterns collected from the as-synthesised LNO materials. The peak positions of the 003 and 110 reflections, which depend on the c and a lattice parameter, respectively, shift towards higher 2θ values with decreasing z. This indicates that increasing Li content per sum formula is accompanied by a decrease in the unit cell volume. There is also considerable peak broadening of the full-width-at-half-maximum (FWHM) observed with decreasing Li content. Patterns of samples with small Li excess

feature weak peaks corresponding to a minor LiOH impurity of 0.9(3) and 1.5(3) wt% for *z* of -0.01 and -0.05, respectively. Such LiOH impurities have been commonly observed on the surface of Ni-rich cathode materials.^{37,38} As we do not observe the 200 peak at about $2\theta \approx 23.0^{\circ}$ ($\lambda = 0.825888$ Å), there is no evidence for the presence of a rock salt type side phase Ni_{1-x}-Li_xO ($x \le 0.3$).³⁹

In order to quantify the trends observed in the diffraction patterns, structural models with space group $R\bar{3}m$ were refined against the diffraction patterns using Rietveld analysis. An example of the typical quality of fit by comparison of the observed *vs.* the calculated intensity including the difference curve is shown in Fig. 3c and d for SXRD and ND patterns of LNO with z = 0.01, and in Fig. S3[†] for the complete series of pattern. The resulting structural parameters are listed in Table 1 and their evolution with varying *z* or refined Ni excess is visualized in Fig. 4. LNO exhibits clear trends with decreasing Ni content (decreasing *z*), as summarized in Fig. 4a–c. The lattice parameters decrease from a = 2.90868(9) Å and c = 14.25917(6) Å in Li_{0.65}Ni_{1.35}O₂ (z = 0.35) to a = 2.87771(9) Å and c = 14.25917(6)



Fig. 3 Stacked plots of (a) SXRD patterns and (b) ND patterns collected from the as-synthesised materials. Example of simultaneous Rietveld refinements of LNO with z = 0.01 to (c) SXRD and (d) ND data.



Fig. 4 Refined structural parameters of the off-stoichiometric LNO series with (a) *a* and *c* lattice parameters (empty and full symbols, respectively), (b) *c/a* ratio *versus* the refined Ni excess and (c) unit cell volume *vs. z* and refined Ni excess. If error bars not visible, they are smaller than the data symbol.

14.19515(6) Å in nearly stoichiometric LNO (z = -0.05). The unit cell volume also decreases linearly with nominal z from 104.476(9) Å³ to 101.8037(8) Å³, as expected based on prior studies.¹⁹ This can be rationalized with the decreasing radii of the Ni-ions once oxidized from the di- to the trivalent state, with an accompanying reduction of the ionic radii from $r(Ni^{2+}) = 0.69$ Å to $r(Ni^{3+}) = 0.56$ Å.⁴⁰ An increase in the c/a ratio from 4.9023 at z = 0.35, near the cubic c/a limit of $2\sqrt{6} \approx 4.8990$, towards 4.9328 at z = -0.05 (near stoichiometric LNO) is a common indicator for low Li/Ni site disorder, good layering and the distortion observed in the trigonal space group.

Rietveld analysis can also provide information about the materials' microstructure when instrumental and sample contributions to peak broadening are properly deconvoluted.41,42 Here, we first characterised the instrument contribution to peak broading by measuring Na2Ca3Al2F14 and performing a Rietveld analysis including a Thompson-Cox-Hastings (TCHZ) pseudo-Voigt peak shape and axial divergence. The obtained parameters for the TCHZ peak shape and axial divergence were included as fixed values in subsequent refinements. This approach allowed to deconvolute angle-dependent Gaussian and Lorentzian contributions to the peak shape broadening (FWHM), which were interpreted as either originating from the coherent diffracting domain size (FWHM \sim $\cos(\theta)^{-1}$) and microstrain (FWHM ~ $\tan(\theta)$). We used the coherent diffracting domain size to estimate the crystallite size $(D_{\rm vol})$, which initially remains relatively constant in the range of 70 to 75 nm for $0.15 \le z \le 0.35$, see Fig. 5a and b. Upon z < 0.15, the defect regime changes as described in the upcoming paragraphs on site occupancies and the crystallites size grows rapidly with a higher amount of Li equivalents (decreasing z), cumulating in a size of 316(8) nm at z = -0.05. The microstrain displays high values for high z values (Ni-rich end), which is greatly reduced once the threshold at z < 0.15 towards low z values (Li-rich regime) is reached, see Fig. 5c. These results are supported by visual observations and quantification of the primary particle size over the whole sample series via SEM. Samples in the $0.15 \le z \le 0.35$ regime feature small, intergrown primary particles, which then grow into larger, well crystallized primary particles beyond $z \leq 0.1$, see Fig. 2. This indicates a threshold for crystal growth around z < 0.15.

For the precise determination of atomic parameters, such as site occupancies, atomic coordinates, and atomic displacement parameters (ADPs), we utilize the complementary elemental contrast of SXRD and ND. The z-coordinate of oxygen, z_0 , is found to increase linearly with decreasing z, see Fig. 6a. In combination with the evolution of the lattice parameters, the change of z_0 affects the commonly used derived descriptors of the NiO_2^- layer height (S) and interlayer height (I), which are visualized in Fig. 1a, the bond distances d(Li–O) and d(Ni–O) as well as the volumes of the LiO₆ and NiO₆ polyhedra. The height of the NiO₂⁻ layer is defined as $S = (2/3 - 2z_0)c$ and decreases by about 0.1 Å from 2.22 Å for the sample $Li_{0.65}Ni_{1.35}O_2$ (z = 0.35) to 2.12 Å in nearly stoichiometric LNO (z = -0.05). For the same sample range, the interlayer space I = (c/3 - S) accordingly increases from 2.54 to 2.62 Å. The descriptor S is highly correlated to the bond distance d(Ni-O) and the polyhedral volume

Table 1 Refined structural parameters of the off-stoichiometric LNO samples

z	$R_{\rm Bragg}/\%$	$R_{\rm wp}/\%$	a/Å	c/Å	$V/\text{\AA}^3$	$D_{\rm vol}/{\rm nm}$	$z_{\rm O}$
0.35	1.23	4.92	2.90868(9)	14.2592(9)	104.476(10)	80(5)	0.2556(3)
0.30	1.71	4.94	2.90455(6)	14.2525(6)	104.130(6)	78(5)	0.2560(2)
0.25	1.01	4.20	2.90003(6)	14.2432(6)	103.739(6)	63(3)	0.2569(2)
0.20	1.89	5.01	2.89593(4)	14.2371(3)	103.402(3)	80(3)	0.25674(12
0.15	1.36	3.75	2.89122(3)	14.2267(3)	102.990(4)	70(3)	0.25710(15
0.10	1.95	4.92	2.88800(2)	14.22304(15)	102.735(2)	116(3)	0.25761(9)
0.05	1.81	5.01	2.88350(2)	14.21127(12)	102.330(1)	163(4)	0.25799(9)
0.01	1.73	5.56	2.88115(1)	14.20480(9)	102.117(1)	219(5)	0.25833(9)
-0.01	1.84	5.90	2.87971(1)	14.20166(9)	101.992(1)	253(6)	0.25839(9)
-0.05	1.69	5.87	2.87771(1)	14.19515(6)	101.804(1)	316(8)	0.25848(9)

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NiO₆, while *I* shows a weaker correlation to *d*(Li–O) and the polyhedral volume LiO₆, as can be seen in Fig. 6b, c and Table 2. In general, the LiO₆ polyhedral volume and Li–O distance barely change, while the NiO₆ polyhedral volume and Ni–O distance strongly decrease, with *d*(Ni–O) starting at values close to NiO ($d \approx 2.09$ Å (ref. 43)) and converging towards 1.97 Å with decreasing off-stoichiometry *z* due to the increasing average Ni oxidation state in nearly stoichiometric LNO. The trend in Ni oxidation state was detected *via* X-ray absorption spectroscopy on the Ni K edge (Fig. S4†), showing a successive oxidation of Ni with decreasing *z* in Li_{1–z}Ni_{1+z}O₂.

For the site occupancies of the Ni (3a), Li (3b) and O (6c) sites, different hypothesis were implemented and evaluated based on improvement of figure of merit parameters (R_{wp} , goodness of fit as gof, R_{Bragg}),⁴¹ number of parameters used per refinement and chemical reasoning. The free refinement of the oxygen site occupancy was also tested, and was found to converge towards 1 within the refinement error in all samples, suggesting the absence of any oxygen vacancies in these materials. The oxygen occupancy was thus set to 1 for all other refinement models in order to reduce the number of free parameters, and the metal sites were assumed to be fully occupied. For the occupancy of the metal sites, two defect models were compared in order to introduce a Ni excess in the unit cell with increasing z. The first model describes a fully occupied Ni site on 3a and a Ni_{Li} defect occupancy on the Li site (the so-called off-stoichiometry). The occupancy of Li on the 3b site was modelled as $Li_{Li} = 1 - Ni_{Li}$ and a shared atomic displacement parameter was used. This is the most commonly encountered model in published literature on LNO and similar compounds. In the second model, additional Ni was allowed on the Li site $(Li_{Li} = 1 - Ni_{Li})$ as well as Li on the Ni site ($Ni_{Ni} = 1 - Li_{Ni}$), so that the two occupancy defect parameters Ni_{Li} and Li_{Ni} were freely refined in parallel. In general, antisite defects appear when two different, neighboring atoms or ions exchange their lattice sites. Thus, the amount of Li_{Ni} matched by an equal amount of Ni_{Li} represents antisite defects in $\text{Li}_{1-z}\text{Ni}_{1+z}\text{O}_2$. Excess Ni is defined as $\text{Ni}_{\text{excess}} = \text{Ni}_{\text{Li}}$ Li_{Ni} , which should approximately correspond to z as found by elemental analysis. In both models, NiLi increases with increasing off-stoichiometry z, as displayed in Fig. 7a. Yet, model 1 leads to unphysically low or even negative atomic displacement parameters on the Li site, hinting at issues with NiLi as the sole defect model. Upon inclusion of antisite defects by refinement of the Li_{Ni} occupancy on the Ni (3*a*) site, the R_{wp} and R_{Bragg} values for the data sets of $z \ge 0.15$ decrease, indicating a better fit of the model. The effect is not significant in models with antisite defects below the limit of Li_{Ni} $\approx 2\%$ (z < 0.15). This indicates that the inclusion of a single additional parameter is not responsible for the drop in R-values, but rather that there is a resolution limit to the refinement despite the availability of an additional scattering contrast from the neutron data sets. To further test this hypothesis, we compared the elemental composition obtained from the two refinement models with the composition obtained from chemical analysis, see Fig. 7b. A high correlation of the Ni and Li content obtained from inductively coupled plasma-optical emission spectroscopy (ICP-OES) and refinement model 2 (Ni_{Li} incl. Li_{Ni}) can be observed. Model 1 with only the NiLi occupancy defect on the other hand shows highly divergent behaviour at higher z values, which is hard to reconcile with quantities of elemental amounts found in our samples. Our results regarding antisite defects, the absence of oxygen vacancies, and the refinement improvement by using combined synchrotron X-ray and neutron data are aligned with a report by Yin et al. for a variety of isostructural $Li_{1-z}Ni_{1-x-y+z}Co_xMn_yO_2$ materials, as well as with the seminal study of Pouillerie et al.26,34 From this, we could confirm that a certain minimum amount of Ni²⁺ ($z \ge 0.15$) is needed to sufficiently enlarge the Ni layer and allow a measurable amount of Li_{Ni} to be present. In addition to the described parameters, we also refined the atomic displacement parameters B_{iso} , which are shown in Fig. 7c for Li, Ni and O. The values are fairly stable between $B_{\rm iso} \approx 0.23$ to 0.3 Å² for Ni and $B_{\rm iso} \approx 0.77$ to 0.82 Å² for O over the range of $-0.05 \le z \le 0.35$. The atomic displacement parameters of Li decrease with increasing z from around $B_{iso} \approx$ 0.92 Å² at z = -0.05 towards $B_{iso} \approx 0.29$ Å² in Li_{0.65}Ni_{1.35}O₂ (z =0.35). This evolution is chemically intuitive, as increasing zstatistically places additional, heavier Ni-ions ($MW_{Ni} = 58.693$ g mol^{-1} vs. $MW_{Li} = 6.938$ g mol⁻¹) on the Li site, thus leading to an average lower displacement from the site at the same temperature. Overall, the observed values are physically meaningful and close to other values obtained in similar studies utilizing combined refinements against synchrotron X-ray and neutron data sets.34,35

Combining the observations from X-ray and neutron diffraction with SEM imaging points towards a correlation of Li_{Ni} defects with inhibited crystallite and particle growth and





Fig. 5 (a) Crystallite size $D_{\rm vol}$ in dependence of the off-stoichiometry parameter *z*, with the dashed line indicating a change in the defect regime as shown in Fig. 7a. (b) Comparison of the crystallite size $D_{\rm vol}$ from PXRD *vs.* the mean equivalent diameter $D_{\rm eq}$ previously determined by SEM and (c) the S_{400} and S_{004} microstrain parameters from the Stephens model *vs. z.* If error bars not visible, they are smaller than the data symbol.

Fig. 6 Refined structural parameters as a function of nominal *z*: (a) refined fractional atomic coordinate *z* of the oxygen site, (b) volume of LiO_6 and NiO_6 polyhedron and (c) height of interlayer space and NiO_2^- slab. If error bars not visible, they are smaller than the data symbol.

Table 2 Calculated bond lengths, polyhedral volumes, refined site occupancy factors (SOF) and atomic displacement parameters (B_{iso}) of the off-stoichiometric LNO samples

z	d(Li–O)/Å	d(Ni–O)/Å	$V(\text{LiO}_6)/\text{\AA}^3$	$V(NiO_6)/Å^3$	SOF Ni_{Li} (3 <i>b</i>)	SOF $\text{Li}_{Ni}(3a)$	$B_{ m iso}$ Li (3b)/Å ²	$B_{\rm iso}$ Ni (3 <i>a</i>)/Å ²	$B_{\rm iso} O (6c)/{\rm \AA}^2$
0.35	2.104(2)	2.012(2)	12.4626	10.1605	0.466(5)	0.113(8)	0.29(4)	0.23(2)	0.77(6)
0.30	2.105(2)	2.007(2)	12.4734	10.1915	0.374(4)	0.076(7)	0.44(3)	0.279(17)	0.87(5)
0.25	2.1106(17)	1.9973(15)	12.4805	10.2122	0.300(3)	0.044(7)	0.38(4)	0.268(15)	0.79(5)
0.20	2.1072(11)	1.9961(10)	12.4602	10.2798	0.245(2)	0.034(6)	0.49(3)	0.272(12)	0.82(4)
0.15	2.1075(13)	1.9907(11)	12.4574	10.3726	0.179(2)	0.023(6)	0.54(4)	0.290(11)	0.86(4)
0.10	2.1105(8)	1.9848(7)	12.417	10.4698	0.1333(14)	0.011(5)	0.62(4)	0.2957(8)	0.78(3)
0.05	2.1109(7)	1.9794(7)	12.4184	10.5599	0.0764(13)	0.012(5)	0.75(5)	0.2882(8)	0.81(3)
0.01	2.1125(7)	1.9754(6)	12.4795	10.5735	0.0505(12)	0.010(5)	0.81(6)	0.296(8)	0.80(3)
-0.01	2.1122(7)	1.9741(6)	12.3961	10.7439	0.0372(12)	0.014(5)	0.88(7)	0.307(8)	0.83(3)
-0.05	2.1116(7)	1.9722(6)	12.3802	10.8367	0.0237(12)	0.016(5)	0.92(7)	0.306(7)	0.82(3)

a high degree of microstrain in the lattice. The role of $\rm Li_{Ni}$ in the impeded layer growth could be rationalised thanks to $\rm Li_{Ni}$ acting as an observable for the average oxidation state of Ni in the NiO_2 layer. In this hypothesis, $\rm Li_{Ni}$ can only reside in the Ni

site (resolution limit $\leq 2 \text{ wt\%}$) when the lattice has a minimum volume of the NiO₆ octahedra at $\approx 10.4 \text{ Å}^3$, which corresponds to a polyhedral volume ratio of $\frac{V_{\text{NiO}_6}}{V_{\text{LiO}_6}} \approx \frac{10.32 \text{ Å}^3}{12.46 \text{ Å}^3} = 0.828$. In



Fig. 7 Refined atomic parameters as a function of nominal z. (a) Site occupancy factors, (b) equivalents of Ni and Li per formula unit, (c) atomic displacement parameters (B_{iso}) and (d) quality of fit indicators. If error bars not visible, they are smaller than the data symbol.

this case, the shrinkage of the NiO₆ polyhedral volume with increasing oxidation state would allow to indirectly quantify Li_{Ni}. Additionally, one could rationalize the presented observations in a similar manner to the established Cabrera-Vermilyea theory on crystal growth inhibition.44 There, impurities act as stoppers by impinging step growth. Viewing the results of our studies through this lens, Li_{Ni} defects present for $z \ge 0.15$ act as a growth inhibitor for the NiO₂⁻ layer based on the ionic Li-O bond disrupting the formation of hybridized Ni-O bonds. On the other hand, one may also recognize that Li ions are likely to be the more mobile cations during the synthesis, hence samples with high z and little Li content have less ion diffusion hence less crystal growth. Either way, these findings also point to the importance of choosing the appropriate Li/Ni ratio when tailoring the size of the particles, in particular in two-steps synthesis aiming at preparing single crystalline cathode materials.45,46

In order to probe changes to the local environment, ex situ ⁷Li MAS NMR spectra of the $Li_{1-z}Ni_{1+z}O_2$ sample series were measured and are displayed in Fig. 8a and b. For ideal LiNiO₂, there is only one Li⁺ local environment, *i.e.* Li⁺ is surrounded by 12 Ni³⁺ ($3d^7$, S = 1/2) within the two neighbouring NiO₂⁻ layers. Six of them are linked to Li⁺ via 90° oxygen bonds and the other six via 180° oxygen bonds.⁴⁷ In off-stoichiometric Li_{1-z}Ni_{1+z}O₂, Ni²⁺ also resides on the Li site, leading to potentially more than 12 Ni surrounding a Li⁺ ion and an increased number of 90° Ni-O-Li bonds. Changing the oxidation state from Ni³⁺ to Ni²⁺ $(3d^8)$, S = 1; increasing z) creates different, statistically distributed local environments, which leads to Ni-O-Li bond angle dependent peak shift and broadening of the signal. The hyperfine shifts and thus peak position are sensitive to the Ni-O-Li bond angle and Ni oxidation state. The values for the shift contributions were determined for the model compound LiNi_{0.02}Co_{0.96}Mn_{0.02}O₂ with highly diluted Ni and Mn ions by Zeng et al.48 and are useful to explain trends in Ni-rich NCM compositions, as observed by Märker et al. for LiNi_{0.8}Co_{0.1}- $Mn_{0.1}O_2$.⁴⁹ When one Ni³⁺ at 180° Ni–O–Li bond (+110 ppm) is replaced by one Ni²⁺ (+170 ppm), the original signal will move to higher ppm positions by 60 ppm. In the 90° Ni–O–Li bond, reducing Ni³⁺ (–15 ppm) to Ni²⁺ (–30 ppm) only provides a minor contribution of –15 ppm to the peak shifts. In our sample series, corresponding shifts in the peak positions can be observed. From $-0.05 \le z \le 0.20$, the peaks shift towards higher ppm values, as 180° Ni–O–Li bonds dominate. As more and more Ni²⁺ resides in the Li⁺ layer, Li⁺ should be influenced by Ni–O–Li 90° bonds with increasing Ni_{Li}. This hypothesis could explain the strong decrease in the ppm values for samples in the range of $0.25 \le z \le 0.35$.

In addition to changes in the peak position, there is a correlation of the peaks' FWHM and the stoichiometry of the samples. Different ratios of Ni : Li on the local scale give rise to various possible environments. The FWHM is expected to be narrow for a uniform environment, which in the present case is a single Li⁺ ion surrounded by 12 Ni³⁺. Once samples are less stoichiometric (increasing *z*), there is a statistical distribution of signals arising from Li⁺ ions from the various sites and environments. With an increasing *z*, the distribution becomes broader, leading to a massive increase in FWHM. This is what we observe in our samples, where the broadest peaks observed for $0.25 \le z \le 0.35$ cover the range of approximately 2000 to -1000 ppm.

Aside from the main peaks, some other, minor bands can be observed in the NMR spectra. There is also a small, broad peak observed at 450 ppm, which carries 5.6%, 3.0%, and 2.5% of the intensity of the main peak for z = -0.05, -0.01, and 0.01, respectively, before completely diminishing. There are two common, yet opposing explanations found in the literature regarding its origin. A recent study argues that Li⁺ in the Ni layer close to Ni⁴⁺ ($3d^6$, S = 0) would produce such a shift.²³ The most extreme cases were described for a system Li₁₋₂Ni₁₊₂O₂ from $0 \le z \le -0.33$. There, ordering of Li⁺ in the Ni layer increases closer to z = -0.33, leading to peak shifts from 450 ppm in $z \approx 0$ towards about 250–300 ppm in z = -0.33 (Li_{1.33}Ni_{0.66}O₂ = Li₂NiO₃). As our diffraction data does not indicate a well-



Fig. 8 (a) ⁷Li MAS NMR spectra of $Li_{1-z}Ni_{1+z}O_2$ ($-0.05 \le z \le 0.35$) sample series with an inset showing the evolution of the NMR shift vs. $z_{nominal}$. The intensities are normalized with respect to the sample mass and the number of scans. (b) Enhanced view of the spectra of $Li_{1-z}Ni_{1+z}O_2$ for 0.1 $\le z \le 0.35$.

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ordered structure with a high amount of Li⁺ in the Ni layer, the signal could originate from a small amount of a solid solution of $LiNiO_2 - Li_2NiO_{3-\delta}$ with $\leq 2\%$ Li^+ excess on the local scale, which would be below the resolution limit of our diffraction study. This hypothesis is further strengthened by the fact that the NMR data from LiNiO₂ prepared by low temperature ion exchange from well-ordered NaNiO₂ (no Li⁺ in the Ni layer) does not show a peak at 450 ppm.²¹ The second explanation for the 450 ppm peak commonly encountered in the literature assumes the presence of a $Ni_{1-x}Li_xO$, rock salt type phase with a large amount of Ni^{2+, 50} If present, the prominent cubic phase reflection 200 would be expected at $2\theta \approx 23.0^{\circ}$ (e.g. Ni_{0.8}Li_{0.2}O)³⁹ at the wavelengths utilized in this study ($\lambda = 0.825888$ Å). However, as no peaks are observed in that region, we exclude the presence of a rock salt type phase. The last remaining, sharp and narrow peak at 0 ppm originates from diamagnetic impurities such as LiOH, which were also found via X-ray and neutron diffraction in this and others studies.51

Overall, there are three regimes which give rise to different observations via NMR: the highly off-stoichiometric Li₁₋₂Ni₁₊₂- O_2 regime (I) from z = 0.35 to 0.25, where 90° Ni–O–Li bonds dominate the signal and lead to a decreasing peak position as well as strongly increasing line width of the main NMR signal with increasing z. In the slightly off-stoichiometric $Li_{1-z}Ni_{1+z}O_2$ regime (II) with z reaching from 0.2 to 0.05, Li⁺ ions within LNO are surrounded by an increasingly uniform environment with decreasing z. There, 180° Ni-O-Li bonds dominate and lead to a decrease in the peak position and a sharpening of the FWHM with lower off-stoichiometry. In the nearly stoichiometric regime (III) from z = 0.01 to -0.05, peak intensity and FWHM are at their maximum and minimum, respectively, as the environment of the Li⁺ ions is the most homogeneous. In addition, a secondary peak arises which increases in intensity with increasing Li content.

Another possible probe, highly sensitive to structural order and inhomogeneities in battery materials, is the study of magnetic properties, which have been intensely reported in $LiNiO_2$.^{52–55} Nearly stoichiometric $Li_{1-2}Ni_{1+2}O_2$ has been described as a glassy antiferromagnet, which features ferromagnetic intralayer coupling and weakly antiferromagnetic coupling between different NiO2⁻ layers.⁵⁶ With increasing offstoichiometry, Ni²⁺ resides on the Li site, leading to local magnetic coupling between neighboring layers via small ferrimagnetic clusters. In order to characterise our samples, we measure the cusp in the magnetic susceptibility vs. T curve as a proximate to the magnetic ordering transition and the lowtemperature magnetization as a function of an applied magnetic field. The magnetic transition temperature measured under zero field cooled conditions changes with composition, ranging from 10 to 247 K in our data, very similar to the data of Barton et al. as displayed in Fig. 9.53 In a simplified picture, it was assumed that increasing the amount of NiLi beyond a critical threshold leads to the formation of ferrimagnetic clusters.52 Prior studies hypothesized that long-range antiferromagnetic ordering in a composition of the $[Li_xNi_{1-x}]_{Li}[Ni]_{Ni}O_2$ type is superseded by short-range, strongly ferrimagnetic behavior in disordered $[\text{Li}_{x/2}\text{Ni}_{(1-x)/2}]_{\text{Li}}[\text{Li}_{x/2}\text{Ni}_{(1-x)/2}]_{\text{Ni}}\text{O}_2$ at $0.1 \le z \le 0.15$



Fig. 9 Evolution of the magnetic ordering temperature determined from the maxima in ZFC curves and data from P. T. Barton *et al.*,⁵³ including the remanent magnetization M_R vs. composition as an inset.

(ref. 53) based on the change in the remanent magnetization $M_{\rm R}$. We investigated the low-temperature magnetization behavior at 2 K between $-7 T \le \mu_0 H \le 7 T$ and observe hysteresis loops, indicating the behavior suggested by Barton et al. The resulting data are presented as an inset in Fig. 9, with the raw data hysteresis loops displayed in the ESI Fig. S4 and S5.† In our samples, a similar correlation between composition, remanent magnetization and magnetic transition temperature has been observed. The high angular resolution X-ray and neutron diffraction data indicates that the bulk presence of Ni_{Li} as well as antisite defects $\geq 2\%$ coincides with the transition to a strongly ferrimagnetic coupled material as postulated by B. T. Barton et al.53 The stoichiometry dependent peak in the remanent magnetization also matches the maximum of the predicted magnetization per ion found by J. B. Goodenough et al. at $x \approx 0.43$ for $\text{Li}_x \text{Ni}_{1-2x}^{2+} \text{Ni}_x^{3+} \text{O} (z \approx 0.14 \text{ in } \text{Li}_{0.86} \text{Ni}_{1.14} \text{O}_2)^{.55}$ Thus, our diffraction results hint at a possible mechanistic explanation and map the border for the transition of the bulk structure: the ordered regime exists until $z \ge 0.15$ ($x \le (1 - z)/2$) \approx 0.425). Afterwards, the Li incorporates into the Ni layer, which possibly separates the ferrimagnetic clusters. The presented data points towards a possible starting point of future studies for enhancing the understanding of Li1-zNi1+2O2 fundamental magnetic properties.

Conclusion

Our study maps the rhombohedral phase space of the Li-ion battery cathode active material $\text{Li}_{1-z}\text{Ni}_{1+z}\text{O}_2$ with $-0.05 \le z \le 0.35$ and reports the correlation of stoichiometry, observed crystal defects, particle growth and magnetic properties. The increase in crystallite size strongly correlates with an increasing LiOH : Ni(OH)₂ ratio once the off-stoichiometry parameter *z* is <0.15, as shown by SEM and SXRD. This suggests the presence of Li_{Ni} defects for $z \ge 0.15$ coincides with an inhibited growth of

NiO₂ layer and LNO crystallization in general. The high angular resolution of SXRD with complementary ND indicates a continuous evolution of lattice parameters and derived metrics, yet delivers new information on the occupancies based on the difference in scattering factor for X-rays and neutrons. Specifically, we observe that the physical meaningful model includes Ni_{Li} occupancy defects as well as antisite defects for z \geq 0.15. While the former is often included in refinement models observed in the literature, the antisite defects are not. However, the difference between the two models is only significant for $z \ge 0.15$, while below that value both models accurately reproduce the diffraction data within error of the refinement. Our results suggest that Li deficiency leads to an incomplete separation of lithium and nickel into different crystallographic sites during the transition from cubic Ni_{1-r}- Li_xO to layered $Li_{1-z}Ni_{1+z}O_2$, leading to antisite defects and Ni_{Li} for $z \ge 0.15$. On the local level, NMR suggests the existence of three regimes: (I) a highly disordered, Ni²⁺ rich environment $(0.25 \le z \le 0.35)$, (II) a single-phase regime with increasing order around Li^+ (0.05 $\leq z \leq$ 0.2) and (III) a two-phase environment in the highly stoichiometric regime $(-0.05 \le z \le 0.01)$, hinting at the presence of a small amount of highly disordered LiNiO₂-Li₂NiO₃ solid solution. Finally, the threshold of Li_{Ni} defects also coincides with the transition from antiferromagnetic behavior in low z LNO to strong ferrimagnetism in disordered LNO. Hence, Li_{Ni} defects could play a role in localizing magnetic interactions within the NiO₂ layer. Our detailed examination of the correlation between stoichiometry, defects, crystal growth, and related properties in rhombohedral Li1-z-Ni_{1+z}O₂ thus opens new avenues for manipulating and improving the cathode materials LNO and its Co- and Mncontaining derivatives.

Experimental

Synthesis

Li_{1-z}Ni_{1+z}O₂ was synthesized from the starting materials Ni(OH)₂ ($D_{50} = 11.8 \mu m$, BASF SE, Germany), LiOH·H₂O (BASF SE, Germany) in a high-temperature reaction under gas flow with *z* values ranging from -0.05 to 0.35. The reactants were dry mixed in a laboratory blender for 30 min under Ar atmosphere in the required ratios with a 1 mol% excess of LiOH·H₂O. The reactant mixtures were calcined in an alumina crucible under an O₂ flow of two volume exchanges per hour in a tube furnace (Nabertherm P330) with heating and cooling ramps of 3 K min⁻¹. The samples were annealed at 700 °C for 6 h, and the furnace was then allowed to cool naturally.

Diffraction

Synchrotron XRD data were collected on the BL04-MSPD beamline at the ALBA Synchrotron, Spain.^{57,58} Powder patterns were collected in Debye–Scherer mode geometry using the onedimensional silicon-based position-sensitive detector MYTHEN, enabling fast data acquisition with excellent statistics and high angular resolution. Data were collected in the angular range $0.4^{\circ} < 2\theta < 57^{\circ}$ (*Q* range 0.0708–9.671 Å⁻¹) at a wavelength of $\lambda = 0.825888(3)$ Å. The wavelength was determined using a NIST Si 640c SRM. The instrumental contribution to the peak broadening was determined by measuring a crystalline Na₂Ca₃Al₂F₁₄:CaF₂ (NAC) sample as a line broadening reference in a 0.5 mm diameter borosilicate capillary and modelled via Thompson-Cox-Hastings pseudo-Voigt functions. An overall acquisition time of 5 minutes was used to measure each sample, which were packed in 0.5 mm diameter borosilicate glass capillaries. Neutron diffraction (ND) data were acquired on the D2B high-resolution powder diffractometer of the Institute Laue-Langevin (Grenoble, France), at a wavelength of 1.594 Å, calibrated with a Na₂Ca₃Al₂F₁₄ reference.⁵⁹ Samples were loaded into cylindrical vanadium cans of diameter 10 mm and data were collected in the $10^{\circ} < 2\theta < 160^{\circ}$ angular range. Rietveld refinement was performed using Topas v6 (Bruker AXS). Combined refinements against the X-ray and neutron data were performed for samples with z = -0.05, -0.01, 0.01, 0.05,0.1 and 0.2, the remaining samples were investigated using synchrotron X-ray data only. The measured intensities of X-ray and neutron data were weighted according to their experimental uncertainties with $1/\sigma(Y_{obs})$.² The background was fitted to the data using a Chebyshev polynomial function with 11 terms for X-ray and 7 terms for neutron data. During combined refinements, the lattice parameters, size broadening and microstrain contributions were refined vs. X-ray data, while the unit cell content (atomic coordinates, SOFs and ADPs) were refined vs. X-ray and neutron data. For refinements, scale factor, zero shift, crystallite size and anisotropic strain broadening parameters based on the Stephens model⁶⁰ were allowed to vary. In the structural model, the unit cell parameters, the oxygen zcoordinate, site occupancy factors (SOFs) and the isotropic atomic displacement parameters B_{iso} for each site were refined. Two site occupancy defects, Ni occupancy on the Li site and antisite defects were refined. Atoms occupying the same site were constrained to have the same B_{iso} , and SOFs were constrained such that each site remained fully occupied. Previous studies have shown that systematic errors in refinement of XRD data from layered cathode materials can be corrected by choosing specific form factors³⁴ or representing them as linear combinations of a charged and uncharged state.35 In our refinements, we chose the form factors of Li⁺, Ni²⁺ and O²⁻ in order to represent the electron density in the unit cell.

Peak shapes were modelled in a double Voigt approach including Gaussian and Lorentzian contributions. The width of the peaks in the synchrotron data evolving with 2θ as $\cos(\theta)^{-1}$ were interpreted as crystallite size broadening. Crystallite size is reported as the volume-weighted average column height (D_{vol}) calculated *via* 1/integral breadth (Gaussian & Lorentzian contribution).⁴¹ Broadening contributions with Voigt components that follow a $\tan(\theta)$ evolution were interpreted as microstrain and analyzed *via* the phenomenological model described by Stephens.⁶⁰ The model allows the description of anisotropic strain parameters S_{hkl} , which are symmetry restricted and related to the variance of the spacing of lattice planes along certain *hkl* directions. Thus, a higher number of local defects on certain *hkl* lattice planes increases S_{hkl} . Both crystallite size and microstrain broadening contributions were determined from

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the X-ray data during initial LeBail fits, fixed and re-refined towards the end of the refinement process. Critical parameters affecting the intensity apart from the choice of the structure factor are the oxygen z-coordinate (z_0), occupancy of excess Ni²⁺ on the Li site Ni_{Li}, antisite defect concentration as well as the isotropic atomic displacement parameters B_{iso} and were refined in this order from X-ray and neutron data, where neutron data was available. Antisite defects are defined as an exchange of a pair of Li and Ni ions from their respective layers into the other layer.²⁴ The average antisite defect occupancy was modelled by a free, parallel refinement of defect occupancies of Li⁺ on the Ni site (Li_{Ni}) and Ni²⁺ on the Li site (Ni_{Li}) and evaluated by the reduction in R_{wp} and the comparison of the overall composition to values measured in elemental analysis.

Elemental analysis

The Li, Ni, and O content of the samples was determined via inductively coupled plasma-optical emission spectroscopy (ICP-OES) using a Thermo Fischer Scientific iCAP 7600 DUO. The mass fraction was determined from three independent measurements. About 10 mg of the samples was dissolved in 6 mL of hydrochloric acid and 2 mL of nitric acid at 353 K for 4 h in a graphite oven. The digestions were diluted, and analysis of the elements was accomplished with four different calibration solutions and an internal standard (Sc). The range of the calibration solutions did not exceed a decade. Two or three wavelengths of elements were used for calculation. The O content was analyzed by carrier gas hot extraction (CGHE) using a commercial oxygen/nitrogen analyser TC600 (LECO). The O concentration was calibrated with the certified standard KED 1025, a steel powder from ALPHA. The standards and samples were weighed with a mass in the range from 1-2 mg together with 5 mg of graphite in Sn crucibles (9-10 mm) and wrapped. Together with a Sn pellet, the wrapped samples were put into a Ni crucible and loaded in an outgassed (6300 W) doublegraphite crucible. The measurements took place at 5800 W. The evolving gases, CO_2 and CO, were swept out by He as inert carrier gas and measured by infrared detectors.

Nuclear magnetic resonance

⁷Li magic-angle spinning (MAS) NMR experiments were conducted on a Bruker Avance 200 MHz spectrometer at a magnetic field of 4.7 T. Spectra were acquired at a Larmor frequency of 77.8 MHz with 1.3 mm rotors and spinning at 55 kHz. A rotor-synchronized Hahn-echo pulse sequence $(90^\circ - \tau - 180^\circ - \tau - acquisition)$ was used with a 90° pulse length of 0.85 µs and a recycle delay of 1 s. The ⁷Li NMR shifts were referenced using an aqueous 1 M LiCl solution (0 ppm). All spectra were normalized with respect to sample mass and the number of scans.

Electron microscopy

The morphology of the samples was investigated utilizing a Merlin thermal field emission scanning electron microscope (FESEM, Carl Zeiss). Prior to the measurements, samples were glued onto conductive carbon pads and coated with an approximately 5 nm layer of Au_{0.8}Pd_{0.2} using an EM ACE 600 coater (Leica). Images were segmented using the trainable WEKA segmentation algorithm in order to count the number of particles and measure their areas using Image2 (Fiji).^{61,62} Each segmentation was visually crosschecked in order to avoid counting artefacts. In this manner, at least three secondary particles and approximately 380 to 530 individual primary particles were characterized for good counting statistics. Pixel-count areas were transformed into physical units *via* magnification based calibration factors from the image metadata. Only particles of an area of at least 500 nm² and a circularity (defined as $4\pi A/[\text{perimeter}]^2$) of ≥ 0.5 were used for counting statistics, similarly to a procedure described in the literature.²⁰ The areas *A* of the particles with a circularity ≥ 0.5 were transformed into an equivalent diameter D_{eq} of a circle of the same area using the formula $D_{eq} = 2\sqrt{A/\pi}$.

Magnetometry

DC magnetometry was measured using a Physical Property Measurement System (PPMS) DynaCool from Quantum Design equipped with a vibrating sample magnetometry (VSM) option. LNO powder was filled into polypropylene sample capsules (Quantum Design QDS-4096-388) in an Ar-filled glove box and transferred to the device. Zero-field cooled (ZFC) and fieldcooled (FC) magnetization vs. temperature was measured at a magnetic field of 500 Oe from 2 to 390 K in temperature settle mode from 2 to 25 K and in sweep mode with 2 K min⁻¹ from 25 to 390 K. The signal was averaged over 10 seconds for each measurement. Magnetization vs. field scans with maximum field of $\mu_0 H = \pm 7$ T were measured at 2 K by first cooling the sample to 2 K in zero field before measuring a full loop (4 quadrants) starting at 7 T. For samples with z = -0.05 and -0.01, which included small amounts of diamagnetic impurity phases, only the LNO phase has been considered for data evaluation. Diamagnetic corrections were applied to all data, with -7.71×10^{-9} emu Oe⁻¹ for the sample capsule and values for the atomic electronic closed shells by the incremental method as described by Lueken.63

X-ray absorption spectroscopy

X-ray absorption spectroscopy (XAS) was performed at the XAS beamline of the KIT synchrotron in transmission mode with the IC Spec ionisation chamber. The measurements were undertaken inside a vacuum chamber to avoid contact with air/ moisture and to maximize the signal-to-noise ratio. The samples were transferred with a sample transfer system. The position of the absorption edge was determined *via* the maximum in the first derivative.

Conflicts of interest

There are no conflicts to declare.

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