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### COMMUNICATION

#### Cite this: DOI: 10.1039/x0xx00000x

# Achieving the Photon Up-conversion Thermodynamic Yield Upper Limit by Sensitized Triplet-triplet Annihilation.

S. Hoseinkhani<sup>a</sup>, R. Tubino<sup>a</sup>, F. Meinardi<sup>a\*</sup>, and A. Monguzzi<sup>a\*</sup>

Received 00th January 2012, Accepted 00th January 2012

DOI: 10.1039/x0xx00000x

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Triplet-triplet annihilation (TTA) based up-conversion is a promising strategy for light harvesting the low-energy tail of the solar spectrum in photovoltaic technologies. Here we present a bi-component system for photon managing via TTA that allows bypassing the classical statistic limit of 2/5 in the singlet generation, achieving a nearly unitary conversion efficiency. This result is obtained thanks to the peculiar relative position of the triplet and singlet energy levels of perylene, used as up-converter and emitter. The system shows under an irradiance of 1 sun, a record red-to-blue external up-conversion yield of ~10%.

Solar technologies are the most common and sustainable strategies for the production of carbon-free renewable energy with a significant impact for long-term worldwide growth. However, the efficiency of photovoltaic and photo-catalytic devices for hydrogen production is limited because they exploit only a fraction of the available light.<sup>1-5</sup> To use efficiently also the low-energy tail of the solar spectrum an improved light harvesting can be achieved by up-conversion (UC) of subbandgap photons through different processes that must be effective in the light managing at the solar irradiance. At the present, this requirement can be fulfilled only by the so-called sensitized triplet-triplet annihilation (sTTA-UC) in multicomponent organic systems. Briefly, an up-converting molecule, the acceptor/emitter, gives rise to high-energy delayed fluorescence upon annihilation of its metastable triplet states, which are populated trough Dexter energy transfer (ET) from the triplet states of a proper light harvester, the donor/sensitizer. In this latter the triplet states are generated via intersystem crossing (ISC) from singlet states excited upon low-energy light absorption.<sup>6</sup> After a very fast development, different groups reported sTTA-UC systems with upconversion yields as high as 20% under an irradiance of few suns. These performances are order of magnitude better than those achievable with up-converters based on other processes, as multi-photon absorption or annihilation of rare-earth excited states.<sup>7-10</sup> Because sTTA-UC materials were also proven to

effectively enhance the light-harvesting efficiency of real PV devices, <sup>3, 5, 11, 12</sup> it is candidate to become a fundamental building block for the next generation of solar-based devices, with a potential yield enhancement as high as 50% for silicon and organic photovoltaic cells, and even larger for photocatalytic water splitting cells (+100%).<sup>8, 13, 14</sup>

The maximum quantum-yield (QY) of the photon UC is 0.5 because, obeying to the thermodynamic requirement  $2E_{in} \ge E_{out}$ , two low-energy  $(E_{in})$  photons are required to generate one photon with higher energy  $(E_{out})$ . However, in the case of the sTTA-UC, the intrinsic probability that emitting states are effectively generated upon TTA introduces an additional statistic requirement, which decreases the limit QY from 0.5 to 0.2 (see below). Here we describe for the first time an upconverting system in which the statistic limit is bypassed obtaining an internal UC efficiency  $QY_{int} \sim 0.5$ . The external sTTA-UC quantum yield  $(QY_{out})$  is 0.38, limited only by the efficiencies of the sensitizer-emitter ET and of the emitter fluorescence at the employed concentration.

The sTTA-UC yield depends on the product of the efficiencies of all the involved photophysical steps

$$QY_{out} = 0.5 f \phi_{ISC} \phi_{ET} \phi_{TTA} \phi_{fI} = \phi_{ISC} \phi_{ET} \phi_{fI} QY_{int}, \qquad \text{Eq. 1}$$

where the pre-factor 0.5 is set by the thermodynamic limit described above. The other parameters are the efficiencies of the sensitizer ISC ( $\phi_{ISC}$ ), the sensitizer-emitter energy transfer ( $\phi_{ET}$ ), the emitter TTA ( $\phi_{TTA}$ ) and fluorescence ( $\phi_{7}$ ). In Eq. 1, *f* represents the probability to obtain a singlet excited state as a result of the annihilation of two triplet states.<sup>15</sup> Cheng and co-authors recently introduced a discussion on this parameter. It depends on the electronic properties of the systems that experience bi-molecular excitonic annihilation, and they suggested how it is possible to overcome the spin statistical limit for TTA assisted up-conversion yield.<sup>11, 16</sup>



**Fig. 1** Sketch of the TTA process involving four triplet pairs. In the case (a), where  $T_2$  levels are energetically accessible, the collision of four triplet pairs destroy five triplets. Only two dead triplet produce a singlet excited state, therefore f = 2/5 = 0.4 with a predicted maximum QY<sub>int</sub>= 0.2 (Eq. 1). In case (b), where the  $T_2$  level is not energetically accessible, the collision of four triplet pairs produces four singlet excited states. Thus f = 8/8 = 1, with a predicted maximum QY<sub>int</sub>= 0.5.

Indeed, TTA is a two-particle collision process, which results in the generation of excitons with different spin-character according to the statistical combination of the spin of the colliding triplets. TTA reactions are described as

$$T_{1} + T_{1} \longleftrightarrow \langle T_{1} \cdots T_{1} \rangle \Longrightarrow \begin{cases} Q + S_{0} \text{ (multiplicity 5)} \\ T_{2} + S_{0} \text{ (multiplicity 3)} \\ S_{1} + S_{0} \text{ (multiplicity 1)} \\ \end{cases} \text{ Eq. 2}$$

Quintet (*Q*) states require the simultaneous excitation of two electrons and are energetically unattainable. On the contrary, usually  $E(T_2) < E(2T_1) + k_B T$  and  $E(S_1) < E(2T_1) + k_B T$  allowing the intermediate collision complex to generate either a singlet excited state  $S_1$  or one of the tree degenerate high-energy  $T_2$  triplet states with a statistical ratio of 1:3. The resulting  $T_2$  states quickly decay back to  $T_1$ , becoming again available for further annihilations (see Fig. 1a). Therefore, upon collision of four triplet exciton pairs five triplets are destroyed, but only two of them give a singlet, which sets f=2/5. However, if  $E(T_2)>E(2T_1)+k_B T$ , not only the formation of quintet state is prevented, but also that of high-energy triplets. In this case, only singlet excitons can be formed upon TTA, thus f = 1 (see Fig. 1b). This latter is the fundamental requirement to bypass the statistic limit and to reach a maximum  $QY_{int}=0.5$ .<sup>11, 16</sup>

The emitters commonly used in the sTTA-UC are rigid polyacenes. They possess a large fluorescence yield ( $\phi_{ll} \sim 1$ ) and long-living metastable triplets suitable for TTA. As sensitizers, metallated porphyrins show the best performance. They have a strong absorption cross-section thanks to the conjugated porphyrinic ring, and fast ISC enhanced by the presence of the central metal atom which gives  $\phi_{ISC}=1$ .<sup>17, 18</sup> Therefore, by using properly paired chromophores of these families we can avoid energy losses by unwanted non-radiative processes. Of course, the lowest excited state of the sensitizer must be resonant with the  $T_I$  level of the emitter in order to allow the Dexter ET. If this requirement is satisfied,  $\phi_{ET}$  can be easily optimized by



**Fig. 2** (a)  $PdPh_4TBP$  molecular structure and energy levels. (b) Absorption/emission of  $PdPh_4TBP$  (dotted red and dashed brown lines, respectively) and up-converted photoluminescence of PY (solid blue line). Numbered arrows indicate the sTTA-UC relevant photophysical steps: 1) low-energy absorption, 2) ISC, 3) sensitizer-emitter Dexter Energy transfer, 4) TTA, 5) high energy emission.

changing the emitter concentration  $(C_E)$ . In order to demonstrate the possibility to overcome the sTTA-UC statistic limit, as emitter we selected in the polyacene family the pervlene (PY).<sup>19, 20</sup> PY is the ideal molecule for this purpose, as its  $\phi_{ll}$  is 0.96 in diluted solution, the  $T_l \leftrightarrow S_0$  transition is strictly forbidden implying a  $T_1$  natural lifetime in the range of 5 ms, and, in particular,  $E(T_2) \sim 4.0$  eV is much larger than twice  $E(T_1) \sim 1.51$  eV.<sup>21-23</sup> As concern the sensitizer we choose meso-tetraphenyltetrabenzoporphyne the palladium(II) (PdPh<sub>4</sub>TBP), a near-infrared emitting phosphor with  $\phi_{ISC}$ =1 and a strong phosphorescence at 1.56 eV, not far from the  $T_1$  state of PY. Moreover, the broad PY photoluminescence ranging from about 2.40 and 2.80 eV falls mainly in the transparency window of PdPh<sub>4</sub>TBP delimited by the  $\beta$ - and the Q- absorption bands at 2.81 and 1.96 eV. Very similar systems has been previously employed by Singh-Rachford and Castellano to achieve red-to-blue sTTA-UC achieving good results for the conversion yield.24

The spectroscopy study was performed by dissolving both the dyes in tetrahydrofuran (THF) with a fixed concentration of PdPh<sub>4</sub>TBP ( $10^{-5}$  M) and a changing that of PY from  $10^{-3}$  M to  $10^{-6}$  M. Absorption measurements were done with a Cary 50 spectrometer. Photoluminescence signals were recorded by a nitrogen cooled CCD coupled with a spectrograph Triax-190 (Horiba Jobin-Yvon), with a spectral resolution of 15 nm. As excitation source a Roithner solid-state laser diode RLTMRL-635-100-5 at 1.95 eV (635 nm) was generally used. Only for the photoluminescence QY measurements this laser was replaced with the second the harmonic of a Ti:Sapphire laser at 3.26 eV (380 nm). QY<sub>out</sub> and PY  $\phi_{fl}$  has been determined by relative photoluminescence intensity measurements by using phthalocyanine in 1-chloronaphthalene as a standard (see ESI for details).<sup>21</sup> All samples were prepared by using anhydrous solvents, and were sealed in a glove box in quartz cuvettes with an optical path d=0.1 cm to prevent oxygen quenching. Chemicals were received from Sigma Aldrich and used as is.

Fig. 2 reports the molecular structure with the relevant energy levels of the employed chromophores (upper panel), and the absorption/emission spectra of PY and PdPh<sub>4</sub>TBP (lower panel). Numbered arrows outline the energy flow in the sTTA-UC process. The sensitizer absorbs light at  $E_{in}$ =1.95 eV (1) and then experience a fast ISC that populates its triplet state at 1.55 eV (2). PY triplets are excited by Dexter energy transfer from donors (3) and experience TTA (4), thus generating fluorescent singlets at  $E_{out} = 2.61 \text{ eV}$  (5). The overall photon-energy gain is  $\Delta E = (E_{out} - E_{in}) = 0.66$  eV. In the case of samples at low PY concentration, the photophysics remains the same, but the upconverted emission slightly shifts to higher energy as described in the Electronic Supplementary Information (ESI) file. Fig. 3 reports the measured QYout plotted vs the excitation power density  $(I_{exc})$  in a log-log scale for samples with different  $C_E$ . The QYout data have been corrected nor for the PY selfabsorption neither for the PdPh<sub>4</sub>TBP re-absorption. These two effects play a minor role in determining the performances of the systems and are discussed in the detail in the ESI. Here we outline that this is a quite conservative approach, as the inclusion of the above-mentioned effects results in performances even better than the reported ones. For all the samples at low excitation power, QYout is below 1%, as the density of PY triplet states is too low to have any efficient annihilation being the spontaneous non-radiative decay the main triplet de-excitation channel. By rising the exciting radiant flux, we observe a corresponding QYout increase up to a constant value. This is reached when the TTA becomes the dominant deactivation channel for the metastable triplets.<sup>22</sup> In some cases, i. e. samples with  $C_E = 10^{-5}$  M and in particular  $C_E=10^{-6}$  M, the regime in which QY<sub>out</sub> is excitation powerindependent is followed by a strong decrease of the conversion yield. This is due to the saturation of the number of acceptors available for the ET occurring when  $I_{exc}$  is so large that a notnegligible fraction of the emitters is in an excited state.<sup>25</sup>

We firstly studied the sample with  $C_E=10^{-3}$  M, the maximum concentration of emitter soluble in THF (Fig. 3, circles). The regime in which the conversion yield assumes a constant value is reached for  $I_{exc} > 10^{16}$ ph cm<sup>-2</sup> s<sup>-1</sup>. Here, we measure QY<sub>out</sub>=0.33. The singlet generation efficiency upon TTA can be now evaluated from Eq. 1 by considering that: i) donor  $\phi_{ISC}$  is 1, because in the PdPh<sub>4</sub>TBP there is no detectable fluorescence from the absorbing  $S_I$  state.<sup>26</sup> ii)  $\phi_{TTA}$  is 1, as we are considering the irradiance range in which QY<sub>out</sub> is independent from  $I_{exc}$ , i. e. in which all the triplet states decay by annihilation. iii) Thanks to the large  $C_E$  concentration,  $\phi_{ET}$ =1 as demonstrated by ET efficiency measurements (ESI, Fig. S2). iv) The  $\phi_{fI}$  of PY at this concentration is only 0.65 because of the concentration quenching effect at the selected  $C_E$  (see ESI, Fig. S1).<sup>27, 28</sup> As a



**Fig. 3** sTTA-UC quantum yield at 2.61 eV under CW excitation at 1.95 eV for a THF solution of PdPh<sub>4</sub>TBP 10<sup>-5</sup> M and PY 10<sup>-3</sup> M (dots), 10<sup>-4</sup> M (circles) 10<sup>-5</sup> M (triangles), and 10<sup>-6</sup> M(squares) as a function of the excitation intensity  $I_{exc}$ . The inset show the sTTA-UC emission of a THF solution (10<sup>-5</sup> M/ 10<sup>-4</sup>M) under broad excitation by a filtered white lamp. The dashed vertical line indicates the amount photons absorbed under 1 sun of irradiance by considering the sensitizer absorption at the concentration of 10<sup>-5</sup> M used in the experiment.

matter of fact, PY fluorescence efficiency is the only the bottleneck for the conversion yield in the investigated system. With these values, Eq. 1 gives  $QY_{int} = QY_{out}(\phi_{ET}\phi_{fl})^{-1} = 0.49$ , or equivalently f=1. This demonstrates for the first time that the thermodynamic upper limit of photon up-conversion yield by TTA is reached. The overall sTTA-UC efficiency can be increased optimizing the system composition by decreasing the emitter concentration down to  $C_E=10^{-4}$  M, in order to limit the concentration quenching of  $\phi_{fl}$  (Fig. 3, dots). In such a way,  $\phi_{fl}$ = 0.80, and  $C_E$  is still high enough to get  $\phi_{ET}$ =0.97 (ESI, Fig. S1). The measured  $QY_{out}=0.38$  is, to our knowledge, the highest value observed for photon sTTA-UC. Again by Eq. 1, the calculated  $QY_{int}=0.50$  confirms an f value of 1. Additional reductions of  $C_E$  allow to further reduce the emitter fluorescence quenching, but limit the ET efficiency and, as a consequence of the described saturation effect, hamper the correct evaluation of f. In the system with  $C_E=10^{-5}$  M, from one side  $\phi_{fl}$  rises up to 0.91±0.04 but from the other one the corresponding  $\phi_{ET}$  decreases down to 0.47 and the maximum measured sTTA-UC efficiency to 0.19. In this case, Eq. 1 gives  $QY_{in}=0.42$  at which corresponds f=0.8. This suggests that the ET saturation at high excitation intensities prevents reaching the maximum achievable  $QY_{out}$  giving a unreliable value of f. This is confirmed by the data collected for the sample with the smallest  $C_E = 10^{-6}$  M that shows a dramatic decrease of  $QY_{out}$ well before its saturation value is reached. Table 1 summarizes the relevant parameters for all the investigate samples measured at  $I_{exc}$  = 8x10<sup>17</sup> ph cm<sup>-2</sup> s<sup>-1</sup> (250 mW cm<sup>-2</sup>). In the inset of Fig. 3 a picture of the bright blue emission of the sample PdPh<sub>4</sub>TBP/PY (10<sup>-5</sup> M/10<sup>-4</sup> M) excited with a white lamp passing through a 520 nm long-pass optical filter demonstrates the high efficiency of the sTTA-UC in our system. For this sample it should be outlined that, even if it is necessary an

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Table 1. Main efficiencies measured/calculated for the investigated				
samples ( $I_{exc}$ = 8x10 <sup>17</sup> ph cm <sup>-2</sup> s <sup>-1</sup> ). * indicates that the corresponding				
value may be underestimated because of an ET saturation effect.				

PdPh <sub>4</sub> TBP/PY Conc. (M)	$\phi_{ET}$	$\phi_{fl}$	QY <sub>out</sub>	QY <sub>int</sub>	f
10-5 : 10-3	1.00	0.65	0.33	0.49	1.0
	±0.05	±0.03	±0.02	±0.07	±0.1
10-5:10-4	0.96	0.80	0.38	0.50	1.0
	±0.05	±0.04	±0.03	±0.07	±0.1
10-5 : 10-5	0.47	0.91	0.18	0.42	0.8
	±0.02	±0.04	±0.01	±0.06*	±0.1*
10-5 : 10-6	0.03 ±0.01	0.95 ±0.05	0.03 ±0.01	-	-

excitation power density larger than the solar irradiance to obtain its maximum efficiency, the  $QY_{out}$  achievable by absorbing a number of photons equal to that provided by the solar irradiance at the A.M. 1.5 condition(Fig. 3 dashed vertical line) is as large as ~10%.

#### Conclusions

In conclusion, the thermodynamic upper limit of ~50% in photon up-conversion yield has been demonstrated for a sTTA-UC system by using an acceptor/emitter dye pair with suitable triplet and singlet energy levels. When the condition  $E(S_1) \le E(2T_1) + k_B T \le E(T_2)$  is satisfied, the singlet generation by TTA is maximized, and the QYout is only limited by the emitter fluorescence efficiency, and/or by the sensitizer-to-emitter energy transfer yield. Our findings demonstrate that by a proper selection of the chromophores it is possible to have upconversion yields not only at low irradiance, 20, 29, 30 but also without photon losses exactly as in the case of non-linear optic materials when they operate with coherent radiation at excitation power densities of MW or GW per square centimetre. Thanks to his record performance, the sTTA-UC system presented show an up-conversion efficiency of 10% under 1 sun of irradiance, demonstrating the potential application of these materials in photovoltaic and photocatalytic technologies.

#### Notes and references

<sup>a</sup> Dipartimento di Scienza dei Materiali, Università of Milano-Bicocca, via Cozzi 55, I-20125 Milano, Italy

Electronic Supplementary Information (ESI) available: Details and discussions on the photoluminescence quantum yield and energy transfer yield measurements. See DOI: 10.1039/c000000x/

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