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# Investigation of the magnetic spin correlations in the layered molybdenates, $Mn_2Mo_3O_8$ and $MnAMo_3O_8$ ( $A = Fe, Co, Zn$ )<sup>†</sup>

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An exotic range of magnetic (and other) properties have been observed in  $A_2Mo_3O_8$  materials (where A is a single or mix of transition metals) making understanding their chemistry and physics timely. We have investigated the structural–property relationships in  $Mn_2Mo_3O_8$  and the related materials,  $MnFeMo_3O_8$ ,  $MnCoMo_3O_8$  and  $MnZnMo_3O_8$ . We report a detailed powder diffraction analysis confirming ferrimagnetic structures for  $Mn_2Mo_3O_8$  and  $MnFeMo_3O_8$ . Differing rates of spin ordering on crystallographically distinct sites (tetrahedral or octahedral) gives rise to magnetic hysteresis, which abruptly disappears in 2 K data. This appears to be correlated with ion displacement and/or electrostriction effects, which also relax at 2 K. We confirm an antiferromagnetic structure type for  $MnCoMo_3O_8$  and no discernible magnetic ordering within the temperature range studied for  $MnZnMo_3O_8$ . For  $MnZnMo_3O_8$  we suggest a small amount of site disorder acts to suppress magnetic ordering. This suggests that magnetic properties can be tuned both through A-site cation order and choice of A-site cations.

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## Introduction

The  $A_2Mo_3O_8$  family of materials (where  $A = Mn^{2+}, Fe^{2+}, Co^{2+}$  or  $Ni^{2+}$ ) have been attracting recent attention due to their exotic magnetic properties and magnetoelectric coupling<sup>1–5</sup> and potential applications for renewable energy technologies (batteries,<sup>6–9</sup> supercapacitors<sup>10,11</sup> and in water splitting<sup>12–15</sup>). These materials exhibit a complex layered arrangement, which crystallizes with a hexagonal structure in the  $P6_3mc$  space group (#186). The structure consists of Kagomé-type  $MoO_6$  layers which are separated by two-dimensional honeycomb layers stacked in the lattice  $c$ -direction (Fig. 1). The AO layer comprises two crystallographically distinct tetrahedral ( $AO_4$ ) and octahedral ( $AO_6$ ) corner shared sites which alternate in the lattice  $a/b$  plane to form a bipartite buckling honeycomb layer.<sup>16</sup> No magnetic contribution (as might be expected from  $Mo^{4+}$ ) arises from the  $Mo_6$  layer due to an orbital driven Peierls effect which gives rise to a trimerization of  $MoO_6$  resulting in a shared electronic ground state and no unpaired electrons.

Instead, magnetic order arises from magnetic  $A^{2+}$  ions situated within the honeycomb layer.<sup>6</sup> Computational studies have demonstrated the lack of Mo contribution to the magnetic ground state in  $A_2Mo_3O_8$  ( $A = Fe, Co$  and  $Mn$ ) materials.<sup>16</sup> At room temperature, the materials are considered pyroelectric, arising as a result of the presence of the  $AO_4$  tetrahedra, with the polarisation vector directed along the crystallographic  $c$ -direction.<sup>17–19</sup> Below the magnetic transition, type 1 multi-ferroic character is realised owing to the coexistence of spontaneous polarisation and magnetic ordering and large linear magnetoelectric coupling in both the  $a/b$  plane and lattice  $c$ -direction have been reported.<sup>20</sup>

By far the most studied members of the family are  $Fe_2Mo_3O_8$  and  $Co_2Mo_3O_8$ , with both compounds reported to exhibit antiferromagnetic ordering at Néel temperatures ( $T_N$ ) of 59.5 K and 40.8 K respectively.<sup>21</sup>  $Fe^{2+}$  ions in  $Fe_2Mo_3O_8$  are antiferromagnetically coupled between tetrahedral and octahedral sites in the  $a/b$  plane with a long range collinear antiferromagnetic structure realised through antiferromagnetic coupling of tetrahedral or octahedral units across layers.<sup>22</sup> Additionally,  $Fe_2Mo_3O_8$  has been shown to exhibit exciting electronic and magnetic properties such as giant magnetoelectric effect,<sup>2,4,23</sup> optical magnetoelectric effect,<sup>24</sup> strong magnon-phonon coupling<sup>22</sup> and distinct electric field and terahertz magnetic excitations.<sup>20</sup>  $Co_2Mo_3O_8$  shows a sharp transition in temperature dependent susceptibility consistent with antiferromagnetic ordering.<sup>5</sup> Neutron diffraction demonstrated the magnetic Bragg peaks identifiable at 10 K could

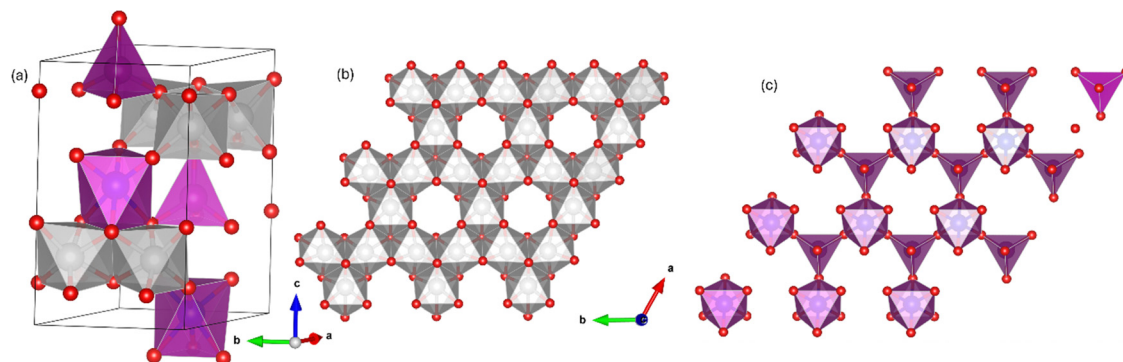
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**Fig. 1** Schematic representation of the  $A_2Mo_3O_8$  structure where (a) shows the stacking of the  $MoO_6$  Kagomé and AO honeycomb lattices in the lattice  $c$ -direction, (b) shows the  $MoO_6$  layer in the lattice  $a/b$  plane showing the trimerization of the Mo ions and (c) shows the alternating honeycomb connectivity of  $AO_6$  octahedra and  $AO_4$  tetrahedra. The pink polyhedra and triangles represent the A-site octahedra and tetrahedra respectively, the grey polyhedral the  $MoO_6$  octahedra and the red sphere the oxygen atoms respectively.

be indexed with  $k = (0,0,0)$  with similar magnitudes for the magnetic moments for  $Co^{2+}$  observed on both the tetrahedral ( $3.44\mu_B$ ) and octahedral ( $3.35\mu_B$ ) sites and C-type connectivity similar to that observed for  $Fe_2Mo_3O_8$ .<sup>5</sup> However, in contrast  $Fe_2Mo_3O_8$ , shows no evidence for a magnetic field induced transition to a ferrimagnetic state as is observed in  $Co_2Mo_3O_8$ .<sup>5</sup> This is suggested to be as a result of the small differences in magnitude of the magnetic moments in  $Co_2Mo_3O_8$  when compared to  $Fe_2Mo_3O_8$ .<sup>5</sup> Recently, the dependence of the magneto-electric effect up to fields of 60 T in  $Co_2Mo_3O_8$  has been studied.<sup>25</sup> These authors reported at high applied fields of 27 T and 31 T spin-flop transitions (towards canted antiferromagnetically ordered states) were observed at 1.7 K which result in colossal changes of the electric polarisation.<sup>25</sup>

In contrast, no magnetic order down to 2 K was initially reported for  $Ni_2Mo_3O_8$  from both computational and experimental studies.<sup>21</sup> Recent computational studies have suggested that the magnetic order in  $Ni_2Mo_3O_8$  is far more complex with strong antiferromagnetic coupling expected within layers whilst weak interlayer coupling is expected due to the small magnetic moment of  $Ni^{2+16}$ . More recently, it has been reported that  $Ni_2Mo_3O_8$  orders non-collinearly with a  $T_N \approx 5.5$  K with the magnetic moments lying in the  $a/b$  plane rather than the crystallographic  $c$ -direction as observed for both  $Fe_2Mo_3O_8$  and  $Co_2Mo_3O_8$ .<sup>1</sup> Initially the magnetic structure was reported to exhibit a zig-zag-type magnetic ordering such that pairs of antiferromagnetically connected ferromagnetic zig-zag chains are formed within the  $a/b$  plane<sup>26</sup> or as a complex mixture between zig-zag and stripy structures.<sup>27</sup> More recently, powder neutron diffraction data has shown the magnetic structure to be stripy (whereby order within these chains is antiferromagnetic rather than ferromagnetic and connectivity between the chains is ferromagnetic).<sup>1</sup> In high magnetic fields metamagnetic phase transitions have also been reported for  $Ni_2Mo_3O_8$ .<sup>28</sup>

Comparatively, very little has been reported on the magnetic behaviour of  $Mn_2Mo_3O_8$ . Both computational and experimental studies have suggested that  $Mn_2Mo_3O_8$  exhibits ferrimagnetic order with a transition temperature of approximately 40 K.<sup>16,21</sup> In real terms the picture is far more complex.

Typically, ferrimagnetic behaviour arises as a result of the coexistence of species with very different magnetic moments on a magnetic lattice such that antiferromagnetic ordering of these species does not result in the complete cancellation of the magnetic moment, leading to a net magnetic moment in a particular crystallographic direction. Neutron diffraction studies performed by Bertrand *et al.* at 4.5 K suggest that the magnetic moments in  $Mn_2Mo_3O_8$  are ordered along the crystallographic  $c$ -axis.<sup>29</sup> The authors proposed four different magnetically ordered states, C-type antiferromagnetic, A-type antiferromagnetic, ferrimagnetic (where connections between a particular site (octahedral or tetrahedral) are ferromagnetic whilst those across sites are antiferromagnetic) and ferromagnetically ordered. From the magnetic Bragg peak line strength the authors proposed that the magnetic moments associated with  $Mn^{2+}$  on the tetrahedral and octahedral sites have different magnitudes leading to ferrimagnetic ordering.<sup>29</sup> However, it is now more commonly accepted (from SQUID magnetometry studies) that below  $T_N$  the magnetic moments associated with the octahedral and tetrahedral sublattices cancel out completely (giving rise to antiferromagnetic ordering) at zero temperatures but not at finite temperatures where ferrimagnetic ordering is observed.<sup>18</sup> However, the mechanism for this remains unclear. Given the plethora of exciting magnetic states that can be realised in this family of materials it can be expected that the magnetic behaviour of  $Mn_2Mo_3O_8$  is perhaps not as simplistic as has been reported thus far, warranting more detailed structural and magnetic studies.

Furthermore, many studies have looked at cooperative doping on the lattice A-site since the presence of both octahedral and tetrahedral A-sites provides a versatile playground to study interesting magnetic phenomenon and control magnetic behaviour.<sup>30–38</sup> For example, giant thermal Hall effects have been reported in  $Fe_{2-x}Zn_xMo_3O_8$  materials.<sup>30</sup> The magneto-electric effect has been shown to be tuneable with the transition between antiferromagnetically and ferrimagnetically ordered states with Zn doping in  $Fe_2Mo_3O_8$ <sup>31,33,34</sup> and  $Co_2Mo_3O_8$ .<sup>39</sup> However, as with the parent materials comparatively few studies have been performed with manganese despite the potential for site preference leading to exotic behaviour. Recently, Chang *et al.*,



prepared single crystals of  $(\text{Mn}_{1-x}\text{Co}_x)_2\text{Mo}_3\text{O}_8$  ( $0 \leq x \leq 1$ ).<sup>17</sup> Magnetic data have been collected using SQUID magnetometry with the applied magnetic field aligned along the crystallographic  $c$  direction (magnetic easy axis). At  $x$  values below 0.35 (corresponding to  $\text{Mn}_{1.3}\text{Co}_{0.7}\text{Mo}_3\text{O}_8$ ) these materials exhibit ferrimagnetic ordering owing to the differences in magnetic moment between  $\text{Co}^{2+}$  and  $\text{Mn}^{2+}$  with suppression of  $T_N$  on increasing  $\text{Co}^{2+}$  contents. Above  $x = 0.35$  there is an abrupt change from ferrimagnetic to antiferromagnetic ordering whereby  $T_N$  increases with increasing  $\text{Co}^{2+}$  contents.<sup>17</sup> Kurumaji *et al.*, have also looked at the variation of the magnetoelectric response in  $\text{Mn}_{2-x}\text{Fe}_x\text{Mo}_3\text{O}_8$ .<sup>18</sup> At  $x = 0$  they report a negative correlation of the spin-induced modulation of the pyroelectric current. They also demonstrated that increasing  $\text{Fe}^{2+}$  incorporation results in a change from ferrimagnetic to antiferromagnetic ordering at  $x \approx 1.2$  and significant changes to the pyroelectric current, which in turn “tunes” magnetoelectric coupling in these materials.<sup>18</sup> In addition, spin-flop behaviour has been reported for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  films ( $\sim 140$  nm) when a 0.5% tensile strain is applied suggesting that further exotic magnetic states might be realised on doping  $\text{Mn}_2\text{Mo}_3\text{O}_8$  materials.<sup>40</sup>

Despite extensive work in the area, there remains a lack of fundamental understanding of the structure–property correlations in the manganese material in particular. In this paper, we report a comprehensive powder neutron diffraction study of  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and  $\text{MnAMo}_3\text{O}_8$  (where A is Co, Fe and Zn). We have determined the magnetic structures of these materials and importantly correlate our findings with temperature dependent structural behaviour and magnetic property measurements. This work highlights that the magnetic behaviour of  $\text{Mn}_2\text{Mo}_3\text{O}_8$  is not a simplistic ferrimagnet. We see clear correlations between the spin behaviour on the tetrahedral site and ionic displacement/electrostriction behaviour in  $\text{Mn}_2\text{Mo}_3\text{O}_8$ . In contrast the octahedral site remains largely unchanged as a function of temperature. These data provide new insight into the complex magnetic behaviour in these materials. Magnetic structure determination from powder neutron diffraction studies for  $\text{MnCoMo}_3\text{O}_8$  and  $\text{MnFeMo}_3\text{O}_8$  favour antiferromagnetic and ferrimagnetic spin arrangements respectively. Furthermore, A-site cation order is important in the  $\text{MnZnMo}_3\text{O}_8$  material for stabilising magnetic states with a small amount of A-site disorder resulting in no magnetic correlations over the temperature range studied. More work needs to be done in order to understand the role of order/disorder in magnetic co-doped materials.

## Experimental

Polycrystalline  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and  $\text{MnAMo}_3\text{O}_8$  ( $A^{2+} = \text{Fe}, \text{Co}, \text{Zn}$ ) were synthesised using the ceramic method in an evacuated, sealed quartz tube.<sup>29</sup> Stoichiometric amounts of MnO, ZnO, FeO or CoO (all Sigma Aldrich, >99%) and  $\text{MoO}_2$  (Alfa Aesar, >99%) were mixed in an agate mortar and sealed in evacuated quartz tubes. The tubes were heated at 1223 K for 16 hours at a heating rate of  $10 \text{ K min}^{-1}$ . The tubes were subsequently cooled to 1073 K and quenched to room temperature. X-ray diffraction

data were collected for these materials at room temperature and 12 K using the PANalytical Empyrean diffractometer ( $\text{Cu } \alpha \lambda = 1.5406 \text{ \AA}$ ) fitted with an Oxford Instruments PHENIX cryostat. Data were collected over a  $2\theta$  range of  $10^\circ$  to  $70^\circ$  with a step size of  $0.05^\circ$  (total run time 10 hours).

Magnetic property measurements were performed using a Quantum Design MPMS SQUID magnetometer. Temperature dependent data were collected between 2 K and 300 K in both zero field cooled (ZFC) and field cooled (FC) environments with an applied magnetic field ( $H$ ) of 0.1 T or 5 T. Field dependent susceptibility data were collected at discrete temperatures of 2 K, 30 K, 60 K and 100 K applying magnetic fields between  $-5$  T and 5 T. Heat capacity measurements were performed using a Quantum Design Physical Properties Measurement System (PPMS). Data were collected with the materials pressed into small pellets ( $\text{Mn}_2\text{Mo}_3\text{O}_8 = 3.2$  mg,  $\text{MnCoMo}_3\text{O}_8 = 3.2$  mg,  $\text{MnFeMo}_3\text{O}_8 = 2.7$  mg,  $\text{MnZnMo}_3\text{O}_8 = 3.0$  mg) over a temperature range of 2 K to 150 K in zero applied fields.

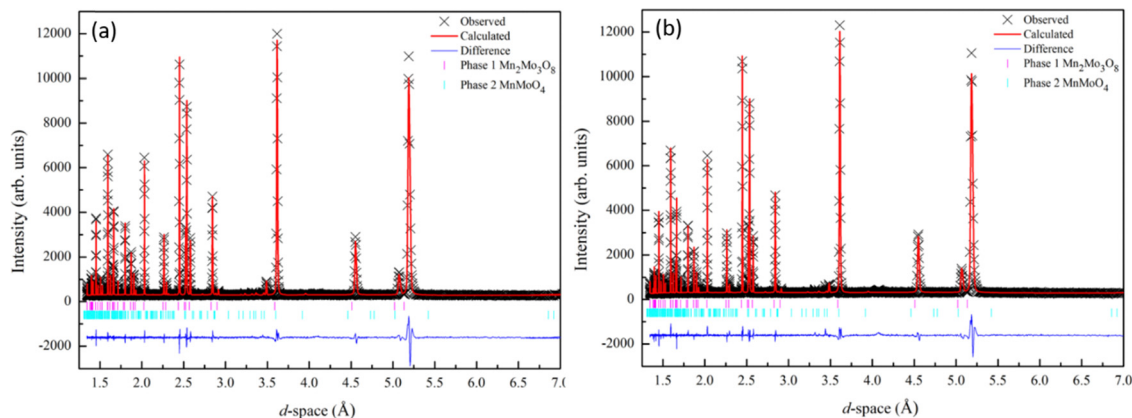
Powder neutron diffraction data for  $\text{Mn}_2\text{Mo}_3\text{O}_8$ ,  $\text{MnCoMo}_3\text{O}_8$  and  $\text{MnFeMo}_3\text{O}_8$  were collected on the WISH diffractometer at the ISIS Neutron and Muon user facility.<sup>41,42</sup> Samples were loaded into 3 mm vanadium cans (265 mg  $\text{Mn}_2\text{Mo}_3\text{O}_8$ , 731 mg  $\text{MnCoMo}_3\text{O}_8$ , 312 mg  $\text{MnFeMo}_3\text{O}_8$ ) and data were collected across 12 temperature points between 2 K and 200 K for the  $\text{Mn}_2\text{Mo}_3\text{O}_8$  material. Data were collected for 15 minutes except for temperatures of 2 K and 200 K where data were collected for 2 hours. Data for  $\text{MnFeMo}_3\text{O}_8$  and  $\text{MnCo}_2\text{Mo}_3\text{O}_8$  were collected at 2 K and 200 K for 2 hours. Powder neutron diffraction data for  $\text{MnZnMo}_3\text{O}_8$  (618 mg) were collected using the GEM diffractometer at the ISIS Neutron and Muon user facility at 200 K and 5 K for 6 hours and at temperatures of 150 K, 100 K and 50 K for 2 hours with the sample loaded into a 3 mm vanadium can.<sup>43,44</sup>

## Results and discussion

Powder diffraction data collected for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  confirmed the formation of the expected hexagonal phase. A small amount of second phase is identified as  $\text{MnMoO}_4$  ( $\sim 5\%$ ). Rietveld refinements of the data collected at both room temperature (298 K) and 12 K were performed using the GSAS suite of programs<sup>45,46</sup> in the proposed  $P6_3mc$  space group.<sup>47</sup> Refinements were performed for 26 variables which included lattice parameters, atomic positions, zero point, 12 shifted Chebyshev background terms and peak shape fitted using a pseudo-Voigt function. The refinement also included the  $\text{MnMoO}_4$  ( $C2/m$ ) phase.<sup>48</sup> Good agreement between the model and the data was observed as shown in Fig. 2 with no perceivable change in structure between room temperature and 12 K, consistent with reported studies for other  $A_2\text{Mo}_3\text{O}_8$  analogues.<sup>1,5,27,29</sup> We see no evidence for symmetry lowering ( $P6_3mc \rightarrow P6_3$ ) as has recently been reported for  $\text{Fe}_2\text{Mo}_3\text{O}_8$  by spectroscopic studies.<sup>49</sup> Full refinement details and refined parameters are given in Table S1 in the ESI.†

Heat capacity measurements were carried out in order to look at potential magnetic phase transitions in  $\text{Mn}_2\text{Mo}_3\text{O}_8$  (Fig. 3(a)). As expected, the molar heat capacity ( $C_p$ ) decreases

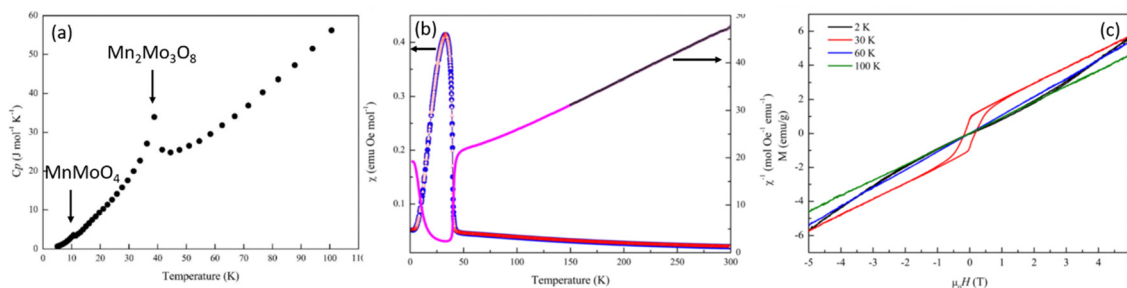




**Fig. 2** Rietveld refinement of the X-ray diffraction data collected for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and fitted to the  $P6_3mc$  model<sup>47</sup> at (a) 298 K (wRp = 7.5%, Rp = 5.74,  $\chi^2 = 2.7$ ) and (b) 12 K (wRp = 8.6%, Rp = 6.3%,  $\chi^2 = 3.5$ ). Black crosses represent observed data, red line represents the calculated model and the blue line represents the difference between the observed and calculated data.  $\text{Mn}_2\text{Mo}_3\text{O}_8$  is represented by the magenta tick marks (top) and  $\text{MnMoO}_4$  by the cyan tick marks (bottom).

with decreasing temperature until  $\sim 40$  K where a sharp peak is observed. This is consistent with the magnetic Néel temperature ( $T_N$ ) reported for  $\text{Mn}_2\text{Mo}_3\text{O}_8$ .<sup>50,51</sup> A second weak peak in  $C_p$  is observed at  $\sim 10$  K and is associated with the expected magnetic transition in the secondary phase,  $\text{MnMoO}_4$ .<sup>52</sup> Magnetic susceptibility data shows a more complex magnetic behaviour. Zero field cooled (ZFC) and field cooled (FC) temperature dependent data collected in an applied magnetic field of 0.1 T are shown in Fig. 3(b). A peak in the susceptibility at 39.6(4) K is observed (extracted from a plot of  $d\chi/dT$  shown in Fig. S1(a) in the ESI<sup>†</sup>) with no deviation between ZFC and FC data consistent with long range antiferromagnetic (AFM) ordering. Whilst the shape of the magnetic curve is consistent with previous reported literature,<sup>7,17,21,47</sup> it is neither suggestive of a sharp phase transition to long-range AFM order nor low dimensional magnetic order (which typically show broader transitions).<sup>53</sup> It has been suggested previously that the magnetic anisotropy observed in the magnetic susceptibility data originates from differences in the magnitude of the magnetic moments associated with the tetrahedral and octahedral sites.<sup>29</sup> However, the differences in energies associated with the crystal field splitting of each of these sites is expected to be small with spin only values on each site

predicted to be almost identical potentially ruling out more traditional origins of ferrimagnetism in this material. Another study has suggested the possibility of mixed valence states (+2 and +3) across the octahedral and tetrahedral sites presumably arising as a result of structural defects such as oxygen vacancies which subsequently leads to ferrimagnetic character.<sup>47</sup> In these cases, we would expect to see divergence between ZFC and FC magnetometry data as a result of large differences in the magnitude of the magnetic moment failing to cancel and resulting in a net magnetic moment in a single crystallographic direction, which we do not see in our studies. It has also been suggested that the magnetic moments associated with the octahedral and tetrahedral sublattices do not cancel each other out over finite temperatures.<sup>18</sup> That is, there is possibly a transition from a partially ordered (ferrimagnetic) to a fully ordered (antiferromagnetic state) such that one or both magnetic sites remain dynamic until well below  $T_N$  or there is an intermediate canted antiferromagnetic spin state (below  $T_N$ ). The shape of the temperature dependent susceptibility curve is, however, consistent with a Néel ferrimagnetically ordered state whereby equal magnitude spins are ordered antiferromagnetically across crystallographically distinct sites but where saturation of



**Fig. 3** Physical property data collected for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  showing (a) molar heat capacity ( $C_p$ ) data indicating a sharp increase in  $C_p$  at approximately 40 K consistent with  $T_N$  for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and a weaker inflection at  $\sim 10$  K attributable to the magnetic transition in  $\text{MnMoO}_4$ , (b) zero field cooled (blue) and field cooled (red) data measured at 0.1 T and inverse ZFC susceptibility data where the black line shows the fit to the Curie–Weiss law and (c) field ( $H$ ) dependent magnetisation data collected at 2 K (black), 30 K (red), 60 K (blue) and 200 K (green).



the spin state has different time scales (temperature) dependencies leading to ferrimagnetic behaviour.<sup>21</sup>

At temperatures between 150 and 300 K  $\text{Mn}_2\text{Mo}_3\text{O}_8$  obeys Curie–Weiss behaviour (Fig. 3(b)). A total effective magnetic moment per formula unit is calculated as  $8.52\mu_{\text{B}}$  consistent with that calculated ( $8.35\mu_{\text{B}}$ ) using the spin only formula. A negative Weiss constant ( $\theta$ ) of  $-132.5(2)$  K is determined consistent with antiferromagnetic ordering. Calculation of the frustration index,  $f$  ( $f = -T_{\text{N}}/\theta$ ) gives a value of 3.2 suggesting some level of magnetic frustration in  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and is consistent with what we have observed in similarly layered materials.<sup>53</sup> Magnetic hysteresis loops collected at temperatures of 60 K and 100 K show a linear relationship of the magnetisation as a function of applied field consistent with paramagnetic behaviour. At 2 K we see no hysteric behaviour with the data exhibiting a slight “s” shape as would be expected for long-range antiferromagnetic ordering consistent with our temperature dependent susceptibility measurements and previous literature.<sup>7,17,21,47</sup> However, at 30 K we see distinct hysteric behaviour with a clear opening of the hysteresis loop at low fields consistent with observations by Das *et al.* who reported similar hysteresis in data collected at 20 K.<sup>7</sup> This indicates that there is a net magnetic moment in these materials, consistent with formation of the ferrimagnetic state (arising from different spin orientations or spin magnitudes on the octahedral and tetrahedral sites) or a transition from a weakly ferromagnetic to antiferromagnetic state within a relatively short temperature range.

In order to shed further insight into the magnetic behaviour of  $\text{Mn}_2\text{Mo}_3\text{O}_8$  we collected ZFC cooled magnetic susceptibility data at an applied field of 5 T (Fig. S1(b) in the ESI†). These data indicated that at 5 T a sharper magnetic transition is observed, consistent with that expected for antiferromagnetic ordering. This is further confirmed by the negative Weiss constant ( $\theta$ ) of  $-121.5$  K extracted from fitting the Curie–Weiss law between 150 and 300 K at 5 T. The magnetic moment per formula unit ( $8.83(1)\mu_{\text{B}}$ ) is also consistent with that expected for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and that observed at 0.1 T and with data published previously

for  $\text{Mn}_2\text{Mo}_3\text{O}_8$ .<sup>21</sup> It can be suggested that increased field strengths enables the simultaneous long-range order and saturation of the magnetic moments on both tetrahedral and octahedral sites resulting in no net magnetic moment being observed. Equally, this could suggest a field driven phase transition to an antiferromagnetically ordered state similarly to those seen for  $\text{Fe}_2\text{Mo}_3\text{O}_8$  and  $\text{Co}_2\text{Mo}_3\text{O}_8$  but we have not considered this further here.<sup>25,31</sup> Lastly, we see no evidence of low temperature spin-flop behaviour, which may have been expected, based on previous studies.<sup>18</sup> However, our data has been collected at the lower limits of both the expected temperature and applied magnetic field range previously reported and we cannot confidently rule this out from our data.<sup>18</sup>

To further investigate the magnetic spin relationships and understand the temperature dependence observed in magnetometry measurements in  $\text{Mn}_2\text{Mo}_3\text{O}_8$  we performed neutron powder diffraction experiments on the WISH diffractometer at the ISIS neutron and muon user facility (UK).<sup>41</sup> Data were refined using the FULLPROF suite of programs to enable determination of both the nuclear and magnetic structures.<sup>54</sup> At temperatures above  $T_{\text{N}}$  the data can be readily be fitted to  $P6_3mc$   $\text{Mn}_2\text{Mo}_3\text{O}_8$  phase with a small contribution from the  $\text{MnMoO}_4$  secondary phase ( $\sim 5\%$ ). Refinements were performed as detailed in the ESI.† The refinement profiles for data collected at 200 K and 2 K are shown in Fig. 4 with refinement profiles and refined parameters for all temperature points given in Fig. S2–S4 and Tables S2 through S5 in the ESI.† respectively. With decreasing temperature, we see no change in the  $P6_3mc$  nuclear structure consistent with the observations from our powder X-ray diffraction study discussed above. Temperature dependence of the lattice parameters are shown in Fig. S5 in the ESI.† We see that generally the lattice parameters and cell volume decrease with decreasing temperature as expected. However, the  $a$  and  $c$  lattice parameters show slightly different behaviour. The  $c$  lattice parameter plateaus at approximately 60 K. This is consistent with what has been seen in  $\text{Fe}_2\text{Mo}_3\text{O}_8$ <sup>55</sup> and other layered systems<sup>53</sup> and is

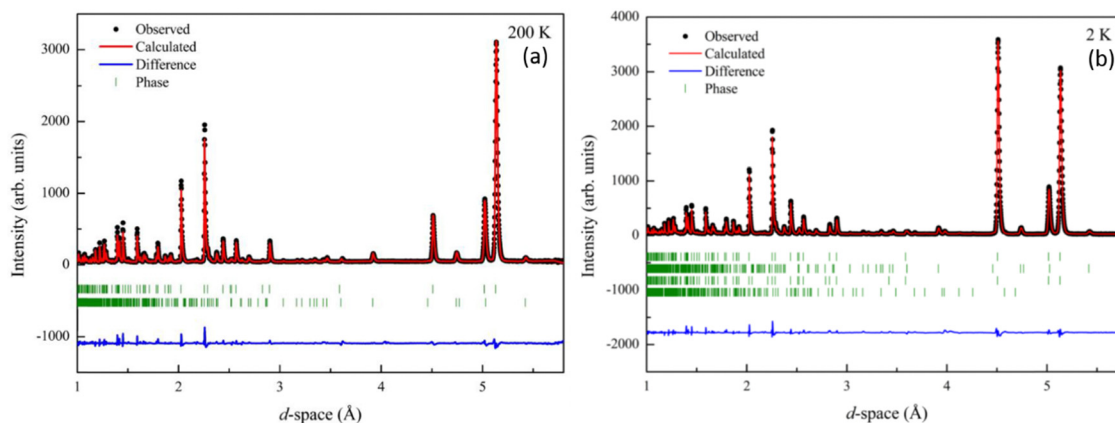


Fig. 4 Rietveld refinement of the powder neutron diffraction (WISH) data collected for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and fitted to the  $P6_3mc$  model<sup>47</sup> at (a) 200 K ( $wR_p = 13.9\%$ ,  $R_p = 11.5\%$ ,  $\chi^2 = 0.8$ ) and (b) 2 K ( $wR_p = 11.9\%$ ,  $R_p = 8.65\%$ ,  $\chi^2 = 0.92$ ). Black crosses represent observed data, red line represents the calculated model and the blue line represents the difference between the observed and calculated data. From top to bottom the tick marks represent the  $\text{Mn}_2\text{Mo}_3\text{O}_8$  (nuclear phase),  $\text{MnMoO}_4$  (nuclear phase),  $\text{Mn}_2\text{Mo}_3\text{O}_8$  (magnetic phase) and  $\text{MnMoO}_4$  (magnetic phase) respectively.



suggestive of the onset of short-range magnetic correlations. In the  $a/b$  plane the lattice parameters show a slight kink at  $\sim 40$  K and a change in slope consistent with the onset of magnetic order at  $T_N$  before reaching a plateau at  $\sim 25$  K. At  $T_N$  we also see an increase in the  $Mn_{tet}$ –O– $Mn_{oct}$  bond angle ( $\sim 1.76\%$ ) with decreasing temperature. These observations are consistent with ionic displacements, which occur in tandem with ferroelectricity,<sup>56</sup> and suggest the onset potentially of either switchable behaviour or symmetric exchange striction<sup>57,58</sup> at  $T_N$  within  $Mn_2Mo_3O_8$ . In order to investigate this further we have considered temperature driven changes in the  $MnO_4$  tetrahedral and  $MnO_6$  octahedral units. Previous work has suggested that the pyroelectric (above  $T_N$ ) and ferroelectric (below  $T_N$ ) behaviour is linked to the  $AO_4$  tetrahedra, with the polarisation vector directed along the crystallographic  $c$ -direction.<sup>17–19</sup> If we first consider the tetrahedral site, we can see that the bond length between the central Mn ion (Mn1) and the oxygen at the apex of the tetrahedron (O2) steadily increases ( $\sim 2.9\%$ ) as temperature decreases below  $\sim 60$  K until we reach  $T_N$  (Fig. S6 in the ESI†). This is consistent with the onset of the invariant behaviour in the  $c$  lattice parameter and ionic displacement in the lattice  $c$ -direction. The (Mn1–O2) bond length is then fairly consistent until 2 K where we see a sudden drop to values more consistent with those observed above  $T_N$ . The origin of this behaviour is not well understood and may signify the loss of ferroelectric character at low temperature. This could be related to the loss of hysteric behaviour observed in the field dependent magnetometry data and be driven by saturation of the magnetic moments on both the tetrahedral and octahedral sites resulting in an equalisation of the observed moment and loss of ferrimagnetic ordering. This is interesting as it would suggest that evolution of any possible ferroelectric state is linked to the temperature dependence of the magnetic spin dynamics as opposed to static magnetic order. Alternatively, this may arise as a result of complexities of the refinements at this temperature with two nuclear and two magnetic phases present due to the magnetic ordering of the impurity phase, although we believe this to be unlikely. The bond lengths at the base of the tetrahedron (Mn1–O3) decrease slightly at  $T_N$ . In contrast the bond lengths in the  $MnO_6$  octahedra vary only slightly (less than 1%) with temperature (Fig. S6 in the ESI†) consistent with thermal effects and isotropic compression of the octahedra with decreasing temperature. This confirms that the onset of multiferroic behaviour is primarily linked to the tetrahedral sites which is consistent with displacements reported

for  $Fe_2Mo_3O_8$ .<sup>17–19</sup> Moreover, Tang *et al.*, suggested that the ferroelectric behaviour is correlated to the ferromagnetic coupling in  $Co_2Mo_3O_8$ .<sup>5</sup> As such it is important to understand the magnetic spin state in  $Mn_2Mo_3O_8$ .

Below 40 K we see the clear onset of increased peak intensity which can be linked to magnetic order on the (101), (103), (201) and (211) reflections. Below this temperature, all data were fit using both the nuclear ( $P6_3mc$ ) structure and a  $Mn_2Mo_3O_8$  magnetic phase discussed below. Additionally, below 10 K we also see the evolution of additional magnetic Bragg peaks which are attributable to the magnetic structure of the  $MnMoO_4$  phase<sup>59</sup> and at 2 K we have refined this phase alongside the  $Mn_2Mo_3O_8$  (magnetic and nuclear) phases. For  $Mn_2Mo_3O_8$  the magnetic reflections were indexed using a commensurate propagation vector,  $k = (0,0,0)$  in the hexagonal unit cell. Irreducible representations and their corresponding magnetic space groups were determined using the ISODISTORT suite.<sup>60</sup> Four common irreducible representations (IR) and their corresponding magnetic space groups and numbers were determined (as shown in Table 1) alongside the direction ( $\uparrow$  or  $\downarrow$ ) of the magnetic moment relative to the crystallographic site and axes. Previous reports have suggested that the magnetic moments aligning along the lattice  $c$ -direction are favoured in hexagonal crystal systems.<sup>21,29</sup> However, in  $Ni_2Mo_3O_8$  the complex magnetic order has been shown to give rise to spins which lie in the lattice  $a/b$  plane.<sup>1</sup> Refinements performed using the magnetic structures determined from the  $\Gamma(5)$  and  $\Gamma(6)$  IRs (where the magnetic moments are orientated within the lattice  $a/b$  plane) failed to provide magnetic intensity in the correct places leading to unstable refinements. This allows us to rule out both of these models. This leaves structures associated with  $\Gamma(2)$  where the magnetic moments are orientated in the so called ferrimagnetic order such that coupling across the two different sites (tetrahedral and octahedral) is AFM whilst between magnetic cations on the same site (either tetrahedral – tetrahedral or octahedral – octahedral) coupling is ferromagnetic and  $\Gamma(3)$  where all interactions are antiferromagnetic. We have evaluated both spin structures using data collected at 10 K (since this data is free from the magnetic impurity phase) using the SARAH<sup>61</sup> and FULLPROF suite of programs<sup>64</sup> (as described in the ESI†). The  $\Gamma(3)$  model resulted in an unstable refinement such that convergence was never achieved whilst refinements using the  $\Gamma(2)$  model resulted in a stable refinement which exhibited an

**Table 1** Irreducible representations (IRs) and corresponding magnetic space groups generated for  $Mn_2Mo_3O_8$  within the parent  $P6_3mc$  space group and  $k = (0,0,0)$  using the ISODISTORT suite. Information related to spin direction and orientation is also provided for each IR. Note TTOO relates to tetrahedral–tetrahedral–octahedral–octahedral spin coupling and 0000 denotes that the spins lie perpendicular to the lattice  $c$ -direction

IR	Magnetic space group	Space group number	Moment parallel to lattice $c$ -direction TTOO	$a/b$ Plane moment allowed
$\Gamma(2)$	$P6_3m'c$	186.207	$\uparrow\uparrow\downarrow\downarrow$	No
$\Gamma(3)$	$P6_3m'c'$	186.205	$\uparrow\downarrow\uparrow\downarrow$	No
$\Gamma(5)$	$Cmc2_1$	36.172	0000	Yes
	$Cm'c'2_1$	36.176	$\uparrow\uparrow\downarrow\downarrow$	Yes
	$P2_1$	4.7	$\uparrow\uparrow\downarrow\downarrow$	Yes
$\Gamma(6)$	$Cmc'2_1'$	36.175	0000	Yes
	$Cm'c2_1'$	36.174	$\uparrow\downarrow\uparrow\downarrow$	Yes
	$P2_1'$	4.9	$\uparrow\downarrow\uparrow\downarrow$	Yes



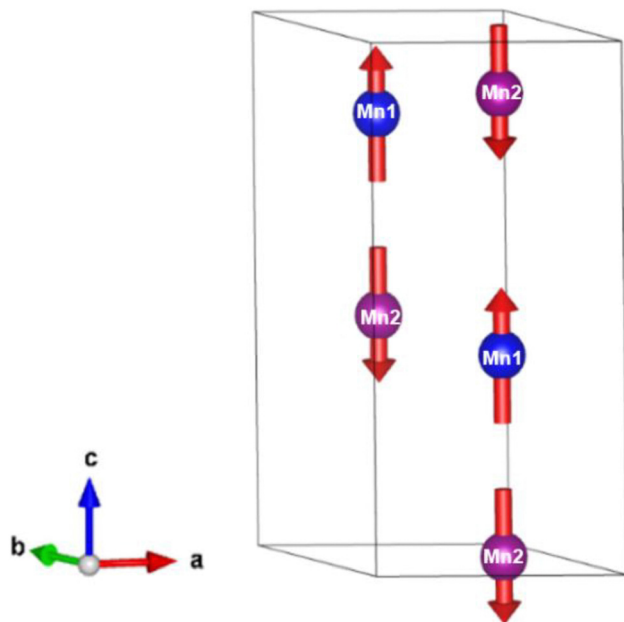


Fig. 5 Magnetic spin structure (red arrows) determined for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  within the unit cell (black outline) at 10 K from the Rietveld refinement of powder neutron diffraction data. The blue and pink spheres represent manganese on the Mn1 (tetrahedral) and Mn2 (octahedral) crystallographic sites respectively.

excellent fit to the data (Fig. S3, ESI<sup>†</sup>). This, confirms that  $\text{Mn}_2\text{Mo}_3\text{O}_8$  exhibits a (TT-OO,  $\uparrow\downarrow\downarrow\downarrow$ ) antiferromagnetic (ferrimagnetic) spin order as shown in Fig. 5(a) and as has been suggested in previous computational<sup>16,49</sup> and magnetometry work<sup>21,62</sup> and by peak indexing.<sup>29</sup> Refinements performed allowing the magnetic moments to be refined independently on the tetrahedral and octahedral sites results in unstable refinements for both the  $\Gamma(2)$  and  $\Gamma(3)$  models. Since both sites are expected to have the same  $d^5$  electron configuration the magnetic moments across the sites were constrained to have the same value in all refinements. At 2 K the same magnetic structure fit consistently with the data as shown in Fig. 2(b). This suggests that no magnetic phase transition occurs at low temperature. The magnetic moment was also determined as  $4.2\mu_B$  on each of the  $\text{Mn}^{2+}$  sites at 2 K consistent with what is expected in neutron diffraction for  $S = 5/2$  ions. We have further evaluated the critical exponent ( $\beta$ ) extracted from the refined magnetic moments ( $M$ ) in our powder neutron diffraction data as a function of temperature ( $T$ ) and given by the equation below (using  $T_N = 39.6$  K) and shown in Fig. S7 in the ESI<sup>†</sup>. This gives  $\beta = 0.31(1)$  which is indicative of a 3D Ising antiferromagnetic consistent with both the SQUID magnetometry and powder neutron diffraction data. Furthermore, the fit is robust over a wide temperature range suggesting that there are no new interactions emerging at the lowest temperature measured consistent with the absence of a secondary magnetic phase transition.

$$M_T = M_0 \left(1 - \frac{T}{T_N}\right)^\beta$$

Given the ferrimagnetic spin structure we note that the model for ferroelectric ordering may also be distinct in  $\text{Mn}_2\text{Mo}_3\text{O}_8$ . In contrast with both  $\text{Fe}_2\text{Mo}_3\text{O}_8$  and  $\text{Co}_2\text{Mo}_3\text{O}_8$

where the ferromagnetic component is coupled inter-site (*i.e.* oct–tet) to form ferromagnetic chains, the ferromagnetic coupling in  $\text{Mn}_2\text{Mo}_3\text{O}_8$  is intra-site (*i.e.* tet–tet or oct–oct). As such  $\text{Mn}_2\text{Mo}_3\text{O}_8$  may show exciting magnetoelectric behaviour and this warrants further investigation.

Doping the A-site in  $\text{Fe}_2\text{Mo}_3\text{O}_8$  and  $\text{Co}_2\text{Mo}_3\text{O}_8$  have been shown to be an effective route for tuning the magnetic properties of these materials.<sup>30–38</sup> We have prepared materials,  $\text{MnAMo}_3\text{O}_8$ , where  $\text{Mn}^{2+}$  is replaced with  $\text{Fe}^{2+}$ ,  $\text{Zn}^{2+}$  or  $\text{Co}^{2+}$  in order to investigate A-site cation dependence (tetrahedral *versus* octahedral) and the role this plays in magnetic ordering. Rietveld refinement of powder X-ray diffraction data collected at 298 K using the GSAS suite of programs<sup>45,46</sup> confirmed the formation of the expected primary hexagonal phase ( $P6_3mc$ ) for all three  $\text{MnAMo}_3\text{O}_8$  materials. Refinement profiles and full details are given in Table S6 and Fig. S8 the ESI<sup>†</sup>. We found no evidence for secondary phases in the  $\text{MnCoMo}_3\text{O}_8$  material but small amounts of  $\text{MnMoO}_4$  were evident in the X-ray diffraction data collected for  $\text{MnFeMo}_3\text{O}_8$  (4.2(1)%) and  $\text{MnZnMo}_3\text{O}_8$  (3.4(1)%) and were included in our refinements. Lattice parameters extracted for these materials show the expected relationships with atomic size when compared with the end members of the solid solutions ( $\text{Zn}_2\text{Mo}_3\text{O}_8$ ,  $\text{Co}_2\text{Mn}_3\text{O}_8$  and  $\text{Fe}_2\text{Mo}_3\text{O}_8$ ) and are consistent with what is expected from previous literature.<sup>29,47</sup>

Heat capacity data collected for both  $\text{MnCoMo}_3\text{O}_8$  and  $\text{MnFeMo}_3\text{O}_8$  show a sharp feature at temperature points 35.7(4) K and 49.5(5) K respectively consistent with what we observed for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and are suggestive of the onset of a magnetically ordered phase (Fig. S9 in ESI<sup>†</sup>). There are clear shifts in temperature on doping which increases  $\text{Co} < \text{Mn} < \text{Fe}$ . In contrast no features are seen in the  $C_p$  data collected for  $\text{MnZnMo}_3\text{O}_8$ , suggesting that no magnetically ordered state is realised in this material over the temperature range studied. For both  $\text{MnFeMo}_3\text{O}_8$  and  $\text{MnZnMo}_3\text{O}_8$  we see small contributions in the  $C_p$  data at  $\sim 10$  K consistent with the magnetic ordering associated with the secondary phase. Temperature dependent SQUID magnetometry data collected for these materials in an applied field of 0.1 T clearly demonstrates that the type of magnetic ordering is critically dependent upon the transition metal, which are doped on to the A-site (Fig. 6). Similarly, to  $\text{Mn}_2\text{Mo}_3\text{O}_8$ ,  $\text{MnFeMo}_3\text{O}_8$  shows a humped shaped transition at  $T_N = 46.8(\text{K})$  (as extracted from a plot of  $d\chi/dT$  *vs.* temperature shown in the inset of Fig. 6(a)) and is consistent with observations from heat capacity data showing an increase in  $T_N$  on incorporating  $\text{Fe}^{2+}$ . We see clear deviation between ZFC and FC data potentially as a result of small differences between the expected magnetic moments for  $\text{Mn}^{2+}$   $d^5$  ( $5.91\mu_B$  spin only) and  $\text{Fe}^{2+}$   $d^6$  ( $4.90\mu_B$  spin only) electronic configurations. These data suggest that the ferrimagnetic structure is still favoured for  $\text{MnFeMo}_3\text{O}_8$  consistent with work performed on the  $\text{Fe}_2\text{Mn}_3\text{O}_8 - \text{Mn}_2\text{Mo}_3\text{O}_8$  solid solution, which suggests the  $\text{Fe}^{2+}$  doping leads to an increase in  $T_N$  with the ferrimagnetic structure stable to  $x \approx 1.2$  (in  $\text{Mn}_{2-x}\text{Fe}_x\text{Mo}_3\text{O}_8$ ).<sup>18</sup> We also see a broad feature in the susceptibility data at approximately 100 K this is consistent with the Verwey transition in  $\text{Fe}_3\text{O}_4$ .<sup>63–65</sup> Whilst we did not observe any iron oxide based secondary phases in our diffraction data for



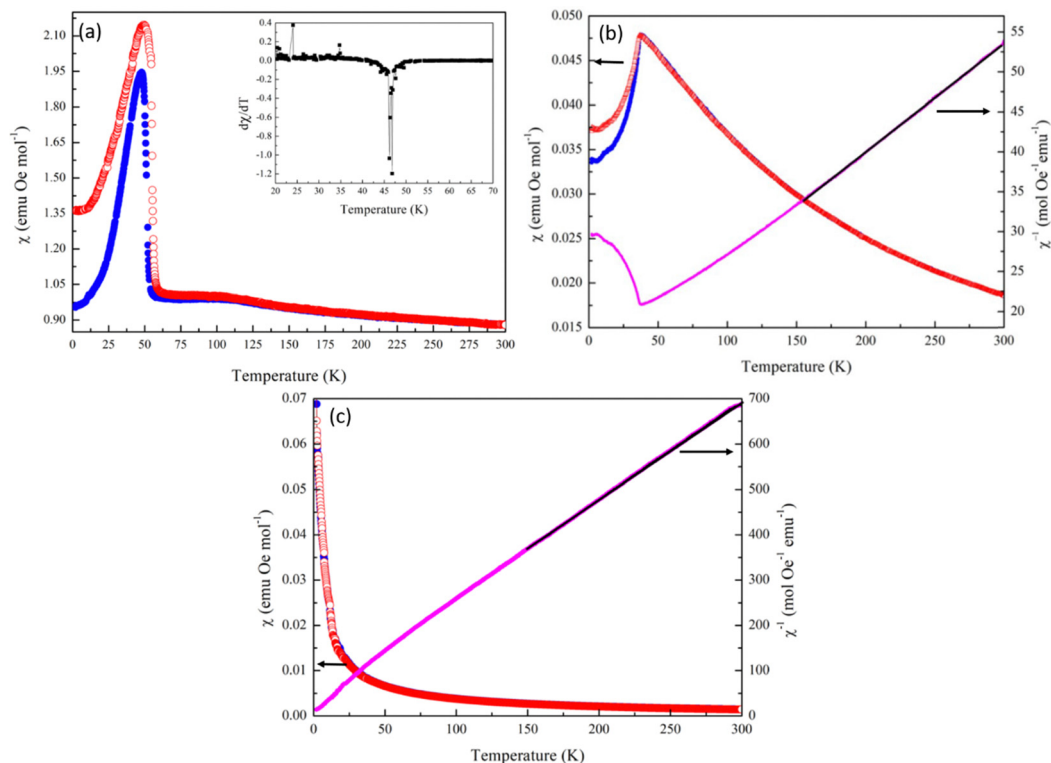


Fig. 6 Zero field cooled (blue) and field cooled (red) SQUID magnetometry data collected at 0.1 T and inverse ZFC susceptibility data where the black line shows the fit to the Curie–Weiss law for (a)  $\text{MnFeMo}_3\text{O}_8$  inset shows the  $d\chi/dT$  data highlighting  $T_N$  at  $\approx 46$  K, (b)  $\text{MnCoMo}_3\text{O}_8$  showing  $T_N \approx 35$  K and (c)  $\text{MnZnMo}_3\text{O}_8$  showing paramagnetic character.

$\text{MnFeMo}_3\text{O}_8$ , it is well known that very small (below the limits of detection in conventional diffraction experiments) iron oxide phases can have a large impact on magnetometry data. Since  $T_C$  for  $\text{Fe}_3\text{O}_4$  is expected to be 856 K<sup>66</sup> we have not been able to extract meaningful data from the Curie–Weiss fits of the inverse susceptibility. Field dependent data (Fig. S10(a) in ESI<sup>†</sup>) showed pinched hysteric behaviour characteristic of  $\text{Fe}_3\text{O}_4$  and no further information can be inferred from these data. However, it would be expected that we would see the same low temperature closure of the hysteresis loops as we observed for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and which is characteristic of the complex interplay between tetrahedral and octahedral sites in these materials.

In contrast with  $\text{Mn}_2\text{Mo}_3\text{O}_8$  we see a sharp antiferromagnetic transition in the magnetic susceptibility in  $\text{MnCoMo}_3\text{O}_8$  at  $T_N = 36.2(1)$  K consistent with what is typically observed for  $\text{Co}_2\text{Mn}_3\text{O}_8$ .<sup>5</sup> This suggests that there is a transition away from the ferrimagnetic structure determined from  $\text{Mn}_2\text{Mo}_3\text{O}_8$  towards the antiferromagnetic spin structure expected for  $\text{Co}_2\text{Mo}_3\text{O}_8$  which is consistent with the expected transition at  $x \approx 0.7$  (in  $\text{Mn}_{2-x}\text{Co}_x\text{Mo}_3\text{O}_8$ ) recently reported by Cheng *et al.*<sup>17</sup> Again we see a some divergence between the ZFC and FC data collected for  $\text{MnCoMo}_3\text{O}_8$  consistent with some traditional ferrimagnetic behaviour (net magnetic moment) arising as a result of the differences in magnetic moments between  $\text{Mn}^{2+}$   $d^5$  ( $5.91\mu_B$  spin only) and  $\text{Co}^{2+}$   $d^7$  ( $3.87\mu_B$  spin only) electronic configurations. This may also be suggestive of some magnetic behaviour arising as a result of incomplete trimerization of the Mo sub-lattice,

clustering effects or glassy behaviour. Between 150 K and 300 K we are able to fit the inverse susceptibility to the Curie–Weiss law giving  $\theta = -100.1(1)$  K confirming antiferromagnetic order with an effective magnetic moment of  $7.69 \mu_B$  per formula unit consistent with what would be expected from the spin only calculation ( $7.08 \mu_B$ ). Calculation of the frustration index gives a value of  $f = 2.8$  in line with the value observed for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and suggestive of some weak geometric frustration in  $\text{MnCoMo}_3\text{O}_8$ . We see no hysteric behaviour at either 300 K or 12 K in  $\text{MnCoMo}_3\text{O}_8$  consistent with type A antiferromagnetic order as is described by  $\text{Co}_2\text{Mo}_3\text{O}_8$  (Fig. S10(b) in ESI<sup>†</sup>).<sup>5</sup>

Finally, we see no evidence of any magnetic order within the measured temperature range in the susceptibility data collected for  $\text{MnZnMo}_3\text{O}_8$ . Previous work investigating Zn doping in  $\text{Fe}_2\text{Mo}_3\text{O}_8$  suggests that  $\text{FeZnMo}_3\text{O}_8$  is ferrimagnetic with an expected transition to a paramagnetic phase at a composition of approximately  $\text{Fe}_{0.75}\text{Zn}_{1.25}\text{Mo}_3\text{O}_8$ .<sup>34</sup> Gao *et al.*, have predicted that  $\text{CoZnMo}_3\text{O}_8$  (where  $\text{Zn}^{2+}$  occupies the tetrahedral sites and  $\text{Co}^{2+}$  the octahedral sites) would be expected to exhibit a striped magnetic order.<sup>67</sup> It therefore, seems reasonable to expect that  $\text{MnZnMo}_3\text{O}_8$  could have been predicted to show long-range magnetic order. However, Gao *et al.* suggested that intersite mixing leads to the suppression of magnetic order in  $\text{CoZnMo}_3\text{O}_8$  materials.<sup>67</sup> This suggests that in  $\text{MnZnMo}_3\text{O}_8$  there may be intersite mixing too, which results in the observation of paramagnetic behaviour on the level of our measurements. At high temperatures  $\text{MnZnMo}_3\text{O}_8$  follows Curie–Weiss





behaviour with fits to the inverse susceptibility providing values for  $\theta = -21.6(1)$  K) and a magnetic moment of  $5.4\mu_B$  consistent with the magnetic moment on  $Mn^{2+}$ . The negative Weiss constant may suggest a weakly AFM ordered state with  $T_N$  below 2 K but equally these may relate to the small amount of  $MnMoO_4$  impurities present in this material. Likewise, field dependent data (Fig. S10(c) in ESI†) collected at 300 K shows paramagnetic behaviour. In contrast, we see a slight “s” shape to data collected at 2 K. This again may be suggestive of weak (short-range) magnetic order in this material or be related to the small amount of  $MnMoO_4$ . Either way, these data provide no evidence for magnetic order in  $MnZnMo_3O_8$  over the temperature range studied.

In order to explore cation (dis)order and magnetic structure in these materials we have performed powder neutron diffraction experiments on the WISH ( $MnFeMo_3O_8$  and  $MnCoMo_3O_8$ )<sup>41</sup> and GEM ( $MnZnMo_3O_8$ )<sup>43</sup> diffractometers at the ISIS Neutron and Muon User facility. As expected, the 100 K data for  $MnFeMo_3O_8$  and  $MnCoMo_3O_8$  and 298 K data  $MnZnMo_3O_8$  show excellent fits to the  $P6_3mc$  model.<sup>47</sup> Refinement profiles (Fig. S11 and S12), parameters (Tables S7–S9) and details are given in the ESI.† Refinements were performed with secondary phases refined as observed in our powder X-ray diffraction study discussed above. We noted a small amount of  $MoO_2$  in the  $MnCoMo_3O_8$  sample, which was not detectable in our powder X-ray diffraction data. Additionally, for  $MnFeMo_3O_8$  it was necessary to include both the  $Fe_3O_4$  nuclear and magnetic phases<sup>68</sup> in our refinements. In order to explore A-site cation (dis)order all refinements were performed with  $Mn^{2+}$  and the dopant A-site cation situated on both tetrahedral (Mn1) and octahedral (Mn2) sites and allowed to refine. For both  $MnFeMo_3O_8$  and  $MnCoMo_3O_8$  we determined that both A-site cations are randomly distributed across both tetrahedral and octahedral sites. This may explain some of the differences observed in previous studies within SQUID magnetometry data which were performed on single crystals and assumed to exhibit A-site order. This suggests that the magnetic phases obtainable

(and thus other properties such as magnetoelectric coupling) can be further tuned through order and/or disorder and more complex cation doping regimes. Refinements performed for  $MnZnMo_3O_8$  suggests that there is a strong preference for  $Zn^{2+}$  to adopt the tetrahedral site with  $Mn^{2+}$  on the octahedral site. However, we do see a small amount of intersite mixing (approximately 10%) which may be enough to destabilise the expected magnetic ordering in this material as has been reported by Gao *et al.*<sup>67</sup>

At low temperature, we see no change in symmetry with all materials readily refined to the  $P6_3mc$  model.<sup>47</sup> Refinement details, full refinement profiles (Fig. S11 and S12) and parameters (Tables S7–S9) are given in the ESI.† On visual inspection of the 2 K powder neutron diffraction data collected for  $MnFeMo_3O_8$  and  $MnCoMo_3O_8$  there are clear differences between the magnetic phases observed, as expected from SQUID magnetometry data. For  $MnFeMo_3O_8$  additional magnetic Bragg intensity is observed on the (101), (103), (201) and (211) reflections similarly to those observed for  $Mn_2Mo_3O_8$ . In contrast,  $MnCoMo_3O_8$  shows additional magnetic Bragg intensity on the (100), (101), (200), (210) and (204) reflections. For  $MnZnMo_3O_8$  no magnetic Bragg contributions were observed as expected from the SQUID magnetometry measurements. Furthermore, we see no ion displacement or exchange striction effects in either the tetrahedral or octahedral bond lengths which remain reasonably constant over the temperature range studied (as shown in Fig. S13 in the ESI†). This confirms the lack of both magnetic and multiferroic character in  $MnZnMo_3O_8$ . Following the same procedure, we outlined for  $Mn_2Mo_3O_8$  using ISODISTORT<sup>69</sup> and  $k = (0,0,0)$ , gives the same IRs shown in Table 1. Refinements were subsequently performed using the  $\Gamma(2)$  and  $\Gamma(3)$  models since those models derived using IRs  $\Gamma(5)$  and  $\Gamma(6)$  failed to successfully account for the magnetic intensity observed for both  $MnFeMo_3O_8$  and  $MnCoMo_3O_8$ . For  $MnFeMo_3O_8$  we only achieved a stable refinement using the  $\Gamma(2)$  model whilst the opposite was true for  $MnCoMo_3O_8$  as expected from our previous

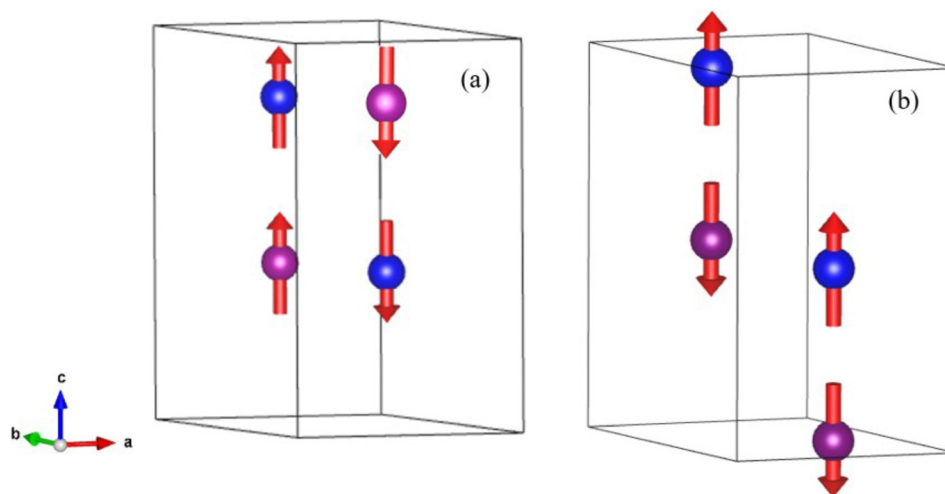


Fig. 7 Magnetic spin structure (red arrows) determined for (a)  $MnCoMo_3O_8$  and (b)  $MnFeMo_3O_8$  within the unit cell (black outline) at 2 K from the Rietveld refinement of powder neutron diffraction data. The blue and pink spheres represent manganese on the Mn1 (tetrahedral) and Mn2 (octahedral) crystallographic sites respectively.



discussions for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and our SQUID magnetometry data. The extracted magnetic structure for  $\text{MnFeMo}_3\text{O}_8$  is identical to the ferrimagnetic model determined for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  (as shown in Fig. 7) where the magnetic spins are antiferromagnetically coupled across the crystallographically distinct A-sites (tetrahedral – octahedral) and ferromagnetically coupled across the same site (tetrahedral – tetrahedral or octahedral – octahedral). The average magnetic moment on both sites was determined to be  $4.20(1)\mu_{\text{B}}$  which is consistent with what we have observed for  $\text{Mn}_2\text{Mo}_3\text{O}_8$  although perhaps a little bit higher than might be expected in a mixed system. However, we note that in the 2 K refinement of the  $\text{MnFeMo}_3\text{O}_8$  data, we have a small amount of intensity, which is unaccounted for. Refinements for this phase were complex containing five phases,  $\text{MnFeMo}_3\text{O}_8$  nuclear and magnetic phases,  $\text{MnMoO}_4$  nuclear phase and  $\text{Fe}_3\text{O}_4$  nuclear and magnetic phases. It is likely that this is either an artefact due to correlations of the fitting parameters across phases or it may be some magnetic intensity we have not accounted for in these refinements. Alternatively, we have considered that this may arise as a result of the Mo trimers not fully compensating. Previous computational studies have suggested that Mo does not contribute to the magnetic ground state.<sup>16</sup> Chen *et al.* investigated the possibility of spin liquid magnetic ground states in  $\text{A}_2\text{Mo}_3\text{O}_8$  materials (where A is non-magnetic ions, Mg, Sc and Zn).<sup>70</sup> They observed weak (low magnetic moment) magnetic ordering in these materials at approximately 15 K using SQUID magnetometry. However, they were unable to determine between ferromagnetic and canted antiferromagnetic ground states with neutron diffraction data demonstrating no discernible magnetic Bragg scattering.<sup>70</sup> Shekelton *et al.* looked at disrupting the Mo trimers through the addition of lithium in the material,  $\text{LiZn}_2\text{Mo}_3\text{O}_8$ .<sup>71</sup> They suggest that  $\frac{2}{3}$  of the Mo magnetic spins condense into singlet states below 96 K. However, no long-range static magnetically ordered state is observed with no magnetic Bragg peaks observed in powder neutron diffraction data.<sup>71</sup> This suggests that whilst small contributions to SQUID magnetometry data may arise as a result of incomplete trimerization of the Mo sub-lattice it is unlikely to be observable within our powder neutron powder diffraction study as either resolvable magnetic Bragg character or additional intensity. Lastly, given that a transition to the antiferromagnetic state is expected at  $x \sim 1.2$ , it is plausible that a mixed magnetically ordered state is observed with both ferrimagnetic and antiferromagnetic order present within our sample potentially as a result of cation inhomogeneity.<sup>18</sup> However, due to the complexity of these refinements we have not been able to investigate this further. Additionally, since that the magnetic structure we have derived for this material is consistent with the SQUID magnetometry data we are confident in our structural solution. Additionally, we did not see any contribution from the magnetic phase of  $\text{MnMoO}_4$  presumably because the signal from this component is too weak to detect. Likewise, for  $\text{MnCoMo}_3\text{O}_8$  we also see no evidence of magnetic contributions from  $\text{MnMoO}_4$  in our data. Refinement of the magnetic structure (shown schematically in Fig. 7) indicates antiferromagnetic coupling both across crystallographically distinct sites (tetrahedral and octahedral) and importantly between

crystallographically identical sites (tetrahedral – tetrahedral and octahedral – octahedral) consistent with what is expected for  $\text{Co}_2\text{Mo}_3\text{O}_8$ .<sup>5</sup> Magnetic moments were calculated to be  $3.38(1)\mu_{\text{B}}$  consistent with what is expected for a mixed  $\text{Co}^{2+}/\text{Mn}^{2+}$  material.

## Conclusions

We have investigated the structure–property correlations in  $\text{Mn}_2\text{Mo}_3\text{O}_8$ ,  $\text{MnFeMo}_3\text{O}_8$ ,  $\text{MnCoMo}_3\text{O}_8$  and  $\text{MnZnMo}_3\text{O}_8$  using powder neutron diffraction and magnetic property measurements. For  $\text{Mn}_2\text{Mo}_3\text{O}_8$  we confirm the ferrimagnetic model for the magnetic structure such that magnetic moments are coupled antiferromagnetically across crystallographically distinct A-sites (tetrahedral–octahedral) and ferromagnetically coupled for individual sites (tetrahedral – tetrahedral or octahedral – octahedral). Interestingly, ionic displacements and/or exchange striction behaviour on the tetrahedral site appears to be critically dependent on the spin behaviour on the tetrahedral site with a sudden drop in the Mn–O bond length at the apex of the tetrahedral unit at 2 K. This is important, as it is coincident with the loss of hysteric behaviour and the realisation of a compensated antiferromagnetic state. The driving forces behind this are not known. It remains undetermined if a switchable ferroelectric state is achieved at  $T_{\text{N}}$  with some kind of re-entrant non-switchable or alternative state realised at 2 K or if a fully switchable ferroelectric state is not obtainable until 2 K. We note that whilst the ferroelectric state has been shown to exist in both  $\text{Fe}_2\text{Mo}_3\text{O}_8$  and  $\text{Co}_2\text{Mo}_3\text{O}_8$  it has yet to be confirmed in  $\text{Mn}_2\text{Mo}_3\text{O}_8$ .<sup>5,72</sup> This warrants further investigation to fully understand any electronic behaviour and potential magnetoelectric coupling (as has been reported for  $\text{Fe}_2\text{Mo}_3\text{O}_8$ ,  $\text{Ni}_2\text{Mo}_3\text{O}_8$  and  $\text{Co}_2\text{Mn}_3\text{O}_8$ <sup>5,23,28,72</sup>) in this material.

The magnetic structures for  $\text{MnFeMo}_3\text{O}_8$  and  $\text{MnCoMo}_3\text{O}_8$  have been determined as ferrimagnetic and antiferromagnetic respectively. In contrast  $\text{MnZnMo}_3\text{O}_8$  shows no long range magnetic order down to 2 K. Our data suggests that these materials are cation disordered with  $\text{A}^{2+}$  and  $\text{Mn}^{2+}$  distributed randomly on both tetrahedral and octahedral sites in both the Co and Fe analogues whilst some site preference is shown in the Zn material ( $\sim 90\%$  site order for Mn on the octahedral site and Zn on the tetrahedral site). Further work is required to understand the roles of cation (dis)order in these systems for tuning the magnetic character in these materials<sup>34,67</sup>

Overall, this work demonstrates that there is still much to unravel with respect to the structure–property correlations in  $\text{Mn}_2\text{Mo}_3\text{O}_8$  and related systems. This is a magnetically rich family of materials with the potential for careful property tuning leading to many exciting and technologically important applications.

## Data availability

ESI† includes all refinement details (including information about which refinement software has been used, what has been refined and how the data has been treated) and refined data alongside supporting magnetic property data for all materials



presented in this work. Powder neutron diffraction raw data is available through the ISIS data gateway with <https://doi.org/10.5286/ISIS.E.RB222055> and <https://doi.org/10.5286/ISIS.E.XB2390084> for the WISH and GEM data respectively.<sup>41,43</sup>

## Conflicts of interest

We report no conflicts of interest.

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