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Broader context

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The functionalization of host materials is crucial for high sulfur loading and ultra-long cycling in lithium-sulfur batteries, which demands efficient and persistent electrocatalysis. Stabilizing catalytic sites and tuning electronic structure in host materials is a promising approach to optimize intermediate adsorption and enhance electrocatalytic efficiency. High-entropy oxide ceramics exhibit strong structural stability and tunable electronegativity/crystal field splitting at their sites. In this work, we optimized the Zr-O bond and Zr electronic structure, promoting Li_2S_4 conversion kinetics. These findings provide in-depth insights into the intrinsic correlation between metal electronic structure and catalytic activity, inspiring entropy engineering of ultra-durable electrocatalysts for lithium-sulfur batteries.



ARTICLE

Unconventional Catalytic Kinetics of Dual Field Regulated Pyrochlore-type High-entropy Ceramics towards Li_2S_4 IntermediateLin Zhou,^a Handing Liu,^{*b} Ji-Xuan Liu,^a Xinrui Zhang,^b Yixi Yao,^b Ruirui Wang,^c Ziliang Chen,^{*d} Prashanth W. Menezes^{*e,f}, Guo-Jun Zhang^{*a}Received 00th January 20xx,
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Electrocatalytic performance of high-entropy ceramics has been recognized as a pivotal prerequisite to realizing ultra-durability for lithium-sulfur batteries. However, the dynamics of accurately capturing Li_2S_4 remains poorly understood, thus a comprehensive understanding of the mechanism between dynamic control factors and electrocatalytic performance remains largely unexplored. In this study, we visually present the Li_2S_4 electrocatalytic process and accurately identify that high-entropy engineering of rare earth sites leads to positive modifications in crystal field splitting energy and electronegativity. In conjunction with theoretical analysis, we demonstrate that the adsorption energy of Li_2S_4 is optimized by the electronic structure and covalency under dual-field (electric field and crystal field) regulation, leading to efficient electrocatalytic performance. These findings have enabled us to develop an ultra-durable ceramic electrocatalyst ($\text{La}_{0.15}\text{Nd}_{0.15}\text{Sm}_{0.40}\text{Eu}_{0.15}\text{Gd}_{0.15}\text{Zr}_2\text{O}_7$), as sulfur cathode (HEZO-S) with a lifespan exceeding 10000 hours. This fundamental understanding of the intrinsic relationship provides a feasible high-entropy strategy for the design of advanced catalysts for lithium-sulfur batteries.

Broader context

The functionalization of host materials is crucial for high sulfur loading and ultra-long cycling in lithium-sulfur batteries, which demands efficient and persistent electrocatalysis. Stabilizing catalytic sites and tuning electronic structure in host materials is a promising approach to optimize intermediate adsorption and enhance electrocatalytic efficiency. High-entropy oxide ceramics exhibit strong structural stability and tunable electronegativity/crystal field splitting at their sites. In this work, we optimized the Zr-O bond and Zr electronic structure, promoting Li_2S_4 conversion kinetics. These findings provide in-depth insights into the intrinsic correlation between metal electronic structure and catalytic activity, inspiring entropy engineering of ultra-durable electrocatalysts for lithium-sulfur batteries.

Introduction

Lithium-sulfur (Li-S) batteries have made significant contributions to the advancement of energy storage technologies owing to their high theoretical specific capacity and the involvement of multi-electron electrochemical conversion¹. However, the sulfur cathode redox reaction (SRR) faces major challenges, including the shuttle effect and sluggish kinetics of intermediate lithium polysulfides (LiPSs) during its complex, multi-phase transformation. To address these issues, the development of sulfur host materials with optimized electrocatalytic properties is essential². Transition metal oxides, as electrocatalysts, offer a viable strategy to enhance the stability and rate performance of Li-S batteries³⁻⁵. Notably, the electrocatalytic activity of transition metal oxides is mainly contributed by the d-orbital electrons of metal atoms⁶⁻⁸. Unfortunately, this activity is often compromised due to the high hybridization degree between the 3d orbital of the metal and the 2p orbital of oxygen in the heterogeneous reaction⁹⁻¹¹. Therefore, enhancing the catalytic activity of transition metal oxides is critical, particularly for improving the SRR process in the multi-phase reaction of Li-S batteries.

Previous studies have shown that binary metal-based oxide (ABO_x) could promote the electrocatalytic effect on LiPSs in Li-S batteries by increasing both conductivity and oxygen vacancy (e.g., spinel, perovskite, and mullite phases)¹²⁻²². Nevertheless, these efforts have mainly focused on increasing the number of active sites available for catalysis rather than optimizing the intrinsic adsorption free energy of ABO_x towards LiPSs, leaving ample room for further improvement of the catalytic performance. Inspired by the above

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considerations, several efforts have recently been devoted to altering the electronic structure of transition metal species in ABO_x compounds to regulate the intrinsic catalytic effect^{23–28}. Despite these advances, the dissolution of B-site transition metals in these ABO_x compounds during prolonged cycling leads to the formation of vacancies and detrimental segregation at the A-site, thereby causing instability in the electronic structure. This, in turn, results in a progressive decline in electron mobility and catalytic activity, ultimately capping the potential for enhancements in device performance^{29–31}. Recent investigations have revealed that high-entropy engineering, which involves incorporating multiple metal elements, could potentially be an effective strategy to counteract phase segregation and maintain a stable electronic structure with high catalytic activity^{32–41}. More importantly, the cocktail effect introduced through high entropy engineering endows the material with enhanced and more stable catalytic activity by optimizing the electronic structure. This synergistic effect often allows high-entropy materials to surpass the performance of single-component materials, achieving a "1+1>2" effect³². As a result, they are gradually emerging as highly promising candidates for next-generation high-efficiency electrocatalytic and energy storage systems³⁷. While these findings are promising, to the best of our knowledge, the underlying mechanisms by which high-entropy engineering of the A-site in ABO_x ceramics enhances catalytic activity remain unclear. Another challenge in understanding Li-S battery performance lies in the behavior of the intermediate Li_2S_4 , which is a key species at 25% theoretical capacity and plays a key role in the liquid-to-solid phase transition during the electrochemical process^{19,42}. However, capturing the dynamic behavior of Li_2S_4 remains extremely challenging to date, possibly due to the complexity of the interfacial environment, leaving significant gaps in our understanding of its interactions and the catalytic effects of various materials on it.

Herein, we developed a high-entropy ceramic ($\text{La}_{0.15}\text{Nd}_{0.15}\text{Sm}_{0.40}\text{Eu}_{0.15}\text{Gd}_{0.15}\text{Zr}_2\text{O}_7$ (HEZO), based on $\text{Sm}_2\text{Zr}_2\text{O}_7$ prototype with pyrochlore structure as an electrocatalyst for Li-S batteries by using a simple rapid molten salt method. This material significantly enhances redox kinetics, as evidenced by the reduction in Tafel slope of the reduction peak to 29.83 and 34.36 mV dec^{-1} , and the oxidation peak to 54.7 mV dec^{-1} . Impressively, the HEZO-S electrode maintains operation for a continuous 10000 hours at a current density of 0.5 C. To the best of our knowledge, this represents the highest areal capacity reported for ABO_x -based sulfur cathodes so far and exhibits catalytic activity that surpasses current state-of-the-art metal oxide catalysts. Our detailed analyses using *in-situ* electrochemical confocal Raman spectroscopy (EC-CRS), X-ray absorption spectroscopy (XAS), UV-Vis diffuse reflection spectroscopy, and density functional theory (DFT+U) calculations reveal that although the introduced high-entropy engineering of the A-site lacks direct catalytic activity towards SRR, it plays a pivotal role in modulating the d-orbital electronic structure and covalency through crystal field splitting energy and adjusting the electronegativity. This modulation optimizes the adsorption free energy for LiPSs, culminating in superior SRR performance. Our work not only achieves a significant breakthrough in fine-tuning the electronic structure of ABO_x for ultra-durable performance but also offers deeper insight into the entropy engineering strategy for

developing efficient electrocatalysts tailored for practical Li-S batteries.
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Results and discussion

Key descriptors for electrocatalytic performance of HEZO ceramics host.

It is important to recognize that the adsorption energy of ABO_x ceramics serves a dual role in the SRR conversion process. Therefore, to effectively enhance electrocatalytic performance while ensuring stability, high-entropy engineering provides a synergistic modulation of the electronic structure and bond property by incorporating multiple elements into ABO_x . This approach is envisioned as a viable strategy for achieving optimal performance. We developed a molten salt method for the synthesis of HEZO catalysts. **Fig. 1A** schematically illustrates the synthesis process. Initially, lanthana, neodymia, samaria, europia, gadolinia, and zirconia were mixed in a molar ratio of 3:3:8:3:3:20 in an ethanolic solution. The resulting mixed powders were then transferred to an alumina crucible and heated in a muffle furnace. The temperature gradually increased at a rate of 5 °C per minute to a range of 1200 °C and was maintained for 1 hour. The elevated temperature further enhances metal atom diffusion, which is crucial for obtaining a uniform high-entropy phase.

Adsorption experiments comparing La_2O_3 , Nd_2O_3 , Sm_2O_3 , Eu_2O_3 , Gd_2O_3 , and ZrO_2 reveal that Li_2S_4 preferentially adsorbs on Zr sites (**Fig. S1**), indicating that the catalytic activity of rare-earth sites is significantly lower than that of Zr sites. In the H-type electrochemical cell, the Li_2S_4 adsorption capacity follows the order of $(\text{LaNdSm})_2\text{Zr}_2\text{O}_7 > (\text{SmEuGd})_2\text{Zr}_2\text{O}_7 > \text{HEZO} > \text{Sm}_2\text{Zr}_2\text{O}_7 > \text{ZrO}_2$. Interestingly, the Tafel slope, Li ion diffusion coefficient, symmetrical battery current density, and constant current charge-discharge platform voltage difference, which reflects electrocatalytic activity in the H-type transparent cell, exhibits the reverse trend: $\text{HEZO} > (\text{LaNdSm})_2\text{Zr}_2\text{O}_7 > (\text{SmEuGd})_2\text{Zr}_2\text{O}_7 > \text{Sm}_2\text{Zr}_2\text{O}_7 > \text{ZrO}_2$ (**Figs. S2, 3**). This observation suggests that high-entropy pyrochlore ceramics exhibit a "volcano-shaped" adsorption behavior for Li_2S_4 (**Fig. 1B**).

To decouple the key descriptors of active sites and electrocatalytic performance, high-entropy pyrochlore ceramics were designed by substituting Sm sites with high-entropy elements (La/Nd/Sm/Eu/Gd). First, rare-earth metals with weak crystal field splitting energies (e.g., Eu and Gd) were introduced⁴³. Using the Tauc plot method from UV-Vis diffuse reflectance spectroscopy, it was determined that the bandgap of $(\text{SmEuGd})_2\text{Zr}_2\text{O}_7$ is lower than that of $\text{Sm}_2\text{Zr}_2\text{O}_7$ (5.45 eV) (**Fig. 1C**). This is attributed to the weaker repulsion between the $4f^7$ orbitals of Eu and Gd and the $4d^2$ orbitals of Zr, which allows better orbital overlap between the f and d states (**Fig. 1D**). Consequently, a highly overlapping electronic "reservoir" is formed between the empty upper Hubbard band (UHB) and the occupied lower Hubbard band (LHB) at the Zr-O* antibonding orbitals (**Fig. 1E**). This electronic overlap significantly enhances the probability of rapid charge migration, resulting in a smaller bandgap at the macroscopic



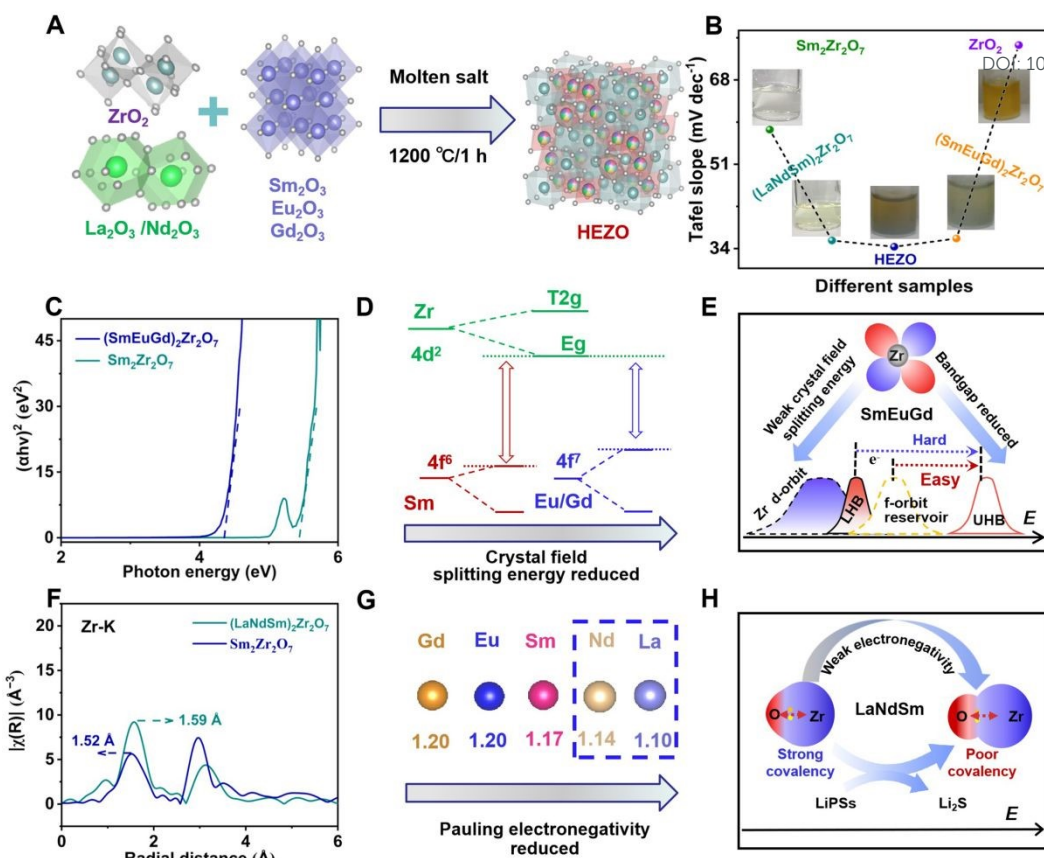


Fig. 1 | Regulation of adsorption of lithium polysulfide by electronegativity and crystal field splitting. **A**, Schematic synthesis procedure of HEZO. **B**, Li_2S_4 permeation measurements in H-shaped glass cells with $\text{Sm}_2\text{Zr}_2\text{O}_7$ (up), HEZO (middle), and ZrO_2 (down) coated PP separator. **C**, Effect of crystal field splitting energy variation on electron structure. **D**, Schematic diagram of the weak crystal field splitting energy on electronic structure. **E**, Tauc plots of the Kubelka–Munk function vs. energy of $(\text{SmEuGd})_2\text{Zr}_2\text{O}_7$ and $\text{Sm}_2\text{Zr}_2\text{O}_7$. **F**, Pauling electronegativity values of high entropy rare earth elements. **G**, Schematic diagram of the effect of electronegativity-regulated covalency of Zr–O on adsorption states. **H**, Modeled FT EXAFS data for mixtures of the HEZO and $\text{Sm}_2\text{Zr}_2\text{O}_7$.

scale. Upon introducing elements with weaker crystal field splitting energies (e.g., La and Nd), extended X-ray absorption fine structure (EXAFS) analysis near the Zr K-edge revealed that the Zr–O bond length in $(\text{LaNdSm})_2\text{Zr}_2\text{O}_7$ extends to 1.59 Å, exceeding the bond length observed in $\text{Sm}_2\text{Zr}_2\text{O}_7$ (Fig. 1F). This elongation is attributed to the lower electronegativity of La and Nd (Fig. 1G), which reduces the ability of Zr^{4+} to withdraw electrons from oxygen, thereby destabilizing the Zr–O covalent bond and enhancing the reactivity of the Zr–O bond (Fig. 1H).

Structural characteristics of HEZO and HEZO-S cathode.

The phase structure of the HEZO oxides was analyzed using X-ray diffraction (XRD). The XRD patterns of individual $\text{La}_2\text{Zr}_2\text{O}_7$ and $\text{Sm}_2\text{Zr}_2\text{O}_7$ phases (Fig. S4) demonstrate that the solid-phase strategy successfully converts metal oxides into pure phase high-entropy oxides. Notably, due to the lattice distortion effects associated with high-entropy engineering, Rietveld refinement analysis of the X-ray diffraction (XRD) peaks of HEZO (Fig. 2A) exhibit a shift to higher angles compared to the single $\text{La}_2\text{Zr}_2\text{O}_7$ phase (PDF#17-0450, space group: $Fd-3m$) where crystal facets (222), (400), (440), and (622) are located at 28.68°, 33.28°, 47.65° and 56.55° respectively. In contrast, the diffraction peaks of HEZO shift to lower angles when compared to the $\text{Sm}_2\text{Zr}_2\text{O}_7$ phase,

indicating lattice expansion. Due to the lattice distortion induced by high-entropy engineering, electron interactions are inevitably triggered among the various elements. To clarify this, X-ray photoelectron spectroscopy (XPS) analysis was conducted on the HEZO composite material, $\text{Sm}_2\text{Zr}_2\text{O}_7$, and ZrO_2 . The Gd 3d, Eu 3d, Sm 3d, Nd 3d, La 3d, and Zr 3d signals, O1s, and other related energy spectral peaks can be clearly observed in the full-spectrum peaks (Fig. S5). As shown in Fig. S6, the Zr 3d3/2 and Zr 3d5/2 peaks in the HEZO composite material appeared at 184.1 and 181.7 eV, respectively. Moreover, compared with ZrO_2 , the peaks of Zr 3d3/2 and Zr 3d5/2 in HEZO and $\text{Sm}_2\text{Zr}_2\text{O}_7$ shifted towards higher energy levels, and the energy of O1s in HEZO and $\text{Sm}_2\text{Zr}_2\text{O}_7$ were also significantly higher than that in ZrO_2 , indicating that the oxygen vacancies in HEZO and $\text{Sm}_2\text{Zr}_2\text{O}_7$ require the high oxidation state of Zr to balance. Further comparison of the high-resolution XPS spectra of $\text{Sm}_2\text{Zr}_2\text{O}_7$, the Zr 3d3/2 and Zr 3d5/2 peaks in the HEZO composite material are slightly shifted towards lower energy. This indicates an increased electron density around Zr following high-entropy engineering. This enhancement enables Zr to accommodate more electrons and greatly increases the probability of rapid conversion of LiPSs at the Zr site. The band gap width of the high-entropy pyrochlore-type HEZO material was further reduced to 4.25 eV.



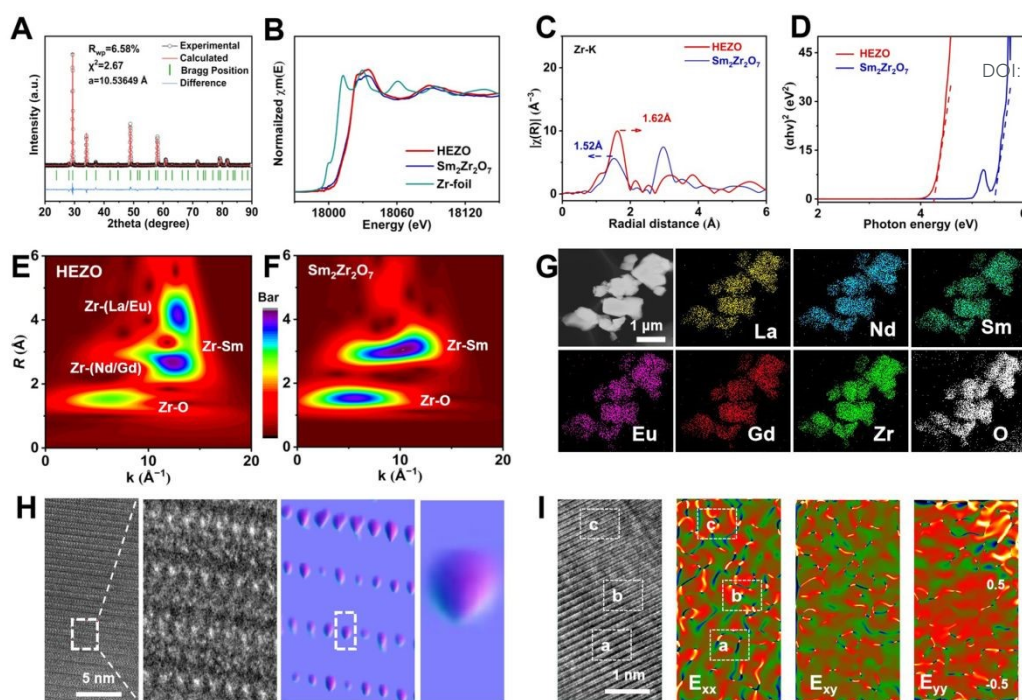


Fig. 2 | Phase, structure and morphology of host materials. **A**, XRD spectrum, and Rietveld refined spectrum of HEZO. **B**, Comparison of XANES spectra of the Zr K-edges of HEZO, $\text{Sm}_2\text{Zr}_2\text{O}_7$, and Zr foil. **C**, Zr K-edge Fourier-transformed EXAFS $k^3\chi(k)$ data of the HEZO. **D**, Tauc plots of the Kubelka–Munk function vs. energy of HEZO and $\text{Sm}_2\text{Zr}_2\text{O}_7$. WT-EXAFS plots of **E**, HEZO, **F** $\text{Sm}_2\text{Zr}_2\text{O}_7$. **G**, High-angle annular dark-field scanning transmission electron microscopy (HAADF-STEM) image of HEZO and EDS elemental mapping of La, Nd, Sm, Eu, Gd, Zr, and O. **H**, Enlarge the 3D AOGF mapping (right) corresponding to HRTEM (left) along the area marked by the white virtual rectangle. **I**, The corresponding dilatation strain maps along ε_{xx} , ε_{yy} and ε_{zz} by TEM using the GPA algorithm for HEZO.

Moreover, X-ray near-edge absorption spectroscopy (XANES) at the Zr K-edge reveals that the oxidation state of Zr in HEZO is nearly identical to the +4 states observed in $\text{Sm}_2\text{Zr}_2\text{O}_7$, which is significantly higher than the Zr foil (**Fig. 2B**). The Zr K-edge XANES results for HEZO, $\text{Sm}_2\text{Zr}_2\text{O}_7$, and ZrO_2 showed that their absorption edge positions are very close, indicating that the Zr oxidation states in these samples are essentially identical (+4). Importantly, the extensive X-ray absorption fine structure (EXAFS) of Zr provides direct evidence of the Zr-O bond length variation (**Fig. 2C**). Compared to $\text{Sm}_2\text{Zr}_2\text{O}_7$, the Zr-O bond length significantly increased to 1.62 Å in the HEZO, indicating weaker hybridization between O 2p and Zr 3d and weaker covalence of the Zr-O bonds. Under the influence of the crystal field splitting energy and electronegativity, the electron migration speed was greatly increased, which is manifested as a small band gap (4.25 eV) in macroscopic properties (**Fig. 2D**). Through wavelet transform (WT) EXAFS analysis, the Zr-O bond lengths in HEZO were found to be slightly longer than those in $\text{Sm}_2\text{Zr}_2\text{O}_7$ (**Figs. 2E, F**). Additionally, analysis reveals two types of rare-earth Zr bonding: one involving rare-earth Zr bonding (Zr-Nd /Gd) at bond lengths from 2 Å to 3 Å, and the other involving type Zr bonding (Zr-La /Eu) at bond lengths greater than 3 Å, suggesting that the surrounding rare-earth elements can significantly influence the electronic structure of Zr.

The HEZO was characterized further by field emission scanning electron microscopy (FESEM) and transmission electron microscopy (TEM). The FESEM images (**Figs. S7A–D**) revealed that the HEZO oxide exhibits a pseudo-spherical shape with particle sizes ranging from 500 nm to 1 μm. The low-magnification TEM images corroborated this morphology,

while the magnified TEM image displayed a large number of lattice fringes within the matrix, with no indication of an amorphous structure. The high-resolution TEM images showed a lattice fringe spacing of 0.605 nm, which is slightly smaller than the theoretical spacing of 0.608 nm for the (111) crystal facet of $\text{La}_2\text{Zr}_2\text{O}_7$ and slightly larger than 0.602 nm spacing observed for the (111) crystal facet of $\text{Sm}_2\text{Zr}_2\text{O}_7$ phase, being consistent with XRD results (**Figs. S7E–F**).

Meanwhile, the high-resolution TEM diffraction pattern showed a series of concentric rings, with reciprocal points distributed and assembled into a reciprocal sphere with a radius of $1/d$, demonstrating characteristics typical of a polycrystalline diffraction pattern. In order to better clarify the distribution of elements and the absence of segregation in the crystal structure of HEZO, the high-angle annular dark-field (HAADF) image and corresponding element mapping were conducted (**Fig. 2G**). The analyses further indicated that the elements La, Nd, Sm, Eu, Gd, Zr, and O were uniformly distributed throughout the particles. Moreover, three-dimensional atomic overlap Gaussian function fitting (3D AOGF) mapping showed only the adjacent upper and lower layers of rare earth metals after subtraction of the Zr atomic layer (**Fig. 2H**). The presence of multiple colors exhibited by the rare earth atoms and the observation of three colors in the layer facing the Zr atoms, provide strong evidence for the bonding characteristics between the rare earth elements and Zr. This finding directly supports the conclusion that only three metal atoms can form direct bonds with the Zr atoms in chaotic systems, which has significant implications for the structure



and properties of high-entropy ceramics. Furthermore, the arrangement of atoms along the (111) crystal plane along HEZO is discontinuous and irregular, indicating that there is no local order at the high entropy sites in the material (**Fig. S7G**). In contrast, the high-resolution aberration-corrected electron microscope images of single-phase $\text{Sm}_2\text{Zr}_2\text{O}_7$ show that atoms of different colors are arranged periodically as indicated within the dashed box, clearly demonstrating the structural order (**Fig. S7H**). To more precisely determine the regions of strain within the crystal, Geometric Phase Analysis (GPA) was employed to compute the strains along the X, Y, and XY directions. This technique begins with the careful selection of two nonlinearly correlated diffraction spots for analysis (**Fig. S7I**). Two-dimensional high-resolution images of positive space were defined and used as a reference to measure the distortion of the high-resolution lattice of the experimental group. Using GPA plug-in software (HREM Research Inc.) in Digital Micrograph software (Gatan), the surface of the HEZO ceramic sample was calculated and analyzed. The offset distance between experimental lattice fringes and theoretical lattice fringes (without strain) is calculated by the Fourier transform of lattice fringes so that more accurate strain information can be obtained. Since tensile strain and compressive strain were paired in the crystal, the inversion points of a large number of light and dark tones in the image correspond to the distribution range of tension-compressive strain within the

nanodomain (**Fig. 2I**). In order to correlate the phenomenon of local strain structure with the defect concentration, three different regions a, b and c were selected to calculate the strain intensity and oxygen vacancy concentration. The results show that the oxygen vacancy defect concentration increases with the increase in strain intensity (**Fig. S8**).

Hosts with different specific surface areas obtained at different milling times have little effect on lithium ion diffusion (**Fig. S9A**). High temperature treatment can produce a rich micropore/mesopore characteristic on the surface, which is conducive to the diffusion and migration of ions in the subsequent electrochemical process. To understand this fact, the Brunauer-Emmett-Teller surface area and pore volume were calculated to be up to $152 \text{ m}^2 \text{ g}^{-1}$ and $2.0 \text{ cm}^3 \text{ g}^{-1}$, respectively (**Fig. S9B**). Such a large surface area and suitable pore distribution enhance the exposure of active sites and accelerate nucleolar migration during electrochemical reactions. Similarly, Thermogravimetric (TG) analysis after sulfur infiltration conducted at a mass ratio of 1:4 and 155°C , showed that the sulfur content in the high-entropy pyrochlore-type oxide reaches 76.6%. This indicates that 95.75% of the elemental sulfur is constrained within the HEZO material (**Fig. S10**).

Electrochemical and electrocatalysis performance of HEZO-S cathode.

Stimulated by the observed electronic and structural

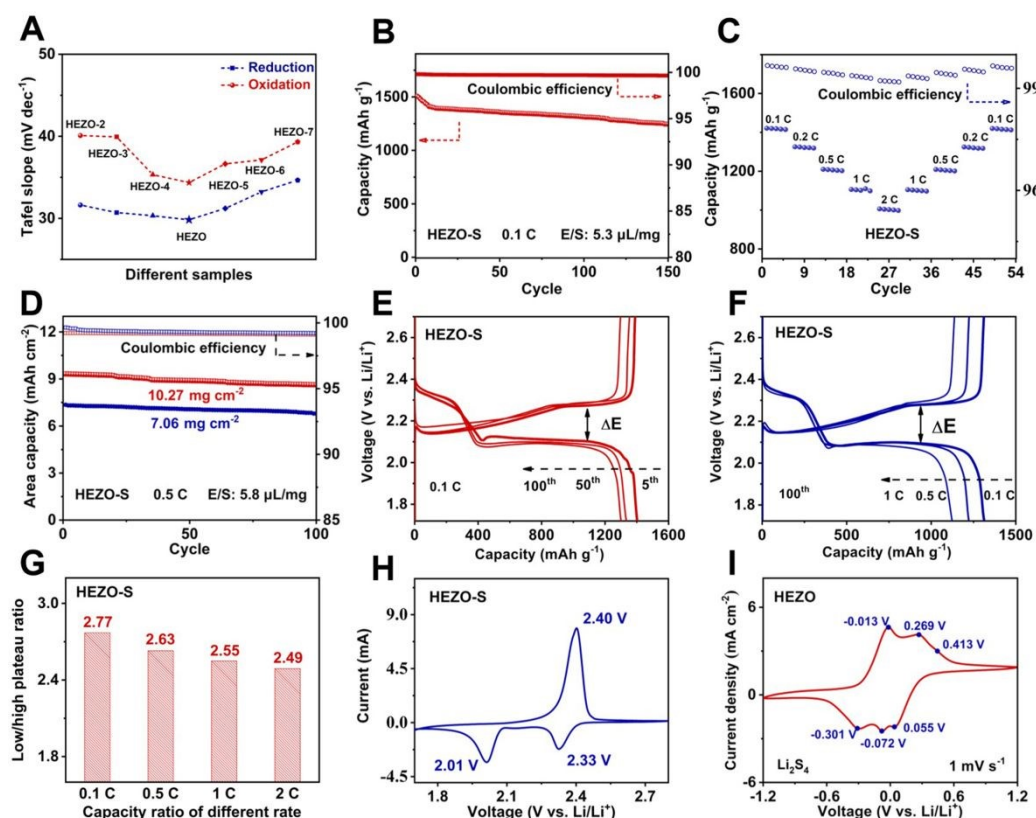


Fig. 3 | Electrochemical performance of HEZO-S cathode. **A**, Tafel slopes of different HEZO components. **B**, Long-cycling performance at 0.1 C. **C**, Rate capabilities from 0.1 C to 2 C. **D**, Long-cycling performance with different sulfur loading at 0.5 C. **E**, Galvanostatic discharge-charge curves of different cycle numbers at 0.1 C. **F**, Galvanostatic discharge-charge curves of different current densities at 100th cycle. **G**, Ratio of low to high platform capacity under different rates. **H**, CV curves of HEZO-S normal cell and **I**, HEZO- Li_2S_6 catholyte symmetric cell.



characteristics, a coin-cell system was assembled to evaluate the electrochemical performance. To investigate the effect of entropy composition on battery performance, seven groups of pyrochlore ceramics with varying molar ratios were synthesized:

$(\text{La}_{0.15}\text{Nd}_{0.15}\text{Sm}_{0.40}\text{Eu}_{0.15}\text{Gd}_{0.15})_2\text{Zr}_2\text{O}_7$,
 $(\text{La}_{0.15}\text{Nd}_{0.20}\text{Sm}_{0.35}\text{Eu}_{0.15}\text{Gd}_{0.15})_2\text{Zr}_2\text{O}_7$,
 $(\text{La}_{0.10}\text{Nd}_{0.25}\text{Sm}_{0.35}\text{Eu}_{0.15}\text{Gd}_{0.15})_2\text{Zr}_2\text{O}_7$,
 $(\text{La}_{0.10}\text{Nd}_{0.25}\text{Sm}_{0.30}\text{Eu}_{0.15}\text{Gd}_{0.20})_2\text{Zr}_2\text{O}_7$,
 $(\text{La}_{0.10}\text{Nd}_{0.20}\text{Sm}_{0.25}\text{Eu}_{0.25}\text{Gd}_{0.20})_2\text{Zr}_2\text{O}_7$,
 $(\text{La}_{0.15}\text{Nd}_{0.20}\text{Sm}_{0.25}\text{Eu}_{0.20}\text{Gd}_{0.20})_2\text{Zr}_2\text{O}_7$, and
 $(\text{La}_{0.20}\text{Nd}_{0.20}\text{Sm}_{0.20}\text{Eu}_{0.20}\text{Gd}_{0.20})_2\text{Zr}_2\text{O}_7$. These ceramics were

labeled as HEZO, HEZO-2, HEZO-3, HEZO-4, HEZO-5, HEZO-6, and HEZO-7, respectively, with their calculated configurational entropy values (R) gradually increasing: 1.504, 1.513, 1.543, 1.544, 1.567, 1.581, and 1.609. The band gaps of seven different high-entropy components were compared using the Tauc curves of UV-Vis diffuse reflection spectra and it was found that $(\text{La}_{0.15}\text{Nd}_{0.15}\text{Sm}_{0.40}\text{Eu}_{0.15}\text{Gd}_{0.15})_2\text{Zr}_2\text{O}_7$ (HEZO) has the lowest bandgap width. The kinetic speed was evaluated by comparing the Tafel slope, lithium ion diffusion ability, and reaction current density of samples with different components. The results all indicated that the HEZO component has the least kinetic delay in the sulfur cathode (Figs. 3A, S11–S13).

Using HEZO-S as the working electrode and lithium foil as the counter electrode, the battery exhibited outstanding performance. At a sulfur loading of 2 mg cm^{-2} and an electrolyte-to-sulfur (E/S) ratio of $5.3 \mu\text{L mg}^{-1}$, it delivered a discharge capacity of 1507 mAh g^{-1} . Even after 150 cycles at a low current density of 0.1 C , the cell maintained a reversible capacity of 1238 mAh g^{-1} , with a capacity retention rate exceeding 80% and an average Coulombic efficiency exceeding 99.68% (Fig. 3B). Comparatively, the composite electrode materials of $\text{La}_2\text{Zr}_2\text{O}_7\text{-S}$, $\text{Nd}_2\text{Zr}_2\text{O}_7\text{-S}$, $\text{Sm}_2\text{Zr}_2\text{O}_7\text{-S}$, $\text{Eu}_2\text{Zr}_2\text{O}_7\text{-S}$, $\text{Gd}_2\text{Zr}_2\text{O}_7\text{-S}$ and $\text{ZrO}_2\text{-S}$ demonstrated lower performance and higher concentration polarization (Figs. S14, 15). In addition, after 3 cycles of stable activation with low current, the HEZO-S cathode demonstrated superior rate performance at varying current densities (Fig. 3C). At current densities of 0.1 , 0.2 , 0.5 , 1.0 , and 2.0 C , the discharge capacities were 1426 , 1322 , 1208 , 1110 , and 1002 mAh g^{-1} , respectively. Upon returning to 0.1 C after a gradient increase in current density, the capacity of the HEZO-S cathode recovered to 1417 mAh g^{-1} with a capacity retention rate of 99.5% and an average Coulombic efficiency above 99%. Compared with the other two groups of electrodes, HEZO-S displayed superior capacity retention and Coulombic efficiency (Fig. S16). Moreover, when the sulfur loading on the circular electrode increased to 7.06 mg cm^{-2} (E/S ratio of $5.8 \mu\text{L mg}^{-1}$), the HEZO-S electrode still delivered an areal capacity of 7.35 mAh cm^{-2} (Fig. 3D). After 100 cycles, the reversible areal capacity remained at 6.79 mAh cm^{-2} . Further increasing the loading to 10.27 mg cm^{-2} resulted in an areal capacity of 9.32 mAh cm^{-2} , maintaining $8.863 \text{ mAh cm}^{-2}$ after 100 cycles. Fig. 3E shows the constant current charge-discharge curve of the HEZO-S electrode at a low current density of 0.1 C that indicated sulfur utilization of 86%, 83%, and 78% in the 5th, 50th, and 100th cycles, respectively, with minimal voltage plateau difference. At the same time, the constant current

charge-discharge curve of the same cycle (100 cycles) under different charge-discharge ratios further proves the advantage of high-entropy oxide HEZO-S cathode (Fig. 3F). Specifically, the effective sulfur utilization of HEZO-S at different current densities was all better than the other two cathodes (Fig. S17).

The efficient utilization of the HEZO-S cathode is attributed to its stable cycling durability and high-rate capacity, facilitated by the high conductivity of the sulfur host and its electrocatalytic effect on intermediate polysulfides. Further, the electrochemical impedance spectroscopy (EIS) fitting analysis was conducted to investigate the charge transfer resistance and Warburg impedance of the HEZO-S, $\text{Sm}_2\text{Zr}_2\text{O}_7\text{-S}$, and $\text{ZrO}_2\text{-S}$ cell cathodes (Fig. S18). Additionally, the voltage profiles of the SZO-S cathode at 0.1 C were performed to further investigate the internal resistance (Fig. S19). It was observed that HEZO-S exhibits significantly lower internal resistance during both the S lithiation and Li_2S decomposition, indicating higher conductivity during electrochemical processes. Under the measurement of voltage curves at 0.1 C . This facilitates the accelerated kinetics of sulfur and intermediate LiPSs. The degree of conversion can be verified by the ratio of low-potential plateau capacity to high-potential plateau capacity. As the current density of the HEZO-S cell increases from 0.1 C to 2 C , the ratio at low and high potentials remained closer to the theoretical value of 3 (measured values of 2.77, 2.63, 2.55, and 2.49), and significantly higher than the other two control cells. Additionally, there is almost no attenuation in the potentials for electrochemical conversion at high and low potentials (Figs. 3G, S20, 21), indicating a more complete conversion of the sulfur cathode.

The CV curves of the three cathodes at a scanning rate of 0.5 mV s^{-1} (Figs. 3H, S22, 23) reveal that HEZO-S exhibits superior electrochemical performance due to enhanced redox kinetics and higher catalytic activity. The current density of the maximum reduction peak for HEZO-S was found to be 1.02 mA cm^{-2} and 1.47 mA cm^{-2} , and the current density of the maximum oxidation peak was 3.33 mA cm^{-2} . Furthermore, the differential CV curves were analyzed to accurately compare the initial potentials of the electrochemical conversion reactions. For the reduction reaction, the initial potentials of the HEZO-S electrode were 2.45 V and 2.08 V , while for the oxidation reaction, the initial potential was 2.15 V . Furthermore, linear sweep voltammetry (LSV) curves (Fig. S24) were conducted to determine Tafel slopes, and was used to evaluate the catalytic kinetics of the SRR. In the HEZO-S reduction, the Tafel slope of peak I and peak II were only 29.83 and $34.36 \text{ mV dec}^{-1}$ (Fig. S25) whereas for oxidation, the Tafel slope was 54.7 mV dec^{-1} (Fig. S26). HEZO-S demonstrated the smallest Tafel slopes in both the reduction and oxidation processes, indicating faster kinetic conversion of lithium polysulfides for HEZO-S. Otherwise, two different lithium polysulfides (Li_2S_4 and Li_2S_6) were used as electrolytes at the same concentration. The HEZO electrode exhibited a larger reaction current density (2.7 mA cm^{-2}) in the CV curve with Li_2S_4 electrolyte (Figs. 3I, S27). Moreover, the HEZO/ Li_2S_4 /HEZO symmetric cell showed more favorable reaction potentials and kinetics. Specifically, the maximum reduction peak currents



corresponded to potentials of 0.055, -0.072, and -0.301 V, while the maximum oxidation peak currents corresponded to potentials of -0.013, 0.269, and 0.413 V. These results essentially indicate that the rapid conversion of Li_2S_4 is the key factor for performance enhancement in high-entropy pyrochlore-type oxides.

In-situ Electrochemical Confocal Raman Spectra and visualization of Li_2S_4 dynamics.

To conclusively demonstrate that Li_2S_4 is the key factor in enhanced electrocatalytic performance, *in-situ* Raman spectroscopy was used to monitor the HEZO-S battery during real-time constant current charge-discharge cycling. Observations indicated that HEZO-S follows the classical stepwise lithiation of S_8 . Remarkably, after the low potential plateau, characteristic Raman peaks for LiPSs were hardly observed (Figs. 4A, B), indicating the sole presence of Li_2S in

the system. This is distinct from the $\text{Sm}_2\text{Zr}_2\text{O}_7\text{-S}$ and $\text{ZrO}_2\text{-S}$ cathodes, where characteristic Raman peaks of liquid-phase LiPSs were still evident (Figs. S28, 29). Significant amounts of LiPSs in HEZO-S started to produce upon charging to 2.3 V, while the other two electrodes exhibited intermittent and scattered LiPSs signals throughout the charging process.

It is well known that *in-situ* Raman spectroscopy provides an average response of the Raman signals within the illuminated laser spot. By integrating confocal technology with Raman spectroscopy, one can acquire the phase distribution through point-by-point scanning within a specified area, thereby enhancing the decoupling of critical information pertaining to the sulfur cathode with improved spatial and temporal resolution. The underlying principle of this technique is depicted in Fig. 4C, where a specially designed battery cell mold was positioned under the optical microscope of the Raman spectrometer. A fixed objective region was chosen for

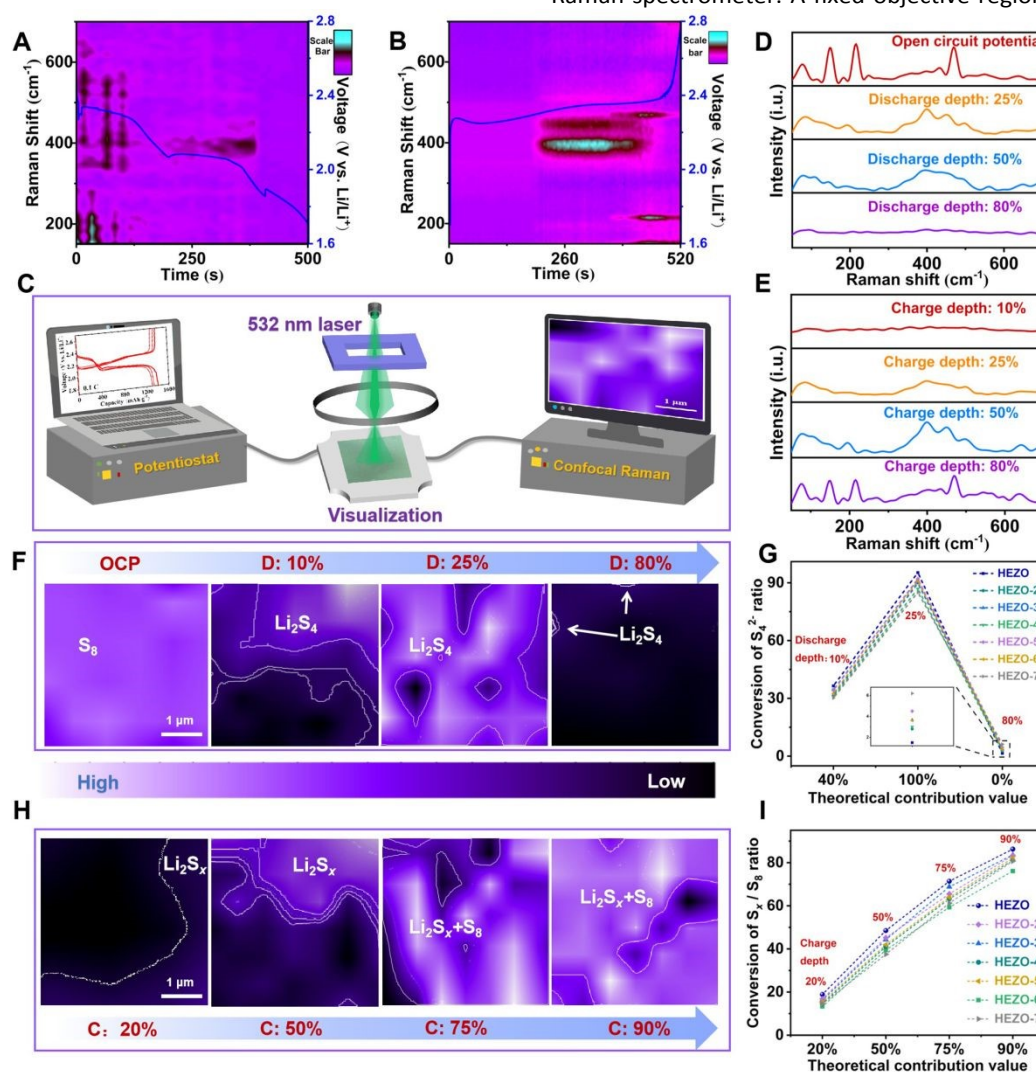


Fig. 4 | *In-situ* monitoring of electrocatalytic processes by Raman spectroscopy. A, HEZO-S of time sequence of Raman spectra obtained during the discharge progress. B, HEZO-S of time sequence of Raman spectra obtained during the charge progress. C, *In-situ* electrochemical confocal Raman spectra diagram. D, Summary of Raman lines at different discharge depths of OCP, 25%, 50%, and 80%. E, Summary of Raman lines at different charge depths of 10%, 25%, 50%, and 80%. F, 2D projection mapping of different discharge depths based on S_8 and Li_2S_4 characteristic peaks with a scale of 1 μm . G, The actual utilization of Li_2S_4 in different discharge states. H, 2D projection mapping of different charge depths based on S_8 and Li_2S_4 characteristic peaks with a scale of 1 μm . I, The actual utilization of Li_2S_4 in different charge states.



the collection of Raman signals, and two external wires were connected to the battery cell mold, which in turn connected to an electrochemical workstation. This setup enables the charge-discharge cycling process at a constant current while simultaneously recording the characteristic peak signals of the products within the microscopic field. Compared to conventional *in-situ* Raman spectroscopy, we focused on *in-situ* electrochemical Raman laser and microscopic imaging on the same confocal area ($4 \times 4 \mu\text{m}^2$). By performing frame-by-frame scanning with the Raman laser (at a rate of $0.02 \times 0.02 \mu\text{m}^2 \text{ s}^{-1}$), the characteristic peaks of LiPSs (range $50\text{--}700 \text{ cm}^{-1}$) with high spatial accuracy were obtained in this confocal region. The confocal acquisition approach offers three distinct advantages: 1) it captures the locational information of the sulfur cathode and intermediate polysulfides within the illuminated laser spot; 2) it monitors the concentration fluctuations of the sulfur cathode and intermediate polysulfides at the same location as the voltage varies; 3) it precisely differentiates between sulfur and intermediate phase information using multi-characteristic peak combination plotting techniques. Based on the above principle, the Raman signals of the three characteristic peaks ($152, 220, 475 \text{ cm}^{-1}$) of S_8 in the initial state were obtained as references (Figs. 4D, E). Meanwhile, the NGS LabSpec software was used to perform subtractive liquid phase background and peak intensity normalization processing on all the obtained spectra. We extracted the intensifications of two characteristic fingerprint vibration peaks of Li_2S_4 at 200 cm^{-1} and 450 cm^{-1} , quantified the projection of the Raman two-dimensional (2D) plane (Fig. 4F), and obtained the superposition of two different Gaussian distribution color mappings. Since the calibration of the Raman characteristic peak intensity of a specific LiPS is directly related to the color contrast of the image, the change in the Raman two-dimensional mapping area can be equivalent to the phase conversion efficiency. This allows for the visualization of the phase distribution within the confocal area. Track the position and concentration details of the Li_2S_4 Raman signal at discharge depths of 25%, 50%, and 80%, and charge depths of 10%, 25%, 50%, and 80%. The superimposed mapping of these two characteristic peaks ($200, 450 \text{ cm}^{-1}$) is helpful for accurately analyzing the actual conversion efficiency of Li_2S_4 .

In this map, the white and purple regions represent the distribution of elemental sulfur (S_8) and Li_2S_4 , respectively, while the black regions indicate the distribution of lithium sulfide (Li_2S). By evaluating the changes in the area of the 2D projection mapping at varying depths of discharge (DOD), we establish a correlation between the actual conversion efficiency of Li_2S_4 and the practical battery capacity under different configurational entropy values. As the discharge depth increases, the peak intensity of S_8 gradually diminishes, and part of the Raman 2D projection mapping corresponding to S_8 is progressively replaced by signals from intermediate LiPSs. As a result, at discharge states of 10% and 25%, the original bright regions gradually differentiate into three color regions: purple, white, and black, representing S_8 , Li_2S_4 , and $\text{Li}_2\text{S}_2/\text{Li}_2\text{S}$, respectively. The mapping area becomes predominantly black as $\text{Li}_2\text{S}_2/\text{Li}_2\text{S}$ does not produce Raman

characteristic signals. When the cutoff discharge depth reaches 80%, with a small amount of white remaining indicating residual Li_2S_4 . To validate the reliability of using the S_8 peak projection area as a reference for quantifying phase evolution, key discharge depths of 10%, 25%, and 80% were selected, where the theoretical proportions of Li_2S_4 distribution in the selected region are 40%, 100%, and 0%, respectively. The corresponding experimental values were found to be 38.6%, 95.3%, and 1.5%, respectively (Fig. 4G), which closely match the theoretical values. In contrast, during the charging process at depths of charge (DOC) of 25%, 50%, 75%, and 90%, the actual conversion proportions of polysulfides (S_x^{2-}) to S_8 were 18.9%, 48.5%, 71.4%, and 86.4%, respectively (Figs. 4H–I, S28, 29). The high-resolution *in-situ* confocal Raman spectroscopy, combined with electrochemical charge-discharge analysis, accurately reflects the critical role of the pyrochlore-structured high-entropy oxides in facilitating the effective conversion of Li_2S_4 . This conversion is essential for enhancing the capacity of Li-S batteries. Comparing the conversion ratios under different high-entropy compositions, it is evident that $(\text{La}_{0.15}\text{Nd}_{0.15}\text{Sm}_{0.40}\text{Eu}_{0.15}\text{Gd}_{0.15})_2\text{Zr}_2\text{O}_7$ ($R = 1.504$) exhibits the optimal electrocatalytic performance for Li_2S_4 conversion.

Electrocatalytic performance under DFT decoupling electric field and crystal field regulation.

The adsorption free energy of intermediate polysulfides ($\Delta G_{\text{LiPSs}^*}$) on ABO_x catalysts is a critical indicator that reflects the intrinsic catalytic activity for the SRR involving LiPSs species^{44–46}. The indicator can be preliminarily assessed through a visualized adsorption experiment of Li_2S_4 solution (Fig. 1B). It is worth noting that the $\text{Sm}_2\text{Zr}_2\text{O}_7$ host exhibits slightly stronger adsorption capability towards Li_2S_4 compared to the HEZO. However, during the evaluation of battery performance, HEZO demonstrated a more efficient utilization of the sulfur cathode. This suggests that the SRR process shares fundamental similarities with other well-studied electrocatalytic reactions, where the adsorption properties of key intermediates govern the reaction kinetics. The volcano-shaped relationship indicates the existence of an optimal adsorption strength that can maximize the reaction rate, highlighting the pivotal role of Li_2S_4 kinetics in the overall electrocatalytic performance. Furthermore, the insights gained from the Zr-O bond activation and band gap reduction emphasize the importance of the electronegativity and crystal field splitting modifications induced by the high-entropy approach. To gain a deeper understanding of the Li_2S_4 transformation mechanism, a DFT analysis of the three key intermediate states (Li_2S_4^* , LiS_2^* , Li_2S_2^*) involved would provide valuable insights.

Within the strongly correlated system of rare earth metals, The DFT+U calculations indicate that as the U value increases, the contraction effect of La-based rare earth metals significantly impacts the electronic structure of the f orbitals (Fig. S30). Therefore, it is essential to determine reasonable values of U by considering the actual UV solid-state diffuse



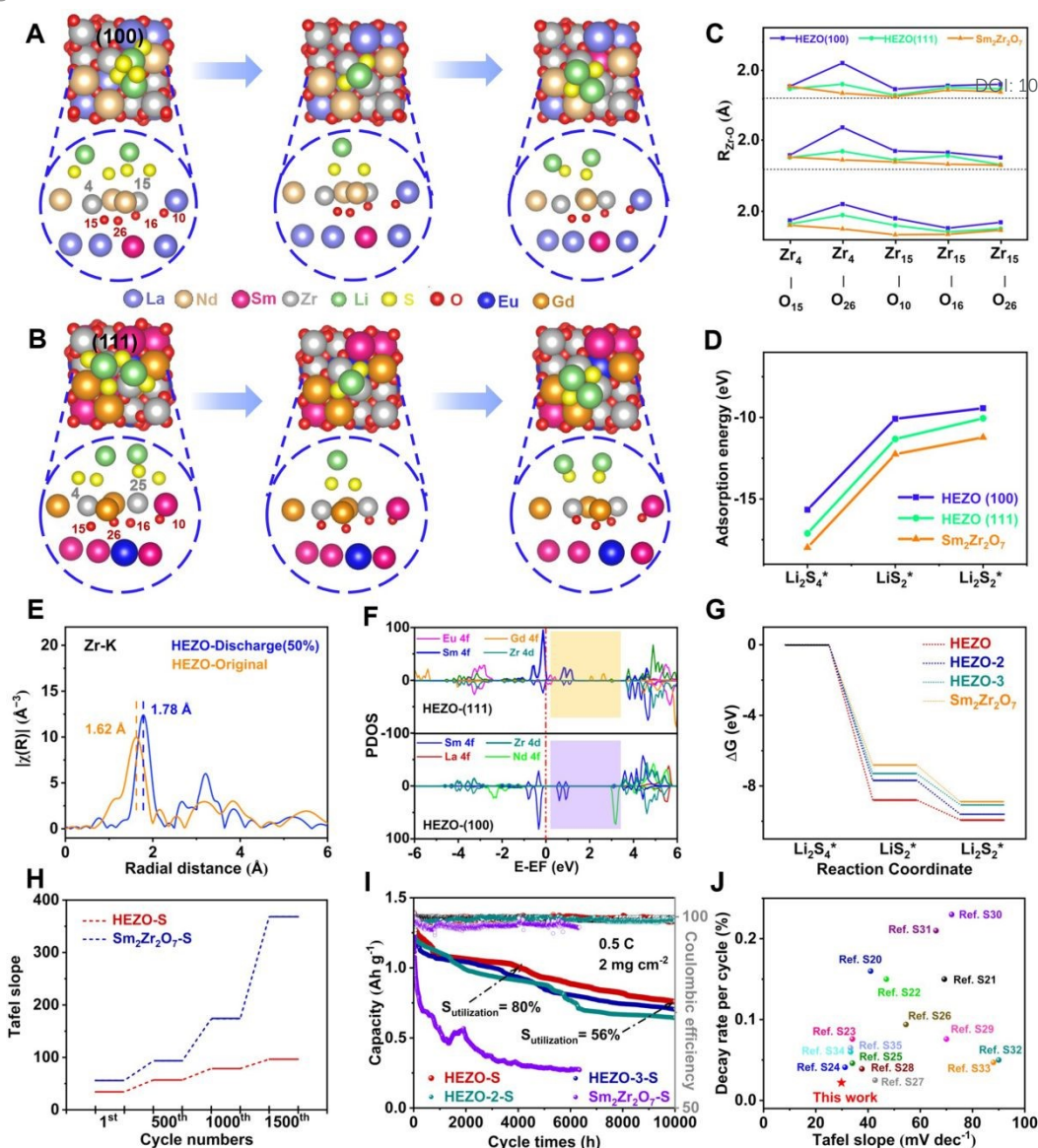


Fig. 5 | First principles calculations and electrocatalytic kinetic characterization Ultra-durable HEZO-S cathode performance. **A**, The steady-state configuration of the adsorption, activation, and desorption of Li_2S_4 by exposed Zr sites on HEZO (100) crystal faces with oxygen vacancy. **B**, The steady-state configuration of the adsorption, activation, and desorption of Li_2S_4 by exposed Zr sites on HEZO (111) crystal faces with oxygen vacancy. **C**, The length of the Zr-O bond at the Zr site of (100) and (111) crystal face under three adsorption states in the transformation of Li_2S_4 . **D**, Adsorption energy at Zr site of (100) and (111) crystal face in three adsorption states. **E**, HEZO-S discharge depth of 0% and 50% Zr k edge Fourier transform EXAFS $k^3 \chi(k)$ data. **F**, PDOS of (top) Zr site of (111) crystal faces and (down) (100) crystal faces. **G**, Gibbs free energy diagram of Li_2S_4 conversion steps of HEZO and $\text{Sm}_2\text{Zr}_2\text{O}_7$ substrate. **H**, HEZO-S, and $\text{Sm}_2\text{Zr}_2\text{O}_7$ -S batteries of the Tafel slope under different cycle periods. **I**, Long cycle performance. **J**, Comparison of HEZO with recently reported capacity decay rates and Tafel slopes of oxide electrocatalysts in extended cycles S^{20-35} .

reflectance spectra to ascertain the positioning of the f orbitals. The values of U were determined to be $U_{\text{La}} = 2.8$ eV, $U_{\text{Nd}} = 5$ eV, $U_{\text{Sm}} = 1$ eV, $U_{\text{Gd}} = 6.9$ eV, and $U_{\text{Eu}} = 4.0$ eV, which are in an appropriate approximately equivalent. In constructing the adsorption model of a complex high entropy system, Zr is more predisposed to interact with the highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO) of Li_2S_4 . The EXAFS analysis result of the Zr clearly demonstrates the existence of specific regularities in the atomic-scale structure of high-entropy materials. The discovery that only three rare earth elements can directly bond with Zr provides strong experimental evidence for the

establishment and validation of the adsorption mechanism model. Based on this, two adsorption configurations, HEZO-(100)-Zr and SmEuGd-Zr , were selected to simulate the steady-state adsorption and the oxygen vacancy was considered in the model (**Figs. 5A, B**). DFT+U computations were executed to formulate three adsorption configurations of Li_2S_4 , LiS_2 , and Li_2S_2 affixed to Zr surfaces, by analyzing the Zr-O bond lengths and correlating them with adsorption geometries of ΔG_{LiS} , ΔG_{LiS_2} , and $\Delta G_{\text{Li}_2\text{S}_2}$, three adsorption configurations of Li_2S , LiS_2 , and Li_2S_2 on the Zr surface were determined using DFT+U calculations (**Fig. 5C**). The (100) and (111) active crystal facets of HEZO were selected as model structures for the simulations.



The results show five Zr-O adsorption sites for Li_2S , LiS_2 , and Li_2S_2 molecules, labeled as $\text{Zr}_4\text{-O}_{15}$, $\text{Zr}_4\text{-O}_{26}$, $\text{Zr}_{15}\text{-O}_{26}$, $\text{Zr}_{15}\text{-O}_{16}$, and $\text{Zr}_{15}\text{-O}_{10}$. During the adsorption, activation, and desorption processes of Li_2S_4 on the surface, under the steady-state adsorption of Li_2S_4^* , LiS_2^* , and Li_2S_2^* , it was observed that the Zr-O bond lengths on the exposed (100) and (111) facets of HEZO are longer than those in $\text{Sm}_2\text{Zr}_2\text{O}_7$. This indicates a further weakening of Zr-O covalency during the discharge process. Conversely, the adsorption energies ($\Delta G_{\text{Li}_2\text{S}_4}$, $\Delta G_{\text{Li}_2\text{S}_2}$) of the Zr sites on the (100) and (111) facets of HEZO are lower than those on $\text{Sm}_2\text{Zr}_2\text{O}_7\text{-Zr}$ (Fig. 5D), suggesting that the adsorption energy of polysulfides decreases as the covalency weakens. Ex-situ extended X-ray absorption fine structure (EXAFS) analysis near the Zr K-edge reveals that compared to the initial Zr-O bond length of 1.62 Å in HEZO, the bond length increases to 1.78 Å at a 50% depth of discharge, consistent with the theoretical model structure (Fig. 5E). The projected density of states (pDOS) of Zr shows enhanced overlap between the Zr f and d orbitals, providing a faster pathway for electron migration (Fig. 5F). Additionally, the adsorption structures on the (100) and (111) facets of HEZO exhibit downhill Gibbs free energy distributions, demonstrating that HEZO with oxygen vacancy defects has superior performance in accelerating the overall sulfur redox reaction (SRR) process in lithium-sulfur batteries (Fig. 5G, S31–34).

To corroborate the theoretical analysis and DFT+U calculation results, HEZO-S, and $\text{Sm}_2\text{Zr}_2\text{O}_7\text{-S}$ electrodes were incorporated into coin cells. As the discharge cycles of the battery devices escalated from 1 to 500, 1000, and 1500 cycles, the Tafel slope of HEZO-S increased from 34.36 to 56.89, 78.63, and 96.38 mV dec^{-1} , representing an increase of approximately 180 % (Fig. 5H). Notably, the HEZO-S battery was still capable of reversible charge and discharge at over 4000 cycles and more than 10000 hours of operation at the time of publication, and an average coulombic efficiency of 99.51% (Fig. 5I). By modulating the crystal field splitting energy and electronegativity of the high-entropy ceramic, we optimize the electronic structure of the active sites and their covalency with oxygen. This adjustment leads to efficient electrocatalytic conversion in the key process of the sulfur redox reaction, providing material support for the full performance of battery devices. In practical applications, the HEZO-S battery can still operate stably even after 10,000 hours of charge and discharge, and the reversible capacity is still 55 % (Fig. 5J). When the surface capacity of the soft pack battery is 2mg cm^{-2} and the E/S ratio is $5.3\text{ }\mu\text{L mg}^{-1}$, it can still maintain 3h illumination for the LED lamp after 150 cycles (Fig. S35). The surface load of the soft pack battery was further increased to 11.2 mg cm^{-2} , the E/S ratio was reduced to $1.7\text{ }\mu\text{L mg}^{-1}$, and the reversible discharge capacity at the current density of 0.5 C was 649 mAh g^{-1} after 100 cycles, with the average Coulomb efficiency of 99.58% (Fig. S36). This shows the significant advantages of high-entropy engineering to improve electrocatalytic activity on battery performance.

Conclusions

In summary, we have developed one novel ultrarapid sintering method to successfully synthesize a pyrochlore-type high-entropy metal oxide, $(\text{La}_{0.15}\text{Nd}_{0.15}\text{Sm}_{0.40}\text{Eu}_{0.15}\text{Gd}_{0.15})_2\text{Zr}_2\text{O}_7$ (HEZO), which serves as an efficient electrocatalyst for Li-S batteries. The reduced electronegativity and crystal field splitting energy jointly modulate the electronic structure of Zr and the covalency of the Zr-O bond, effectively mitigating the intrinsic adsorption strength of Li_2S_4 . Furthermore, localized electrons, derived from the f orbitals, contribute to the formation of an electronic buffer band that acts as a reservoir between the UHB and the LHB, significantly enhancing the catalytic activity towards the sulfur redox reaction. Notably, within this highly disordered high-entropy system, a form of inherent ordering was found. This not only establishes a new benchmark for ABO_x -based catalysts but also surpasses the electrocatalytic performance of hierarchical porous carbon materials. It furthermore demonstrates exceptional durability, sustaining stable operation for 10000 hours at a current density of 0.5 C. These are all exciting evidence that the application of high-entropy engineering in the design of electrocatalysts offers an innovative strategy to enhance the high-rate capability and ultra-durable performance of Li-S batteries, thereby boosting their competitiveness in the market.

Methods

Synthesis of the $(\text{La}_{0.15}\text{Nd}_{0.15}\text{Sm}_{0.40}\text{Eu}_{0.15}\text{Gd}_{0.15})_2\text{Zr}_2\text{O}_7$ (HEZO) Hosts: 10 mmol of ZrO_2 , 0.75 mmol of La_2O_3 , Nd_2O_3 , Eu_2O_3 , Gd_2O_3 , and 2 mmol Sm_2O_3 were accurately weighed and placed in a planetary ball mill. The ball-to-material mass ratio was set at 6:1, and a sufficient amount of ethanol was added to completely immerse the powder. The mixture was then ball-milled at 560 rpm min^{-1} for 10 hours. Afterward, the slurry was transferred to a rotary evaporator to remove the ethanol. The obtained slurry was then dried overnight at $60\text{ }^\circ\text{C}$ in an oven, resulting in a pale white powder. Subsequently, the dried powders were mixed in a mass ratio of 1:5 and blended in a molten salt mixture of NaCl/KCl (1:1). The mixture was then heated in a muffle furnace at a rate of $5\text{ }^\circ\text{C min}^{-1}$ until reaching $1200\text{ }^\circ\text{C}$, and the powders were sintered at this temperature for 1 h. After the furnace cooled down to room temperature, the crucible was immersed in water to dissolve NaCl/KCl. Finally, after washing with water and absolute ethanol several times, then dried at $80\text{ }^\circ\text{C}$ overnight.

Preparation of $\text{Sm}_2\text{Zr}_2\text{O}_7$ Hosts. 0.01 mol of ZrO_2 , and 0.005 mol Sm_2O_3 were accurately weighed and placed in a planetary ball mill. The ball-to-material mass ratio was set at 6:1, and a sufficient amount of ethanol was added to completely immerse the powder. The mixture was then ball-milled at 560 rpm min^{-1} for 10 hours. Afterward, the slurry was transferred to a rotary evaporator to remove the ethanol. The obtained slurry was then dried overnight at $60\text{ }^\circ\text{C}$ in an oven. Subsequently, the dried powders were mixed in a mass ratio of 1:5 and blended in a molten salt mixture of sodium NaCl/KCl (1:1). The mixture was then heated in a muffle furnace at a rate of $5\text{ }^\circ\text{C min}^{-1}$ until reaching $1200\text{ }^\circ\text{C}$, and the powders were sintered at this temperature for 1 h. After the furnace cooled down



to room temperature, the crucible was immersed in water to dissolve NaCl/KCl. Finally, after washing with water and absolute ethanol several times, then dried at 80 °C overnight.

Preparation of $(\text{La}_{0.15}\text{Nd}_{0.15}\text{Sm}_{0.40}\text{Eu}_{0.15}\text{Gd}_{0.15})_2\text{Zr}_2\text{O}_7\text{-S}$ (HEZO-S) Cathode. HEZO and pure sulfur powder (1: 4 in mass ratio) were blended and ground for 15 min. Then, the mixture was shifted into an autoclave under 155 °C for 10 h. After cooling down, the product was annealed at 255 °C for half an hour under a flow of nitrogen gas to eliminate the residuary sulfur particles. For comparison, $\text{Sm}_2\text{Zr}_2\text{O}_7\text{-S}$ and $\text{ZrO}_2\text{-S}$ composites were prepared with a procedure similar to those of $(\text{La}_{0.15}\text{Nd}_{0.15}\text{Sm}_{0.40}\text{Eu}_{0.15}\text{Gd}_{0.15})_2\text{Zr}_2\text{O}_7\text{-S}$ composite instead of zinc atomic cluster with zinc single atom and without zinc cluster, except that the dopamine hydrochloride, respectively.

Synthesis of the HEZO with different Proportion Components. All the synthesis steps are the same as the HEZO mentioned above, with the difference in molar ratio from the initial raw material. Specifically speaking, 10 mmol of ZrO_2 , 0.5 mmol of La_2O_3 , 1.25 mmol of Nd_2O_3 , 0.75 mmol of Eu_2O_3 , Gd_2O_3 , and 1.75 mmol Sm_2O_3 , defined as high-entropy pyrochlore (HEZO-2). 10 mmol of ZrO_2 , 0.75 mmol of La_2O_3 , Eu_2O_3 , Gd_2O_3 , 1 mmol of Nd_2O_3 , and 1.75 mmol Sm_2O_3 , defined as medium entropy pyrochlore (HEZO-3). 10 mmol of ZrO_2 , 0.5 mmol of La_2O_3 , 1.25 mmol of Nd_2O_3 , 0.75 mmol of Eu_2O_3 , 1 mmol of Gd_2O_3 , and 1.5 mmol Sm_2O_3 , defined as medium entropy pyrochlore (HEZO-4). 10 mmol of ZrO_2 , 0.5 mmol of La_2O_3 , 1 mmol of Nd_2O_3 , 1.25 mmol of Eu_2O_3 , Sm_2O_3 , and 1 mmol Gd_2O_3 , defined as medium entropy pyrochlore (HEZO-5). 10 mmol of ZrO_2 , 0.75 mmol of La_2O_3 , 1 mmol of Nd_2O_3 , Eu_2O_3 , Gd_2O_3 , and 1.25 mol Sm_2O_3 , defined as medium entropy pyrochlore (HEZO-6). 10 mmol of ZrO_2 , 1 mmol of La_2O_3 , Nd_2O_3 , Eu_2O_3 , Gd_2O_3 , and Sm_2O_3 , defined as medium entropy pyrochlore (HEZO-7).

Materials Characterization. X-ray diffraction (XRD) measurements with Cu K α radiation (60 kV, 200 mA) were performed by the Panalytical X'Pert3 X-ray Powder Diffractometer. Field-emission scanning electron microscopy (FESEM, Hitachi S-4800, Japan) images and energy dispersive X-ray (EDX) spectra were captured using the S-4800 field-emission scanning electron microscope. High-resolution transmission electron microscopy (HRTEM) images were obtained from the transmission electron microscope assembled with a JEOL-2200FS Dual SDD system. Atomic-resolution HAADF-STEM images were obtained on a FEI Titan Cubed Themis G2 300 working at 200 kV. Thermogravimetric analysis (TGA) tests were using America Q600SDT analyzer under the N_2 atmosphere. The nitrogen adsorption-desorption isotherms were collected using a Micromeritics ASAP 2000 system at 77 K. The corresponding pore size distribution was calculated by the Barrett-Joyner-Halenda model using the adsorption branch. X-ray photoelectron spectra were obtained on an AXIS Supra instrument from Kratos using monochromatic Al K α radiation. All binding energies were calibrated by setting the measured C 1s peak to 284.5 eV. X-ray photoelectron spectroscopy (XPS) measurements were conducted on the AXIS Supra instrument. The *in-situ* Raman measurement was performed using a Horiba Jobin Yvon LabRAM ARAMIS system with an excitation laser line of 532 nm with the electrochemical cycling of an *in-situ* battery (Beijing Science Star Technology Co. Ltd). The

instrument was calibrated with respect to the silicon peak at 520.8 cm^{-1} . DOI: 10.1039/D5EE01215E

Electrochemical Measurements. To prepare the composite cathode, a mixture composed of 70 wt.% sulfur host, 20 wt.% conductive carbon black, and 10 wt.% polyvinylidene fluoride (PVDF) in N-methyl-2-pyrrolidinone (NMP) solvent (98%) was firstly stirred for 10 hours to form the homogeneous slurry. Following that, the slurry was carefully painted onto the collector and dried in the vacuum oven at 60 °C overnight to achieve the composite cathode. Coin-type CR2032 cells were prepared in an Ar-filled glovebox (H_2O and O_2 , < 0.1 ppm) by using Celgard 2500 membrane as separators and Li metal foil as counter electrodes. The electrolyte was 1 M LiTFSI in a mixture of DOL and DME (1:1 in volume) with 1 wt.% additive of LiNO_3 . Linear sweep voltammetry (LSV) and Cyclic voltammetry (CV) were handled in a voltage window range of 1.7–2.8 V by using a Land CT2001A battery measurement instrument and CHI760 electrochemical measurement in a thermostatic test box, respectively. Electrochemical impedance spectroscopy (EIS) gathered in a frequency range from 0.01 Hz to 100 kHz was conducted on a system. To further analyze the influence of different systems on the redox process of lithium polysulfides, the symmetrical cell was conducted to perform CV tests to analyze the redox behavior of three different polysulfide electrolytes within the voltage window from –1.2 to 1.2 V at a scan rate of 2 mV s^{-1} . All electrochemical parameters in terms of current densities and specific capacities mentioned in this paper are computed based on the sulfur content.

Density Functional Theory (DFT+U) Calculations. Density functional theory calculations were performed using the Vienna ab initio simulation package (VASP) with a plane-wave basis set and the projector augmented-wave (PAW) method^{47–50}. The exchange-correlation potential was treated using the generalized gradient approximation (GGA) with the Perdew-Burke-Ernzerhof (PBE) parametrization⁵¹. The valence states of the elements were defined as follows: La (11 valence electrons) - $5s^25p^65d^16s^2$, Nd (14 valence electrons) - $4f^45s^25p^66s^2$, Sm (14 valence electrons) - $4f^65s^25p^66s^2$, Eu (14 valence electrons) - $4f^75s^25p^66s^2$, Gd (14 valence electrons) - $4f^75s^25p^66s^2$, and Zr (12 valence electrons) - $4s^24p^65s^24d^2$. To address the limitations of GGA, we employed the GGA + U method in our calculations. The effective Hubbard U values were chosen as follows: U(4f) = 2.8 eV for La^{52} , U(4f) = 5.0 eV for Nd^{52} , U(4f) = 1.0 eV for Sm, U(4f) = 6.9 eV for Gd^{53} , and U(4f) = 4.0 eV for Eu, based on previous studies and DFT+U tests for Eu and Sm. We also applied the van der Waals correction of Grimme's DFT-D3 model⁵⁴. The energy cutoff was set to 550 eV, and Brillouin-zone integration was performed using a single Γ point ($1 \times 1 \times 1$). The structures were fully relaxed until the maximum force on each atom was less than 0.05 eV \AA^{-1} , and the energy convergence criterion was set to 10^{-6} eV. The Gibbs free energies of the intermediate evolution were calculated using the following expression:

$$\Delta G = \Delta E + \Delta \text{EZPE} - T\Delta S$$

where ΔE represents the change in electronic energy obtained from DFT, ΔEZPE is the change in zero-point energy, and ΔS is the change in entropy at standard conditions ($T = 298$ K) and at the potential versus the normal hydrogen electrode (NHE).



In-situ Electrochemical Confocal Raman Spectroscopy (EC-CRS) Measurement Method. *In-situ* confocal Raman spectroscopy characterization was performed as follows: The L2BRAMARAMIS confocal Raman spectroscopy and imaging system (placed in an air environment, controlled at a laboratory temperature of $20 \pm 2^\circ\text{C}$) was used to acquire Raman spectroscopic signals and mapping images. *In-situ* electrochemical Raman laser and microscopic imaging are focused on the same area ($4 \times 4 \mu\text{m}^2$). Raman laser frame-by-frame scanning (at a speed of $0.02 \times 0.02 \mu\text{m}^2\text{s}^{-1}$) obtained a series of LIPSs characteristic peaks with high spatial accuracy (ranging from 50 to 700cm^{-1}). All the obtained spectra were subjected to liquid phase background subtraction and peak intensity normalization using the NGS LabSpec software. The intensity of the specific characteristic peak was extracted, the projection of the Raman two-dimensional plane was quantified, and the color mapping of the intensity of the characteristic peak was obtained. Extract the intensities of the three characteristic peaks (151 cm^{-1} , 219 cm^{-1} , and 475 cm^{-1}) of S_8 under the open-circuit potential condition, and perform Gaussian distribution superposition on the color mapping of the intensities of these three characteristic peaks, the initial mapping area of the sulfur cluster monomer was selected as a reference value for the active surface area. The 2D mapping area of Li_2S_4 at open circuit voltage can be considered as the initial concentration, and the change in the 2D mapping area under Li_2S_4 is compared by altering the charge-discharge states. In the constant potential experiments, the change in area is converted into corresponding concentration and plotted against time. Constant potential and constant current measurements were achieved by using an electrochemical workstation (CHI660C) to control the voltage/reaction rate of the battery and monitor the current-time/voltage-time response.

Conflicts of interest

The authors declare that there is no conflict of interest.

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Data availability

- The data supporting this article have been included as part of the Supplementary Information.

