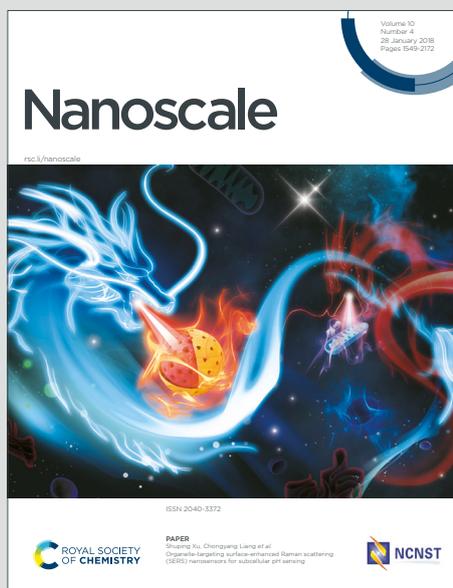


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# Insights into the structural features of crumpling graphene nanoribbons

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## Abstract

The exploration of graphene nanoribbons (GNRs) offers promising prospects by leveraging their unique physical properties and expanding their versatile applications. Here, we investigate the crumpling behavior of GNRs via coarse-grained molecular dynamics (CG-MD) simulations. By systematically varying the size and geometry (i.e., width and aspect ratio), we systematically examine the potential energy, configuration, mechanical state, and internal structure of crumpled GNRs in detail. Our findings indicate that as the size of GNRs increases, the self-adhering and self-folding behaviors during the crumpling process become more pronounced. Crumpled GNRs with large sizes exhibit greater adhesion energy but lower out-of-plane strain energy due to the formation of more planar regions and fewer sharp crumples compared to smaller GNR. By evaluating the relative shape anisotropy and representative configuration during the crumpling, we identify two aspect ratio-dependent crumpling modes for GNRs, namely, the edge-bending dominated (EBD) and sliding and folding dominated (SFD) crumpling modes, respectively. Notably, the width-dependent critical aspect ratio controlling the transition between these modes provides valuable insights into understanding and predicting the crumpling behavior of GNRs with varying geometries. Moreover, our assessment of curvature and stress distributions, and cross-sectional patterns of crumpled GNRs further reveals a reduction of mechanical heterogeneity with increased sheet size. Our study highlights the critical role of geometry in the crumpling behavior of GNRs, which has significant implications for the tailored design of crumpled ribbon-like sheet materials.

## Keywords:

Coarse-grained modeling, Molecular dynamics simulation, Graphene nanoribbon, Crumpling behavior, Mechanical heterogeneity



## 1. Introduction

Quasi-one-dimensional (Q1D) nanomaterials have recently garnered considerable attention due to their intriguing physical properties for extensive applications.<sup>1,2</sup> As a notable example, atomically thin graphene nanoribbons (GNRs) exhibit anisotropic mechanical properties,<sup>3</sup> boundary-dependent electronic properties,<sup>4</sup> ultra-high thermal conductivity,<sup>5</sup> and light absorption capabilities,<sup>6</sup> promising applications in composites,<sup>7</sup> optical materials,<sup>8</sup> sensors,<sup>9</sup> catalysts,<sup>10</sup> etc. Over recent decades, GNRs have been realized from the theoretical modeling<sup>11,12</sup> to large-scale preparation.<sup>13,14,15,16</sup> Specifically, GNRs are strips of graphene less than 100 nm in width, featuring a honeycomb structure composed of carbon atoms with  $sp^2$ -orbitals.<sup>17</sup> This nanostructure grants GNRs more flexible and tunable physical properties compared to graphene, e.g., width-dependent band gaps and all-semiconducting characteristics,<sup>18</sup> due to quantum confinement and edge effects.<sup>19,20</sup> GNRs with varying shapes and sizes can be fabricated using multiple approaches, including electron-beam lithography,<sup>21</sup> chemical vapor deposition,<sup>22</sup> sonochemical exfoliation,<sup>18</sup> gas-phase etching,<sup>23</sup> squashing carbon nanotubes,<sup>24</sup> and epitaxial synthesis on semiconductor substrates,<sup>25</sup> etc. Despite promising aspects of GNRs in various practical applications, inevitably, flaky and ribbon-like graphene with low out-of-plane bending stiffness often exhibits significant ripples, wrinkles, and crumples in reality due to thermal fluctuations,<sup>26</sup> structural defects,<sup>27</sup> polycrystalline,<sup>28</sup> and edge effects.<sup>29</sup> Such conformational versatility affects the physical performance of graphene in different shapes, such as mechanical performance<sup>30</sup> and carrier mobility,<sup>31</sup> making the exploration of rippled, wrinkled, and crumpled graphene a focus of research in recent years.

Considerable efforts have been made toward understanding the structural behavior, mechanical properties, and applications of crumpled graphene sheets.<sup>32,33</sup> Typically, factors such



as size,<sup>34</sup> defect type,<sup>35,36,37</sup> functional groups,<sup>38,39</sup> stickiness,<sup>40</sup> and processing conditions (e.g., temperature and crumpling rate)<sup>41</sup> influence the crumpling pattern of graphene sheets by affecting their self-folding behavior during the crumpling process. The resulting crumpled sheets with varying internal structures have remarkably different mechanical properties. For instance, sticky crumpled sheets possessing a larger effective compressive modulus than the non-sticky ones,<sup>42</sup> and crumpled graphene with the grain boundaries and reconstructed vacancy defects exhibits a larger bulk modulus than pristine ones,<sup>35,36</sup> making them a promising additive for functional nanocomposites.<sup>43</sup> Moreover, crumpled graphene boasts considerable packing efficiency, solvent accessible surface area, aggregation resistance, and self-dispersion, which are advantageous for supercapacitor and tribological applications.<sup>44,45,46,47</sup>

Previous studies on crumpled materials primarily focused on graphene sheets with relatively low aspect ratio close to  $\sim 1$ . Given the larger aspect ratio of GNRs, their crumpling behavior is expected to vary with sheet sizes and geometries. The successful preparation of straight GNRs with smooth edges, less defects, and large aspect ratios ( $\sim 387$ ) on liquid metal substrates has laid the foundation for the fundamental study of GNRs.<sup>48</sup> Notably, GNRs detached from the substrate and suspended in solvent tend to develop significant wrinkles and curls due to thermal fluctuations. Studies have shown that the size, aspect ratio, and surface modifications control the three main conformations of graphene sheets in equilibrium, i.e., planar membrane-like, ribbon-like, and scroll-like.<sup>49</sup> Despite progress made, the crumpling behavior of graphene sheets with different aspect ratios under hydrostatic pressure has not been well understood.

To unravel the relationship between sheet geometry (e.g., width and aspect ratio) and crumpling modes, in this study, we perform a series of coarse-grained (CG) molecular dynamics (MD) simulations to provide insights into the size dependent crumpling patterns of GNRs.



Specifically, we study the evolution of the total potential energy and its contribution for GNRs with different geometries during the crumpling process and in various crumpled states, which emphasizes the effect of geometry on the self-adhering and self-folding effects of the crumpled GNRs. Moreover, we analyze the relative shape anisotropy of GNRs to gain insight into the effect of sheet geometry on their structural changes upon crumpling. Remarkably, we identify two distinct geometry-dependent crumpling modes of GNRs, i.e., edge-bending dominated (EBD) and sliding and folding dominated (SFD) crumpling modes, along with the critical aspect ratio for the transition between them as a function of width. Finally, our exploration of the local curvature, stresses, and cross-section patterns of the crumpled GNRs further reveals the geometry-dependent mechanical states. Our research emphasizes the pivotal role of sheet geometry in shaping the crumpling mechanism of GNRs. This newfound understanding paves the way for the meticulous design of intricately crumpled ribbon-like materials.

## 2. Methods

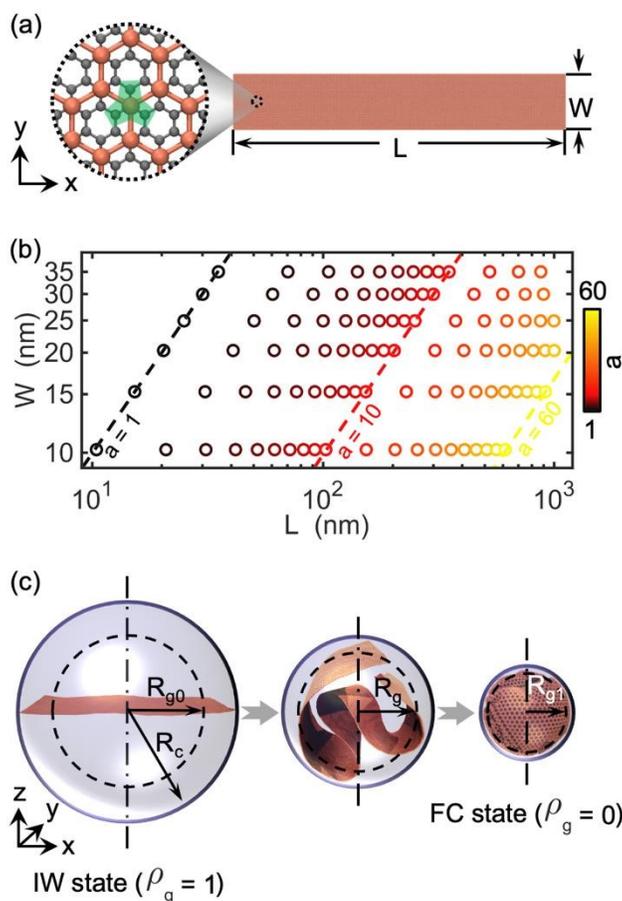
### 2.1. Overview of the coarse-grained modeling

CG-MD modeling, which not only overcomes the spatiotemporal limitations of all-atom (AA) MD simulations and greatly improves computational efficiency, but also preserves the essential characteristics of molecules, has been increasingly applied in recent years to study various complex systems at extended length and time scales.<sup>50,51,52</sup> Here, the GNRs are represented by a CG model with the hexagonal lattice derived based on the AA model, where each CG bead represents four carbon atoms, with a mass of 48 g/mol (Fig. 1(a)). The CG force field developed based on the strain energy conservation approach includes interactions from bonds  $V_b$ , angles  $V_a$ ,



dihedrals  $V_d$ , and pairwise non-bonded interaction  $V_{nb}$ .<sup>53,54</sup> The CG force field parameters are calibrated employing the mechanical properties of graphene (e.g., in-plane Young's and shear moduli, bending rigidity per unit width, and adhesion energy per surface area) obtained from experiments and density functional theory. The functional forms and parameters of the CG force field are listed in Table S1 in the Supporting Information. This CG model not only effectively captures the mechanical behavior of graphene, such as large deformation, fracture, interlayer anisotropic shear response, and nonlinear elastic deformation, but also significantly improves the computational speed and access to greater spatiotemporal scales compared with AA simulations,<sup>53,55</sup> and has been applied to MD simulation studies of structures such as nanostructured or architected sheet assembly systems,<sup>56,57</sup> multilayer graphene assemblies,<sup>58,59</sup> and graphene-reinforced polymers,<sup>43,60</sup> etc. Refer to our previous study for details on the building of the CG model.<sup>53</sup>





**Fig. 1** CG model of the GNRs considered and the setup of the crumpling simulation. (a) CG model of a GNR with width  $W$  and length  $L$  ( $L > W$ ). The zoom-in shows the 4-to-1 mapping scheme of the CG model, where one CG bead (brick red bead) represents four connected carbon atoms (the gray atoms highlighted in the green region). (b) The lengths and widths corresponding to all GNR models considered in this work. The color bar indicates the aspect ratio  $a$  ( $a = L/W$ ) of the model. Models with the same  $a$  can be fitted by a dashed line with a matching color to  $a$ , e.g.,  $a = 1$ ,  $a = 10$ , and  $a = 60$ . (c) Conformational evolution of GNR during the crumpling process.  $R_{g0}$ ,  $R_g$ , and  $R_{g1}$  represent the radii of gyration of GNR in the initial wrinkled (IW) state, during the crumpling process, and in the final crumpled (FC) state, respectively.  $R_c$  denotes the radius of the confining



sphere.  $\rho_g$  is the compaction ratio ( $0 \leq \rho_g \leq 1$ ), and a smaller value implies a greater degree of compaction of the model.

The geometry of a graphene nanoribbon (GNR) is defined by its width  $W$  and aspect ratio  $a$ , as shown in Fig. 1(a). Note that  $a = L/W$  and  $L$  is the length of the GNR ( $L > W$ ); moreover, as the edge shapes of graphene sheets along the length direction ( $x$ -direction), i.e., armchair, zigzag, and chiral, have very minor influences on their structural and mechanical properties,<sup>61</sup> we only focus on GNRs with zigzag edges along the length direction in this work. We study GNRs with  $W$  and  $a$  ranging from 10 nm to 35 nm and 1 to 60 (Fig. 1(b)), respectively, avoiding the GNRs from forming a scroll-like structure at the initial equilibrium state.<sup>49</sup> Taking advantage of our CG model, we are able to test the GNR having a wide range of length up to  $\sim 1 \mu\text{m}$ .

## 2.2. Coarse-grained molecular dynamics simulation details

All CG-MD simulations in this study are conducted with the Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS) software,<sup>62</sup> and the visualization of the CG-MD simulations is realized by Visual Molecular Dynamics (VMD).<sup>63</sup> In our CG-MD simulation, the flat GNR model without any wrinkles is initially laid in the  $xy$  plane (Fig. 1(a)) and is located at the center of the simulation box ( $1200 \text{ nm} \times 1200 \text{ nm} \times 1200 \text{ nm}$ ). The simulations are performed using periodic boundary conditions (PBCs) in all directions with a time step of 6 fs and a temperature of 300 K, which are consistent with our prior studies.<sup>36,40</sup> Once the initial system is set up, the energy of the system is minimized according to an iterative conjugate gradient algorithm.<sup>64</sup> Then, equilibrium simulation with a time duration of 2 ns is carried out using the NVT



ensemble until the total potential energy of the system becomes independent of time. Following that, as shown in Fig. 1(c), we employ a pseudo “confining spherical volume” to compact the GNR from the initial wrinkled (IW) state (i.e., state after equilibrium simulation) to the final crumpled (FC) state. This crumpling process is inspired by the mechanical compaction observed in aerosol evaporation experiments. While graphene in such experiments typically stays on the surface of a shrinking droplet,<sup>46,65,66,67,68</sup> in our model, the GNR adheres to the inner surface of a spherical boundary. This analogy captures a key physical feature: the droplet acts as a curved substrate and evaporation-induced surface tension generates a quasi-spherical inward driving force. Despite this idealization, our simulation approach facilitates a systematic exploration of geometry-dependent crumpling mechanisms, in line with previous computational studies.<sup>34,36</sup> Specifically, the boundary of the confining sphere, which completely encompasses the GNR model, exerts a repulsive force  $F$  perpendicular to the surface of the confining sphere at a certain cutoff distance, which can be written as:

$$F(r_i) = \begin{cases} -K_c(r_i - R_c)^2, & \text{for } r_i \geq R_c \\ 0, & \text{for } r_i < R_c \end{cases} \quad (1)$$

where  $r_i$ ,  $R_c$ , and  $K_c$  denote the distance between the  $i^{\text{th}}$  bead and the center of the confining sphere, the radius of the confining sphere, and the spring force constant ( $K_c = 2.31 \times 10^5$  kcal/(mol nm<sup>3</sup>)), respectively. The GNR model is progressively compacted into a crumpled state as the radius of the confining sphere decreases at a rate of 50 m/s. The spring force constant and compaction rate are adopted from previous studies on crumpling of graphene via spherical confinement,<sup>44</sup> and provide a balance between effective compression and numerical stability, despite the fact that neither of them corresponds directly to an experimental value (e.g., capillary force or evaporation rate).<sup>68</sup> Moreover, according to previous tests, we found that the compaction rate of 50 m/s can



improve the computational speed of the simulation while capturing the basic crumpling behavior of the sheet at low velocities. Note that the density of the crumpled GNR in the FC state is equal to the bulk density of graphite (i.e., 2.267 g/cm<sup>3</sup>), and no further compaction is performed to avoid amorphous collapse or damage of the model, which is consistent with the modeling protocol in our recent studies.<sup>34,36,37,40</sup> We emphasize that the compaction here does not aim to replicate the exact pressure conditions in aerosol evaporation, but rather to achieve a representative crumpled structure for analyzing geometry-dependent behaviors. Refer to our previous studies for more details on the crumpling simulation of the nanosheets.<sup>34,36</sup> Moreover, we have provided additional analyses in the Supporting Information, including the effects of temperature, post-crumpling relaxation at different relaxation rates, and relaxation timescales in the quasi-equilibrium state. We also discuss the comparison between CG-MD and AA-MD simulations, where the AA-MD simulations use the adaptive interatomic reactive empirical bond-order (AIREBO) potential.<sup>69,70</sup> Additionally, we examine the influence of GNR edge type on crumpling behavior. These results are presented in Fig. S1-S5 in the Supporting Information.

### 2.3. Property calculations

We calculate the radius of gyration tensor  $\mathbf{R}_g^2$  of the GNR model at each time step to obtain the compaction ratio  $\rho_g$  and the relative shape anisotropy  $\kappa^2$  of the system upon crumpling. Briefly,  $\mathbf{R}_g^2$  can be expressed as:

$$\mathbf{R}_g^2 = \begin{bmatrix} R_{xx}^2 & R_{xy}^2 & R_{xz}^2 \\ R_{yx}^2 & R_{yy}^2 & R_{yz}^2 \\ R_{zx}^2 & R_{zy}^2 & R_{zz}^2 \end{bmatrix} \quad (2)$$



and the radius of gyration  $R_g$  can be obtained as follows:

$$R_g = \sqrt{\Lambda_1 + \Lambda_2 + \Lambda_3} \quad (3)$$

where  $\Lambda_k$  ( $k = 1, 2, 3$ ) are the principal eigenvalues of  $\mathbf{R}_g^2$ , and  $\Lambda_1 \leq \Lambda_2 \leq \Lambda_3$ .

The compaction ratio  $\rho_g$  in our work is given as:

$$\rho_g = \frac{R_g - R_{g,FC}}{R_{g,IW} - R_{g,FC}} \quad (4)$$

where  $R_{g,IW}$  and  $R_{g,FC}$  are the radii of gyration of the model in the IW and FC states, respectively.

As the crumpling simulation proceeds,  $\rho_g$  of the system decreases from 1 to 0, i.e., a smaller value of  $\rho_g$  indicates a more compacted GNR.

Moreover, the relative shape anisotropy  $\kappa^2$  can be obtained by the following formula:

$$\kappa^2 = 1 - 3 \frac{\Lambda_1\Lambda_2 + \Lambda_2\Lambda_3 + \Lambda_3\Lambda_1}{(\Lambda_1 + \Lambda_2 + \Lambda_3)^2} \quad (5)$$

Note that  $0 \leq \kappa^2 \leq 1$ , and  $\kappa^2 = 0$ ,  $\kappa^2 = 0.25$ , and  $\kappa^2 = 1$  represent the ideal spherical structure, ideal symmetrical flat sheet, and the ideal straight rod, respectively.

Additionally, the von Mises stress  $\sigma_v$  can be calculated as:

$$\sigma_v = \sqrt{\frac{(\sigma_{11} - \sigma_{22})^2 + (\sigma_{22} - \sigma_{33})^2 + (\sigma_{33} - \sigma_{11})^2 + 6(\sigma_{12}^2 + \sigma_{23}^2 + \sigma_{31}^2)}{2}} \quad (6)$$

where  $\sigma_{ij}$  ( $i, j = 1, 2, 3$ ) the components of stress tensor. The von Mises stress is commonly used as a yielding criterion rather than a real stress and is normalized with respect to the volume of the system in this paper. Besides, the effective stress  $\sigma_e$  is calculated as:



$$\sigma_e = \frac{\sum_{i=1}^N \sigma_{v,i}}{N} \quad (7)$$

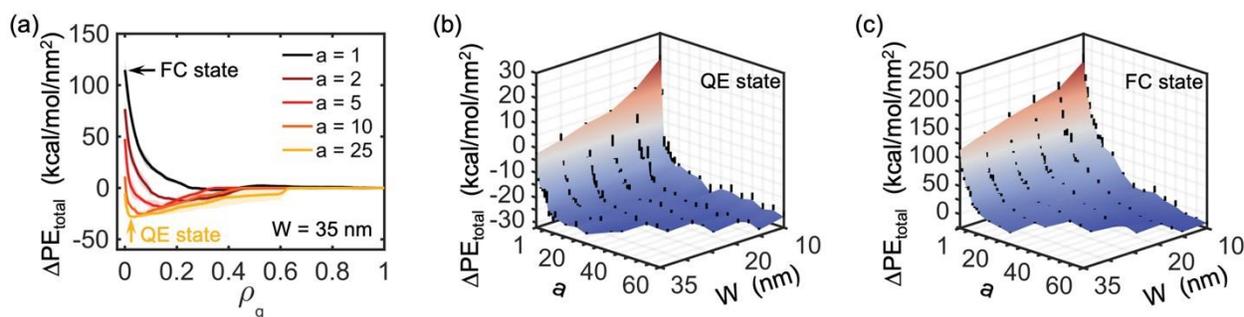
where  $\sigma_{v,i}$  is the von Mises stress of the  $i^{\text{th}}$  bead with local curvature satisfying  $K \geq 0.1 \text{ \AA}^{-1}$ ;  $N$  is the total number of beads with  $K \geq 0.1 \text{ \AA}^{-1}$  in the crumpled model. The threshold  $K \geq 0.1 \text{ \AA}^{-1}$  is selected to isolate highly crumpled regions that dominate internal stress accumulation, while minimizing contributions from nearly flat areas that are mechanically inactive. This curvature-based filtering approach is consistent with prior observations that link high local curvature to stress concentration in crumpled 2D materials.<sup>71</sup>

### 3. Results and discussion

#### 3.1. Potential energy evolution upon crumpling

We first explore the total potential energy change during the crumpling process for GNRs with different width  $W$  and aspect ratio  $a$ , aiming to better understand the influence of geometry on the crumpling behavior of GNRs at the molecular level.  $\Delta PE_{\text{total}}$  considered in Fig. 2 is the total potential energy increment per unit area of the GNR, defined as  $\Delta PE_{\text{total}} = (PE - PE_{\text{initial}})/A$ , where  $A$  is the surface area of the flat GNR, and  $PE$  and  $PE_{\text{initial}}$  are the total potential energy of the system during the crumpling process and in IW state, respectively. Moreover, we introduce the compaction ratio  $\rho_g$  to describe the degree of crumpling of GNRs. Note that  $\rho_g$  decreases from a value of 1 in the IW state to 0 in the FC state during the crumpling process, and thus a smaller  $\rho_g$  corresponds to a more compacted crumpled system.





**Fig. 2** Total potential energy increment of crumpled GNRs in different states. (a) Evolution of change of the total potential energy increment per unit area  $\Delta PE_{\text{total}}$  with the compaction ratio  $\rho_g$  for GNRs ( $W = 35$  nm) having different aspect ratios ranging from 1 to 25. The orange and black arrows exemplify the quasi-equilibrium state (QE state) and the FC state of the GNR during the crumpling process, respectively. Shaded areas correspond to the standard deviation from three independent crumpling simulations for each specific case.  $\Delta PE_{\text{total}}$  of the crumpled GNRs in the (b) QE state and (c) FC state as a function of width  $W$  and aspect ratio  $a$ , respectively. The black line indicates the standard deviation.

Fig. 2(a) shows the evolution of  $\Delta PE_{\text{total}}$  for GNRs ( $W = 35$  nm) with different  $a$  during the crumpling process. It can be found that the GNRs of different  $a$  all have relatively steady  $\Delta PE_{\text{total}}$  at the beginning of the crumpling as none of the GNRs have formed the sharp fundamental crumples (e.g., folds, bends, developable cones, and stretching ridges) at this early stage.<sup>34,36,72</sup> In the intermediate stage of the crumpling,  $\Delta PE_{\text{total}}$  of GNRs with large  $a$  (e.g.,  $a = 10$  and  $a = 25$ ) drop significantly to reach a valley, and this process is mainly influenced by the self-adhering and self-folding behaviors of the system.<sup>40,73</sup> Subsequently,  $\Delta PE_{\text{total}}$  of all GNRs increases dramatically at the later stage of the crumpling, which can be explained by the fact that the sheet is further compacted, causing the potential energy of the system to increase sharply.<sup>34</sup> In addition



to the final crumpled (FC) state, we define the quasi-equilibrium state (QE state) of the crumpled GNR as the state of the system when  $\Delta PE_{\text{total}}$  reaches a local minimum trough, at which the self-adhering and self-folding behaviors of the GNR basically saturate.<sup>44</sup> As observed in Fig. 2(a),  $\rho_g$  of GNRs at the QE state decreases with the increase of  $a$ .

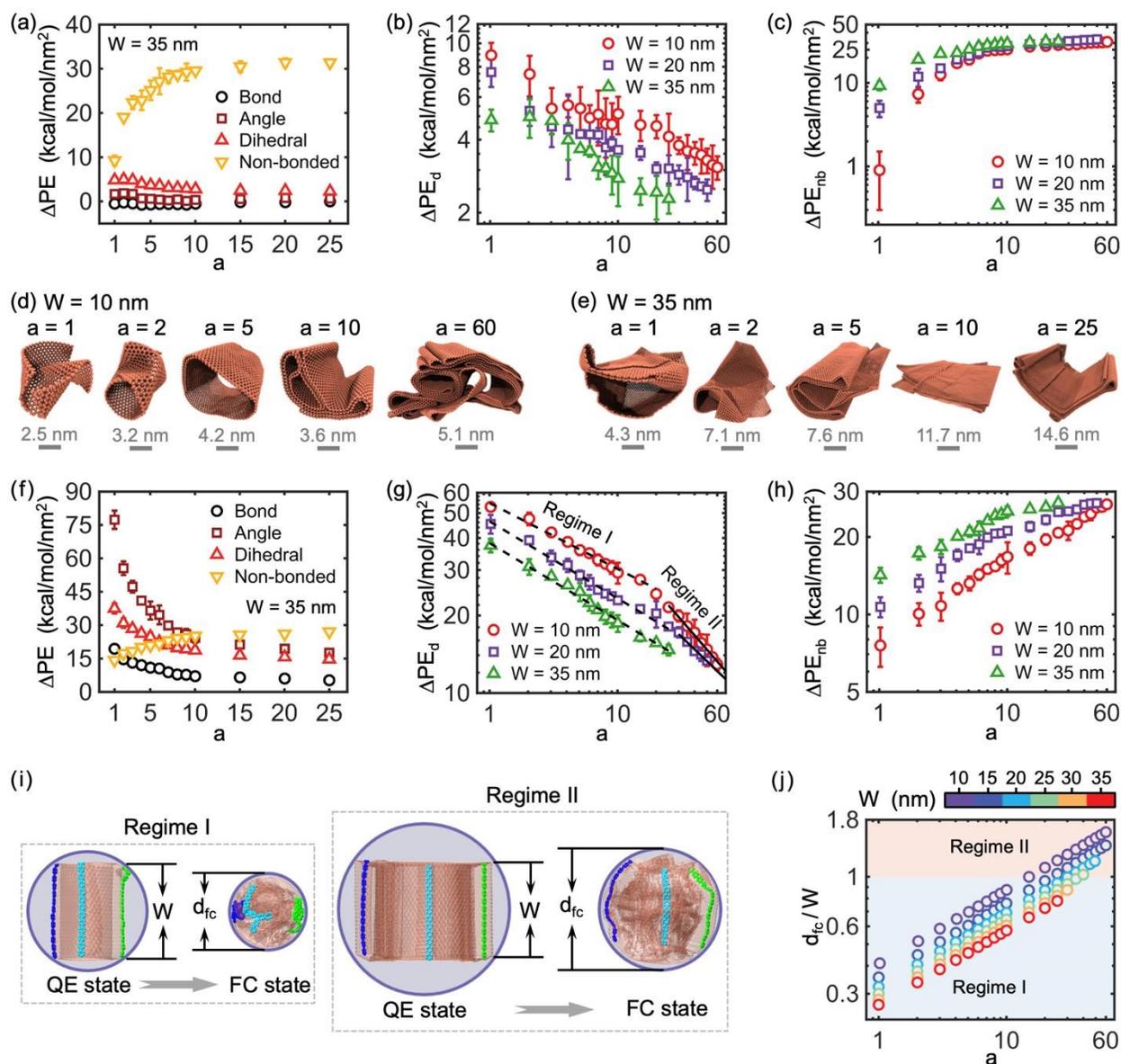
Moreover, we analyze the effect of  $W$  and  $a$  on  $\Delta PE_{\text{total}}$  of crumpled GNRs in the QE state (Fig. 2(b)) and FC state (Fig. 2(c)). Clearly,  $\Delta PE_{\text{total}}$  in both states decreases with the increase of  $W$  and  $a$ . This is attributed to the significant self-adhering and self-folding behaviors of GNRs with large sizes that fold more easily upon crumpling compared to small sizes, resulting in a low total potential energy of the system.<sup>34,74</sup> This trend is further supported by the localization factor calculated for the GNRs in the QE state, which increases with both  $W$  and  $a$ , indicating the formation of more extensive and localized interfacial contact in larger GNRs (Fig. S6 in the Supporting Information). Meanwhile, Fig. 2(c) reveals that the GNRs with large width and large aspect ratio are easier to be compacted and crumpled into a spherical shape as less energy is required.

To gain further insights, we analyze the contribution of bond, angle, dihedral, and pairwise non-bonded potential energies characterizing the in-plane deformation, out-of-plane deformation, and adhesion properties of the model, respectively, to the total potential energy increment of the crumpled GNRs. In our CG model, in-plane deformation is primarily governed by bond and angle energies, while out-of-plane deformation is captured by the dihedral energy contribution.<sup>53</sup> Taking the crumpled GNRs with  $W = 35$  nm as a representative case, as shown in Fig. 3(a), increasing  $a$  has no marked influence on the bond and angle potential energies of the system in the QE state; however, the dihedral and non-bonded potential energies decrease slightly and increase significantly with increasing  $a$ , respectively; these trends are more pronounced when  $a$  becomes



smaller. In addition, the crumpled GNRs with larger  $W$  have relatively smaller dihedral potential energy  $\Delta PE_d$  (Fig. 3(b)) and larger non-bonded potential energy  $\Delta PE_{nb}$  (Fig. 3(c)) in comparison with those with small  $W$ . According to the representative configurations of GNRs in the QE state in Fig. 3(d) and (e), it can be observed that, firstly, the GNRs with large  $a$  tend to develop scroll-like lamellar structures in the QE state and therefore have relatively large adhesion energy, while GNRs with smaller  $a$  tend to form comparatively more sharp crumples (e.g., developable cones), and thus have large out-of-plane deformation potential energy. Secondly, the GNRs with large  $W$  form more planar regions and less crumpled regions than those with small  $W$ , resulting in larger  $\Delta PE_{nb}$  and smaller  $\Delta PE_d$ . The analysis of the configuration of crumpled GNRs in the QE state corroborates the previously reported configuration evolution of GNRs in the lowest energy state, i.e., the GNRs transform from a bent-folded configuration to a rolled structure as the length increases.<sup>75</sup>





**Fig. 3** Contribution of the total potential energy increment for crumpled GNRs and two crumpling regimes of GNRs from the QE state to the FC state. (a) The contribution of the total potential energy increment  $\Delta PE$  as a function of the aspect ratio  $a$  for GNRs with  $W = 35$  nm in the QE state. Here, the contributions of the bond, angle, dihedral, and pairwise non-bonded interactions to the total potential energy increment are analyzed. The non-bonded potential energy is taken in absolute value. Relationship between (b) the dihedral potential energy increment  $\Delta PE_d$ , and (c) the pairwise non-bonded potential energy increment  $\Delta PE_{nb}$  with respect to  $a$  for crumpled GNRs



with different widths in the QE state. Representative configurations of crumpled GNRs with (d)  $W = 10$  nm and (e)  $W = 35$  nm and different  $a$  in the QE state. The gray line represents the scale bar. (f)  $\Delta PE$  as a function of  $a$  for GNRs with  $W = 35$  nm in the FC state. Relationship between (g)  $\Delta PE_d$ , and (h)  $\Delta PE_{nb}$  with respect to  $a$  for crumpled GNRs with different widths in the FC state. The black dashed and solid lines indicate the power function fittings. (i) Illustration of two distinct regimes of crumpled GNRs from the QE state to the FC state. In regime I, the diameter  $d_{fc}$  of the crumpled GNR in the FC state is smaller than the width  $W$  of the GNR, while in regime II,  $d_{fc}$  is larger than  $W$ . As examples, the blue, cyan, and green colors emphasize the configuration of the strip lattices along the width direction of GNRs in the QE and FC states, respectively. (j) The ratio  $d_{fc}/W$  of GNRs of different  $W$  as a function of  $a$ .

Fig. 3(f)-(h) show the total potential energy increment contribution of GNRs in the FC state, where the GNRs form highly crumpled spherical structures. It can be found that all the potential energies are negatively correlated with  $a$  except for the non-bonded potential energy of the system which is positively correlated with  $a$ , and the increase of  $W$  leads to smaller  $\Delta PE_d$  and larger  $\Delta PE_{nb}$ . Similar to the QE state, increasing the  $a$  and  $W$  of GNRs enables the system in the FC state to have more laminated structures while causing a relative decrease in the sharp crumples formed per unit area, resulting in an increase and decrease in the adhesion energy and out-of-plane strain energy of the system, respectively. Interestingly, for the adhesion energy ( $\Delta PE_{nb}$ ) of the system in the QE and FC states (Fig. 3(c) and (h)), it has different rates of change for small and large  $a$ , which is relevant to the internal laminar structure of the crumpled GNRs. In particular, the adhesion energy reaches a saturation state when  $a$  is large enough in the QE state (Fig. 3(c)). Furthermore, it is meaningful to introduce two different crumpling regimes of scroll-like crumpled



GNRs in the late crumpling process (from QE state to FC state) defined based on the sheet width and the diameter of the system in the FC state ( $d_{fc}$ ). As shown in Fig. 3(i), the further compaction makes the lattice along the width direction of the system (as examples, the strip lattices emphasized by blue, cyan, and green colors) undergo significant fold deformation as  $d_{fc} < W$  (i.e., regime I), while only slight bending of the lattice along the width direction appears when  $d_{fc} > W$  (i.e., regime II). Note that the ratio  $d_{fc}/W$  as a function of  $a$  for all the GNR models studied in this study is presented in Fig. 3(j). One can note that in different regimes, the lattices of the crumpled GNRs have different levels of folding, which affects the out-of-plane deformation energy of the whole system, making the  $\Delta PE_d$  about  $a$  of the system decrease at different rates in the FC state (see the different fitted lines in Fig. 3(g)). In general, the geometry of graphene nanoribbons controls the potential energy of the system by influencing its internal structures, e.g., sharp crumples and scroll-like laminated structures. The above analysis helps us to gain a deeper understanding of the contribution of various potential energies in the crumpled GNRs.

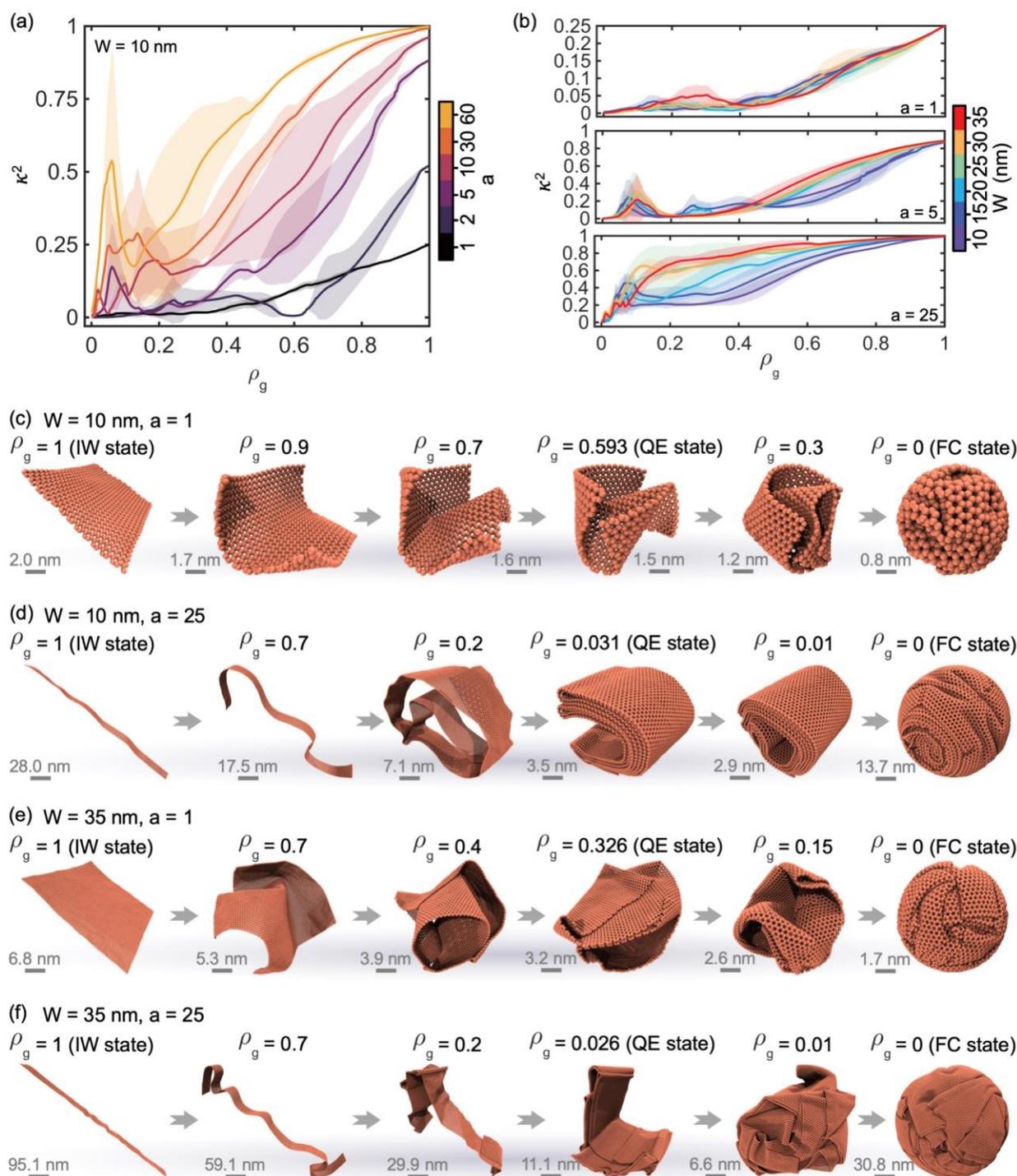
### 3.2. Shape descriptor of crumpled structures

Evaluating the shape descriptor, i.e., relative shape anisotropy  $\kappa^2$ , of GNRs during the crumpling process helps us to better characterize the effect of geometry on the structural features of the system.  $\kappa^2$  is commonly adopted to describe characteristics such as symmetry and dimensionality of the structure and ranges from 0 to 1.<sup>56,76,77</sup> In particular,  $\kappa^2$  is equal to 1, 0.25, and 0 for ideal straight rod, ideal symmetrical flat sheet, and ideal spherical structures, respectively. Fig. 4(a) and (b) exhibits the evolution of  $\kappa^2$  with decreasing compaction ratio  $\rho_g$  for crumpled GNRs with different width  $W$  and aspect ratio  $a$ , and Fig. 4(c)-(f) shows the representative configurations of



the models during the crumpling process. As shown in Fig. 4(a), increasing  $a$  raises  $\kappa^2$  of the GNRs ( $W = 10$  nm) at  $\rho_g = 1$  (IW state), suggesting that, in comparison to a square sheet ( $a = 1$ ), the larger the  $a$ , the more the system tends to the ideal rod shape at this state (Fig. 4(c) and (d)). Moreover,  $\kappa^2$  of all cases shows a decreasing trend as the crumpling proceeds, and the larger the  $a$ , the smaller the  $\rho_g$  of the system compacted into a planar-like structure ( $\kappa^2 \approx 0.25$ ). The continuous compaction causes the crumpled GNRs showing a tendency to shift toward the rod-like configuration, which is known from the rebounded  $\kappa^2$  when  $0.07 \lesssim \rho_g \lesssim 0.2$ , and the system with larger  $a$  has a larger increase in  $\kappa^2$ . This is mainly due to the adhesion energy that allows systems with large  $a$  more prone to exhibit self-adhering and self-folding behaviors, forming scroll-like laminar structures and making their  $\kappa^2$  rebound (Fig. 4(d)). Further compaction leads all systems to a sphere-like crumpled structure ( $\kappa^2 \approx 0$ ).  $\kappa^2$  of GNRs with large  $a$  is overall larger than that of GNRs with small  $a$  during the crumpling process.





**Fig. 4** Shape descriptor and representative configurations of GNRs during crumpling process. The relative shape anisotropy  $\kappa^2$  as a function of the compaction ratio  $\rho_g$  for GNRs with (a)  $W = 10$  nm having different aspect ratio  $a$ , and (b)  $a = 1, 5, 25$ , respectively, having different  $W$ .



Shaded areas of the curves correspond to the standard deviation. Representative configurations of crumpled GNRs for different compaction ratios ranging from 0 to 1 with (c)  $W = 10$  nm and  $a = 1$ , (d)  $W = 10$  nm and  $a = 25$ , (e)  $W = 35$  nm and  $a = 1$ , and (f)  $W = 35$  nm and  $a = 25$ . The gray arrow indicates the process of crumpling from the IW state to the QE state and then to the FC state. The gray line represents the scale bar for the configuration size.

Meanwhile, the analysis of the effect of width on  $\kappa^2$  evolution reveals that the increase in  $W$  for square graphene nanosheets ( $a = 1$ ) makes the  $\kappa^2$  of the system rebound significantly at the late stage of the crumpling, as shown in Fig. 4(b). This can be attributed to the fact that graphene sheets with large  $W$  form relatively more planar regions (e.g., QE state in Fig. 4(c) and (e)) under the effect of adhesion energy, which affects  $\kappa^2$ . However, for GNRs with larger  $a$ , especially when  $a = 25$  shown in Fig. 4(b), the increase in width allows the system to have a highly rod-like conformation during the crumpling process, and a laminated structure is developed at the late stage of the crumpling (Fig. 4(f)). Overall, the GNRs of small  $W$  and  $a$  tend to form bent structures that occupy 3D space upon crumpling, and their  $\kappa^2$  curves have no apparent rebound.<sup>34</sup> In contrast, GNRs with large  $W$  and  $a$  commonly exhibit remarkable self-adhering and self-folding behaviors,<sup>40</sup> making their crumpled configurations tend to be laminated rod-like with relatively large  $\kappa^2$ .

The analysis of the crumpling process of GNRs with different geometries reveals two distinct crumpling modes. In general, the GNRs with small aspect ratios are first bent up out-of-plane on all four edges upon crumpling, and then the developed crumpled structures occupying 3D space are further compacted into crumpled spheres (Fig. 4(c) and (e)). Based on this observation, we classify the crumpling mode of GNRs with small aspect ratio as the edge bending dominated (EBD)



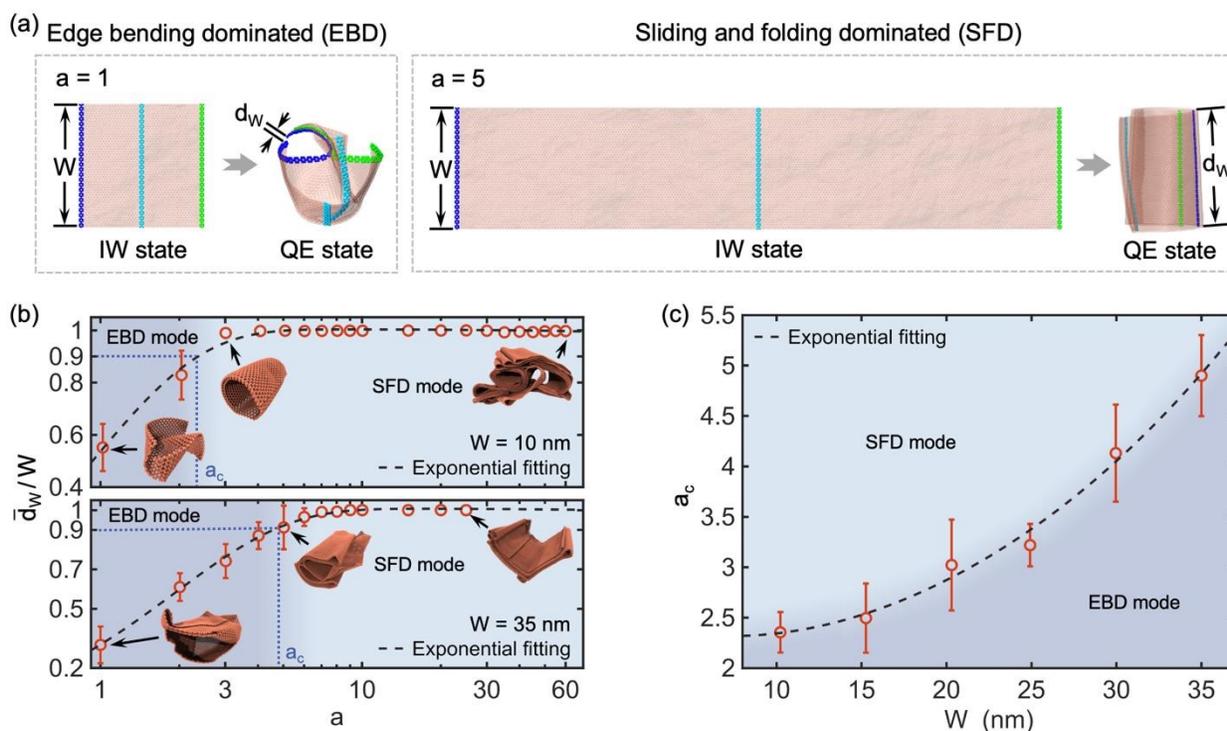
crumpling mode. Moreover, as the aspect ratio is sufficiently large, GNRs tend to bend and wrinkle along the length direction under the action of the confining sphere, followed by local sliding and self-folding due to adhesion and forming scroll-like laminated structures, and finally the GNRs are compacted into spherical crumpled structures (Fig. 4(d) and (f)). This crumpling mode of GNRs with large aspect ratios is classified as the sliding and folding dominated (SFD) crumpling mode. We can trace the mechanical mechanisms of the above two crumpling modes from the previous studies.<sup>78</sup> Specifically, for EBD crumpling mode (corresponding to GNRs with small aspect ratios), the strain in the corner region of GNRs is larger than that in the middle region, and the corners buckle first under compression, followed by buckling in the middle regions. For SFD crumpling mode (corresponding to GNRs with large aspect ratios), the distance from the corners to the middle of the edges in the width direction is shorter, and their buckling is synchronized, so that buckling along the length direction is developed under compression to form a rolled structure. Understanding these two crumpling modes will provide deeper insights into the crumpling behavior and structural features of GNRs. Therefore, it is essential to study the transition between these two crumpling modes.

### 3.3. Transition of crumpling modes.

To determine the transition between EBD crumpling mode and SFD crumpling mode, we introduce a parameter  $\bar{d}_W/W$  that characterizes these two crumpling modes. Here,  $\bar{d}_W$  is the average distance between the upper and lower edges of the crumpled GNRs, and  $\bar{d}_W \approx W$  for the system in the IW state. In the EBD crumpling mode, the four edges of the crumpled GNRs bend upward in the QE state, resulting in  $\bar{d}_W/W < 1$ . Conversely, the crumpled GNRs in the SFD crumpling mode have  $\bar{d}_W/W \approx 1$  in the QE state, which is attributed to the fact that the system



forms scroll-like laminated structure in the QE state without significant deformation along the width direction. As shown in Fig. 5(a), the crumpled systems (QE state) with EBD crumpling mode and SFD crumpling mode satisfy  $d_W < W$  and  $d_W \approx W$ , respectively, where  $d_W$  is the distance between the two ends of the highlighted strip lattices. The analysis of the effect of  $a$  on  $\bar{d}_W/W$  in Fig. 5(b) reveals that  $\bar{d}_W/W$  increases first with increasing  $a$  and then reaches a constant value of 1, following an exponential evolution relationship with  $a$ . Here, we define that the system experiences EBD crumpling mode when  $\bar{d}_W/W < 0.9$  and SFD crumpling mode when  $\bar{d}_W/W \geq 0.9$ . Thus, we can obtain the critical aspect ratio  $a_c$  for the transition from EBD crumpling mode to SFD crumpling mode, and  $a_c$  increases with increasing  $W$  (Fig. 5(b)).



**Fig. 5** Two distinct crumpling modes of GNRs. (a) Illustration of two crumpling modes, i.e., edge bending dominated (EBD) crumpling mode, and sliding and folding dominated (SFD) crumpling mode. As examples, the blue, cyan, and green colors emphasize the configuration of the strip



lattices of GNRs along the width direction. These highlighted strip lattices have endpoint spacings (i.e., the distance between the upper and lower edges) of  $W$  and  $d_W$  in the IW and QE states, respectively. (b) The average distance between the upper and lower edges  $\bar{d}_W$  (normalized by  $W$ ) as a function of aspect ratio  $a$  of the crumpled GNRs with  $W = 10$  nm and  $W = 35$  nm, respectively, in the QE state. The blue dotted lines denote the critical aspect ratio  $a_c$ . (c) Change in critical aspect ratio  $a_c$  as a function of sheet width  $W$ . The black dashed lines in (b) and (c) indicate the exponential fitting.

Remarkably, the evolution of the critical aspect ratio with respect to the sheet width is obtained in this work, as shown in Fig. 5(c). The relationship between  $a_c$  and  $W$  can be described by the exponential function:

$$a_c = b_1 e^{b_2 W} + d_1 e^{d_2 W} \quad (8)$$

where  $b_1 = 1.431 \pm 6.969$ ,  $b_2 = -0.0818 \pm 1.170$ ,  $d_1 = 1.131 \pm 4.473$ , and  $d_2 = 0.0415 \pm 0.097$  are adjustable constant coefficients from the fitting ( $R^2 = 0.9903$ ). Notably, the GNRs exhibit the EBD crumpling mode when  $a < a_c$ , while they show the SFD crumpling mode when  $a > a_c$ . It is of significance to explore the crumpling modes of GNRs since different modes inevitably lead to different internal crumpled patterns. The above analyses allow us to have more in-depth simulation-based insights for predicting the crumpled structure of GNRs.

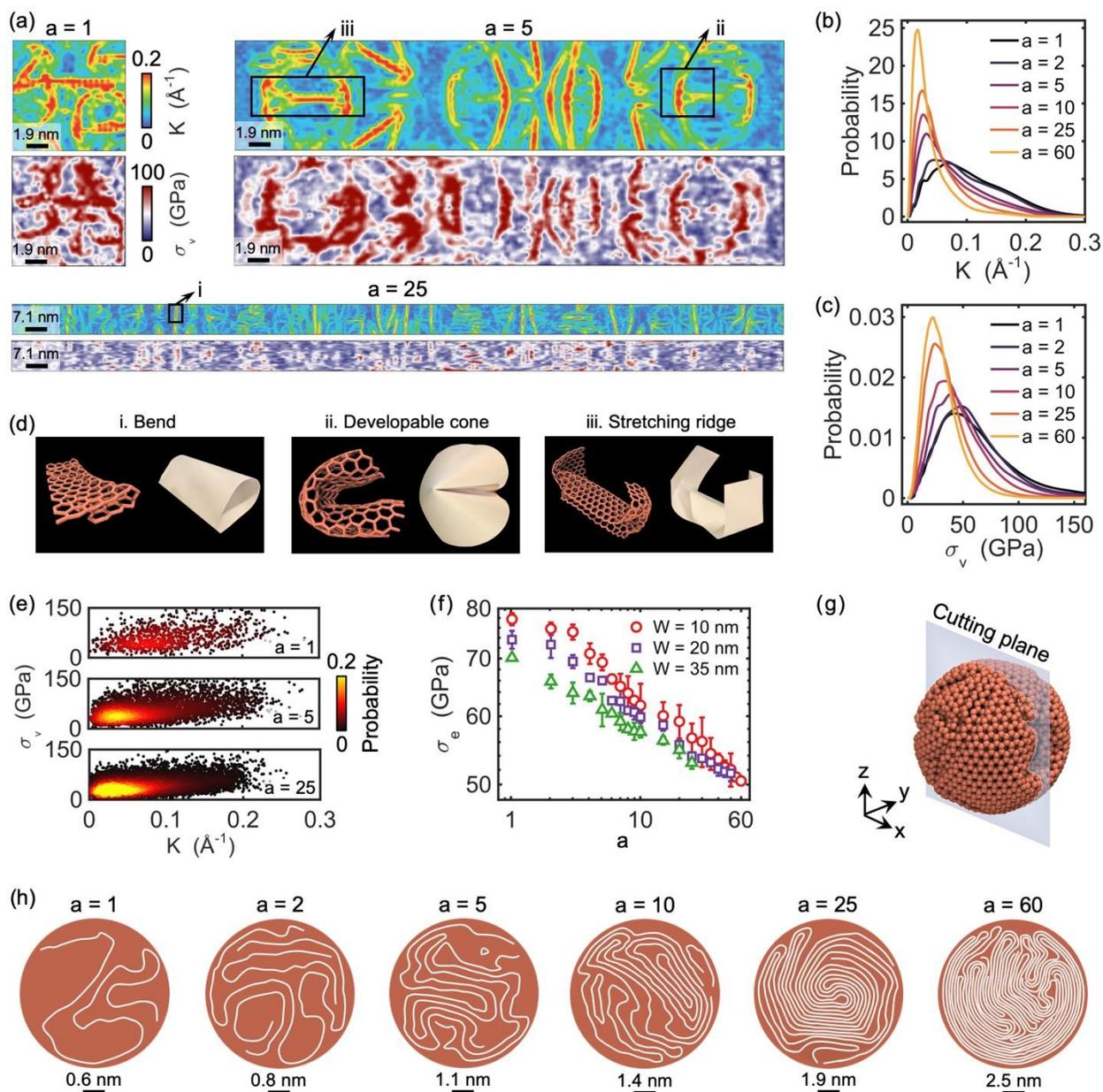
### 3.4. Mechanical heterogeneity

To facilitate a better understanding of the internal structure of the crumpled GNRs and provide insights into their mechanical states, we proceed to analyze the local curvature  $K$ , local von Mises



stress  $\sigma_v$ , effective stress  $\sigma_e$ , and cross-section patterns of the crumpled GNRs in FC state. Fig. 6(a)-(c) show the distributions of  $K$  and  $\sigma_v$  as well as their probability profiles of the crumpled GNRs with  $W = 10$  nm and different aspect ratio  $a$ . Here,  $K$  and  $\sigma_v$  are mapped to a 2D planar model for better visualization. It can be observed that the high curvature regions correspond to the high stress regions for all cases (Fig. 6(a)); the peaks of the probability distributions of  $K$  and  $\sigma_v$  (skewed Gaussian distributions) tend to increase and shift to smaller  $K$  and  $\sigma_v$  as  $a$  increases, and their distributions become concentrated and narrower, which implies that the degree of mechanical heterogeneity of the crumpled GNRs decreases with the increase of  $a$  (Fig. 6(b) and (c)). These curvature distribution profiles also serve as the basis for a principal component analysis (PCA) to quantitatively classify the crumpled morphologies (Fig. S7 in the Supporting Information). Moreover, the heterogeneous stress distributions observed in Fig. 6(a) are mainly attributed to the fundamental building blocks that constitute the crumpled system,<sup>36,42</sup> such as bends, developable cones, and stretching ridges, as shown in Fig. 6(d). Briefly, the fundamental structures constituting the crumpled GNRs are mostly developable cones and stretching ridges when  $a$  is small (see  $a = 1$  and  $5$  in Fig. 6(a)); for larger  $a$ , such as  $a = 25$ , the internal structures are mostly bends as GNRs form scroll-like laminated structures through the SFD crumpling mode (Fig. 6(a) and Fig. 5(c)). That is, the sharp crumples raise the stress heterogeneity of the system. Fig. 6(e) shows the distribution of  $K$  versus  $\sigma_v$  for the crumpled GNRs ( $W = 10$  nm) with different aspect ratios. It can be verified that the overall  $K$  and  $\sigma_v$  are smaller for the crumpled system with larger  $a$ ;  $K$  and  $\sigma_v$  maintain a certain correlation, i.e., small  $K$  corresponds to small  $\sigma_v$  and large  $K$  corresponds to large  $\sigma_v$ .





**Fig. 6** Mechanical state of crumpled GNRs in the FC state. (a) Maps of the local curvature  $K$  and local von Mises stress  $\sigma_v$  distributions for crumpled GNRs ( $W = 10$  nm) with aspect ratio  $a = 1, 5$ , and  $25$ , respectively. Probability distribution of (b)  $K$  and (c)  $\sigma_v$  for crumpled GNRs having various  $a$ . (d) Representative configurations of the three fundamental building blocks found in crumpled GNRs ( $W = 10$  nm), i.e., bend, developable cone, and stretching ridge, which are recreated by origami. These three representative configurations are sequentially located in the



rectangular regions i, ii, and iii in panel (a). (e) Distribution of  $K$  versus  $\sigma_v$  for crumpled GNRs ( $W = 10$  nm) with  $a = 1, 5,$  and  $25,$  respectively. (f) The effective stress  $\sigma_e$  as a function of  $a$  for crumpled GNRs having different  $W$ . (g) Schematic for analyzing the cross-section pattern of the crumpled GNR. The cutting plane passes the center of mass of the model and is perpendicular to the  $y$ -axis. (h) The cross-section patterns for crumpled GNRs having various  $a$ . Here, the black line represents the scale bar.

Fig. 6(f) presents the power-law scaling relationship between  $\sigma_e$  and  $a$  for crumpled GNRs with different widths. Here,  $\sigma_e$  is defined as the average of the von Mises stresses of all CG beads with curvature greater or equal to  $0.1 \text{ \AA}^{-1}$ . It is evident that  $\sigma_e$  decreases approximately linearly with increasing  $a$  and that the width of the sheet is negatively related to  $\sigma_e$ . This can be explained by the fact that sharp crumples (e.g., developable cones and stretching ridges), commonly observed in crumpled GNRs with relatively small widths and aspect ratios, possess higher stresses, whereas crumpled GNRs with larger initial sizes have comparatively low stresses due to their internal structures, which are mainly composed of bends.<sup>36</sup> We point out here that the effective stress is somehow positively correlated with the mechanical properties (e.g., bulk modulus and effective compressive modulus) of the crumpled system.

To gain a deeper understanding into the effect of aspect ratio on the internal structure of crumpled system, we analyze the cross-section patterns of the crumpled GNRs ( $W = 10$  nm) with various aspect ratios by cutting the models with the virtual cutting plane (Fig. 6(g)). From Fig. 6(h), it can be found that the cross-section of the crumpled GNRs with small aspect ratio (e.g.,  $a = 1$  and  $2$ ) shows a disordered folding pattern, which is due to the EBD crumpling mode that the



system possesses ( $a < a_c$ ). However, for the systems with large aspect ratios (e.g.,  $a = 25$  and  $60$ ), the cross-section exhibits a scroll-like laminated and highly ordered pattern, which is attributed to the SFD crumpling mode of the system ( $a > a_c$ ). In addition, although some systems (e.g.,  $a = 5$  and  $10$ ) possess SFD crumpling mode, their cross-sections exhibit a relatively disordered layered pattern, and this is because the crumpling process of the systems being compacted from the QE state to the FC state falls into regime I ( $d_{fc} < W$ ), making the scroll-like laminated structures highly squeezed and deformed (see Fig. 3(i) and (j)). Overall, the increase of aspect ratio can improve the structural ordering and packing of crumpled GNRs.

#### 4. Conclusions

In the present study, we investigated the crumpling behavior of graphene nanoribbons (GNRs) via CG-MD simulations by systematically varying the width of GNRs and their aspect ratio at fixed sheet width. Our findings reveal that at the molecular level, the geometries of GNRs strongly impact several key aspects, including their potential energy, configuration, mechanical state, and internal structure. Specifically, the total potential energy per unit area of GNRs decreases with the increase of their width and aspect ratio in the intermediate and late stages of the crumpling process, attributed to enhanced self-adhering and self-folding behaviors for larger GNRs. Analyses of the total potential energy contribution indicates that smaller sheets tend to form more sharp crumples with higher dihedral energy that characterizes the out-of-plane deformation properties, whereas larger GNRs develop more planar regions due to the self-adhering and self-folding behaviors, leading to higher adhesion energy. By systematically evaluating the relative shape anisotropy and conformational features, we identify two aspect ratio-dependent crumpling modes for GNRs: the edge-bending dominated (EBD) mode for smaller aspect ratios, and the sliding and folding



dominated (SFD) mode for larger aspect ratios. The investigation of the transition between these two crumpling modes determines width-dependent critical aspect ratio, offering insights for design of crumpled graphene nanostructures. Remarkably, increasing the aspect ratio of the crumpled GNRs reduces the mechanical heterogeneity and effective stress, facilitating the compact formation of crumpled structures. Furthermore, the analysis of cross-section patterns highlights the shift in the internal structures of the crumpled systems from disordered crumples to ordered scroll-like laminated structures as the aspect ratio increases. Our study highlights the critical role of geometry (i.e., width and aspect ratio) in shaping the crumpling dynamics of GNRs, facilitating the tailored design of ribbon-like materials.

### **Author contributions**

Yangchao Liao: methodology, software, formal analysis, validation, writing - original draft, writing - review & editing. Long Chen: software, formal analysis, validation, writing - review & editing. Wenjie Xia: conceptualization, supervision, project administration, funding acquisition, resources, writing - review & editing.

### **Data availability**

The data that support the findings of this study are available upon reasonable request from the authors.

### **Conflicts of interest**



The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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## Data Availability Statement

All the data that support the findings of this study are included within the article.

