

Cite this: *Chem. Sci.*, 2025, 16, 4469

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On the nature of the triplet electronic states of naphthalene dimers†

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Elucidating the photophysical mechanisms within multi-chromophore assembly (MCA) is essential for many key technological and biological processes. Although it has been established that one of the most important photoactivated applications of MCA is intimately linked to efficient intersystem crossing (ISC) to triplet states and the interplay between delocalized/localized triplet excited states, the underlying mechanism between such equilibrium and the observed optical properties remains elusive. Herein, four suitably designed dinaphthyl compounds, covalently bonded in a face-to-face configuration and encompassing the primary possible stacking geometries, were prepared and their triplet state properties investigated by combining transient absorption spectroscopy experiments with quantum chemistry calculations. Our results offer direct evidence of both localized and delocalized triplet states, with the most stable and long-lived triplet state consistently localized on a single naphthalene unit, irrespective of the stacking configuration. Moreover, depending on the stacking geometry, even if localized, the triplet transient absorption spectrum was demonstrated to be significantly different from that of an isolated naphthalene.

Received 25th November 2024

Accepted 27th January 2025

DOI: 10.1039/d4sc07982e

rsc.li/chemical-science

1 Introduction

The triplet electronic states of aggregates containing many interacting chromophores (hereafter, generically, multi-chromophore assembly, MCA) have been unequivocally demonstrated to hold paramount significance in a multitude of biological processes^{1–3} and technological advancements.^{4–8} In particular, these applications are attributed to the direct involvement and regulation of triplet states among different molecular processes in MCA, such as phosphorescence,⁹ triplet–triplet annihilation,^{10–12} delayed fluorescence,^{13,14} triplet energy transfer,¹⁵ or circularly polarized luminescence (CPL).^{16,17} Consequently, any enhancement in our comprehension of the

nature and properties of the MCA triplet states is of critical importance. In this field, naphthalene dimers have emerged as an extremely interesting model system,^{18–39} as prototypes of a very important family of compounds, polyacenes,^{40–42} that are promising components for optoelectronic devices.^{43–46} In the last two decades the nature and the properties of the lowest energy triplet electronic states of the dimers composed of two units of naphthalene (or some of its derivatives) have been, indeed, quite intensively debated. Firstly, several experimental studies^{28,30–33,47} showed that the lowest energy triplet state in different dinaphthyl compounds has spectral properties (for example its phosphorescence energy) different from those of the naphthalene triplet and suggested that it was an ‘excimer’. Several computational studies^{20,24,36} proposed that the excimer triplet, characterized by a dimerization energy substantially larger than that of the ground state,⁴⁸ is delocalized over the two moieties. The existence of a triplet excimer in dinaphthyl has been criticized, and the related red-shifted phosphorescence attributed to impurities.²⁵ Secondly, additional controversies arose concerning the preferential geometries adopted by the triplet excimer (e.g. face-to-face, in the following f2f, bent, T-shape etc.).^{24,36} The scarcity of experimental results has been an important bottleneck, preventing a firm assessment of these issues. For example, the absence of ‘excimer-like’ phosphorescence does not allow their presence to be ruled out, since for a perfectly parallel face-to-face structure it is forbidden by symmetry.³² Moreover, the results obtained on covalently bonded dimers are not easily generalized, since not only their

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† Electronic supplementary information (ESI) available. CCDC 2405198, 2405200, 2405201, and 2405218. For ESI and crystallographic data in CIF or other electronic format see DOI: <https://doi.org/10.1039/d4sc07982e>

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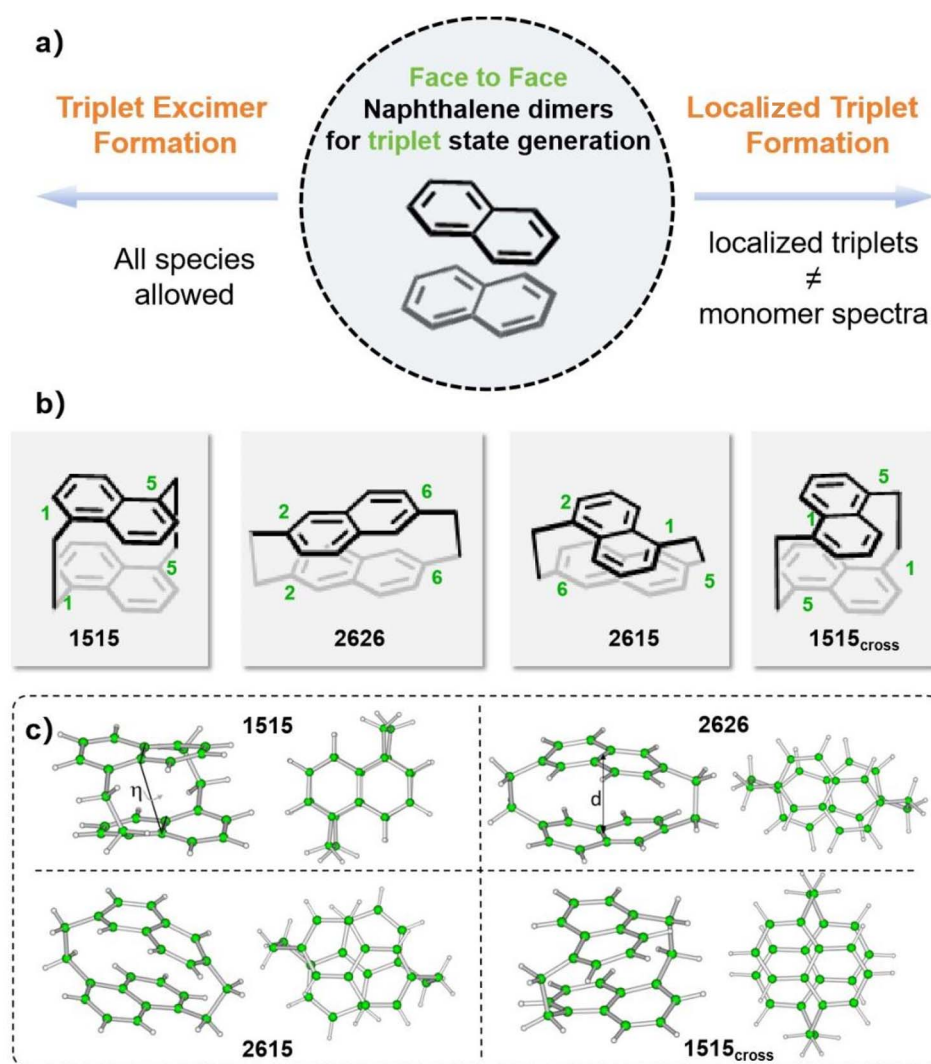
structural restraints can have an overwhelming effect on the nature of the triplet minima,³¹ but the substituents (*e.g.* carbonyl groups, as in the 'Agosta' dimers)^{31,49} can also affect the electronic properties of the naphthalene moieties.

In particular, in the presence of a suitable electron donor bridge substituent, naphthalene^{50–52} and naphthalene derived molecules (as the naphthalene mono-imide (NI)^{53,54} and di-imide (NDI))⁵⁵ have been shown to be involved in very interesting (symmetry breaking) charge separation processes.^{56–58}

In order to advance the understanding of the effects ruling the behaviour of the triplet states of naphthalene dimers, we have here synthesized and characterized four different dinaphthyl compounds where two stacked naphthalenes are rigidly locked with a specific orientation by covalent bonds (Scheme 1(b)). We show that in all of them UV irradiation leads to triplet electronic states with a quantum yield (QY) ≥ 0.5 ,

which we characterize by integrating steady state and time resolved spectra and quantum mechanical calculations.

The four compounds studied all have an f2f arrangement, but they exhibit different stacking geometries and degrees of asymmetry (Scheme 1(b) and (c)), enabling a more detailed and general picture of the relationship between the structure of the dimers and the properties of their triplet electronic states to be obtained. In parallel, the same computational approach has been applied to study the interplay between the localized and delocalized triplet electronic states of 'free' naphthalene dimers in toluene solution. We show that for all the species the lowest energy triplet state is essentially localized on a single naphthalene moiety, although it can exhibit quite different spectral properties depending on the dimer, especially for the more symmetric 1515 compound. On the other hand, we find that delocalized triplet excimer minima are possible for all the species examined, *i.e.* also for stacking geometries different



Scheme 1 (a) Schematic diagram of triplet states involved in face-to-face naphthalene dimers. (b) Chemical structure of the dinaphthalene studied in this work. (c) Schematic drawing of the ground state optimized structures of the different dinaphthalene compounds. For each compound both the side (on the left) and the top (on the right) views are reported. η is the dihedral formed by the two rings, and d is the distance between the middle point of the inner C–C bonds.



from the face-to-face one. Excimer minima are disfavoured by inclusion of vibrational and entropic effects with respect to the localized one, which are characterized by shallower potential energy surfaces (PES). Finally, we show that it cannot be taken for granted that 'localized' triplets in a dimer have exactly the same spectral behaviour as the monomer, since they are affected by the presence of a closely stacked partner. Since many of these conclusions are expected to be valid also for other organic multimers, this study, besides providing fresh insights on an "old problem", provides new information on the effects that determine the properties of the triplet electronic states in closely stacked systems.

2 Results and discussion

2.1 Triplet state properties of 1515

Although the synthesis of 1515 has already been reported, its photophysical properties have never been examined in depth.^{59,60} The steady-state absorption spectrum of 1515 in dichloromethane (DCM) exhibits a low-energy absorption band centred at 285 nm (Fig. 1(a)). The emission band centered at 450 nm can be quenched by O₂ and display a significant Stokes shift relative to the absorption peak (Fig. 1(a) and (b)). Nano-second time-resolved transient absorption (TA) measurements with 285 nm excitation in N₂-saturated DCM are depicted in Fig. 2. Excitation at 285 nm results in the generation of a very broad excited state absorption (ESA) band (Fig. 2(a)), with maxima at 425 nm, 475 nm and 600 nm. In the next ~100 ns, a significant decay can be observed centered at 425 nm and 525 nm. When the time delay is 130 ns, two distinct ESA bands can be detected with maxima at 475 nm and 600 nm. Then the TA data decay to zero in ~5 μs without an apparent change in spectral shape. The TA data can be best fit with a two-

exponential decay function, yielding lifetimes of 32 ± 1 ns and 1.4 ± 0.1 μs, and the relative Decay Associated Difference Spectra (DADS) are shown in Fig. 2(b). DADS1 (blue) shows a broad band covering the entire 360–600 nm region, the dip present at 460 nm being likely associated with stimulated emission, as suggested by the steady state emission spectrum (Fig. 1(b)), suggesting DADS1 is contributed by a triplet state. DADS2 shows two ESA bands peaking at 475 nm and 600 nm. To further study the two species that survive to the nanosecond time scale, the O₂ concentrate dependent and triplet state sensitization experiments have been carried out. As shown in Fig. S1,† the lifetime of 1515 is quenched by the presence of dissolved oxygen in DCM, suggesting that the observed excited state species are likely contributed by triplet states. Moreover, triplet state sensitization experiments were carried out, employing benzophenone (Bp) as the triplet state energy donor. A wavelength of 355 nm was selected for excitation, which is specific to the excitation of Bp. As shown in Fig. S2a,† BP exhibits a triplet state spectrum with a maximum at 530 nm.^{61,62} After adding 1515, the lifetime of BP is quenched significantly in lockstep with the generation of several new bands that resemble the spectral shape of the measured TA spectra of 1515 (Fig. S2b and S3a†), confirming that these two components are associated with triplet states, which are formed with a total triplet state QY of 0.88 (Table S5†).

In Section 2.2 of the ESI† we report the TA spectra measured for 1515 in the more polar acetonitrile solvent. The DADS are very similar to those found in DCM, indicating that long-lived charge separated triplet states are not involved in the photo-activated dynamics.

In order to assign these spectra, we resorted to Quantum Mechanical (QM) calculations. We used different basis sets and density functionals (namely ωB97XD⁶³ and M052X⁶⁴), and the double hybrid B2LYPD3^{65,66} (Section 4 in the ESI†), since the latter have recently emerged as very promising tools for the calculation of the excited state properties.⁶⁷ In the following we shall use ωB97XD and B2LYPD3 as reference methods. We have performed our study both in the gas phase and in DCM solution, including a study on solvent effects using the Polarizable Continuum Model (PCM).⁶⁸ In the ESI† we discuss our approach in more detail, which is also adopted in a parallel study on the naphthalene dimer in the gas phase⁶⁹ and in the study of other closely stacked MCA.⁷⁰

We succeeded in locating the minima of two different triplet electronic states, both in the gas phase and in DCM solution, with all the adopted computational methods. In one of them, the analysis of the Molecular Orbitals (MO) and Mulliken spin densities indicates that the triplet is essentially localized over a single naphthalene moiety. In the following we shall label this excited state as T₁-loc (Fig. 3(a)). The other minimum corresponds to the 'excimer' introduced above, the triplet is equally delocalized over the two naphthalene rings (Fig. 3(b)), and we shall label it as T₁-exc (and its minimum, T₁-exc-min). In T₁-exc-min, the bond lengths are intermediate between those of a naphthalene in its lowest energy singlet or triplet state. In T₁-loc-min, instead, one of the moieties keeps the geometry of ground state singlet while the other adopts one close to that of

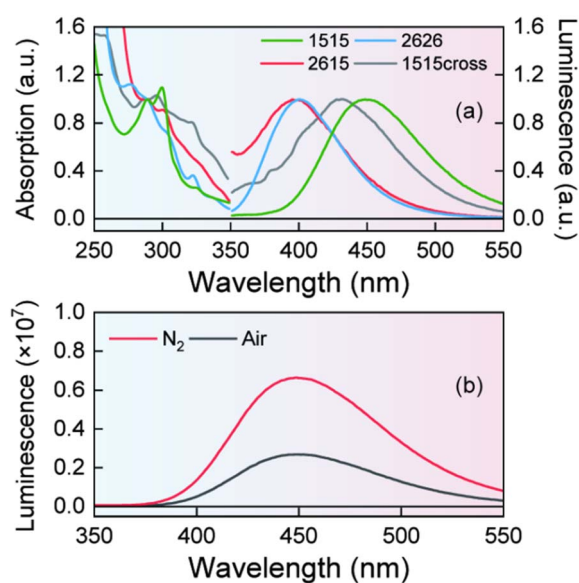


Fig. 1 (a) Steady-state absorption and emission spectra of 1515, 2626, 2615 and 1515_{cross} in DCM. (b) The emission spectrum of 1515 under N₂- and air-saturated conditions in DCM.

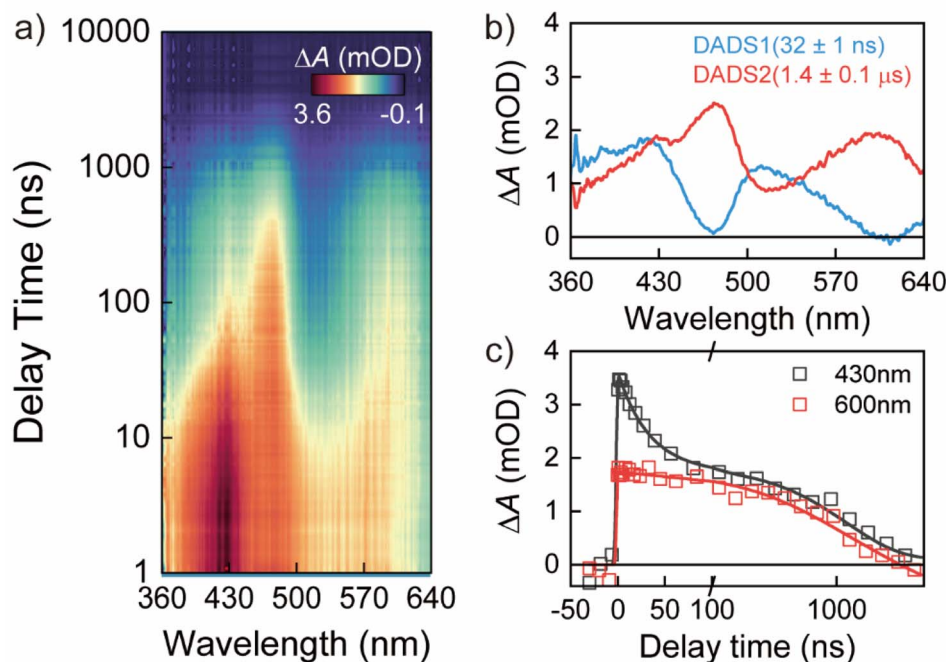


Fig. 2 (a) Nanosecond time-resolved transient absorption spectra of 1515 excited at 285 nm in DCM under N_2 -saturated conditions. (b) Decay-associated difference spectra (DADS) and (c) kinetic traces probed at 430 nm and 600 nm.

a triplet naphthalene monomer. Moreover, T_1 -exc-min is characterized by a closer approach of the two rings, $d \sim 3$ Å, with respect to the value of ~ 3.2 Å, found for S_0 -min and T_1 -loc-min (Section 4.2. in the ESI†). As collected in Table 1, all the adopted computational approaches predict that T_1 -loc-min is the most stable minimum, both in the gas phase (Section 4 in the ESI†) and in DCM. T_1 -loc-min is also relatively favoured by the inclusion of vibrational and entropic effects. Confirming the indications obtained on stacked naphthalene dimers,⁶⁹ standard density functionals underestimate the relative stability of T_1 -exc-min, whereas inclusion of the solvent effect has a negligible effect (Table S6†).

Then, we simulated the absorption spectra of T_1 -loc-min and T_1 -exc-min, by computing the excitation energies to the lowest 30 excited states at the TDA/6-31+G(d,p) level and by broadening the stick transitions with a Gaussian with a half width at half maximum of 0.25 eV. This simple procedure reproduces well the vibrationally resolved spectrum of the monomer⁶⁹ and the spectra obtained at the TD level, or by using larger basis sets, but for a weak blue-shift (10–20 nm, depending on the method) of the absorption maximum (Section 4.3.1 in the ESI†). The computed TDA/B2LYPD3/6-31+G(d,p) absorption spectra of T_1 -loc-min and T_1 -exc-min in the gas phase are shown in Fig. 4.

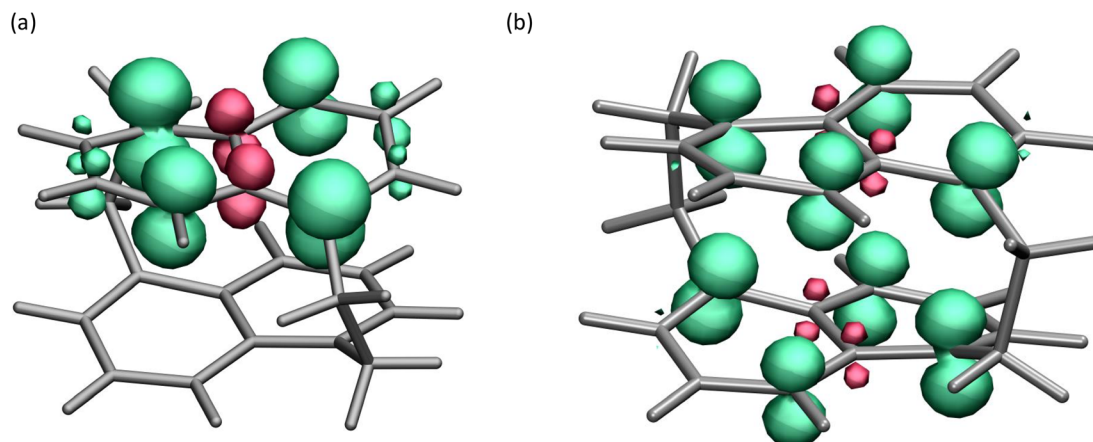


Fig. 3 Spin density computed at the B2LYPD3/6-31+G(d,p) level in the gas phase for T_1 -loc-min (a) and T_1 -exc-min (b). Color code: red, negative spin density; green, positive spin density.



Table 1 Relative energy (in eV) of T_1 -loc-min with respect to T_1 -exc-min, located for the dinaphthalene compounds here studied, in DCM solution and, for the naphthalene dimer in toluene. Electronic energy in black, free energy in red

Compound	B2PLYPD3 6-31+G(d,p)	ω B97XD 6-31+G(d,p)	ω B97XD aug-cc-pvtz
1515	-0.02 ^b -0.10	-0.45 ^b -0.51	-0.45 -0.53
2626	-0.22 -0.27	-0.65 ^b -0.74	-0.65 -0.74
2615 ^a	-0.07 -0.16	-0.49 ^b -0.60	-0.50 -0.61
1515 _{cross}	-0.21 -0.27	-0.65 -0.70	-0.66 -0.74
Naphthalene ^c	+0.04	-0.35	-0.35
Dimer	-0.15	-0.58	-0.47 ^d

a) Other localized triplet: ω B97XD: -0.473 -0.626; B2BLYPD3: -0.046 -0.136; b) cc-pvtz level: 1515: +0.005; 2626: -0.189; 2615 -0.049 c) in toluene. T_1 -loc-f2f : -0.34 eV d) one negative frequency (-3 cm^{-1} in T_1 -loc-min)

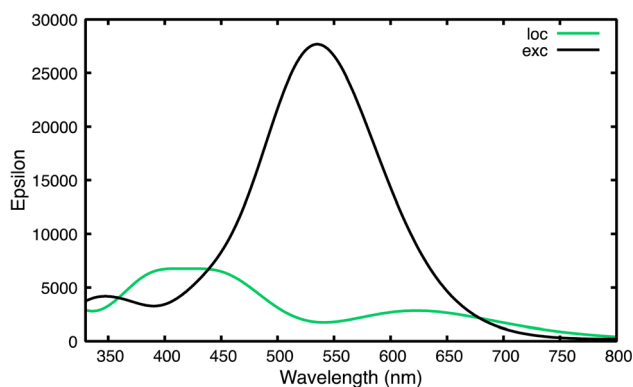


Fig. 4 TDA-B2LYPD3/6-31+G(d,p) computed absorption spectra for the 1515 triplet minima: T_1 -loc-min (green) and T_1 -exc-min (black) in the gas phase.

The spectrum of T_1 -loc-min is very similar to that of the long-lived DADS (DADS2), with a maximum above 450 nm and another shallow band at ~ 600 nm. On the other hand, the spectrum of T_1 -exc-min exhibits a single, extremely intense band peaking at 540 nm. Moreover, ADC(2) calculations predict for the triplet excimer minimum of a stacked naphthalene dimer a very intense band at ~ 500 nm, which moderately aligns with the ESA spectrum of DADS1 extracted from the TA experiment.²³ The indications provided by TDA/B2LYPD3 double hybrid calculations are confirmed by TDA/ ω B97XD and TDA/M052X methods, when

applied in DCM solution, also when using large basis sets (e.g. aug-cc-pvtz) (Section 4.3.1 in the ESI†).

We do not find any indication of stable charge separated triplet states, in line with the experimental results in acetonitrile. Naphthalene is indeed a poorer electron acceptor of NI and NDI, and the ethylenic bridges are not suitable electron donors. Moreover, in our closely stacked arrangement, Frenkel excitonic couplings are very large, and the steric restraints of the short covalent bridges prevent substantial structural rearrangements in the excited state minima, reducing the reorganization energy, which is an important factor for the population of CT states in closely stacked MCA.^{70,71} Finally, calculations for stacked naphthalene dimers in the gas phase indicate that the contribution of CT states to triplet excitons is smaller than for singlet excited states²⁰

2.2 Triplet state properties of 2626, 2615 and 1515_{cross}

Different from 2626,^{59,60} to the best of our knowledge, the synthesis of 2615 has never been reported. As detailed in the ESI,† we produced it by using a suitable etherifying group. We have measured the TA spectra for these species following excitations at 285 nm, and in the presence of Bp (excited at 355 nm). The TA signals and the DADS obtained by their fitting are reported in Fig. 5. The three compounds exhibit quite similar spectral features, and, therefore we shall discuss them together. In all cases examined, there are indeed two distinct DADS species with lifetimes extending into the nanosecond time



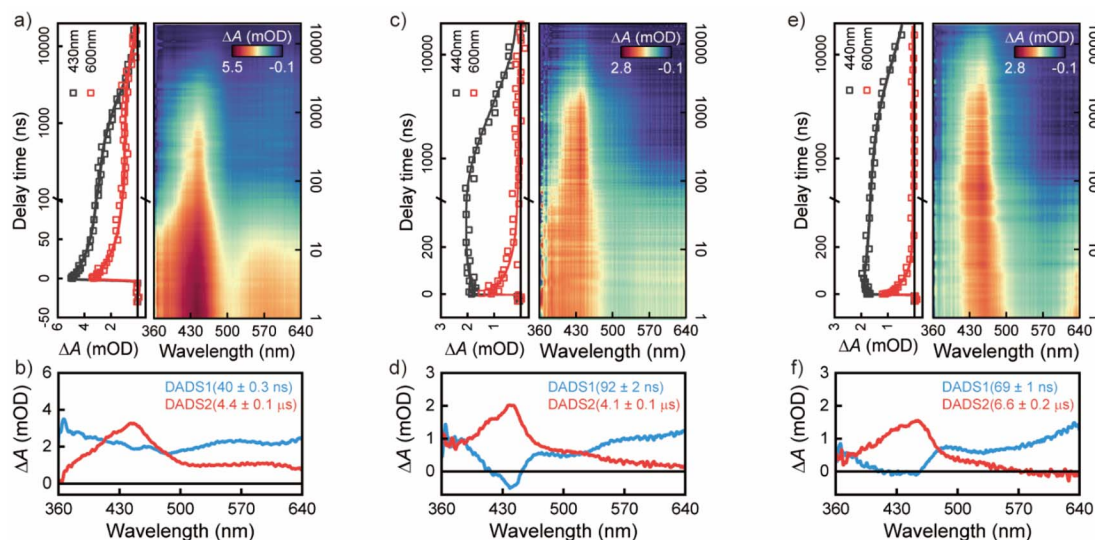


Fig. 5 Nanosecond time-resolved transient absorption spectra of (a) 2615, (c) 2626 and (e) 1515_{cross} excited at 285 nm in DCM under N₂-saturated conditions. Decay-associated difference spectra (DADS) of (b) 2615, (d) 2626 and (f) 1515_{cross}. Excited state absorption kinetic traces probed at 430 nm and 600 nm of (a) 2615, and at 440 nm and 600 nm of (c) 2626 and (e) 1515_{cross}.

scale. The spectral shapes of these species are very similar to the corresponding feature present after sensitization with Bp (Fig. S3–S7†). Such observations allow for a confident assignment of these species to triplet excited states (Fig. S8–S10†). This DADS exhibits a maximum at ~ 440 nm, with a long tail in the red wing, more prominent for 2615, where a shallow maximum at ~ 550 nm can be recognized. As detailed in the ESI,† the triplet QY is large in all of these three compounds: it is >0.7 for 2615 and 2626, and >0.5 for 1515_{cross} (Table S5†).

As reported in Table 1 we succeeded in localizing both the T₁-loc and the T₁-exc minima for all of these three species, with the T₁-loc minimum always being the most stable, both in the gas phase and in DCM solution (Table S6†). For 2626, we succeeded in locating two localized minima, differing in the stacking geometry of the two rings (Fig. S14†). In the most stable one (T₁-loc-min), they are rotated with respect to the other ($\eta = -39.3^\circ$). In the other one, less stable by 0.12 eV, they are close enough to be face-to-face ($\eta = -7.5^\circ$, T₁-loc-f2f). For 2626, in T₁-exc-min $\eta = -39.7^\circ$, showing that delocalized minima do not necessarily require f2f arrangements. However, due to the structural restraints imposed by the inter-ring bonds, d is 3.30 Å, *i.e.* longer than what found for the 1515 excimer minimum. As a consequence, for 2626 T₁-exc-min is much less stable than T₁-loc-min, when compared to 1515.

2615 is the only compound among those investigated here where the two naphthalene rings are different, as one is substituted in 1,5 positions and the other one in 2,6 positions (Scheme 1). We succeeded in optimizing two different localized triplet minima, T₁-loc (triplet localized on the 15 naphthalene moiety, see Fig. S15a†) and T₁-loc1 (triplet localized on the 26 naphthalene moiety, see Fig. S15b†), with very similar stability (T₁-loc-min is 0.01 more stable). Considering that the two naphthalene rings are different, for this compound T₁-exc-min (0.40 eV less stable than T₁-loc-min) is not perfectly

symmetric, *i.e.* different from all the excimer minima considered until now, the structural parameters and the spin density are not the same in the two moieties. The long axes of the rings are almost perpendicular ($\eta = 85.3^\circ$), while d is 3.13 Å, much shorter than that found for T₁-loc-min (3.37 Å). For 1515_{cross}, in T₁-exc-min, significantly less stable than T₁-loc-min, the rings are very close ($d \sim 3.0$ Å) with $\eta = 16.9^\circ$.

We have computed the TDA absorption spectra for all the minima (Fig. 6 and S19†) both in the gas phase and in DCM.

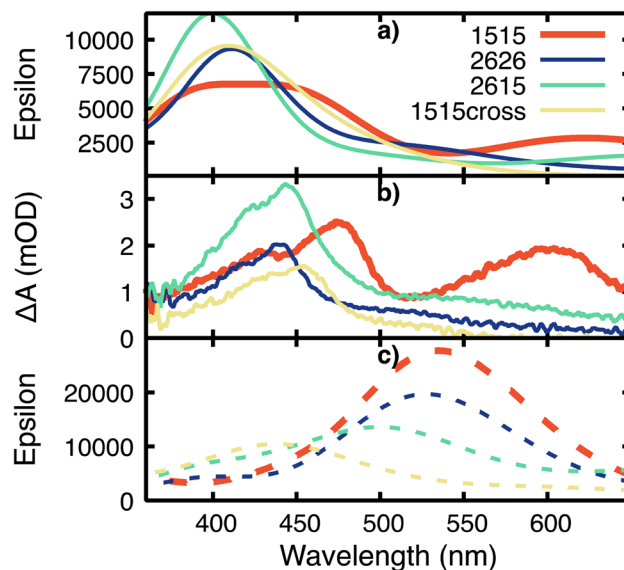


Fig. 6 (a) TDA-B2LYPD3/6-31+G(d,p) computed absorption spectra for the T₁-loc-minima in the gas phase. (b) Experimental μ s decay-associated difference spectra (DADS2) for all the dimers (the red traces in Fig. 2 and 5). (c) TDA-B2LYPD3/6-31+G(d,p) computed absorption spectra for the T₁-exc-minima in the gas phase.

The lineshapes of the B2LYPD3 computed spectra for T_1 -loc-minima (panel a in Fig. 6) are very similar to those of the experimental long-lived DADS2 (panel b in Fig. 6), but for a small, expected, uniform blue-shift (~ 20 nm). The most significant differences between the different compounds are also well reproduced. For example, for 2615, a shallow band at ~ 600 nm is present, and the main peaks (those above 400 nm) are slightly blue-shifted with respect to that of 1515. The spectra associated with T_1 -exc minima are reported in Fig. 6(c) and they are very different from the spectrum associated with the long-lived, most stable triplet state. In analogy with those reported above for 1515, at the B2LYPD3 level, they all exhibit an extremely intense peak in the red, whose maximum (in the range 450–550 nm) changes depending on the molecule considered. Moreover, the absorption intensity above 600 nm is always larger with respect to that found in the experiments (2626 and 2615 have strongly absorption until 800–900 nm). As reported in Fig. S17–S25,[†] the TDA spectra computed with ω B97XD and M052X functionals in DCM solution provide the same picture obtained with double hybrid TDA-DFT, where TD- ω B97XD spectra provide a similar qualitative picture. The signature of the excimer minimum is, thus, a very strong absorption band at 500–600 nm, whose intensity and position depends on the structural and electronic features of the minimum. The closer the approach of the bases, the more intense and red-shifted is the absorption band.

2.3 Triplet state properties of the stacked naphthalene dimer in toluene

In the dinaphthalene species studied here, the covalent bonds connecting the two naphthalene moieties lead to some distortion of the ring planarity, and obviously induce some structural restraints, which could affect the relative stability of localized and delocalized minima. In order to assess this issue and to increase the generality of our conclusions, we have applied our computational approach to the study of naphthalene monomers and dimers in toluene solution, for which the experimental triplet spectrum is available. As shown in Fig. 7, it exhibits a strong band at ~ 420 nm, but, as the concentration

increases, a weak shoulder at longer wavelength appears, which has been attributed to the presence of a triplet excimer involving two stacked naphthalene molecules (*i.e.* the T_1 -exc species we have discussed in the previous Section).⁴⁷

In addition to the triplet of the naphthalene monomer, we succeeded in locating both T_1 -loc and T_1 -exc for a dimer. For T_1 -loc different stationary points are possible. In the most stable one (hereafter T_1 -loc-min), the two monomers exhibit a slipped parallel arrangement (Fig. S26[†]), but a perfect ‘face-to-face’ arrangement is also possible. On the other hand, this latter structure (hereafter T_1 -loc-f2f) exhibits a small negative frequency (< 50 cm^{-1}) and it is not an absolute minimum of the T_1 -loc PES. In T_1 -exc-min, the monomers adopt a perfect ‘face-to-face’ parallel arrangement, and two moieties are much closer than in the ground state minimum, with d decreasing by 0.4–0.5 Å. As reported in Table 1, for a naphthalene dimer the relative stability of T_1 -exc strongly increases. From the electronic point of view it is slightly more stable than T_1 -loc, as predicted also by ADC(2) calculations in the gas phase. T_1 -loc-min, likely due to its much shallower PES than T_1 -exc, is however relatively stabilized (by ≥ 0.2 eV) when vibrational and entropic corrections are included, resulting in the most stable triplet minimum also at the B2LYPD3 level.

The TDA spectrum computed for the triplet monomer is in good agreement with the experimental one (Fig. S27[†]), but for the expected weak blue-shift of the maximum. In agreement with the ADC(2) calculations in the gas phase, an extremely strong band, with a maximum at ~ 550 nm, is associated with the T_1 -exc minimum of the dimer. The spectrum of T_1 -loc, though its maximum falls at ~ 400 nm, is different to that of the monomer. As detailed in the ESI,[†] in addition to a ‘monomer-like’ transition at ~ 400 , quite similar to that typical of isolated naphthalene, we find two additional weaker transitions, on the red-wing of the main absorption band, involving also the stacked naphthalene molecule. The position and the intensity of these transitions depend on the stacking geometry of the dimer. For T_1 -loc-min, they simply produce a weak red-tail in the spectrum. On the other hand, for T_1 -loc-f2f, an intense band appears just below 500 nm, extending until 600 nm.

3 Conclusions

We here reported a comparative study of different stacked naphthalene dimers in the triplet electronic states, where the two moieties are either covalently bonded or simply stabilized by van der Waals interactions. In the former case, we have explored different stacking geometries, from cases where the two ring molecular axes are almost parallel (as in 1515) to other molecules where they are almost perpendicular (as in 2615). Triplet electronic states are always formed in high yield (> 0.5), and time-resolved absorption experiments always show the presence of two components with decay lifetimes extending into the nanosecond and microsecond time scales, whose shapes are the same recorded after photosensitization experiments, confirming their identification as triplet states. Our calculations (by using either standard hybrid or double hybrid DFT calculations) indicate that for all the molecules the most stable triplet is

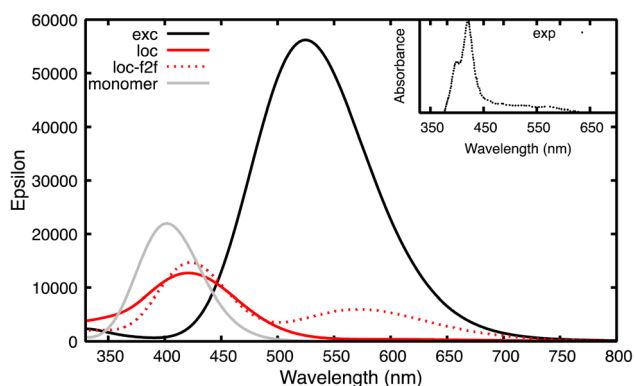


Fig. 7 TDA-PCM/B2LYPD3/6-31+G(d,p) computed absorption spectra in toluene. The experimental absorption spectrum of naphthalene in toluene⁴⁷ is shown in the inset on the right.



localized on one of the two rings (T_1 -loc). This assignment is confirmed by the experimental phosphorescence spectra and by the remarkable agreement between the shape of the experimental spectra and that computed for the localized minima. The absorption spectra of the localized triplet are similar to that of a triplet naphthalene monomer, with a strong peak slightly above 400 nm. However, a tail appears in the red (until 550–650 nm), which, depending on the stacking arrangement, can gain significant intensity. For 1515, where the rings are close to being f2f, a second intense band, peaking at 600 nm is indeed present both in experimental and in computed T_1 -loc spectra. The computed spectra for delocalized 'excimer-like' triplet minima (T_1 -exc) are instead not consistent with the experimental ones at longer times, exhibiting a very strong band at 500–550 nm, and extending until 800 nm. Interestingly, also the T_1 -exc spectrum strongly depends on the stacking geometry, with the main absorption band red-shifting and gaining intensity for f2f arrangements (as in 1515). According to our calculations, the relative stability of T_1 -exc is also larger for f2f stacking, which enables a larger decrease of the inter-ring distance, a major stabilizing factor for excimer minima.

Charge separated triplet electronic states are not expected to play a significant role in the compounds here examined, also in more polar solvents, as confirmed by the test experiments performed in acetonitrile. Suitable modifications in the bridge (*e.g.* increasing its electron donor efficiency and reducing the steric hindrance) and in the naphthalene moieties (increasing their electron acceptor properties) are likely necessary to observe symmetric breaking charge separation in covalently bridged stacked naphthalene dimers.

For a free stacked dimer, which does not suffer from the small distortion of the ring planarity (necessary to reduce the steric hindrance) of covalently bonded dimers, the most accurate electronic methods (*e.g.* double hybrids density functionals or ADC(2))²⁴ predict indeed that 'excimer' minima are more stable (by 0.1–0.2 eV). However, localized minima, for which a large number of almost isoenergetic minima are available, are strongly relatively favoured by entropic and vibrational effects, and, at least at the double hybrid level, are slightly more stable also in this latter case. Based on our calculations, it cannot be thus taken for granted that the shallow absorption band appearing above 500 nm when the naphthalene concentration in toluene increases is due to triplet excimers, as the f2f localized triplet would have a spectral signature consistent with the experimental features.

Based on our experimental and computational analysis, the possibility that for stacked naphthalene dimers the absolute triplet minimum is a delocalized excimer is expected to be more an exception than a rule. At the same time, our calculations show that 'excimer' minima are relative minima also when the axes of the rings are perpendicular, although they are relatively more stable for symmetric face-to-face arrangements, and when ring planarity is not distorted. In these cases, their stability is comparable to that of localized minima. On these grounds, excimer triplet minima can be transiently populated following light absorption and/or triplet sensitization of dinaphthalene and, therefore, their presence has to be considered when

interpreting TR spectra. Moreover, when naphthalene dimers are trapped inside rigid hosts, which decreases the weight of entropic effects, the excimer can become the most stable triplet minima.

These conclusions are expected to be valid for several other MCAs, with the role played by delocalized excimers being more important for more symmetric stacking arrangements and when a strong decrease of the inter-ring distance in the triplet minimum is sterically feasible. Another general consideration concerns the expected spectral features of the localized and excimer minima, which, for closely stacked systems, can significantly depend on the stacking geometry of the chromophores, and, therefore, on their electronic interactions. In other words, we cannot expect that 'localized' minima have exactly the same spectra of the free monomer.

Data availability

The data that support the findings of this study are available in the ESI† of this article and are available on request from the corresponding authors.

Author contributions

Conceptualization, L. M. F., X. W., W. W., H. Y., J. C. and R. I.; methodology, L. M. F., X. W., W. W., H. Y., J. C. and R. I.; formal analysis, all authors; investigation, all authors; writing – original draft, L. M. F., X. W., J. C. and R. I.; writing – review and editing, all authors; supervision, H. Y., J. C. and R. I.; funding acquisition, L. M. F., H. Y., J. C. and R. I. All authors have read and agreed to the published version of the manuscript.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

This research project is part of the activities of the National Center for Gene Therapy and Drugs Based on RNA Technology, funded by the European Union – Next Generation EU, Project CN00000041, CUP B93D21010860004. R. I. also thanks CNR, program "Progetti di Ricerca@cnr", project UCATG4 and NUTRAGE funded by FOE-2021 DBA.AD005.225 for financial support. This research project was made possible through the access granted by the Galician Supercomputing Center (CESGA) to its supercomputing infrastructure. The supercomputer FinisTerra III and its permanent data storage system have been funded by the Spanish Ministry of Science and Innovation, the Galician Government and the European Regional Development Fund (ERDF). This study was funded by the National Natural Science Foundation of China (No. 92156024 to J. Chen, No. 92056203 and 92356307 to H. Yang). We thank the Materials Characterization Center of East China Normal University for help with the measurement of the ns-TA spectra.



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