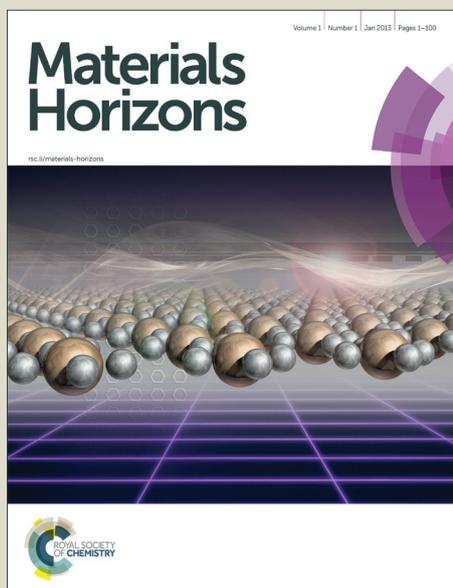


# Materials Horizons

Accepted Manuscript



This is an *Accepted Manuscript*, which has been through the Royal Society of Chemistry peer review process and has been accepted for publication.

*Accepted Manuscripts* are published online shortly after acceptance, before technical editing, formatting and proof reading. Using this free service, authors can make their results available to the community, in citable form, before we publish the edited article. We will replace this *Accepted Manuscript* with the edited and formatted *Advance Article* as soon as it is available.

You can find more information about *Accepted Manuscripts* in the [Information for Authors](#).

Please note that technical editing may introduce minor changes to the text and/or graphics, which may alter content. The journal's standard [Terms & Conditions](#) and the [Ethical guidelines](#) still apply. In no event shall the Royal Society of Chemistry be held responsible for any errors or omissions in this *Accepted Manuscript* or any consequences arising from the use of any information it contains.

## Conceptual Insights

Fullerenes are a technologically important class of materials and scientifically interesting because of the possibility of modulating the energy levels through functionalisation, but without otherwise changing the electronic structure. Simulation of electronic properties of experimentally relevant sizes of molecular assemblies is difficult from an atomistic perspective because of computer time constraints. In this paper we overcome those constraints by developing and using a coarse grained approach to the film growth, which incorporates disorder due to multiple isomers. The method is capable of distinguishing clearly between the effects of disorder in molecular packing and disorder in chemical structure on charge transport. The results are consistent with experimental time-of-flight and field-effect transistor measurements.

The methodology can be translated to a wide range of other molecular materials, can be applied to investigate energy transport and spin transport, and has implications for chemists and material scientists.

## COMMUNICATION

# Distinguishing the Influence of Structural and Energetic Disorder on Electron Transport in Fullerene Multi-Adducts

Cite this: DOI: 10.1039/x0xx00000x

Florian Steiner, Samuel Foster, Arthur Losquin, John Labram, Thomas D. Anthopoulos, Jarvist M. Frost<sup>†\*</sup>, Jenny Nelson<sup>\*</sup>Received 00th January 2012,  
Accepted 00th January 2012

DOI: 10.1039/x0xx00000x

www.rsc.org/

Fullerene multi-adducts offer a method to tune the open-circuit voltage of organic solar cells but generally lead to poor photocurrent generation which has been linked to poor electron transport in the fullerenes. The poor electron transport may result from the effect of multiple side-chains in hindering close packing of the fullerene cages or from disorder in energy levels due to the presence of multiple isomers. Here, we present time-of-flight and field-effect transistor measurements of mobility in [6,6]-phenyl-C-61-butyric acid methyl ester (PCBM) and its higher adducts. To understand the origin of the poor electron mobility, we develop a coarse-grained molecular dynamics model to build isomeric mixes of the multi-adducts. The coarse grained model massively speeds up the simulation relative to atomistic molecular dynamics, enabling assemblies of 100,000 molecules to be studied. We simulate electron transport in the structures using a kinetic Monte Carlo method, accounting for variations in site energy using electronic structure calculations. This allows us to separate the influence of packing disorder (poorer contact between fullerenes due to steric hindrance) from the influence of energetic disorder (due to varying acceptor energies of the isomers) on electron mobility. We find that energetic disorder due to different isomers dominates the trend in charge transport. Consequently, pure isomeric samples of higher fullerene adducts should enable higher efficiency solar cells.

## Introduction

Higher adducts of fullerene derivatives such as [6,6]-phenyl-C-61-butyric acid methyl ester (PCBM) and the indene-C<sub>60</sub> mono-adduct (ICMA) have attracted interest as a means to raise the open-circuit voltage  $V_{oc}$  of polymer solar cells. The most widely used acceptor is a

derivative of C<sub>60</sub>, [6,6]-phenyl-C-61-butyric acid methyl ester (PCBM), and its C<sub>70</sub> based analogue. These fullerene derivatives offer many advantageous features such as high acceptor strength, the ability to self organise into partly crystalline charge transport networks and a sufficiently high electron mobility to avoid recombination in optically thick films<sup>1,2,3</sup>.

There are various routes to manipulate the LUMO energy by changing (a) the chemical structure of side chains<sup>4</sup>, (b) the bonding between side chain and fullerene<sup>5</sup> (c) the number of side chains. Examples for the latter are the indene-C<sub>60</sub> bis-adduct (ICBA)<sup>6</sup> and the higher adducts of PCBM, bis-PCBM and tris-PCBM, with two and three phenyl butyric acid methyl ester (PBM) side-chains respectively<sup>7,8</sup>.

Although bis-adducts succeed in increasing the power conversion efficiency when substituted for PCBM in poly(3-hexylthiophen-2,5-diyl) (P3HT) : fullerene blends<sup>6,7</sup>, higher-fullerene adducts fail in general to improve upon PCBM mainly due to poor short-circuit current densities  $J_{sc}$ <sup>9,10</sup>. Lenes et al. proposed that the origin of the diminished  $J_{sc}$  is a low electron mobility in the fullerene phase. This is supported by observations of efficient charge separation in blends of polymers with PCBM multi-adducts despite poor photocurrent<sup>3,11</sup>.

We identify two potential mechanisms by which electron transport in multi-adducts may be influenced, namely, (a) packing disorder leading to variation in electronic wavefunction overlap between neighbouring molecules and (b) energetic disorder resulting from variations in energy of electron transport states. We investigate the relative importance of structural and energetic disorder on charge carrier transport in PCBM and the multi-adducts bis- and tris-PCBM with the aim of separating the relative influence of the two mechanisms.

Previously we showed that the LUMO energy of different PCBM multi-adduct isomers varies by hundreds of meV<sup>12</sup>. The successive cyclo-addition of fullerenes to form higher adducts raises the reduction potential by removing successive electrons from the  $\pi$ -system to form side-chain bonds. The location of the side chains relative to each other profoundly affects the electronic structure of the fullerene leading to variations in the reduction potential (and hence the LUMO energy) of hundreds of meV. By connecting the side chains of bis-PCBM, Bouwer et al. could isolate single bis-isomer derivatives and obtained higher short-circuit currents; this study indicates the value of eliminating energetic disorder in higher-fullerene-adducts<sup>13</sup>. This observation is shared with Wong et al. who isolated single isomers of ICBA<sup>14</sup>. On the other hand, it is suggested that the packing disorder results from the greater volume taken up by phenyl butyric acid methyl ester (PBM) side chains in higher fullerene adducts which ultimately reduces the number of available pathways for charge carriers<sup>15</sup>.

In this work we present experimental charge transport data from field-effect transistor (FET) and time-of-flight (ToF) measurements quantifying the difference in electron mobilities in PCBM, bis-PCBM and tris-PCBM and estimating energetic disorder from fits to the experimental data. In order to relate those findings to the relative influence of structural and energetic disorder, kinetic Monte Carlo transport simulations are carried out on molecular assemblies constructed using coarse-grained molecular dynamics. A computationally efficient algorithm is developed to enumerate the different isomers, construct their coarse grained representations and assemble starting configurations with given distributions of isomers. To describe hopping transport, electronic transfer integrals, internal reorganisation energies and site energies are calculated using semi-empirical quantum chemical calculations.

## Experimental

Temperature-dependent time-of-flight measurements are an effective tool to determine the energetic disorder influencing charge transport. In order to prepare optically thick ( $> 1 \mu\text{m}$ ) films of PCBM we dispersed the fullerene in a matrix of polystyrene (33 wt% PCBM) by codeposition<sup>16</sup> and extracted electron mobilities using the integral method of time-of-flight photocurrent<sup>17</sup>. From the Gaussian Disorder Model (GDM)<sup>18</sup> we derive an energetic disorder of  $\sigma_{\text{GDM}} = 77 \text{ meV}$  which is in good accordance with literature<sup>19</sup>. Transients obtained for similar samples of bis- and tris-PCBM were too dispersive to obtain reliable mobilities.

To compare electron mobilities in all three fullerene types we measured FET mobility in top-contact bottom-gate FET structures<sup>20</sup> as a function of temperature. At room temperature and at a gate voltage  $V_G$  of 30 V, PCBM exhibits a mobility of  $5 \times 10^{-2} \text{ cm}^2/\text{Vs}$ ; bis-PCBM,  $3 \times 10^{-3} \text{ cm}^2/\text{Vs}$ ; and tris-PCBM,  $3 \times 10^{-5} \text{ cm}^2/\text{Vs}$  (see Figure 1). The mobilities follow an Arrhenius type temperature dependence with increasing activation energy in the order PCBM < bis-PCBM < tris-PCBM (see also supporting information). This indicates increasing energetic disorder with adduct number but it is not possible to extract a Gaussian disorder from the data.

## Generating Molecular Assemblies

Charge transport simulation requires large representative morphologies to avoid finite size effects. Here we generate a minimalist, coarse-grained molecular-dynamics forcefield for the fullerene adducts which allows isomer-specific intermolecular side

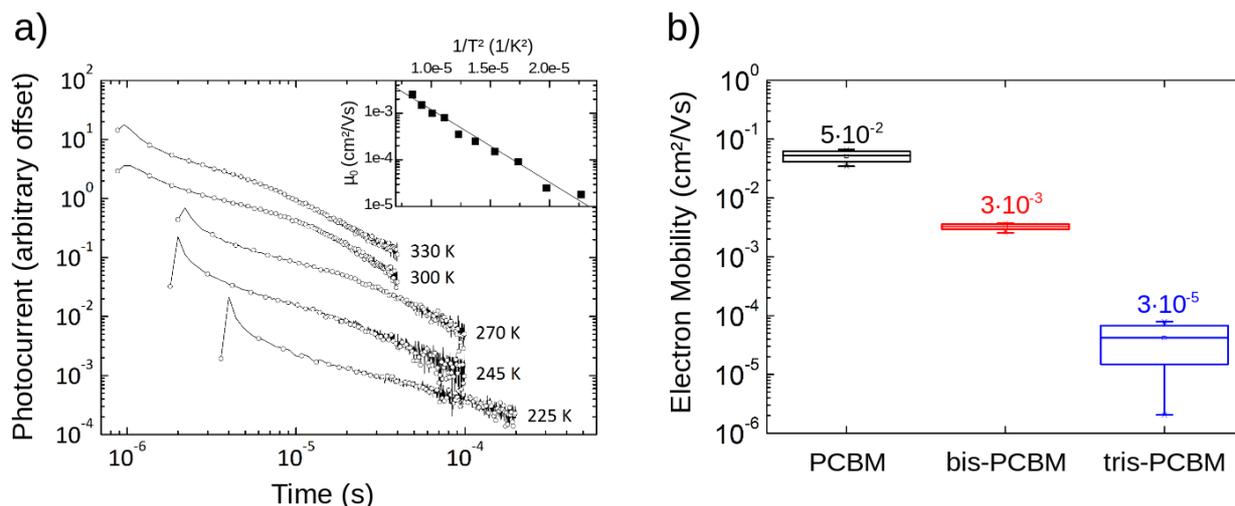


Figure 1. Experimental transport data. a) Temperature-dependent time-of-flight electron mobilities of PCBM dispersed in polystyrene (33 wt.% PCBM). Using the Gaussian Disorder Model, an energetic disorder of  $\sigma_{\text{GDM}} = 77 \text{ meV}$  can be extracted. b) Field-effect electron mobilities of pristine PCBM, bis-PCBM and tris-PCBM films at room temperature (300 K) for several gate-voltages  $V_G$  (between 20 V and 80 V) (see also SI1). At room temperature and  $V_G = 30 \text{ V}$ , PCBM shows a mobility of  $5 \times 10^{-2} \text{ cm}^2/\text{Vs}$ , bis-PCBM a mobility of  $3 \times 10^{-3} \text{ cm}^2/\text{Vs}$  and tris-PCBM a mobility of  $3 \times 10^{-5} \text{ cm}^2/\text{Vs}$  (also shown in figure).

chain interactions to be included explicitly. Our intent is to simulate the various PCBM adducts, modelling the fullerene cage as a bead and each side chain as an additional bead, and allowing beads to interact only through a Lennard-Jones potential for computational efficiency. This model for the side-chain of a single spherical super-atom is likely to be more accurate for more spherically symmetric side-chains such as indene-functionalised fullerenes than PCBM.

For the fullerene cage we adopt the Girifalco<sup>21</sup> coarse-grain buckminsterfullerene ( $C_{60}$ ) potential. In doing so we assume that the smearing out of the effective Lennard-Jones interactions of 60 graphitic-like carbons over the surface of the  $C_{60}$  cage is a valid approximation for the interaction of the fullerene cages in functionalised adducts.

For the PBM side-chain bead we choose the interaction energy to be the same as the Girifalco parameter for the fullerene site, scaled by the mass of the side-chain (190 Da for PBM versus 720.6 Da for  $C_{60}$ ), making the approximation that the side-chain interacts as graphitic carbon. We consider the bond between the fullerene cage and side-chain super-atoms to be arbitrarily stiff (though some flexibility of the side-chain is parametrised into its Lennard-Jones parameter), thus bond lengths and angles for the cage-sidechain attachments in the multi-adducts are fixed at the values of the relaxed geometry of each isomer. We are then left with two free parameters – one describing the sidechain-to-other distance minimum of the inter-molecular Lennard-Jones parameter ( $\sigma_{PBM}$ ), the other being the fullerene-sidechain bond length ( $r_{C_{60}-PBM}$ ).

To fit these parameters we generate pair distribution functions for mono-PCBM using atomistic MD. Our atomistic model for mono-PCBM is based on the OPLS<sup>22</sup> empirical force-field, with the reference geometry from a gas-phase quantum chemistry calculation (b3lyp/6-31g\*) and the fullerene cage simulated as arbitrarily stiff. We then generate a coarse-grained assembly of mono-PCBM using the atomistic structures as a starting configuration and fit the coarse-grain model parameters to reproduce the atomistic pair distribution function between fullerene cage centers (see Figure S14). The parameters used for the PBM sidechains in the atomistic MD are given in S15.

For the Lennard-Jones potential,  $V_{LJ} = 4\epsilon[(\sigma/r)^{12} - (\sigma/r)^6]$  with  $\epsilon$  being the depth of the potential well,  $\sigma$  referring to the finite distance where the potential is zero and  $r$  being the distance between sites. The  $C_{60}$  parameters  $\epsilon_{C_{60}} = 26.823$  kJ/mol and  $\sigma_{C_{60}} = 0.895$  nm are taken from the work of Girifalco et al.<sup>21</sup> and  $\epsilon_{PBM}$  is set to the  $C_{60}$  value weighted by relative mass of the sidechain, hence  $\epsilon_{PBM} = 10.0$  kJ/mol. Fitting of the coarse grained to the atomistic pair distribution function yields the remaining parameters,  $\sigma_{PBM} = 0.704$  nm and for the  $C_{60}$ -PBM bond  $r_{C_{60}-PBM} = 0.64$  nm. Having fitted a coarse-grained model for PCBM, we extend this to the various fullerene isomer adducts by adding extra PBM side-chains, with the same interaction parameters, at the bonded locations of the side-chains. The parameters for the irreducible set of eight bis and 45 tris isomers were generated by computationally efficient direct enumeration of all possible bonding configurations. Reduction of the set by point group symmetry was made by a simple canonical representation.

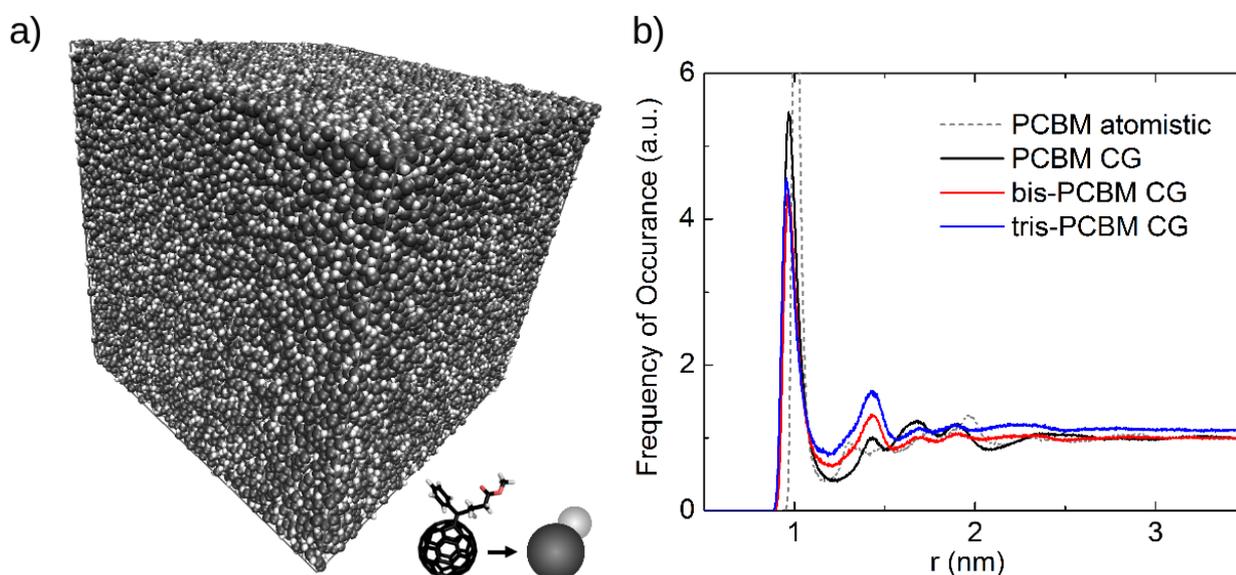


Figure 2. a) Coarse-grained molecular-dynamics (MD) structures of PCBM. The side length of the cube is 45.4 nm. The  $C_{60}$  cage (black) and the side chains (white) have been replaced by pearls. b) Radial distribution function of coarse-grained (CG) PCBM, bis-PCBM, tris-PCBM (structures of Figure 2a and Figure S11) and of atomistic PCBM. Atomistic MD and coarse-grained MD structures of PCBM have been compared (see dashed grey and black line) and the parameters of the Lennard-Jones interaction for the coarse-grained model have been fitted accordingly. An identical set of parameters has been used for the coarse-grained bis- and tris-PCBM structures.

We generate both single-isomeric (of PCBM, bis-E1-PCBM and tris-EEE-PCBM) and uniform mixes of all possible isomers (for bis-PCBM and tris-PCBM). All MD configurations contain 100,000 molecules, initially randomly packed loosely. The assemblies are compressed and equilibrated by simulated annealing with a barostat and then representative equilibrium configurations are sampled from a NPT ensemble (300 K, 1 atm). As expected, the volume of the equilibrated MD configurations increases with the number of side-chains (mono-PCBM: 0.094  $\mu\text{m}^3$ , bis-PCBM: 0.118  $\mu\text{m}^3$  and tris-PCBM: 0.155  $\mu\text{m}^3$ ) and is slightly larger for the selected single isomer configurations (bis-E1-PCBM: 0.121  $\mu\text{m}^3$  and tris-EEE-PCBM: 0.180  $\mu\text{m}^3$ ) than for isomeric mixes. Densities of around 1.5 g/cm<sup>3</sup> and an average displacement of molecules of less than 0.2 Å (over a period of 400 ps) indicate that all structures are solid at room temperature.

Using the fitted coarse grained molecular dynamics model in place of an atomistic model accelerates the structure generation by around three orders of magnitude. This advantage results from the reduced number of sites in the system, the neglect of charge interactions, (only Lennard-Jones inter-molecular parameters are needed), and the use of a longer time step, enabled by the greater mass of the pseudo-atoms. The coarse graining sacrifices any knowledge of the microscopic orientation of the fullerenes, preserving only information about the C60-C60 separations and coordination number. The separation data remains useful because of the approximately spherical symmetry of the fullerene frontier orbitals [23] which leads to an electronic transfer integral that depends only on separation, rather than on six degrees of freedom as in the general atomistic case, and is rapidly evaluated.

The size of the resulting coarse-grained MD generated assemblies, at 40-50 nm thick, is of relevant thickness for solar cells and is considerably larger than achievable assemblies from atomistic MD. In order to evaluate the influence of the system size on simulated charge carrier mobilities, we also generated smaller assemblies (1,000 molecules) of mono-, bis- and tris-PCBM (see SI6). All generated structures appear amorphous.

### Charge Transport Simulations

We use the ToFeT package<sup>23</sup> to simulate charge transport across the coarse-grained fullerene assemblies. This uses a kinetic Monte Carlo algorithm with rates from semi-classical Marcus theory. The hopping rate  $\Gamma_{ij}$  is defined as

$$\Gamma_{ij} = \frac{2\pi}{\hbar} \frac{|J_{ij}|^2}{\sqrt{4\pi\lambda k_B T}} \exp\left(\frac{-(\Delta E_{ij} + \lambda)^2}{4\lambda k_B T}\right) \quad (1)$$

where  $J_{ij}$  refers to the electronic transfer integral,  $\lambda$  to the total reorganisation energy,  $k_B$  is Boltzmann's constant,  $T$  is temperature and  $\Delta E_{ij}$  is the energy difference between the hopping sites  $i$  and  $j$ . We calculate internal reorganisation energies  $\lambda_{in}$  with hybrid-DFT (b3lyp/6-31g\*) and a four-point method<sup>24</sup>. We find  $\lambda_{in} = 155$  meV for PCBM and a range of isomer specific values for the different bis and tris adducts, with average values of 229 meV for bis-PCBM and 254 meV for tris-PCBM. The outer-sphere contribution  $\lambda_{out}$  is hard to

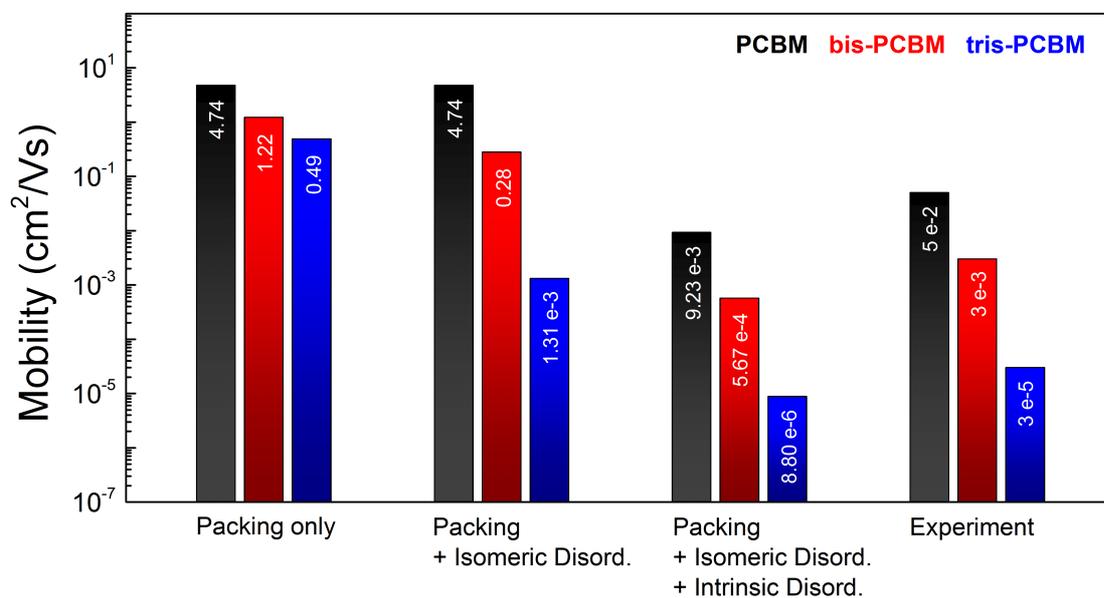


Figure 3. Simulated electron mobility data for reorganisation energies of  $\lambda = 200$  meV and structures containing 100,000 molecules. The bar chart compares the experimental results with simulated results for the three different levels of disorder studied. Note that because of the uncertainty in the value of  $\lambda$ , the relative values of electron mobilities have to be compared between experiment and simulation.

estimate and is commonly neglected<sup>23,25,26</sup>. In order to estimate the importance of varying reorganisation energies, we calculate Marcus hopping rates for all possible combinations between isomers. Two cases are studied: (a) a generic  $\lambda$  of 0.2 eV for all isomers and (b) using the isomer specific  $\lambda_m$  values (see S17). The effect of using the isomer specific  $\lambda_m$  values in place of the generic value is to vary the transfer rate by less than a factor of four, usually much less, and thus is small compared to the variations in experimental mobilities between fullerene adducts (see S17). Therefore, we assume in the following simulations identical reorganisation energies of 0.2 eV for all higher fullerene adducts.

We approximate the electron transfer integral  $J$  between fullerenes with the isotropic expression  $J(r) \propto \alpha \exp(-d/\beta)$  where  $d$  is inter-fullerene cage distance,  $\alpha$  is 15 keV and  $\beta$  is 0.5 Å. This functional relationship is based on a calculation of electron transfer integral as a function of separation for pairs of PCBM, bis-PCBM and tris-PCBM molecules (see S18). The values of  $\alpha$  and  $\beta$  extracted are in good agreement with previous calculations of  $J(r)$  for  $C_{60}$ <sup>27</sup>. Gajdos et al. found that transfer integrals between two PCBM molecules depend on their mutual orientation only for very small distances<sup>28</sup>. It is known that for slightly larger distances the influence of specific molecular structure weakens and the transfer integral follows an exponential relationship<sup>25,27</sup>. We therefore expect our isotropic expression for  $J$  to be an appropriate approximation.

The different distributions of LUMO energies for bis-PCBM and tris-PCBM are approximated by Gaussian distributions of width  $\sigma_{\text{isom}}$  of 56 meV and 121 meV respectively, following our previous work<sup>12</sup>. For completeness we also study discrete, isomer-specific energy levels (S19). We refer to this type of energetic disorder as isomeric disorder. For tris-PCBM we also consider a distribution with  $\sigma_{\text{isom}} = 72$

meV which neglects two outlier isomers. PCBM has no energetically distinct isomers and therefore has  $\sigma_{\text{isom}} = 0$  meV.

Despite possessing no isomeric disorder, in practice PCBM shows a temperature dependent mobility consistent with a degree of energetic disorder  $\sigma_{\text{GDM}} = 77$  meV as determined from GDM analysis of our ToF mobility measurements and similar to a previous study of SCLC mobility measurements<sup>19</sup>. This energetic disorder may arise from chemical impurities or from inductive effects of neighbouring fullerenes on the orbital energies<sup>18,29,30</sup>. In the following transport calculations we will refer to this component of disorder as intrinsic disorder  $\sigma_{\text{intr}}$ . Since the experimental disorder  $\sigma_{\text{GDM}}$  is determined using the GDM which is based on Miller-Abrahams transfer rates and our transport simulations invoke hopping rates from semiclassical Marcus theory, we have to convert the empirical quantity before it can be integrated into the disorder parameter used in transport simulations. This is done by extracting an empirical value from simulated temperature and field dependent mobilities using the GDM and comparing with the width of a Gaussian density of states input into the simulation (see S110). By this method the empirical (GDM) disorder of 77 meV is converted into a density of states broadening of  $\sigma_{\text{intr}} = 135$  meV.

For all transport simulations we use 10 frozen representations extracted from the 1 ns equilibrium 100 kDa coarse grain molecular dynamics trajectory (snapshots are separated by tens of ps). During the time-of-flight simulation an electric field of 0.01 V/nm is applied and we use regenerative contacts. The mobilities are calculated from collection times after convergence of the simulation. Coulomb interactions are neglected since simulations are run in the limit of low charge carrier concentrations. We consider three different regimes of energetic disorder. First, we assign the same energy to all sites ( $\sigma = 0$ )

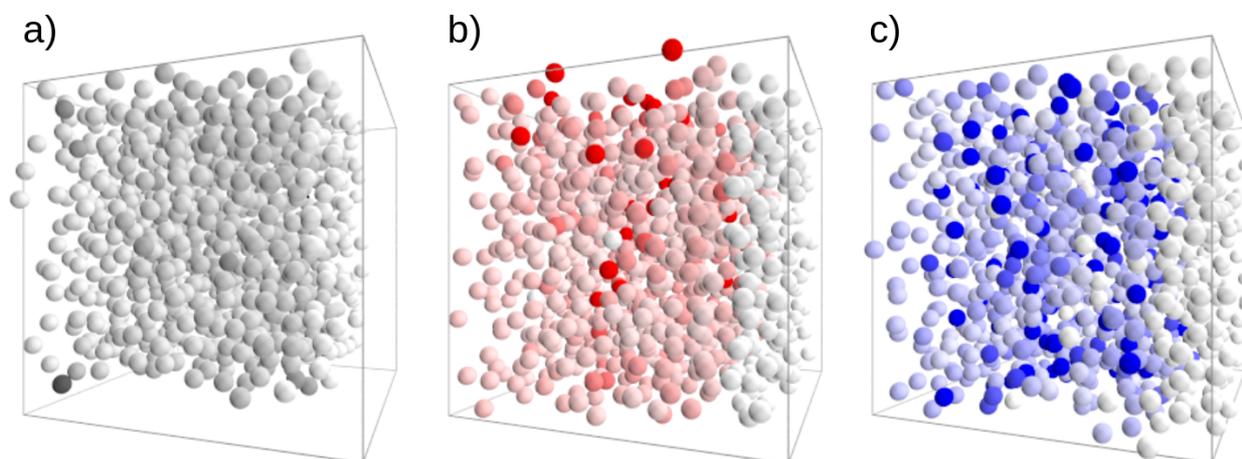


Figure 4. Density mapping of charge transport behaviour for a) PCBM, b) bis-PCBM and c) tris-PCBM in the case where structural, isotropic and intrinsic disorder are included. The pearls represent the C60 cages of the fullerene derivative (note that the beads are smaller than the C60 cage) and the charge-carriers travel from the left to the right. Colour intensity related to the cumulative electron residence time on the given hopping site. A homogeneous colour distribution (as in PCBM) indicates good transport whereas high contrast (as for tris-PCBM) indicates the presence of electron trap sites.

to study the role of molecular packing alone. Second, we introduce isomeric disorder ( $\sigma = \sigma_{\text{isom}}$ ) for the bis and tris assemblies. Third, we combine isomeric and intrinsic disorder in all cases by convolution of the Gaussian distributions ( $\sigma^2 = \sigma_{\text{isom}}^2 + \sigma_{\text{intr}}^2$ ). We assume the same intrinsic disorder  $\sigma_{\text{intr}}$  for all fullerene multi-adducts.

The simulated electron mobility values for  $\lambda = 200$  meV are shown in Figure 3. In the case of no energetic disorder the mobility difference between the fullerene derivatives depends only on the effect of packing on connectivity and transfer integral. Compared to the experiment, the relative differences between PCBM, bis-PCBM and tris-PCBM are too small ( $\mu_{\text{mono}}/\mu_{\text{bis}} = 4$  and  $\mu_{\text{mono}}/\mu_{\text{tris}} = 10$ ). Structures comprising only one isomer type (bis-E1-PCBM and tris-EEE-PCBM) exhibit slightly lower mobilities than corresponding structures with mixed isomers (see SI11), which is not surprising as the isomers we chose produce larger volume MD structures. The results indicate that packing is important, but not sufficient to explain the experimental observations.

Including isomeric disorder  $\sigma_{\text{isom}}$  increases the mobility ratios between the fullerenes close to the experimental finding ( $\mu_{\text{mono}}/\mu_{\text{bis}} = 17$  and  $\mu_{\text{mono}}/\mu_{\text{tris}} = 3600$ ). Neglecting the two deep trap-forming isomers for tris-PCBM the isomeric disorder drops from 121 meV to 72 meV. The relative mobility difference between PCBM and tris-PCBM would be reduced to 120 revealing the importance of such deep trap forming isomers. For the following calculations we retain the isomeric disorder of 121 meV for tris-PCBM.

Transport calculations combining packing, isomeric and intrinsic disorder with  $\lambda = 0.2$  eV yield absolute electron mobilities close to our FET measurements. We obtain for PCBM,  $(9.3 \pm 0.2) \times 10^{-3}$  cm<sup>2</sup>/Vs; for bis-PCBM,  $(5.7 \pm 0.1) \times 10^{-4}$  cm<sup>2</sup>/Vs; and for tris-PCBM,  $(8.8 \pm 0.3) \times 10^{-6}$  cm<sup>2</sup>/Vs. The mobility ratios between PCBM and its higher adducts are marginally reduced compared to the case considering exclusively isomeric disorder ( $\mu_{\text{mono}}/\mu_{\text{bis}} = 16$  and  $\mu_{\text{mono}}/\mu_{\text{tris}} = 1100$ ) and are still in good accordance with the experimental ratios.

Charge transport calculations with reorganisation energies of  $\lambda = 0.5$  eV lead to similar trends as for 200 meV (see SI11). The absolute mobility values are reduced by a factor of three however the relative mobility ratios are preserved. Simulations based on small molecular assemblies (1,000 molecules) show an increased variance in resulting mobilities but the mean values compare surprisingly well with mobilities from large structure simulations (see SI6).

A visual representation of the general transport characteristics is provided in Figure 4. It refers to a study on small molecular assemblies (1,000 molecules) where the colour intensity corresponds to the time that a transport site is visited. A uniform colour intensity indicates good transport where all molecules participate in the transport process (PCBM in Figure 4a). Poor transport behaviour is apparent for high contrast where traps appear as isolated, intensely coloured sites (tris-PCBM in Figure 4c).

## Conclusions

By building a multi-scale model up from an atomistic basis, with careful consideration of what physically justifiable approximations can be made at each level, we are able to reproduce quantitatively experimental values and trends in electron mobility. The separation of structural and energetic disorder in our model allows us to conclude that the low electron mobility observed in higher fullerene adducts is primarily due to the energetic disorder that results from the presence of different isomers. The relative insensitivity of mobility to structural disorder is assigned to the unique spherical symmetry of the electronic coupling in fullerene derivatives. On the basis of these results we predict that single isomer samples of the higher fullerenes will have mobilities within an order of magnitude of PCBM and, in some cases, will be capable of delivering greater power conversion efficiencies than PCBM. The coarse grained method saves several orders of magnitude in computing time relative to fully atomistic simulations. A similar approach can be recommended for transport simulations in other molecular materials provided that the most significant degrees of freedom in molecular packing and conformation can be identified.

## Acknowledgements

Florian Steiner would like thank Xerox Foundation / Xerox Research Centre of Canada (XRCC) for helpful discussions and their financial support and the DAAD for their financial support. Jarvist M. Frost, Samuel Foster and Jenny Nelson acknowledge the support of the Engineering and Physical Science Research Council (grant numbers EP/J500021, EP/F061757, EP/J017361 and EP/G031088). John G. Labram and Thomas D. Anthopoulos acknowledge the support of the the Engineering and Physical Sciences Research Council (EPSRC) grant number EP/F023200 and Research Councils UK (RCUK) for financial support. Jenny Nelson acknowledges the Royal Society for the award of a Wolfson Merit Award. Computer time was provided by the Imperial High Performance Computing Service<sup>31</sup>.

## Notes and references

<sup>a</sup> Department of Physics and Centre for Plastic Electronics, Imperial College London, London SW7 2AZ, UK.

\* Corresponding authors: jenny.nelson@imperial.ac.uk; j.m.frost@bath.ac.uk

† Now at Department of Chemistry, University of Bath, Bath BA2 7AY, UK

Electronic Supplementary Information (ESI) available: SI1 Temperature-dependent field-effect-transistor measurements of electron-mobilities, SI2 Time of flight measurements, SI3 MD-structures of PCBM, bis-PCBM and tris-PCBM, SI4 Coarse-grained vs. atomistic RDF, SI5 Fullerene side-chain enumeration, SI6 Small MD structures, SI7 Reorganisation energy, SI8 Charge transfer integrals, SI9 Discrete energy levels for isomers, SI10 Disorder conversion, SI11 Full table of charge-carrier mobilities for large MD structures, SI12 Coarse grain fullerene force field. See DOI: 10.1039/b000000x/

- 1 F. C. Jamieson, E. B. Domingo, T. McCarthy-Ward, M. Heeney, N. Stingelin, J. R. Durrant, *Chem. Sci.*, 2012, **3**, 485.
- 2 M. A. Faist, T. Kirchartz, W. Gong, R. S. Ashraf, I. McCulloch, J. C. de Mello, N. J. Ekins-Daukes, D. D. C. Bradley, J. Nelson, *J. Am. Chem. Soc.*, 2011, **134**, 685.

- 3 M. A. Faist, P. E. Keivanidis, S. Foster, P. H. Woebkenberg, T. D. Anthopoulos, D. D. C. Bradley, J. R. Durrant, and J. Nelson, *J. Polym. Sci. B Polym. Phys.*, 2011, **49**, 45.
- 4 P. A. Troshin, H. Hoppe, J. Renz, M. Egginger, J. Y. Mayorova, A. E. Goryachev, A. S. Peregodov, R. N. Lyubovskaya, G. Gobsch, N. S. Sariciftci, V. F. Razumov, *Adv. Funct. Mater.*, 2009, **19**, 779.
- 5 C. Zhang, S. Chen, Z. Xiao, Q. Zuo, L. Ding, *Org. Lett.*, 2012, **14**, 1508.
- 6 Y. He, H. Y. Chen, J. Hou, Y. Li, *J. Am. Chem. Soc.*, 2010, **132**, 1377.
- 7 M. Lenes, G.-J. A. H. Wetzelaer, F. B. Kooistra, S. C. Veenstra, J. C. Hummelen, P. W. M. Blom, *Advanced Materials*, 2008, **20**, 211.
- 8 M. Lenes, S.W. Shelton, A.B. Sieval, D.F. Kronholm, J.C. Hummelen, P.W.M. Blom, *Adv. Funct. Mater.*, 2009, **19**, 3002.
- 9 N. C. Cates, R. Gysel, Z. Beiley, C. E. Miller, M. F. Toney, M. Heeney, I. McCulloch, M. D. McGehee, *Nano Lett.*, 2009, **9**, 4153.
- 10 H. Azimi, A. Senes, M. C. Scharber, K. Hingerl, C. J. Brabec, *Adv. Energy Mater.*, 2011, **1**, 1162.
- 11 M. A. Faist, S. Shoaee, S. Tuladhar, G. F. A. Dibb, S. Foster, W. Gong, T. Kirchartz, D. D. C. Bradley, J. R. Durrant and J. Nelson, *Adv. Energ. Mater.*, 2013, **3**, 744.
- 12 J. M. Frost, M. A. Faist, J. Nelson, *Adv. Mater.*, 2010, **22**, 4881.
- 13 R. K. M. Bouwer, G.-J. A. H. Wetzelaer, P. W. M. Blom, J. C. Hummelen, *J. Mater. Chem.*, 2012, **2**, 15412.
- 14 W. W. H. Wong, J. Subbiah, J. M. White, H. Seyler, B. Zhang, D. J. Jones, A. B. Holmes, *Chem. Mater.*, 2014, **26**, 1686.
- 15 X. Meng, G. Zhao, Q. Xu, Z. Tan, Z. Zhang, L. Jiang, C. Shu, C. Wang, Y. Li, *Adv. Funct. Mater.*, 2013, **24**, 158.
- 16 S. M. Tuladhar, D. Poplavskyy, S. A. Choulis, J. R. Durrant, D. D. C. Bradley, J. Nelson, *Adv. Funct. Mater.*, 2005, **15**, 1171.
- 17 A. J. Campbell, D. D. C. Bradley, H. Antoniadis, *Appl. Phys. Lett.*, 2001, **79**, 2133.
- 18 H. Bässler, *Phys. Stat. Sol. (B)*, 1993, **175**, 15.
- 19 V. D. Mihailetschi, J. K. J. van Duren, P. W. M. Blom, J. C. Hummelen, R. A. J. Janssen, J. M. Kroon, M. T. Rispens, E. J. H. Verhees, M. M. Wienk, *Adv. Funct. Mater.*, 2003, **13**, 43.
- 20 J. Zaumseil, H. Sirringhaus, *Chem. Rev.*, 2007, **107**, 1296.
- 21 L. A. Girifalco, M. Hodak, R. S. Lee, *Phys. Rev. B*, 2000, **62**, 13104.
- 22 W. L. Jorgensen, D. S. Maxwell, J. Tirado-Rives, *J. Am. Chem. Soc.*, 1996, **118**, 11225.
- 23 J. J. Kwiatkowski, J. Nelson, H. Li, J. L. Bredas, W. Wenzel, C. Lennartz, *Phys. Chem. Chem. Phys.*, 2008, **10**, 1852.
- 24 K. Sakanoue, M. Motoda, M. Sugimoto, S. Sakaki, *J. Phys. Chem. A*, 1999, **103**, 5551.
- 25 V. Rühle, A. Lukyanov, F. May, M. Schrader, T. Vehoff, J. Kirkpatrick, B. Baumeier, Björn, D. Andrienko, *Journal of Chemical Theory and Computation*, 2011, **7**, 3335.
- 26 C. Poelking, E. Cho, A. Malafeev, V.A. Ivanov, K. Kremer, C. Risko, J.L. Bredas, D. Andrienko, *J. Phys. Chem. C*, 2013, **117**, 1633.
- 27 J. J. Kwiatkowski, J. M. Frost, J. Nelson, *Nano Letters*, 2009, **9**, 1085.
- 28 F. Gajdos, H. Oberhofer, M. Dupuis, J. Blumberger, *J. Phys. Chem. Lett.*, 2013, **4**, 1012.
- 29 O. D. Jurchescu, J. Baas, T. T. M. Palstra, *Appl. Phys. Lett.*, 2004, **84**, 3061.
- 30 D. P. McMahon, D. L. Cheung, L. Goris, J. Dacuna, A. Salleo, A. Troisi, *J. Phys. Chem. C*, 2011, **115**, 19386.
- 31 Imperial College High Performance Computing Service, URL: <http://www.imperial.ac.uk/ict/services/teachingandresearchservices/hi ghperformancecomputing>

## Table of Contents Entry

A combination of coarse-grained molecular dynamics and kinetic Monte-Carlo modeling shows that electron transport in fullerene multi-adducts is limited by energetic disorder due to different isomers rather than by structural disorder.

