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Double-hybrid density functionals applied to a large set of INVEST systems: validating the (SOS1-)PBE-DH-INVEST expressions

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Abstract

We thoroughly assess here the recently developed PBE-DH-INVEST expression and its SOS1-PBE-DH-INVEST variant, both belonging to the family of Double-Hybrid (DH) density functionals, against the NAH159 dataset of organic molecules displaying a very low (positive or even negative) energy gap, ΔE_{ST} , between the lowest-energy excited-state of singlet (S_1) and triplet (T_1) multiplicity. The NAH159 dataset comprises a large set of substituted derivatives of azulene, azupyrene, isopyrene, heptalene, cyclazine (or monoazaphenalene), pentazine (or pentaazaphenalene), and heptazine (or heptaazaphenalene) systems, thus covering most of the chemical templates so far discovered displaying $\Delta E_{ST} < 0$ values. The performance of any model able to deliver correct ΔE_{ST} values, both in sign and magnitude, is critical for further studies in OLEDs and related applications. Given the robustness and accuracy of the results obtained by the (SOS1-)PBE-DH-INVEST functionals, together with their moderate basis set dependence, we can recommend them as an alternative to more costly wavefunction-based methods or other DH density functionals.

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1 Introduction

INVEST (INVErted Singlet-Triplet excited-state energies) systems are those defined as molecules violating the (natural) order of the energy of (at least one of) their singlet and triplet molecular pairs, in the sense that a singlet electronic state can be found lower in energy than the associated triplet electronic state, thus violating the extension of Hund's rules to molecules. In the context of excited-state energies relevant to photophysics and Organic Light-Emitting Diodes (OLEDs), to which this study pertains, that violation mostly applies to the lowest-energy singlet-triplet pair, and thus implies that the singlet $(S_1 \leftarrow S_0)$ excitation energy might become lower than the triplet $(T_1 \leftarrow S_0)$ excitation energy, thus leading to a negative singlet-triplet energy difference (or gap) $\Delta E_{ST} < 0$ after subtracting the values $E(S_1 \leftarrow S_0) - E(T_1 \leftarrow S_0)$. Hence, a negative ΔE_{ST} value contradicts the positive (and large) values typically found for the singlet-triplet excited-states gap in conjugated chromophores, oligomers, and polymers, ^{1,2} but as we will see next it is far from being just a theoretical anomaly or a physical curiosity.

Although the possibility of having a singlet-triplet inversion leading to $\Delta E_{ST} < 0$ values was experimentally^{3,4} and theoretically^{5,6} predicted time ago, already in the 80s, it has been recently invigorated by some modern yet challenging discoveries at both levels too. First of all, not only the original set of the very few molecules historically investigated (e.g. cycl[3.3.3]azine, or simply cyclazine, or 1,4,7-triazacycl[3.3.3]azine) are also shown to behave so particularly in modern experimental studies, but there has also been the corresponding confirmation along the last years for many other derivatives, $^{7-17}$ both in solution and thin-film environments. Therefore, these systems are also receiving now a large interest 18,19 for practical applications, thus constituting a new platform for further advances in photophysics [e.g. Organic Light Emitting Diodes (OLEDs)] or photocatalysis. For the former, the barrierless

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energy recovery of the (dark) triplet excitons could foster the performance of OLEDs upon increasing the internal quantum efficiency,²⁰ while for the latter the larger singlet excitation lifetimes could compensate other energy losses during the photocatalytic process.²¹

Regarding the computational studies performed so far, the application of theoretical calculations has allowed to first isolate, and then understand, the quantum-chemical origin of that phenomenon, ^{22–25} as well as to screen/predict possible candidates based on a larger variety of molecular scaffolds, ^{26–37} which is also fostering the corresponding experimental search. The correct prediction of $\Delta E_{ST} < 0$ values should of course rely on the correct prediction of the individual excitation energies $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$, hopefully avoiding any error cancellation. As simple as it seems, the pronounced stabilization of the S_1 state in these systems, with respect to the corresponding T_1 state, is driven by electron correlation effects beyond single-particle excitations. ^{22,23} This fact precludes the blind use of Time-Dependent Density Functional Theory (TD-DFT), independently of the underlying exchange-correlation functional chosen, and prompts for the use of wavefunction-based methods introducing n-tuple particle excitations. $^{38-52}$ However, it is also well-known that these latter excitations unfavorably scale with the system size, thus hindering the application to large (real-world) systems or its use in massive (low-cost) high-throughput screenings.

On the other hand, a set of recent studies has popularized the use of DH density functionals for this issue, ^{53–57} which goes beyond standard TD-DFT applications, thanks to their capacity to introduce double excitations to electronic states of any multiplicity. The accuracy of these methods critically depends on their specific formulation, and more particularly to the weight given to correlation effects beyond single-particle excitations ⁵³ in analogy with wavefunction-based methods. Very recently, with the lessons gained so far for

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the optimal formulation of a DH functional able to correctly deliver $\Delta E_{ST} < 0$ values, the so-called PBE-DH-INVEST functional was developed by some of us. ⁵⁸ The original goal behind developing a tailored DH density functional was to provide a systematic and as low as possible error with respect to wavefunction-based reference results, upon calculations performed on a set of (mostly) triangle-shaped molecules. Given these antecedents, we will thus systematically assess here the accuracy of PBE-DH-INVEST on a significantly more extended dataset of molecules (i.e., the NAH159 set ³² of compounds shown in Figure 1, see the Supplementary Materials for the detailed list) for the individual $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ excitation energies and the corresponding ΔE_{ST} values. We will complementarily check the basis set dependence of the model and the performance of the spin-scaled SOS1-PBE-DH-INVEST version, based again on a non-empirical derivation reached before for DH density functionals. ⁵⁹

2 Theoretical and computational details

A DH density functional 60,61 represents a step further with respect to the very popular hybrid functionals, for which the EXact-eXchange (EXX) is coupled to an exchange functional ($E_x[\rho]$) by a parameter a_x . Complementarily to this, in the case of double-hybrid expressions the correlation contribution is also splitted between the correlation functional ($E_c[\rho]$) and a wavefunction-based correlation component by a parameter a_c . For the sake of having a computational cost as low as possible, the latter correlation component is that offered by a perturbation treatment at second-order. Following this simple yet effective philosophy, many DH density functionals do exist now in literature, like those related to the pioneering B2-PLYP expression, 62 the DSD-based family of expressions, 63 or the non-empirical expressions 64 such as PBE0-DH⁶⁵ or PBE-QIDH, 66 to name just a few of the existing ones.

2.1 The PBE-DH-INVEST expression

The recently derived PBE-DH-INVEST functional follows the aforesaid general expression for a DH density functional, where the values of the coefficients a_x and a_c are chosen (vide infra) to better represent the INVEST systems under consideration here:

$$E_{xc}^{\text{PBE-DH-INVEST}}[\rho] = \left(\frac{5}{3}\right)^{-1/3} E_x^{\text{EXX}}[\psi_i] + \left[1 - \left(\frac{5}{3}\right)^{-1/3}\right] E_x[\rho] + \frac{3}{5} E_c^{\text{PT2}}[\psi_i, \psi_a] + \left(1 - \frac{3}{5}\right) E_c[\rho]. \tag{1}$$

These (non-parameterized) coefficients weight the EXact-eXchange (EXX) expression, $a_x = \left(\frac{5}{3}\right)^{-1/3}$, and the 2nd. order Perturbation Theory (PT2) contribution, $a_c = \frac{3}{5}$, and are: (i) based on the relationship $a_c = a_x^3$ used for deriving ^{65,66} non-empirical double-hybrid functionals; and (ii) originally derived very recently ⁵⁸ as a compromise to obtain accurate values for INVEST systems, yet keeping an affordable computational cost. The wavefunction-based terms entering into Eq. (1) are given by the well-known (for the example of a restricted calculation) first-principles expressions:

$$E_x^{\text{EXX}}[\psi_i] = -\frac{1}{2} \sum_{ij}^{N/2} \int \int \psi_i^{\star}(\mathbf{r}) \psi_j^{\star}(\mathbf{r}') \frac{1}{|\mathbf{r} - \mathbf{r}'|} \psi_j(\mathbf{r}) \psi_i(\mathbf{r}') d\mathbf{r} d\mathbf{r}', \quad (2)$$

$$E_c^{\text{PT2}}[\psi_i, \psi_a] = -\frac{1}{4} \sum_{i,j}^{N/2} \sum_{a,b}^{N \ge N+1} \frac{|\langle \psi_i \psi_j | | \psi_a \psi_b \rangle|^2}{(\epsilon_a + \epsilon_b) - (\epsilon_i + \epsilon_j)},$$
(3)

where the set of occupied ($\{\psi_i\}$) and virtual ($\{\psi_a\}$) orbitals are obtained self-consistently yet excluding the PT2 term, with their corresponding energies given by ϵ_i and ϵ_a , respectively. The parameter-free exchange, $E_x[\rho]$, and correlation, $E_c[\rho]$, functionals of Eq. (1) are those given by the Perdew-Burke-Ernzerhof (PBE) model, ⁶⁷ which is also in agreement with the philosophy of minimally empirical double-hybrid functionals.

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2.2 The SOS1-PBE-DH-INVEST expression

On the other hand, the PT2 term of Eq. (1) can be decomposed into samespin and opposite-spin correlation contributions, 68 scaled by the corresponding coefficients c_{ss} and c_{os} :

$$E_c^{\text{PT2}} = c_{ss} E_c^{ss-\text{PT2}} + c_{os} E_c^{os-\text{PT2}}.$$
 (4)

By setting $c_{ss} = 0$ and $c_{os} = 4/3$ in Eq. (4) for the corresponding PBE-DH-INVEST functional, we obtain its Spin-Opposite-Scaled version, named SOS1-PBE-DH-INVEST, which performs similarly to the former functional. However, the neglect of the same-spin term might bring some technical advantages ^{69,70} since recent implementations of SOS-based models for ground or excited states yielded a reduction of the formal cost of these methods from $O(N^5)$ to $O(N^4)$, with N being related to the system size.

2.3 Extension to excited states

Importantly, the extension 71,72 to calculate the excitation energies $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ (indistinctly called Ω in the following) by DH expressions relies on a correction, termed $\Delta(D)$, to the standard excitation energies calculated at the TD-DFT level (denoted as Ω' in the following) given by:

$$\Omega = \Omega' + a_c \Delta(D), \tag{5}$$

which is a state- and system-dependent Double (D) excitations contribution⁷³ weighted by the same coefficient (a_c) than that of the PT2 term in Eq. (1). Thus, DH density functionals are able to naturally overcome the single-excitation picture provided by standard TD-DFT treatments,⁵³ which are unable to provide the correct ΔE_{ST} values for INVEST systems^{22,23} due to the missing $\Delta(D)$ term. Note that these calculations are done in a two-step fashion. First, values of Ω' are calculated discarding the $E_c^{PT2}[\psi_i, \psi_a]$ term in Eq. (1), which is thus equivalent to run a standard TD-DFT calculation Open Access Article. Published on 05 June 2025. Downloaded on 6/8/2025 9:03:28 AM.

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with a hybrid functional bearing the amount of EXX given by a_x . The results from this first step are labelled as PBE-DH-INVEST(SCF) in the following, according to the notation followed in previous publications. Note also that the molecular orbitals and their energies are self-consistently obtained with this PBE-DH-INVEST(SCF) hybrid functional, thus further motivating this Self-Consistent-Field (SCF) notation used.

The extension to excited states of the SOS1-PBE-DH-INVEST functional follows the implementation 74,75 for which the SOS1-based excitation energies are given by $\Omega = \Omega' + \Delta(\text{SOS1-D})$. That implementation is based on an energy correction to the total Configuration Interaction Singles (CIS) energy of an excited state:

$$E_c = \left\langle \Phi_{\text{CIS}} | \hat{V} | \hat{U}_2 \Phi_0 \right\rangle + \left\langle \Phi_{\text{CIS}} | \hat{V} | \hat{T}_2 \hat{U}_1 | \Phi_0 \right\rangle, \tag{6}$$

where Φ_0 is the 0th-order determinant, $\Phi_{\text{CIS}} = \hat{U}_1 \Phi_0 = \sum_{ia} t_i^a \Phi_i^a$ is the CIS determinant with t_i^a single-excitation amplitudes and Φ_i^a singly-excited determinant, \hat{U}_1 and \hat{U}_2 are operators generating the singly and doubly excited wave functions from Φ_0 , respectively, \hat{V} is a perturbation potential, and \hat{T}_2 is an operator generating the double excitation of two CIS-inactive electrons. The first and second terms above are known as the "direct" and "indirect" terms, respectively. The scaling into same- and opposite-spin components leads to:

$$E_c = \left\langle \Phi_{\text{CIS}} | \hat{V} | \left(c_U^{os} \hat{U}_2^{os} + c_U^{ss} \hat{U}_2^{ss} \right) \Phi_0 \right\rangle + \left\langle \Phi_{\text{CIS}} | \hat{V} | \left(c_T^{os} \hat{T}_2^{os} + c_T^{ss} \hat{T}_2^{ss} \right) \hat{U}_1 | \Phi_0 \right\rangle. \tag{7}$$

In this case, the values of the coefficients are given by $c_T^{ss} = c_U^{ss} = 0$ and by $c_T^{os} = c_U^{os} = 4/5$ (note that $a_c \cdot c_{os} = 4/5$) for the corresponding SOS1-PBE-DH-INVEST model, according to the above implementation and notation described by Goerigk *et al.* in Ref. 75.

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2.4 Computational details

The geometries of all the compounds are those optimized at the ω B97X-D/aug-cc-pVTZ level in Ref. 32. All the calculations reported here are done with the ORCA 5.0.3 release ⁷⁶ employing the sufficiently large aug-cc-pVTZ basis set, ⁷⁷ if not otherwise stated, which also allowed us to compare them with previously available results in the literature at the LR-CC2 level using the same basis set. The complementary calculations done here with the def2-TZVP basis set, ⁷⁸ for some selected compounds, did not bring any meaningful difference, confirming the minor influence of the basis set size beyond a ξ -triple basis set for a DH density functional. On the other hand, we will also assess the influence of reducing the basis set size comparing the results obtained using the aug-cc-pVDZ with those using the aug-cc-pVTZ basis set.

We will also use the Tamm-Dancoff Approximation⁷⁹ (or TDA in the following) to compute the Ω' values, given its importance for practical calculations and seen its reduced computational cost with respect to the full solution of the TD-DFT equations. This is of interest since: (i) TDA is the default option in some computational packages; (ii) TDA is the most accepted option to excited-state studies of large chromophores; $^{80-82}$ and (iii) simplified treatments based on TDA start to be available in the literature, 83 further reducing the computational cost for excited state calculations of large samples of compounds. Furthermore, the set of optimal (a_x, a_c) pair of values for the PBE-DH-INVEST model were originally derived using TDA, and its use without that option might lead to some inconsistencies.

2.5 Choice of the NAH159 dataset

The NAH159 dataset (see Figure 1 again) was originally³² compiled by Garner *et al.*, and comprises a large set of substituted derivatives of triangle-shaped (e.g. cyclazine, pentazine, and heptazine) as well as non-alternant

hydrocarbon systems. The set was later used 47 by Mewes et~al. to crosscheck the performance of $\Delta \mathrm{DFT}$ and ROKS methods and by Odoh et~al. to assess 84 the impact of ground-state geometries for vertical excitation energies. More specifically, the dataset comprises azulene, azupyrene, isopyrene, cyclopenta [e,f] heptalene, azuleno [2,1,8-k,i,a] heptalene, benzo [f] cyclopenta [c,d] azulene, cyclazine or monoazaphenalene, pentazine or pentazaphenalene, and heptazine or heptazaphenalene derivatives. Due to the structural diversity and relatively large number of systems included, it is believed to constitute and excellent dataset for assessing other computational methods.

Mewes et al. obtained LR-CC2/aug-cc-pVTZ values for all the systems of the dataset, which compared favourably against other highly accurate, yet more costly methods, like Mk-MR-CCSD(T), and also against theoretically best estimates ⁴⁵ by Loos et al.. The ΔE_{ST} values are between 0.39 and -0.32 eV, thus spanning a relatively large range of values, with $\Delta E_{ST}^{LR-CC2} > 0$ for 40 systems and $\Delta E_{ST}^{LR-CC2} < 0$ for the rest. Therefore, for all the reasons exposed above, these LR-CC2/aug-cc-pVTZ values will serve as reference to compare those calculated with (SOS1-)PBE-DH-INVEST, thus allowing us to analyze in detail their performance for ΔE_{ST} values of positive and negative sign.

2.6 Statistical analysis

The 'Mean-Signed Deviation' (MSD), 'Mean Absolute Deviation' (MAD), and the 'Root Mean-Squared Deviation' (RMSD) will be used to quantitatively compare the PBE-DH-INVEST with the LR-CC2 results. Recall that both set of calculations use the same aug-cc-pVTZ basis set and are performed at the same (ground-state) geometries. More specifically, they will be calculated as $MSD = \frac{1}{n} \sum_{i}^{n} x_{i}$, $MAD = \frac{1}{n} \sum_{i}^{n} |x_{i}|$, and $RMSD = \sqrt{\frac{1}{n} \sum_{i}^{n} x_{i}^{2}}$, respectively, with n being the number of excitation energies $(S_{1} \leftarrow S_{0} \text{ or } T_{1} \leftarrow S_{0})$

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or the ΔE_{ST} values, with $x_i = \Omega^{\text{PBE-DH-INVEST}} - \Omega^{\text{LR-CC2}}$, in the former case, or $x_i = \Delta E_{ST}^{\text{PBE-DH-INVEST}} - \Delta E_{ST}^{\text{LR-CC2}}$ in the latter. According to some recent recommendation for optimal statistical analysis, we will also consider the Δ_{err} value, which is the difference between the most positive and the most negative deviation of the results with respect to the LR-CC2 values, as well as the kurtosis value, which for a normal distribution should follow $\frac{\text{MAD}}{\text{RMSD}} = \sqrt{\frac{2}{\pi}} \approx 0.8$ thus indicating minor systematic errors. The corresponding values for the PBE-DH-INVEST and SOS1-PBE-DH-INVEST methods are gathered in Table 1. For the sake of completeness, we will also show (vide infra) the values for the (hybrid) PBE-DH-INVEST(SCF) calculations, to clearly disentangle the role played by double excitations.

3 Results and discussion

3.1 Assessment of the PBE-DH-INVEST model

First of all, we will compare in the following the values (see the Supplementary Material) obtained by the PBE-DH-INVEST model for the $S_1 \leftarrow S_0$, $T_1 \leftarrow S_0$, and ΔE_{ST} energies with respect to the LR-CC2 results (see Figure 2). Furthermore, to clearly disentangle the prominent effect played by the $\Delta(D)$ -based correction for the final excitation energies, see Eq. (5), we will also include the Ω' values in the figures and the accompanying discussion. Recall that Ω' are the excitation energies obtained with a standard TD-DFT treatment discarding the $E_c^{PT2}[\psi_i, \psi_a]$ term in Eq. (1), which thus translates to neglecting that $\Delta(D)$ -based correction in the final excitation values. The values obtained with this approximation are termed as PBE-DH-INVEST(SCF), to emphasize that they are obtained after a Self-Consistent-Field (SCF) typical of a hybrid expression, with an exact-exchange weight as high as $a_x = \left(\frac{5}{3}\right)^{-1/3}$ and do not consequently include the effect of the double excitations at all.

Inspecting Figure 2 we can easily see how the $S_1 \leftarrow S_0$ excitation energies

are strongly overestimated by the hybrid PBE-DH-INVEST(SCF) method, and how the deviations progressively increase with the value of the excitation energies. For instance, while the difference between PBE-DH-INVEST(SCF) and LR-CC2 is 0.46 eV for the lowest $S_1 \leftarrow S_0$ excitation energy of the dataset (1.361 vs. 0.897 eV, respectively), that difference increases to 1.45 eV for the highest $S_1 \leftarrow S_0$ excitation energy (5.437 vs. 3.989 eV, respectively). Fitting the PBE-DH-INVEST(SCF) data by a linear regression, we obtain $\Omega'(S_1) = 0.143 + 1.30 \ \Omega^{LR-CC2}$ and a squared correlation coefficient $r^2 = 0.9814$, with a considerably high value obtained for the slope in agreement with the large deviations found. On the other hand, the PBE-DH-INVEST method shows a very robust performance, practically matching the LR-CC2 reference values for all the range of values, with minimal differences irrespective of the molecules and their excitation energies. Going into more detail, the LR-CC2 values are slightly but almost systematically overestimated by PBE-DH-INVEST, that overestimation ranging from 0.01 to 0.19 eV, with an average value of 0.11 eV. The fitting now for the PBE-DH-INVEST values gives $\Omega(S_1) = 0.061 + 1.02 \ \Omega^{LR-CC2}$, with $r^2 = 0.9984$, with a slope close to the value of 1.0 for a perfect correlation between the PBE-DH-INVEST and LR-CC2 methods.

Analyzing now the $T_1 \leftarrow S_0$ excitation energies (see again Figure 2) we observe a similar but much more attenuated performance compared with the $S_1 \leftarrow S_0$ excitation energies, with less deviations between the PBE-DH-INVEST(SCF) and PBE-DH-INVEST values. The LR-CC2 values are now under- or overestimated by both methods, although the general trend is again an overestimation, slightly more marked for the PBE-DH-INVEST(SCF) model. Fitting the PBE-DH-INVEST(SCF) data by a linear regression, we obtain $\Omega'(T_1) = -0.226 + 1.19 \Omega^{LR-CC2}$, with $r^2 = 0.9724$. Doing the same with the PBE-DH-INVEST data, the result is now $\Omega(T_1) = 0.035 + 1.03 \Omega^{LR-CC2}$, with $r^2 = 0.9959$. The fitting shows again the robust performance of the

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PBE-DH-INVEST model for the whole set of molecules, with a similar slope calculated for both $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ excitation energies (i.e., 1.02 vs. 1.03) and a very high correlation coefficient r^2 (0.998 vs 0.996) for both cases. Generally speaking, the role of double excitations introduced by the PBE-DH-INVEST model is the reason for their greater performance (vide infra) for both $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ excitation energies.

The performance of PBE-DH-INVEST(SCF) and PBE-DH-INVEST models for the ΔE_{ST} values is also presented in Figure 2. The values are more scattered and largely overestimated by using the hybrid PBE-DH-INVEST(SCF) functional, since double corrections are not introduced at this level, as it is also evidenced by the linear fitting done: $\Delta E_{ST}^{\text{PBE-DH-INVEST(SCF)}} = 0.613 + 1.43 \ \Delta E_{ST}^{\text{LR-CC2}}$, $r^2 = 0.7326$. On the other hand, the ΔE_{ST} values are again robustly calculated by PBE-DH-INVEST and fitted to the expression $\Delta E_{ST}^{\text{PBE-DH-INVEST}} = 0.018 + 1.05 \ \Delta E_{ST}^{\text{LR-CC2}}$, $r^2 = 0.9375$. Note the low slopes (1.02–1.05) obtained for the $S_1 \leftarrow S_0$, $T_1 \leftarrow S_0$, and ΔE_{ST} fittings, which are behind the good results systematically obtained. Indeed, the ΔE_{ST} deviations between the LR-CC2 and the PBE-DH-INVEST oscillate between -0.21 and 0.11 eV, showing the great performance of the PBE-DH-INVEST values.

Not surprisingly, the MSD, MAD, and RMSD errors at the PBE-DH-INVEST(SCF) level are considerably higher, see Table 1, than the values for the PBE-DH-INVEST once the double corrections are introduced in the latter case for both the $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ excitation energies. The values at the former level are unreliable for making any robust prediction for this kind of systems, as a consequence of the poor performance of the PBE-DH-INVEST(SCF) method shown in Figure 2, which would be shared by standard TD-DFT treatments employing a hybrid functional. Strikingly, the error for the $T_1 \leftarrow S_0$ excitation energies are largely reduced with respect to the

 $S_1 \leftarrow S_0$ values (e.g. compare a MAD value of 0.77 eV for the former with respect to 0.23 eV for the latter) which reflects the triplet instability problem ⁸⁶ typical of TD-DFT calculations. The use of the Tamm-Dancoff approximation helps to reduce the error affecting the $T_1 \leftarrow S_0$ excitation energies, ^{87–89} which is known to markedly depend on the a_x value (i.e., the greater the a_x values is, the larger the influence of the Tamm-Dancoff approximation for the $T_1 \leftarrow S_0$ excitation energies). Following the error metrics commented before, we can also calculate the difference between the more positive and the more negative deviation of the results with respect to the LR-CC2 values, or Δ_{err} in the following, which amounts to values as high as 1.14, 1.34, and 0.91 eV for the $S_1 \leftarrow S_0$, $T_1 \leftarrow S_0$, and ΔE_{ST} results, respectively. This Δ_{err} range also remarks once again the unreliability of the PBE-DH-INVEST(SCF) calculations.

Interestingly, the values of the MSD errors from the PBE-DH-INVEST calculations are as low as 0.1 eV, for both the $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ excitation energies, and of the same size which translates to an even lower (and thus very competitive) MSD value of less than 0.02 eV for the corresponding ΔE_{ST} . This also explains the low values, of only 0.04 and 0.05 eV respectively, for the MAD and RMSD errors. The Δ_{err} values are 0.18, 0.37, and 0.31 eV for the $S_1 \leftarrow S_0$, $T_1 \leftarrow S_0$, and ΔE_{ST} results, respectively, and thus are also considerably reduced with respect to the previous PBE-DH-INVEST(SCF) values. These error metrics clearly emphasize the key role played by the double excitations to bring the results much closer to the reference LR-CC2 ones. That influence will be analyzed in more detail in the next section. Additionally, the ΔE_{ST} values closely follow a normal distribution, according to a kurtosis value around 0.8, with a larger kurtosis value for $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ excitation energies indicating a distribution with a more flattened peak and shorter tail (i.e., a platykurtic distribution)

We discuss next the case when the PBE-DH-INVEST ΔE_{ST} value differs

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in sign with respect to that calculated by LR-CC2. A false negative, when $\Delta E_{ST}^{\mathrm{LR-CC2}} > 0$ but $\Delta E_{ST}^{\mathrm{PBE-DH-INVEST}} < 0$, only occurs for molecule 132. On the other hand, false positives, when $\Delta E_{ST}^{\mathrm{LR-CC2}} < 0$ but $\Delta E_{ST}^{\mathrm{PBE-DH-INVEST}} > 0$

The sign with respect to that calculated by ER-CC2. A laise negative, when $\Delta E_{ST}^{\rm LR-CC2} > 0$ but $\Delta E_{ST}^{\rm PBE-DH-INVEST} < 0$, only occurs for molecule 132. On the other hand, false positives, when $\Delta E_{ST}^{\rm LR-CC2} < 0$ but $\Delta E_{ST}^{\rm PBE-DH-INVEST} > 0$, happens for several molecules, namely 3, 5, 7, 8, 10, 30, 40, 100, 102, 103, 104, 133, and 153. Therefore, in just 14 out of the 159 systems (8.8 % of the cases) there is a wrong prediction of the ΔE_{ST} sign. However, we also note that for these cases the absolute value of $\Delta E_{ST}^{\rm LR-CC2}$ is quite small, $0.01 < |\Delta E_{ST}^{\rm LR-CC2}({\rm in~eV})| < 0.06$, and of the same size than the MAD or RMSD values. Therefore, a minimal deviation between the two methods could reverse the sign. Hence, for future uses of PBE-DH-INVEST in e.g. massive and blind screenings of candidate molecules, we always recommend to impose some thresholds (e.g. $\Delta E_{ST}^{\rm PBE-DH-INVEST} < 0.05$ eV) to not completely discard possible INVEST systems.

3.2 Comparison with related models

We would also like to compare the performance of the PBE-DH-INVEST model with respect to other methods and results available in the literature. First of all, we note that the ratio $\frac{a_x}{a_c} \approx 1.4$ satisfied by the PBE-DH-INVEST model, without any parameterization, is very close to the one recently disclosed 90 after independently optimizing both coefficients for a similar DH density functional, and thus relaxing the condition $a_c = a_x^3$ typical of minimally empirical double-hybrid density functionals. The authors searched the best performance of a DH density functional with the expression given by Eq. (1) employing also the PBE exchange and correlation functionals, which led to final values of $a_x = 0.75$ and $a_c = 0.55$, and thus to a corresponding ratio of $\frac{a_x}{a_c} \approx 1.4$ too. However, those authors employed (a limited set of) triangle-shaped molecules and a smaller (aug-cc-pVDZ) basis set. It is thus quite satisfying to note the excellent performance of the non-parameterized PBE-DH-INVEST model for a much larger (i.e., 159 vs. 12 molecules) dataset.

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The Δ SCF method has also been applied before to the NAH159 dataset, ⁴⁷ correctly predicting the ΔE_{ST} sign in 83% of cases using the PBE0 functional and the smaller def2-SVP basis set. However, this method is known to largely depend on: (i) the window or molecular orbitals selected; in fact when the HOMO and LUMO orbitals are used (instead of the set HOMO-1, HOMO, LUMO, LUMO+1) to build all the involved electronic states, the percentage of correct predictions reduces from 83% to 77%; and (ii) the underlying exchange-correlation functional used, with large differences between them depending on the a_x value; i.e., the authors tested PBE ($a_x = 0$), PBE0 ($a_x = 1/4$), PBE38 ($a_x = 0.38$), and PBE50 ($a_x = 1/2$). The best results were obtained at the PBE0/def2-SVP level with the HOMO-1, HOMO, LUMO, LUMO+1 window of orbitals: MSD, MAD, and RMSD values (all in eV) of 0.002, 0.056, and 0.063 for ΔE_{ST} , and thus slightly larger than the best results obtained here with the PBE-DH-INVEST double-hybrid functional.

3.3 Oscillator strength values

We also inspected the oscillator strength values, f_{osc} , necessarily calculated at the PBE-DH-INVEST(SCF) level according to the existing implementations, and tried to correlate them with the ΔE_{ST} values (see Figure 3). As it was expected from the poor overlap between the orbitals (e.g. HOMO and LUMO) involved in the formation of the S_1 state, typical of these systems, 91,92 the f_{osc} values are relatively low for all them (see the Supplementary Material) and even a large percentage of molecules show dark S_1 states, with vanishing oscillator strengths.

Only a few systems (molecules numbered as 63, 156, and 157) show $f_{osc} > 0.05$ while concomitantly having $\Delta E_{ST} < 0$ values. These molecules are dimethylamine-substituted heptazine, triamine-substituted pentazine, and trimethylamine-

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substituted pentazine, see Figure 5. On the other hand, Figure 6 shows the pair of molecules (diamine-substituted pentazine and dimethylamine-substituted pentazine) holding the largest f_{osc} values ($f_{osc} > 0.10$) from all the NAH159 dataset but in this case for $\Delta E_{ST} > 0$ values. These results show how the introduction of electroactive amine-based substituents might be a good strategy to increase the f_{osc} values, together with low ΔE_{ST} values (independently of its sign). The exploration of other cores and/or substituents might lead to increased f_{osc} values, which is the subject of current investigations, as recently exemplified by the design of INVEST molecules with conjugated branches as substituents, 93 to have an appreciable emission of light. In this regard, the PBE-DH-INVEST model might be also considered as a good alternative to perform further screenings of the chemical space of candidate molecules.

3.4 The influence of double excitations

We now apply Eq. (5) to both $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ excitation energies calculated by the PBE-DH-INVEST model, that is:

$$\Omega(S_1) = \Omega'(S_1) + \frac{3}{5}\Delta(D)(S_1),$$
 (8)

$$\Omega(T_1) = \Omega'(T_1) + \frac{3}{5}\Delta(D)(T_1), \tag{9}$$

thus leading to the corresponding ΔE_{ST} expression:

$$\Delta E_{ST} = \Omega(S_1) - \Omega(T_1) = \Omega'(S_1) - \Omega'(T_1) + \frac{3}{5} \left[\Delta(D)(S_1) - \Delta(D)(T_1) \right], (10)$$

or simply:

$$\Delta E_{ST}^{\mathrm{PBE-DH-INVEST}} = \Delta E_{ST}^{\mathrm{PBE-DH-INVEST(SCF)}} + \Delta \left[\Delta(\mathrm{D}) \right], \tag{11}$$

to clearly emphasize the prominent role played by the double excitations introduced by the model, quantified by Δ [Δ (D)], making the difference between (inaccurate) $\Delta E_{ST}^{\rm PBE-DH-INVEST(SCF)}$ and (accurate) $\Delta E_{ST}^{\rm PBE-DH-INVEST}$. These double excitations are system- and state-dependent, affecting any molecule of

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the NAH159 dataset. Actually, since $\Delta E_{ST}^{\mathrm{PBE-DH-INVEST(SCF)}}$ is always positive, the only possibility left to have an excited-state inversion is that: (i) $\Delta \left[\Delta(\mathrm{D})\right] < 0$, and (ii) $|\Delta E_{ST}^{\mathrm{PBE-DH-INVEST(SCF)}}| < |\Delta \left[\Delta(\mathrm{D})\right]|$. Figure 4 (top) presents the $\Omega(S_1) - \Omega'(S_1)$ and $\Omega(T_1) - \Omega'(T_1)$ values for all the molecules contained into the NAH159 dataset, for which several conclusions immediately arise: (i) the $\Omega(S_1) - \Omega'(S_1)$ values are always negative, spanning values from -0.32 to -1.30 eV (average value of -0.66 eV); (ii) the $\Omega(T_1) - \Omega'(T_1)$ values can be positive, reaching up to 0.47 eV, or negative, as low as -0.68 eV (average value of -0.09 eV); (iii) the corresponding $\Delta \left[\Delta(\mathrm{D})\right]$ values are consequently negative in all cases, ranging from -0.18 to -0.99 eV, and thus confirming their key role. Figure 4 (bottom) also shows in detail the magnitude of that $\Delta \left[\Delta(\mathrm{D})\right]$ correction for all the systems, with an average value of -0.58 eV.

Additionally, an alternative formulation is often found in the literature, where $\Delta E_{ST} \approx 2K$, with K being the exchange integral $(\phi_i \phi_a | \phi_j \phi_b)$ between the corresponding orbitals from a single-excitation (e.g. Configuration Interaction Singles or CIS) picture. The corresponding extension to TD-DFT involves an additional term based on the exchange-correlation kernel, the salways leads to $\Delta E_{ST} > 0$ in practical calculations. If a wavefunction-based correlation treatment is instead invoked, the extension is often simplified to $\Delta E_{ST} \approx 2K + \Delta E_c$, with the ΔE_c contribution arising from e.g. the n-tuple excitations introduced by the particular method selected. In this context, the advantage of using of a DH density functional is the affordable computation of single and double excitations, thanks to the decomposition made in Eq. (11) and shown in Figure 4, thus allowing to merge the lessons gained so far from both DFT-based and wavefunction-based studies of INVEST systems.

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3.5 Exploring the reduction in computational cost

3.5.1 Assessing the basis set dependence

We will next assess the influence of the basis set size for the PBE-DH-INVEST model, comparing the aug-cc-pVDZ and the aug-cc-pVTZ results (see Table 1). Note that both basis sets share an augmentation, with respect to the corresponding cc-pVDZ and cc-pVTZ parent ones, of an extra diffuse function in each orbital angular momentum (aug-cc-pVDZ is (10s,5p,2d) contracted to [4s,3p,2d] and aug-cc-pVTZ is (11s,6p,3d,2f) contracted to [5s,4p,3d,2f]) We deduce from Table 1 that the results are only very slightly influenced by the use of a smaller basis set, such as aug-cc-pVDZ, with error metrics marginally affected for the individual $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ excitation energies, which negligibly translates to the ΔE_{ST} values too. Those minimal deviations between aug-cc-pVDZ and aug-cc-pVTZ results do not advise to use any extrapolation scheme for double-hybrid density functionals 95 or excited states energies. ⁹⁶ Furthermore, the (small) number of false negative or positive (i.e., when the sign of the ΔE_{ST} value differs with respect of that calculated by the LR-CC2 method) remains the same when employing the aug-cc-pVDZ basis set instead of the larger aug-cc-pVTZ one.

Furthermore, to clearly illustrate the reduction in computational time going from the aug-cc-pVTZ to the aug-cc-pVDZ basis set, we have considered the total time required for running the calculations on the whole NAH159 dataset employing the same technical details and the same number of cores for both basis sets. The total time needed is drastically reduced going from about 1560 to about 340 hours when the aug-cc-pVDZ is used instead of the aug-cc-pVTZ one, thus representing just a 22 % of the time needed for the larger one (see the Supplementary Material for further details including the relative time for each of the molecules of the NAH159 dataset)

3.5.2 Assessing the SOS1-PBE-DH-INVEST variant

Finally, we will also assess the SOS1-PBE-DH-INVEST variant with the aug-cc-pVDZ basis set too (see Table 1) in the search of the lowest possible computational cost. The error metrics (e.g. MAD and RMSD) are slightly larger than for the pristine PBE-DH-INVEST model, although SOS1-PBE-DH-INVEST becomes competitive for the ΔE_{ST} energy difference, with a MAD of 0.06 eV and a kurtosis value around 0.8 again. The number of molecules displaying a different sign for ΔE_{ST} with respect to LR-CC2 is reduced now to 9 out of 159 (5.7%) with molecules 18, 20, 21, 39, 46, 82, 91, and 132 showing a false negative value (i.e., $\Delta E_{ST}^{\text{LR-CC2}} > 0$ but $\Delta E_{ST}^{\text{SOS1-PBE-DH-INVEST}} < 0$) and molecule 153 showing a false positive value (i.e., $\Delta E_{ST}^{\text{LR-CC2}} < 0$ but $\Delta E_{ST}^{\text{SOS1-PBE-DH-INVEST}} > 0$). Overall, we can also recommend this variant for rapidly estimating ΔE_{ST} values if the software used would allow to exploit the lower (formal) cost associated to recent implementations of SOS-based expressions. $^{97-100}$

4 Conclusions

This study explores the possibility of using a recently developed double-hybrid density functional (PBE-DH-INVEST) as a computationally viable method to accurate predict singlet-triplet energy gaps (ΔE_{ST}) of INVEST molecules (i.e., those molecules for which the singlet-singlet $S_1 \leftarrow S_0$ excitation energy lies lower than the corresponding singlet-triplet $T_1 \leftarrow S_0$ one) For that purpose, we applied the method to the NAH159 dataset of organic molecules containing very popular scaffolds for these INVEST systems, such as cyclazine, pentazine, and heptazine, as well as non-alternant hydrocarbons of various types. The large sample of 159 molecules thus differ not only in their molecular core but also on the number and position of electron-donating and electron-withdrawing substituents. Since the PBE-DH-INVEST method goes

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beyond a single-reference (standard) TD-DFT treatment for excited states, we have systematically quantified and confirmed the importance of the double excitations introduced by the double-hybrid expression, which is known to play a key role for INVEST systems. Overall, the method shows a very robust performance with respect to reference results previously computed at the LR-CC2 level, as well as a small basis set dependence after comparing results with the aug-cc-pVDZ and aug-cc-pVTZ basis sets. We have also explored the SOS1-PBE-DH-INVEST variant, with a slightly worse performance with respect to the pristine PBE-DH-INVEST form. These features seem to confirm the accuracy and robustness of this model chemistry (i.e., PBE-DH-INVEST/aug-cc-pVDZ) for e.g. exploratory calculations, high-throughput screenings or machine-learned applications at a very affordable computational cost.

Supplementary Material

In the Supplementary Material we include all the raw data used for the statistics and figures: (i) the detailed list of all the molecules comprising the NAH159 dataset; (ii) the individual values for the $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ excitation energies at the LR-CC2, PBE-DH-INVEST(SCF), PBE-DH-INVEST, and SOS1-PBE-DH-INVEST levels, with both the aug-cc-pVDZ and aug-cc-pVTZ basis sets for the PBE-DH-INVEST case; (iii) the oscillator strength values with both the aug-cc-pVDZ and aug-cc-pVTZ basis sets; (iv) the total time needed for each of the NAH159 molecules at the PBE-DH-INVEST level with both the aug-cc-pVDZ and aug-cc-pVTZ basis sets, as well as the corresponding relative time; (v) technical details of the CPUs used for the calculations; (vi) an example input file for the (SOS1-)PBE-DH-INVEST calculations.

Data Availability

The data that supports the findings of this study are available within the article [and its supplementary material] or are available from the corresponding authors upon reasonable request.

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Figure 1: Chemical description of the systems composing the NAH159 dataset, with electron-donating (ED) and electron-withdrawing (EW) groups designed as R_1 (in blue) and R_2 (in red), respectively, with R_3 being another ED/EW group.

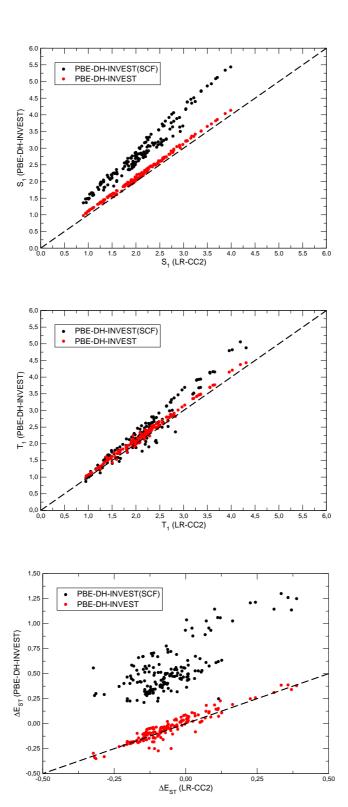


Figure 2: Correlation between CC2 and PBE-DH-INVEST results for the $S_1 \leftarrow S_0$, $T_1 \leftarrow S_0$, and ΔE_{ST} energies (from top to bottom, all in eV) of the molecules composing the NAH159 dataset. All calculations are done with the aug-cc-pVTZ basis set and under the Tamm-Dancoff approximation.

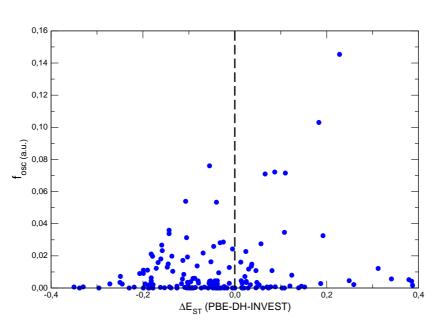
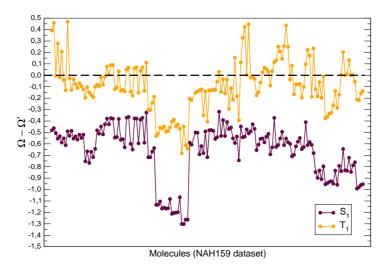


Figure 3: Correlation between the oscillator strength values (f_{osc}) and the ΔE_{ST} energies (in eV) of the molecules composing the NAH159 dataset.

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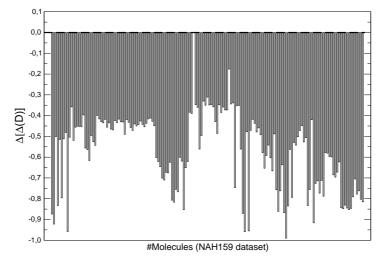


Figure 4: Top: Influence (in eV) of double excitations for the $S_1 \leftarrow S_0$ and $T_1 \leftarrow S_0$ excitation energies of the molecules composing the NAH159 dataset. Bottom: Final $\Delta \left[\Delta(\mathrm{D}) \right]$ values (in eV) for the molecules composing the NAH159 dataset. All calculations are done with the aug-cc-pVTZ basis set.

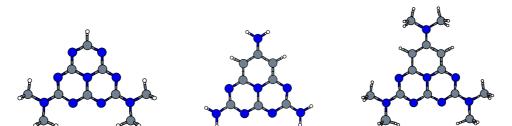


Figure 5: Molecules presenting a $\Delta E_{ST} < 0$ value with the largest calculated f_{osc} values.

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Figure 6: Molecules presenting a $\Delta E_{ST} > 0$ value with the largest calculated f_{osc} values.

Table 1: MSD, MAD, RMSD, and Δ_{err} values (all in eV) for the $S_1 \leftarrow S_0$, $T_1 \leftarrow S_0$, and ΔE_{ST} energies (all in eV) of the molecules composing the NAH159 dataset. All calculations are done under the Tamm-Dancoff approximation.

Basis set	Method	MSD	MAD	RMSD	Δ_{err}	Kurtosis
aug-cc-pVTZ						
	PBE-DH-INVEST(SCF)					
	$S_1 \leftarrow S_0$	0.768	0.768	0.813	1.136	0.94
	$T_1 \leftarrow S_0$	0.184	0.232	0.300	1.339	0.77
	ΔE_{ST}	0.584	0.584	0.610	0.910	0.96
	PBE-DH-INVEST					
	$S_1 \leftarrow S_0$	0.107	0.107	0.115	0.179	0.93
	$T_1 \leftarrow S_0$	0.092	0.099	0.114	0.373	0.87
	ΔE_{ST}	0.015	_0.038_	0.050	0.308	0.76
aug-cc-pVDZ						
	PBE-DH-INVEST(SCF)					
	$S_1 \leftarrow S_0$	0.761	0.761	0.803	1.102	0.95
	$T_1 \leftarrow S_0$	0.182	0.230	0.296	1.330	0.78
	ΔE_{ST}	0.578	0.578	0.603	0.906	0.96
	PBE-DH-INVEST					
	$S_1 \leftarrow S_0$	0.116	0.116	0.122	0.190	0.95
	$T_1 \leftarrow S_0$	0.098	0.103	0.117	0.368	0.88
	ΔE_{ST}	0.018	0.039	0.050	0.297	0.78
	SOS1-PBE-DH-INVEST					
	$S_1 \leftarrow S_0$	0.162	0.162	0.176	0.302	0.92
	$T_1 \leftarrow S_0$	0.211	0.211	0.231	0.418	0.92
	ΔE_{ST}	-0.049	0.058	0.073	0.282	0.79

All the data that supports the findings of this study are available within the article [and its supplementary material] or are available from the corresponding authors upon reasonable redirecticle Online supplementary material] or are available from the corresponding authors upon reasonable redirection of the corresponding authors upon reasonable redirection.

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