



Opto-hydrodynamic tweezers†

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Optical fiber tweezers offer a simple, low-cost and portable solution for non-invasive trapping and manipulation of particles. However, single-fiber tweezers require fiber tip modification (tapering, lensing, etc.) and the dual-fiber approach demands strict alignment and positioning of fibers for robust trapping of particles. In addition, both tweezing techniques offer a limited range of particle manipulation and operate in low flow velocity regimes (a few $100 \mu\text{m s}^{-1}$) when integrated with microfluidic devices. In this paper, we report a novel opto-hydrodynamic fiber tweezers (OHT) platform that exploits the balance between the hydrodynamic drag force and optical scattering forces to trap and manipulate single or multiple particles of various shapes, sizes, and material compositions in a microfluidic channel. 3D hydrodynamic flow focusing offers an easy and dynamic alignment of the particle trajectories with the optical axis of the fiber, which enables robust trapping of particles with high efficiency of $>70\%$ and throughput of 14 particles per minute (operating flow velocity: $1000 \mu\text{m s}^{-1}$) without the need for precision stages or complex fabrication. By regulating the optical power and flow rates, we were able to trap single particles at desired positions in the channel with a precision of $\pm 10 \mu\text{m}$ as well as manipulate them over a long range upstream or downstream with a maximum distance of $500 \mu\text{m}$. Our opto-hydrodynamic tweezers offer an alternative to conventional optical fiber tweezers for several applications in physics, biology, medicine, etc.

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Introduction

Optical tweezers, which were first demonstrated by Arthur Ashkin in the 1970s, continue to be the preferred approach for contactless and non-invasive manipulation of single particles ranging from colloids, hard spheres, polymers, gels, cells, bacteria, and viruses to biological macromolecules.^{1–6} Based on strong optical gradient forces, conventional tweezers use high numerical aperture (NA) microscope objective lenses to trap particles at the focus of the laser. The integration of tweezers with other investigative techniques such as microscopy and spectroscopy has advanced our understanding of single particles

particularly within the fields of biology and medicine. For example, a single *E. coli* bacterium has been trapped by optical tweezers to characterize its “run and tumble” swimming behaviour.¹ In another study, a single DNA strand was trapped and manipulated to measure its spring constant.⁷ It was also possible to resolve the angstrom-level stepwise motion of motor proteins on microtubules by manipulating a protein-tethered bead with optical tweezers. Although optical tweezers presented an elegant way to probe single particles, certain constraints, such as the need for high NA lenses, small working distances, complex instrumentation and operation, and lack of portability, have limited its widespread applicability.

Optical fiber tweezers overcome the limitations imposed by traditional optical tweezers and provide a simple, cost-effective, and portable solution to trap particles. Among several fiber-based tweezer designs, dual-beam fiber tweezers that use two opposing diverging beams for trapping a particle are most popular and have been used for several applications such as rotation of particles, Raman spectroscopy of single cells, and, most importantly, as optical stretchers to study single-cell deformability.^{8–12} Nonetheless, robust trapping of particles requires strict positioning and axial alignment of the two fibers with a precision down to one micron, otherwise the particles tend to oscillate within the trapping region.¹³ To achieve precise alignment and positioning of the fibers, high-precision motion stages or fabrication of fiber-guiding structures on the chip are necessary.^{14,15} The use of

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† Electronic supplementary information (ESI) available: Supplementary Video S1: 3D hydrodynamic flow focusing in a microfluidic channel. Supplementary Video S2: continuous trapping of single polystyrene particles with high efficiency and throughput in an OHT. Supplementary Video S3: simultaneous trapping of multiple polystyrene particles forming linear chains in an OHT. Supplementary Video S4: trapping of a single $15 \mu\text{m}$ polystyrene particle in an OHT. Supplementary Video S5: auto-alignment of particle trajectory by optical gradient force in OHT. Supplementary Video S6: trapping of particles of different sizes, shapes, and refractive indices, including mammalian cells, with OHT. See DOI: <https://doi.org/10.1039/d3lc00733b>

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high-precision stages increases the cost and form factor of the dual-fiber tweezers while fiber-guiding structures increase the device complexity and rigidity, offering no flexibility to the alignment process in case of fabrication errors *etc.* Although with excellent alignment, the dual-beam fiber tweezers can efficiently trap particles; their ability to manipulate the trapped particle is limited along their optical axis—*i.e.*, over the width of the channel (typically $<100\ \mu\text{m}$)—if the fibers are positioned perpendicular to the flow direction.¹⁰ Furthermore, their operation is restricted to slow flow rates in the channel. Since gradient forces are mainly responsible for trapping of particles in the flow direction, at high flow rates, the drag force acting on the particle/cell overcomes the optical gradient force, yielding poor trapping efficiencies and limiting application throughput.

Because single-fiber tweezers do not need any fiber alignment, they are preferred over dual-beam fiber tweezers. They can provide a significant gradient force to capture particles but require fiber tip modification in the form of a taper or machining to create a lens.¹⁶ Furthermore, particle manipulation necessitates physical movement of the fiber and hence cannot be employed for on-chip particle manipulation. Because of the increased fabrication complexity, high optical intensity operation, and limited particle manipulation capability, single-fiber tweezers are a less appealing solution for many applications.^{17–22}

In this paper, we present a novel optofluidic platform for trapping and manipulation of single as well as multiple particles and cells. The device utilizes laminar flow in microchannels to hydrodynamically focus and deliver particles

or cells to the trapping zone. In contrast to the standard orthogonal alignment of the fibers with the flow direction, in our device a single optical fiber embedded in the microchannel is oriented parallel to the flow direction (see Fig. 1(a) and (b)). As a result, particles can be trapped at specific locations in the channel, where there is a balance between the optical and hydrodynamic (shear and drag) forces acting on the particle as shown in Fig. 1a and b.

The synergy of laminar flow in microfluidic channels along with the compactness of optical fibers creates opto-hydrodynamic tweezers (OHT). The trajectory of particles in the channel can be altered by adjusting the sheath flow rates, which allows for easy and dynamic alignment of particles with the optical fiber resulting in efficient trapping of particles.

Moreover, since the drag force is balanced by the optical scattering force rather than by the gradient force as in the case of conventional optical fiber tweezers, OHT can work at significantly higher flow velocities (up to $4300\ \mu\text{m s}^{-1}$), which is more than ten times the operating flow velocities of conventional optical fiber tweezers.¹⁰ By regulating the optical power and flow rates in the channel, the trapped particle can be manipulated/translated over a long range along the length of the channel up to a maximum distance of $500\ \mu\text{m}$.

The ability to dynamically control and align the trajectory of particles with the optical axis of the fiber by simply modulating the sheath flow rates is one of the distinguishing features of OHT. It enables robust trapping of particles with high efficiency (given by the number of trapped particles/

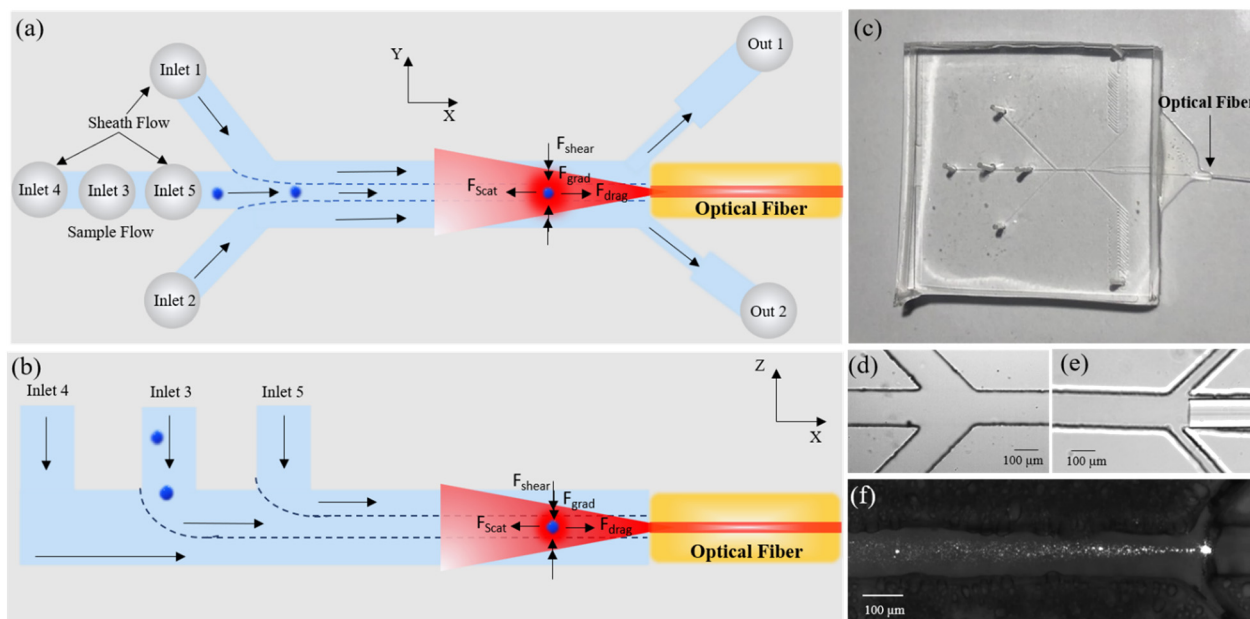


Fig. 1 Opto-hydrodynamic tweezers. (a) and (b) Schematic illustrations of the top view and side view of OHT, respectively, along with the major various forces acting on the particle flowing in the microfluidic channel. (c) Image of the fabricated microfluidic chip integrated with a single-mode optical fiber to build the OHT device. (d) Microscope image of the inlet section of the OHT. (e) Microscope image of the outlet section of the OHT. (f) Spatial profile (XY) of the laser beam from the optical fiber within the microfluidic channel, visualized through laser scattering by the $500\ \text{nm}$ polystyrene particles filled in the channel.



total number of particles flowed in the channel). Moreover, OHT offers long-range manipulation of particles along the length of the channel by varying either the optical power or flow rates. This is in direct contrast to dual-fiber-based trapping approaches, where the fiber-particle alignment is static, prone to misalignment, and has a small particle manipulation range. OHT also offers several additional benefits over conventional optical fiber tweezers: the use of a single optical fiber as compared to two used in dual-beam fiber tweezers minimizes the overall optical radiation intensity on the particle, hence limiting damage to the trapped particle.

The unique design of OHT, which places the fiber directly in the flow channel, eliminates material interfaces between the fiber and the particle, which are common in dual-beam fiber tweezers. This prevents unwanted scattering of the output laser beam, which can degrade trapping performance owing to changes in the laser beam profile or a drop in absolute trapping power.

OHT can be empowered further by incorporating more fiber sources and detectors along the length of the channel to integrate optical investigation schemes such as Raman spectroscopy, fluorescence imaging, *etc.* With a facile design and easy alignment process, OHT offers a portable, robust, and cost-effective lab-on-chip platform for particle trapping and manipulation (Table 1).

Experimental

Design and fabrication of microfluidic device

A polydimethylsiloxane (PDMS)-based microfluidic device (Fig. 1c) was fabricated using soft lithography according to standard procedure.³³ Briefly, photomasks were designed in AutoCAD (AutoCAD 2020, Version 1.4) and printed at 3200 dpi to a flexible plastic film. SU-8 2100 negative photoresist (Kayaku Advanced Materials, USA) was used to fabricate the channel mould on a 4 inch silicon wafer using a standard UV lithography process. To achieve a channel thickness of 125 μm , similar to the cladding diameter of the optical fiber, the

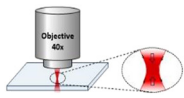
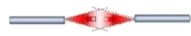

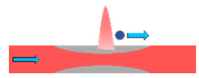

resist was spin-coated at a speed specified by the manufacturer. The master mould was obtained after UV exposure over the photomask and subsequent development. PDMS (Sylgard 184, Dow Corning, USA) was poured onto the master mould after mixing it in a 10:1 ratio with the curing agent. After removing the bubbles and curing for 2 hours at 75 $^{\circ}\text{C}$, the solidified clear PDMS was peeled off from the master mould and a 0.5 mm biopsy puncher (inner diameter: 0.5 mm, Electron Microscopy Sciences, USA) was used to punch inlet/outlet ports. In the next step, the PDMS block was bonded to a cover glass (48 mm \times 60 mm, No. 1 thickness, Brain Research Lab, USA) after plasma treatment for 60 seconds (Harrick plasma, PDC-002-CE, USA). After bonding, a single-mode optical fiber (Thorlabs, USA; NA: 0.1, core diameter: 6.2 μm , cladding: 125 μm) was inserted by slipping it from the side through an open end into the dedicated channel (as shown in Fig. 1e) and glued with the help of a UV-curable, epoxy-based resin (Drei Bond 6020, Germany).

Opto-hydrodynamic tweezers set-up and working principle

Experimental set-up. Our proposed OHT device consists of a microfluidic chip and optical fiber as its main components (see Fig. 1c and ESI,† S1). A fiber-coupled diode laser (3S Photonics, France) operating at the wavelength of 973 nm with a single-mode fiber output (NA: 0.1, core diameter: 6.2 μm , cladding: 125 μm) was chosen as the optical source. The laser wavelength of 973 nm was selected due to its low absorption by water and minimum damage to biological specimens.³⁴ However, laser wavelengths in the visible region can also be used for OHT, as long as they do not induce strong heating effects and are compatible with the trapping specimen.

After bonding the PDMS mould to glass, an end of the optical fiber was stripped, cleaved and inserted from the side into the dedicated fiber-guide channel as shown in Fig. 1e and S1b.† The fiber is inserted flat up until the main channel of the device without blocking the adjacent outlets and the

Table 1 Comparison of the features of OHT with some typical optical trapping approaches

	Objective-based optical tweezers	Dual-beam fiber tweezers	Single-beam fiber tweezers	Evanescent wave trapping	Opto-hydrodynamic tweezers
					
Trapping force (dominant)	Optical gradient	Optical gradient and scattering	Optical gradient	Optical near-field gradient	Optical scattering and hydrodynamic drag
Direction of flow (with respect to trapping laser direction)	Orthogonal	Orthogonal	Orthogonal	Orthogonal	Parallel
Trapping particle size	0.2 nm–5 μm	50 nm–100 μm	100 nm–15 μm	10 nm–5 μm	3–50 μm
Numerical aperture	1.2–1.4	0.1–0.2	0.1–0.2	0.17–0.19	0.12
Operational flow velocities	Up to 1400 $\mu\text{m s}^{-1}$	Up to 100 $\mu\text{m s}^{-1}$	Up to 100 $\mu\text{m s}^{-1}$	NA	190–4500 $\mu\text{m s}^{-1}$
References	23	14, 24, 25	16, 18, 26–29	30–32	Present work



face of the fiber must be cleaved to obtain a flat uniform cut. A drop of UV epoxy (Drei Bond 6020, viscosity 2200–2900 cP @ 25 °C) was used to fix the position of the optical fiber and simultaneously block the channel to avoid leakage. The glue flows into the channel *via* capillary action and the process is monitored under a microscope. When the glue covers most of the fiber uniformly and is just a few microns away from the main channel, it is cured with the help of a spot cure UV gun for 30 s. The fiber insertion process might result in an offset of the core position, especially during insertion and gluing. We note, however, that utilizing all 5 inlets enables precise control of beads/cell positioning along three axes and allows one to offset any error in the position of the fiber ($\pm 10 \mu\text{m}$ deviation) during insertion or fixation into the waveguide. For more details on the process please see the ESI† (S8). Sample and sheath liquid solutions were injected from 1 mL glass syringes (Hamilton, USA) *via* PTFE tubes (0.46 mm inner diameter, Adtech, UK) individually into each of the 5 inlet ports of the microfluidic device to perform 3D hydrodynamic flow focusing. The flow was controlled by high-precision, low-pressure syringe pumps (NemesYS, Cetoni, Germany). The microfluidic chip was placed on the stage of an inverted microscope (Nikon Ti2 Eclipse) and imaged using a 10 \times microscope objective (Nikon, Plan Fluor 10 \times NA 0.3, WD 16 mm) connected to a CMOS detector (Andor Zyla, UK). A short pass filter (Thorlabs, FES0750, cut-off wavelength 750 nm) was inserted between the objective lens and CMOS camera to block the scattered laser beam from the trapped particle.

Sample preparation. To demonstrate the trapping, and manipulation of particles by the OHT, polystyrene particles with average diameters of $\sim 15.0 \mu\text{m}$ and $\sim 5.0 \mu\text{m}$ and human white blood cells (THP-1 monocytes) were used. The cells (the biological samples used in our experiments were obtained from the Instytut Hematologii i Transfuzjologii (Institute of Hematology and Transfusion Medicine); address: ul. Indyry Gandhi 14, 02-776 Warsaw, Poland) were cultured in RPMI-1640 medium supplemented with 2-mercaptoethanol (0.05 mM) and fetal bovine serum (FBS). For sheath flows filtered phosphate-buffered saline (PBS) solution was used. A high-concentration suspension of 500 nm polystyrene particles (0.0001% w/v) diluted in distilled water was flowed in the sample channel to visualize the spatial profile of the laser beam output from the optical fiber. The scattering of light by a large number of particles present in the channel allowed clear visualization of the beam profile (see Fig. 1f).

Working principle. Trapping of particles in an OHT is primarily based on the equilibrium between the optical forces, hydrodynamic drag and shear lift forces acting on the particles flowing in the microfluidic channel as shown in Fig. 1a. A perfect balance between the opposing scattering and drag forces results in the trapping of particles along the longitudinal axis, *i.e.* in the *X*-direction along the length of the channel. In the transverse *Y*- and *Z*-direction *i.e.* along the width and height of the channel, the particle is trapped due to the optical gradient force and the net-zero shear

gradient and wall-induced lift forces acting perpendicular to the flow direction.³⁵ The net lift forces acting on the particle are zero as they are equal and opposite in direction (see Fig. 1a and b); thus, a single particle can be trapped in three dimensions within the microfluidic channel. The key factor that enables the trapping of a particle in an OHT is the alignment of the particle's trajectory with the optical axis of the fiber, placed opposite the flow direction. As a result of this alignment, the particle experiences a strong optical scattering force (maximum at the beam axis due to its Gaussian intensity profile) in a direction exactly opposite to the drag force. By controlling the magnitude of the scattering and drag force *via* regulation of the optical power and flow rate, respectively, a particle can be trapped at an arbitrary location in the channel along the optical axis, where the two forces balance each other. To achieve good alignment of the trajectory of particles with the optical axis of the fiber, 3D hydrodynamic flow focusing was used in a four-way sheath around the sample flow arrangement as demonstrated previously³⁶ (see ESI† Video S1). The 3D flow focusing technique takes advantage of laminar flows in microfluidic channels to spatially confine and manipulate the flow of the sample-containing liquid by sheathing it with surrounding flows. The lateral sheath flows from inlets 1 and 2 were used to focus the sample flow in the horizontal direction, as shown in Fig. 1a (*Y*-axis, along the width of the channel).

Similarly, the top and bottom sheath flows from inlets 4 and 5 were employed to compress the sample flow in the vertical direction (*Z*-axis, along the height of the channel). The flow rates of the sheathing liquids (*via* inlets 1, 2, 4, 5) can be independently controlled to change the flow trajectories of particles within the microfluidic channel and dynamically align them with the optical axis of the fiber by varying the ratio of sheath flow rates, thus enabling the trapping of particles with high efficiency and throughput.

Force analysis. Forces acting on a trapped particle or cell in OHT include the optical (gradient and scattering), hydrodynamic drag, shear gradient, wall-lift, gravitational and buoyant forces. For particles much larger than the wavelength of light with a refractive index larger than the surrounding medium, the optical scattering and gradient forces within the channel can be calculated using:

$$F_{\text{scat,grad}}(x, y) = \frac{n_m Q_{\text{scat,grad}} P}{2c}$$

where n_m is the refractive index of the medium, c is the speed of light, Q_{scat} and Q_{grad} are the dimensionless coefficients of the scattering and gradient force similar to that found in Ashkin's work³⁷ and P is the incident optical power on the particle (for a more detailed description, see ESI† S2). Fig. 2a shows the spatial distribution of the optical scattering force that would be exerted on a $15 \mu\text{m}$ polystyrene particle flowing in the microfluidic channel, by the laser output from the optical fiber ($\lambda_{\text{laser}} = 973 \text{ nm}$; $P = 550 \text{ mW}$, MFD = $6.6 \mu\text{m}$) (ESI† Fig. S2). For locations less than $\sim 100 \mu\text{m}$ from the



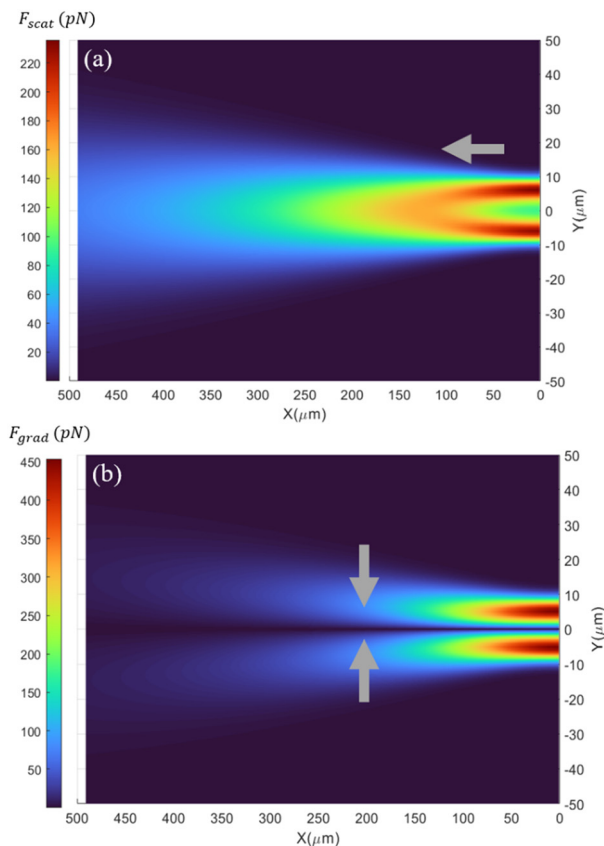


Fig. 2 Spatial distribution of (a) the optical scattering force and (b) the gradient force exerted by the laser beam from an optical fiber on a 15 μm polystyrene particle flowing in the microfluidic channel. The centre of the core of the fiber (core diameter: 6.4 μm , $\lambda_{\text{laser}} = 973 \text{ nm}$, $P = 550 \text{ mW}$) is placed at the origin facing towards the positive X -axis. The magnitudes of the forces are represented in absolute values and the directions of the forces are illustrated as arrows.

optical fiber's tip, the beam diameter is smaller than the size of the particle (15 μm), due to which the scattering force is maximum at transverse positions comparable to the radius of the particle from the beam axis. This is because of the larger overlap between the diverging beam and the particle, resulting in strong momentum transfer and hence a large optical scattering force. However, at a distance beyond 100 μm from the tip of the fiber, the diameter of the beam is larger than the size of the particles and therefore the scattering force is maximum at the laser beam axis and decreases as one moves away from it in the direction perpendicular to the optical axis. This is due to the Gaussian intensity distribution of the laser beam output from the fiber. Along the beam axis ($Y = 0$), the scattering forces decrease as one moves away from the optical fiber. This is due to the divergence of the laser beam that results in radially weakening intensity and consequently lower scattering forces.

In addition to the scattering force, the optical gradient force also acts on particles flowing in the channel. The gradient forces pull the particle towards the region of maximum intensity (*i.e.* towards the laser beam's optical axis) and are

calculated using eqn (1) (see ESI† S2). The optical gradient forces are zero in the transverse direction for particles perfectly aligned with the laser beam axis. With increasing displacement from the beam axis, the gradient forces initially increase and then decrease, reaching a maximum at displacements nearly equal to the radius of the particle. The optical gradient forces contribute to the particle trapping in the transverse direction, *i.e.* perpendicular to the laser beam's axis. Particles that flow slightly off-track from the beam axis can get pulled into the beam and ultimately get trapped by OHT. Once aligned, gradient force confines the particle in the transverse plane. However, along the axial direction, the gradient force acting on the particle is smaller compared to the scattering force due to the low numerical aperture of the optical fiber ($\text{NA} \sim 0.1$) and therefore does not play a major role in the trapping process.

The trapping location depends on the magnitude of the hydrodynamic drag force acting on the particle, which is calculated using Stokes' law. At low Reynolds numbers, (negligible) inertial forces in homogenous viscous media and for a rigid non-rotating spherical particle Stokes drag is given by:

$$F_{\text{drag}} = 6\pi\eta av$$

where η is the dynamic viscosity of the fluid medium, v is the flow velocity relative to the particle and a is the radius of the particle.

Particles can be trapped at different positions along the laser beam axis depending on the flow velocity in the channel, where the scattering force equals the drag force. According to the scattering map shown in Fig. 2a, if a 15 μm polystyrene particle moving in the channel at a velocity of 1000 $\mu\text{m s}^{-1}$ with its trajectory exactly aligned with the optical axis of the optical fiber and the fiber emits a Gaussian laser beam at an output power of 550 mW, then the particle would be trapped 123 μm from the fiber's tip, where the scattering force is equal to the anticipated drag force (125 pN).

Fig. 2a also highlights the importance of the alignment of the trajectory of particles with the optical axis of the fiber for enabling the trapping process. As the particle trajectory deviates from the laser beam axis, it experiences weaker or almost negligible optical scattering force, depending on the extent of the deviation. For example, a 15 μm polystyrene particle at the distance of 100 μm from the fiber's tip experiences 55% and 99% lower scattering force for a deviation of 10 and 20 μm , respectively, from the beam's axis (Fig. 2a). Consequently, a particle flowing at a speed of 1000 $\mu\text{m s}^{-1}$ would not be trapped if its trajectory deviates by more than 5 μm from the beam axis as opposed to when perfectly aligned with the beam axis.

The necessity for exact alignment of particle trajectories with the beam axis is relaxed to some extent by the strong optical gradient forces acting on the particle near the beam axis. For example, a 15 μm polystyrene particle travelling at a speed of 1000 $\mu\text{m s}^{-1}$ in the channel experiences larger gradient forces than the drag force at distances less than 130 μm from the fiber (Fig. 2b). Particles whose paths deviate by



less than $9\ \mu\text{m}$ from the optical axis will be pulled to the centre of the beam, where they spontaneously align with the beam and get trapped.

In addition to the optical gradient forces, in the transverse directions, the particle also experiences shear gradient- and wall-lift forces, but the forces are almost three orders of magnitude smaller than the optical forces for particles flowing at the centre of the channel. While the shear gradient lift force tries to move the particles toward the walls of the channel, the wall-induced lift force acts oppositely and moves the particles away from the wall.³⁸ For our channel geometry ($125\ \mu\text{m} \times 125\ \mu\text{m}$) and the trapping position at the centre of the channel, both the shear stress and the net lift forces acting on the particle are negligible compared to the optical gradient forces. The density of the particle and the surrounding liquid is nearly equal; thus gravitational and buoyancy forces can be neglected (see ESI† S3).

Results and discussion

3D hydrodynamic flow focusing and trapping of microparticles

Trapping of particles in OHT is initiated by aligning the trajectories of particles flowing in the channel with the optical axis of the fiber. First, the sample solution of 0.02% (w/v) of polystyrene particles (diameter: $15\ \mu\text{m}$) was flowed from inlet 3, without the sheath flows. During this time, the polystyrene particles flowed across the whole cross section of the channel, resulting in poor trapping efficiency of 5% as shown in Fig. 3 (we define trapping efficiency as the percentage of particles trapped by the OHT with respect to the total number of particles flowed through the entire cross section of the channel at the trapping location). The poor efficiency, in this case, is because particles flow arbitrarily across the channel cross section and only a few particles which are aligned with the optical axis of the fiber are trapped. In the next step the trajectories of particles

were spatially confined in the *Y*-direction, *i.e.* along the width of the channel, by slowly increasing the side sheath flow rates (inlets 1 and 2). The sheath-to-sample flow rates were adjusted to a ratio of 5 : 1, for which the trajectories of particles coincided with the optical axis of the fiber in the *Y*-direction. This is referred to as 2D focusing. We now observed a trapping efficiency of 35% as almost all the particles were aligned with the core of the fiber in the *Y*-direction, but only a fraction of them were at the correct position along the *Z*-direction, *i.e.*, along the height of the channel. To further increase the trapping efficiency, both the top and bottom sheath flows (inlets 4 and 5) were steadily increased such that the particles were also confined in the *Z*-direction and aligned completely with the fiber axis, resulting in continuous trapping of particles with an efficiency of $>70\%$ (see ESI† Video S2). A detailed description of the process of alignment of the trajectory of particles with the optical axis of the fiber is given in ESI† S4. To achieve 100% trapping efficiency, all the particles flowing in the channel need to be aligned with the optical axis with high precision. This requires extremely high sheath flow rates, which results in strong drag forces that cannot be balanced by the optical scattering forces in our system. In addition to enabling robust and highly efficient particle trapping, 3D flow focusing in OHT also provides the flexibility to correct for positional inaccuracy in fiber placement within the channel by altering the ratio of sheath flow rates to help particles align with the optical fiber's axis.

Depending on the applications, particles either can be trapped and released continuously to collect information about the specimen in a high-throughput manner or a single particle can be analysed for a long duration by stopping the sample flow (inlet 3) while maintaining all the sheath flows. We note that the concentration of the particles can be adjusted to maintain a specific average frequency of incoming particles in the trap such that the particle can be released after collecting the required information before the arrival of another. In our case for a particle concentration of 0.02% (w/v) flowing at a speed of $1000\ \mu\text{m}\ \text{s}^{-1}$, we obtained a high trapping efficiency of 14 particles per min. We also observed the trapping of multiple particles simultaneously in the OHT, interestingly in a chain format (see ESI† Video S3). At a laser power of 860 mW, the OHT were capable of trapping up to 12 beads. Beyond 12 beads, the optical scattering and gradient forces acting on the incoming particles become weak and no further trapping of beads was observed. The length of the chain of trapped particles is dependent on the optical power and flow velocity in the channel. Trapping of particles in the form of linear chains might be advantageous for cell–cell interaction studies.^{39,40}

Manipulation of trapped microparticles in OHT

A particle is trapped once it is at the location of the microchannel where the optical and hydrodynamic forces acting on it are equal in magnitude (and opposite in direction). The trap is located along the optical axis of the fiber (along the *x*-axis), but its exact position depends on the

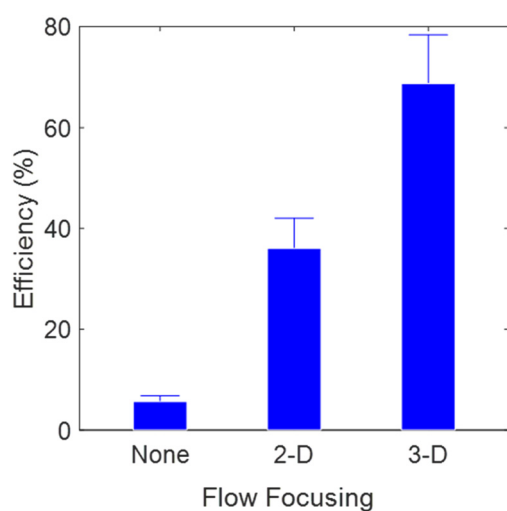


Fig. 3 Comparison of trapping efficiencies with and without 3D flow focusing.



laser's power and the flow velocity in the channel. Fig. 4a shows the optical image of a single 15 μm polystyrene bead trapped at a distance of 150 μm from the tip of the fiber by OHT (see ESI† Video S4). The particle flowed at an average velocity of $\sim 1400 \mu\text{m s}^{-1}$ inside the microfluidic channel. Fig. 4b shows the optical scattering and drag forces acting on the bead, flowing along the optical axis of the fiber in the microfluidic channel. The scattering force is maximum at a distance of $\sim 100 \mu\text{m}$ from the tip of the fiber ($X = 0$) and decreases as one moves away from it due to lower laser intensities. Since the flow velocity is almost constant along the channel, the hydrodynamic drag force acting on the particle remains constant. For an output laser power of 860 mW, the magnitude of the optical scattering forces equals the drag force at the furthest distance of 134 μm from the fiber tip, which is the position where we expected the particle to be trapped as shown in Fig. 4b. The theoretically estimated trap position is comparable to that observed experimentally, $\sim 150 \mu\text{m}$ from the fiber tip as shown in Fig. 4a. In the lateral direction, *i.e.*, the Y - and Z -directions, the particle is confined due to the optical gradient force and equal and opposing shear lift force.

We also experimentally observed the role of optical gradient forces in the auto-alignment of particles flowing off the optical axis in OHT and thus aiding the trapping process. In our experiments, we observed that particles flowing at a velocity of $800 \mu\text{m s}^{-1}$ that deviated slightly ($\sim 10 \mu\text{m}$ from

the beam axis) from the main trajectory at the center of the channel were seen to be pulled to the beam axis at a distance of approximately 143 μm from the tip of the optical fiber (at an applied laser power of 850 mW). This is because the optical gradient forces dominated the drag forces, resulting in the pulling of particles towards the beam axis. This led to “auto-alignment” of the particles with the beam axis and ultimately trapping of these particles (see ESI† Video S5). For particles whose trajectories deviated from the beam axis by more than 20 μm or flowed at higher flow velocities ($>4000 \mu\text{m s}^{-1}$), the gradient forces were not sufficient to overcome the drag forces. As a result, no particles were pulled towards the beam axis and no trapping was observed. Trapping of particles using OHT is robust and stable.

To assess the trapping stability, we measured the trap stiffness of the trapped particle. The variance in position fluctuations was used to calculate the trap stiffness based on the equipartition method.⁴¹ The trap stiffness in the X - and Y -directions is given by

$$k_{x,y} = \frac{K_B T}{\langle x, y^2 \rangle},$$

where $k_{x,y}$ is the trap stiffness in the X and Y directions, K_B is the Boltzmann constant ($\approx 1.38 \times 10^{-23} \text{ N m K}^{-1}$), and $\langle x, y^2 \rangle$ is the variance in the position of the trapped particle. Fig. 4(c) and (d) show the histogram of the positional fluctuations of the trapped particle about the mean trapped position. The trapped particle showed a stiffness of 0.1 $\text{pN } \mu\text{m}^{-1}$ and 342 $\text{pN } \mu\text{m}^{-1}$ in the X - and Y -direction, respectively. Because of the symmetrical laser beam and flow profile in the channel cross section, *i.e.*, the YZ plane, trapping stability in the Z -direction is similar to that in the Y -direction. The trap stiffness was found to be 1000 times lower in the flow direction compared to the orthogonal. The low value of trap stiffness in the flow direction arises due to the high variance in the mean trap position. This is a result of the flow fluctuations in the microfluidic channel (due to use of mechanical pumps) that adds a fluctuating drag force on the particle in addition to the thermal fluctuations.

Trapping versatility

OHTs show high versatility in trapping particles of different sizes, shapes, and material compositions. As long as sufficient scattering forces larger than the hydrodynamic drag force can be exerted on particles, it is possible to trap particles with OHT. As a demonstration, we show the trapping of polystyrene particles of diameters 5 μm and 15 μm as shown in Fig. 5a and b, respectively. Single mammalian cells like leukaemia cells (THP-1; received from the Institute of Hematology and Transfusion Medicine, Warsaw, Poland) of size ranging from 10 to 30 μm (Fig. 5d) as well as microorganisms such as yeast (3–5 μm) were also trapped to demonstrate trapping of particles with lower refractive index, almost identical to that of the medium (see ESI† Video S6). However, smaller-sized particles, such as polystyrene beads smaller than

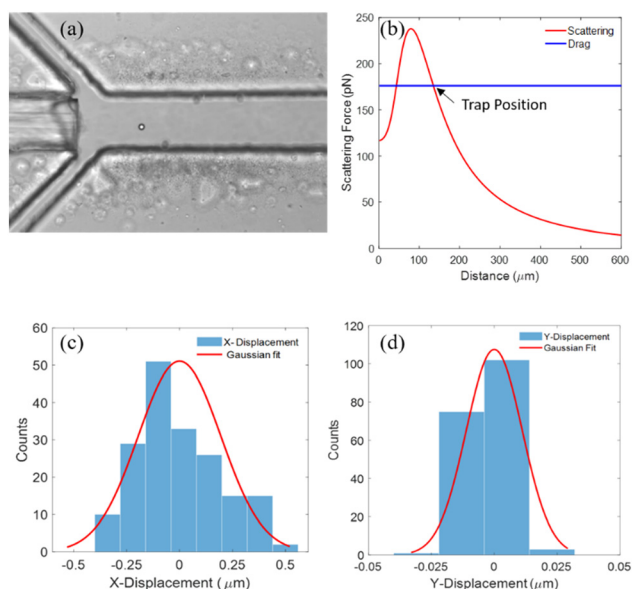


Fig. 4 (a) Optical image of a single 15 μm polystyrene particle trapped in the microfluidic channel using OHT. (b) Theoretically calculated optical scattering force and drag force acting on a 15 μm polystyrene particle as a function of the particle's position along the length of the channel. The fiber tip is positioned at $X = 0$. The flow velocity used to calculate the drag force on the particle within the channel was extracted from the time trajectory of the trapped particle once it was released from the trap (see ESI† S6). (c) and (d) Histogram of the positional fluctuations of the trapped particle (15 μm PS) in the X - and Y -direction, respectively.



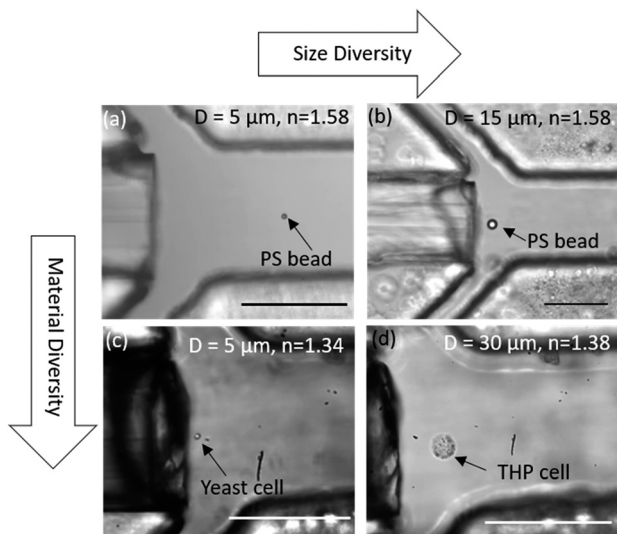


Fig. 5 Trapping versatility of OHT. Optical image of a single (a) 5 μm polystyrene particle, (b) 15 μm polystyrene particle, (c) 5 μm yeast cell, and (d) 30 μm THP cell trapped in the OHT.

1 μm and bacterial *E. coli* cells (1–2 μm), could not be stably trapped in OHT due to relatively small optical scattering and gradient forces acting on them compared to the drag force, even when operating OHT at the minimum flow velocity. Our demonstrations clearly show the wide applicability of OHT including for single-cell studies in a fully lab-on-chip format.

Long-range manipulation of particles in OHT

The position of a trapped particle in the OHT is dependent on both the magnitude of the optical scattering force and the drag force acting on it. One can control either the flow velocity or the output optical power from the fiber to trap particles at the desired locations and also manipulate them over long distances along the length of the channel. The ability to precisely position and manipulate particles by simply regulating the optical power or flow rates makes the OHT particularly attractive over conventional fiber-tweezer approaches with limited manipulation capability. The functionality of OHT can be expanded through precise and well-controlled single-particle manipulation. For instance, by integrating multiple fiber sources and detectors along the length of the channel and moving the trapped particle into different detection zones within the channel, multimodal analysis of trapped particles based on optical scattering, fluorescence, or Raman spectroscopy can be performed within a single platform.

Fig. 6a shows the heat map distribution of the trapping positions of 15 μm polystyrene particles with respect to the tip of the optical fiber for different optical power and flow rate combinations in OHT. For fiber output powers and flow velocities, where the drag forces dominate over the optical scattering force, no particle can be trapped as indicated by the non-trapping zone. For other combinations of fiber power and flow velocities, there always exists a position within the

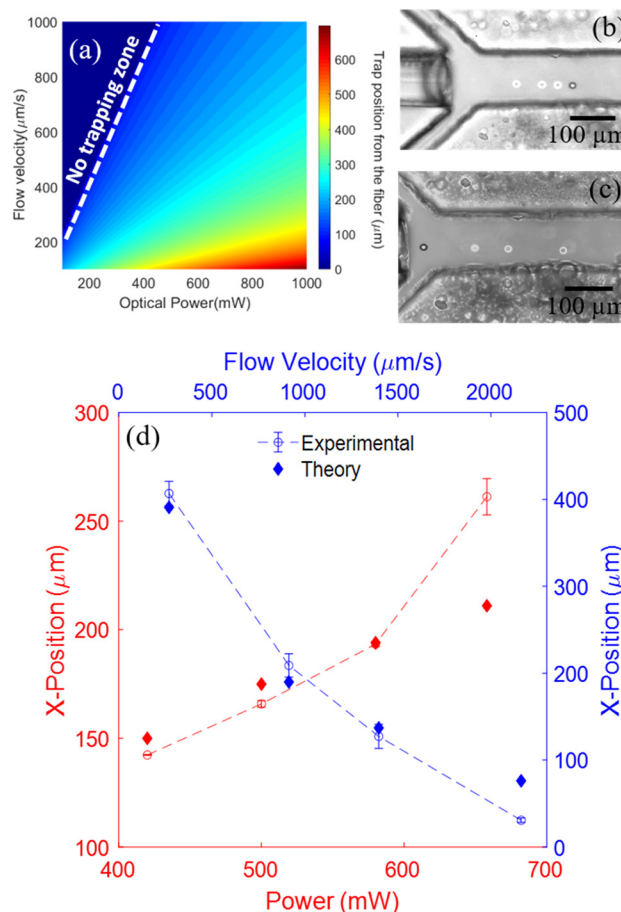


Fig. 6 (a) Distribution of the trap positions of a 15 μm polystyrene particle in OHT at different optical powers and flow velocities in the channel. The region to the left of the dashed line corresponds to the no-trapping zone where no particle can be trapped by OHT for the given power and flow velocity combinations. (b) and (c) depict images obtained from a video sequence by (b) increasing the optical power while keeping the flow velocity constant at 600 $\mu\text{m s}^{-1}$ and (c) by increasing the flow velocity while operating at a fixed input laser power of 860 mW. These images are created by superimposing the frame featuring the trapped bead in its final position with three subtracted frames (the frame containing the bead at a specific location minus the background frame with no bead). Consequently, the circles in the final image indicate only the bead's position and not its actual appearance. The bead images in the first three distinct locations closely resemble the bead image in the final position, with no variation in the Z-location. (d) Position of the trapped particle from the tip of the optical fiber at different laser powers (constant flow velocity) and flow velocities (constant fiber output power) in the channel.

channel along the beam axis where the two opposing forces balance each other, resulting in the trapping of particles at those specific locations.

As a demonstration, we trapped and manipulated a single polystyrene particle of diameter 15 μm in the channel by modulating the output optical power and flow velocity. The range and precision of particle manipulation by OHT were subsequently evaluated. First, we trapped a single polystyrene particle flowing at a velocity of 600 $\mu\text{m s}^{-1}$. Subsequently, by varying the fiber laser's optical power from 420 mW to 660 mW



in steps of ~ 80 mW, the particle was moved along the length of the channel from ~ 140 to $260 \mu\text{m}$ from the tip of the fiber as shown in Fig. 6b. As we increase the laser power, the optical scattering forces acting on the particle are increased, shifting the balance position of the two forces, *i.e.* the trapping location further away from the fiber tip. The trapping positions observed in the experiments were found to be close to the expected trap locations calculated theoretically (Fig. 6d). It should be noted that the laser power can be increased beyond the maximum power used in our demonstrations to further increase the range of manipulation. The maximal power is limited to values beyond which the localized heating of the surrounding medium causes bubble formation or damage to the trapped particle. The lowest power is set to the minimum value at which the scattering forces are just enough to overcome the drag forces in OHT. To test the precision of particle manipulation by OHT *via* optical power modulation a single trapped particle was moved multiple times between two positions in the channel by switching between two optical powers (P1: 182 mW; P2: 500 mW). The position of the bead (centroid) was measured for each iteration to determine the precision of particle manipulation using OHT (see ESI† S7). OHTs were able to manipulate particles with a positional precision of less than $\pm 10 \mu\text{m}$ by varying the output optical power.

Another parameter that can be exploited to manipulate particles in the OHT is the flow velocity in the channel. By varying the flow velocity in the microfluidic channel, the drag force acting on the particle can be modulated due to which the position at which two forces balance each other, *i.e.* the trap location, can be shifted, resulting in the manipulation of the trapped particle. We trapped a $15 \mu\text{m}$ polystyrene particle and then moved it along the length of the channel by slowly increasing the flow velocity as shown in Fig. 6c. Once the particle was trapped, only the side sheath flow rates (inlets 1 and 2) were changed proportionally to increase the average flow velocity in the channel, while flow rates *via* other inlets were maintained at a minimum value (the lowest pulsation-free flow rate supported by the syringe pump for a $1000 \mu\text{L}$ glass syringe was $2 \mu\text{L h}^{-1}$). The optical output power from the fiber was kept constant at 860 mW. This way we were able to manipulate particles by the OHT over a long range of $370 \mu\text{m}$ ranging from 30 to $407 \mu\text{m}$ from the tip of the fiber by modulating the average flow velocity in the channel (270 – $2100 \mu\text{m s}^{-1}$) as shown in Fig. 6d. The higher the flow velocity in the channel, the closer the particles are trapped to the fiber's tip, where large optical scattering forces compensate for the particle's high drag force. To trap or move particles

away from the fiber, the overall flow velocity in the channel can be reduced by decreasing sheath flow rates proportionally. The minimum operational flow velocities required in the OHT are those at which inertial forces (drag and lift) are sufficient to overcome diffusion and gravitational forces. At these flow velocities, the particle can be trapped furthest from the optical fiber for a given power without leaving the trap. The maximum drag force that can be balanced by the optical scattering force at the given output optical power determines the flow velocity's upper limit. The precision of particle manipulation by OHT *via* regulation of flow velocity in the channel was measured by moving a single trapped particle multiple times between two positions in the channel by switching between two flow velocities. The position of the bead (centroid) was measured for each iteration to determine the precision of particle manipulation. OHTs were able to manipulate particles with a positional precision of $\pm 10 \mu\text{m}$ by varying the average flow velocity in the microfluidic channel. We note that the precision of particle manipulation by modulation of flow velocities is susceptible to flow fluctuations caused by mechanical syringe pumps, particularly when operating at low flow rates.

The maximum range of particle manipulation in OHT for a $15 \mu\text{m}$ polystyrene particle was $\sim 500 \mu\text{m}$, which was achieved by operating it at a maximum laser power of 880 mW and the lowest average flow velocity of $190 \mu\text{m s}^{-1}$. The maximum fiber power was limited to the magnitude beyond which there was bubble formation due to the heating of the surrounding medium. The flow velocity, on the other hand, was kept to the minimum below which syringe pump induced flow fluctuation becomes significant and the particle moves out of the trap. In summary, OHT allow long-range manipulation of the trapped particle along the length of the channel by regulating either the optical power or flow velocity, thus offering superior manipulation capabilities over conventional fiber tweezers which have limited manipulation range or require physical movement of the optical fiber (Table 2).

Conclusions

We demonstrated novel opto-hydrodynamic tweezers (OHT) for trapping and manipulating single particles and cells of varying sizes, shapes, and compositions. OHT combines 3D flow focusing and optical forces *via* fiber optics in microfluidic channels, where flow focusing allows for simple and dynamic alignment of particle trajectories with the fiber

Table 2 Summary of the trap translation range and precision of particle manipulation in an opto-hydrodynamic trap by varying the fiber laser power and flow velocity. Trap translation range values refer to the positions a trapped particle can be translated along the length of the channel by varying either the input optical power or the overall fluid flow velocity

Manipulation approach	Trap translation range (μm)	Precision (μm)
Fiber optical power (flow velocity = $600 \mu\text{m s}^{-1}$)	140–260	± 10
Flow velocity (optical power = 860 mW)	30–407	± 10



axis, resulting in efficient and high-throughput particle trapping. By regulating the optical power and flow velocity in the channels individual particles can be trapped at specific spots and manipulated over a wide range, extending up to several hundred microns along the channel length with a precision of $\pm 10 \mu\text{m}$. With a simple design, small form factor, dynamic alignment of a particle with fiber optical axis, versatile manipulation, and the possibility of integrating various optical investigation schemes, this optofluidic tweezers platform offers a multipurpose solution for single-particle analysis—all in a fully lab-on-chip device.

Data availability

Data underlying the results presented in this paper are not publicly available at this time but may be obtained from the authors upon reasonable request.

Author contributions

Abhay Kotnala and Shreyas Vasantham: conceptualization, formal analysis, methodology, validation, writing – original draft. Yurii Promovych: methodology, validation. Piotr Garstecki: funding acquisition, resources, supervision, writing – review & editing. Ladislav Derzsi: funding acquisition, project administration, resources, methodology, supervision, writing – review & editing. All authors have approved the final version of the manuscript.

Conflicts of interest

Patent applications for the demonstrated approaches and designs are pending.

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