

PCCP

Accepted Manuscript



This is an *Accepted Manuscript*, which has been through the Royal Society of Chemistry peer review process and has been accepted for publication.

Accepted Manuscripts are published online shortly after acceptance, before technical editing, formatting and proof reading. Using this free service, authors can make their results available to the community, in citable form, before we publish the edited article. We will replace this *Accepted Manuscript* with the edited and formatted *Advance Article* as soon as it is available.

You can find more information about *Accepted Manuscripts* in the [Information for Authors](#).

Please note that technical editing may introduce minor changes to the text and/or graphics, which may alter content. The journal's standard [Terms & Conditions](#) and the [Ethical guidelines](#) still apply. In no event shall the Royal Society of Chemistry be held responsible for any errors or omissions in this *Accepted Manuscript* or any consequences arising from the use of any information it contains.

Prediction of the Chapman-Jouguet Chemical Equilibrium State in a Detonation Wave from First Principles Based Reactive Molecular Dynamics

Cite this: DOI:

10.1039/x0xx00000x

Dezhou Guo,^{a,b} Sergey V. Zybin,^b Qi An,^b William A. Goddard III FRSC^{b,*}, and Fenglei Huang,^a

Received 00th January 2012,
Accepted 00th January 2012

DOI: 10.1039/x0xx00000x

www.rsc.org/

ABSTRACT: The combustion or detonation of reacting materials at high temperature and pressure can be characterized by the Chapman-Jouguet (CJ) state that describes the chemical equilibrium of the products at the end of the reaction zone of the detonation wave for sustained detonation. This provides the critical properties and product kinetics for input to macroscale continuum simulations of energetic materials. We propose the ReaxFF Reactive Dynamics to CJ point protocol (Rx2CJ) for predicting the CJ state parameters, providing the means to predict the performance of new materials prior to synthesis and characterization, allowing the simulation based design to be done in silico. Our Rx2CJ method is based on atomistic reactive molecular dynamics (RMD) using the QM-derived ReaxFF force field. We validate this method here by predicting the CJ point and detonation products for three typical energetic materials. We find good agreement between the predicted and experimental detonation velocities, indicating that this method can reliably predict the CJ state using modest levels of computation.

Key words: energetic materials, reactive molecular dynamics, ReaxFF, detonation, Crussard curve, Chapman-Jouguet state

1 Introduction

Environment and energy needs demand development of maximally efficient propulsion combustion systems and energetic materials that minimize products detrimental to the environment. Moreover, the behaviour of materials under extreme conditions of high temperature and pressure is of critical importance in many fields of physics, astrophysics, planetary science, and hydrodynamics^{1,2}, where the difficulty in extracting atomistic understanding of reaction mechanisms in hot compressed materials from experiments makes it particularly important to predict the processes from the computational modelling and simulation. The complexity of the combustion and detonation processes might seem to preclude applications of first principles to predict the performance and reaction kinetics for new materials in advance of their synthesis and characterization. However, we propose a practical simulation approach based on first principles theory for predicting the performance of energetic materials, which we validate for three well-known materials.

A critical characteristic of energetic materials is the Chapman-Jouguet (CJ) state, which describes the chemical

equilibrium of the products at the end of the reaction zone of the detonation wave before the isentropic expansion. In the classical Zel'dovich–Neumann–Döring (ZND) detonation model, the detonation wave propagates at the constant velocity for which the CJ point characterizes the state of reaction products in which the local sound speed decreases to the detonation velocity as the product gases expand. Although a simple concept, the time and length scale of CJ state have thwarted experimental characterization³. These laboratory challenges have stimulated theoretical developments, such as variational perturbation theory⁴ and integral equation theory^{5,6}, to provide numerical models. Unfortunately, these approaches have been hampered by a lack of knowledge about the atomistic chemical and physical processes and by inaccuracy in the assumed equations of state (EOS).

Thus, we need new simulation tools that are capable of establishing the CJ state parameters for proposed materials directly from first principles. These simulation tools must provide an accurate description of the various reaction processes that convert materials to detonation products and they must be capable of making predictions in advance of experiment.

Quantum mechanics (QM) can in principle describe reaction processes for new materials but the time and length scales required are many orders of magnitude beyond the capability of current QM methods.

We demonstrate in this paper a practical approach to reactive molecular dynamics (RMD) predictions of the CJ state in which the QM-derived ReaxFF reactive force field is used to provide the detailed description of the atomistic processes occurring in a detonation wave. This allows a practical determination of the CJ parameters for new materials prior to experiment.^{3, 7-12}

Here, for the first time the Crussard curve and the CJ point are predicted from first-principles based reactive molecular dynamics (RMD) simulations without the need for ad hoc definitions of reaction products. We demonstrate this approach by applying it to three energetic materials that are currently widely used in industry:

- Cyclotrimethylene-trinitramine (RDX),
- Cyclotetramethylene tetranitramine (HMX), and
- Pentaerythritol-tetranitrate (PETN).

2. Methodology

The ReaxFF reactive force field combines

- charge equilibration method (EEM or QEq¹³) to predict the changes in the partial charges on atoms at every time step of the reaction dynamics. Here the parameters were determined to fit QM charges of isolated molecules. In this method the charges of bonded atoms are allowed to interact, but they decreased by shielding based on atomic sizes.
- a bond order versus bond distance sigmoid-like relationship and a bond energy versus bond order relationship adjusted to fit the results of QM calculations as function of bond distance for numerous systems
- van der Waals type nonbond interactions adjusted to describe long range London attraction, intermediate range steric effects, and short range Pauli repulsion between all atoms (including bonded atoms)
- various other valence interactions (bond angle and torsion) that all go to zero as bonds are broken with parameters fitted to a large data set of QM calculations.

ReaxFF has now been established to provide nearly the accuracy of QM calculations¹⁴⁻¹⁶ with computational costs nearly that of molecular dynamics (MD) with ordinary force fields (FFs).^{17, 18} This has enabled the simulation of complex sequence of reactions and multiple intermediates during shock transformation and thermal decomposition of energetic materials, with application to 3.7 million atoms for ~100 nanoseconds.¹⁹⁻²⁶ Thus, ReaxFF enables the atomistic description of the chemical reactions and products in detonation wave defining the CJ state. Moreover, the reactive molecular dynamics (RMD) using ReaxFF provides the means for obtaining the equation of state (EOS) of reacting materials at the atomistic level without the necessity of *ad hoc* assumptions about reaction products and their properties. Indeed we obtain a detailed

description of all chemical reactions during the decomposition processes, including the formation of carbonaceous clusters generally ignored in previous models. This allows a direct comparison of the theory with experiment through the CJ state parameters while providing atomistic information about the chemical reaction processes and products on each dynamics step inaccessible from experiments. Moreover it allows the prediction of these detonation properties prior to experimental synthesis and characterization, to enable in silico design of new energetic materials.

According to the classical ZND model, the thermodynamic quantities of a material in the initial unshocked state and the final shocked state are related by the conservation equations of mass, momentum, and energy across the shock front as

$$\rho_0 D = \rho(D-u) \quad (1),$$

$$p - p_0 = \rho_0 u D \quad (2),$$

$$e + pv + \frac{1}{2}(D-u)^2 = e_0 + p_0 v_0 + \frac{1}{2}D^2 \quad (3),$$

where D is the constant velocity of the unsupported detonation wave, ρ is the density, u is the velocity of the products behind the detonation wave, p is the pressure, e is the specific internal energy, and v is the specific volume. The term “specific” refers to the quantity per unit mass, while the subscript ‘0’ refers to the quantity in the initial unshocked state. To determine the thermodynamic parameters (p, v, T) of the states in detonation wave, we search for zeroes of the Hugoniot function, derived from the equations (1)-(3), similarly to the procedure outlined by Erpenbeck⁹ and related approaches^{3, 27-29}

$$H = e - e_0 - \frac{1}{2}(p + p_0)(v_0 - v) \quad (4).$$

The Hugoniot function relates the energy of two thermodynamic states: the initial unshocked state and the shocked state, so that $H = 0$ simply expresses the energy conservation in the shock or detonation wave. The set of (p, v, T) parameters for which $H = 0$ determines the Hugoniot curve of shocked states in the inert (unreacted) material as well as the states along the Rayleigh line in the reacting material. According to the ZND model, the explosive material remains inert during the shock compression at the detonation front, which is considered as a sudden step-like increase in the temperature and pressure. Then the chemical reactions start, followed by further increase in the temperature due to the exothermic energy release and decrease in the pressure due to the expansion of the reaction products. As a result, the states in the reacting material follow the expansion pathway along the Rayleigh line down to the CJ state on the Crussard curve, which is an expansion isentrope of the detonation products. In fact, there are many expansion isentropes corresponding to different product compositions, but only one has a tangent point to the Rayleigh line, which satisfies CJ condition and is called the CJ state.

Our first test of this ReaxFF Reactive Dynamics to CJ point protocol (Rx2CJ) is on RDX. Here we start with equilibration of the RDX supercell containing 96 molecules (or 2016 atoms) at constant temperature $T_0 = 300$ K and pressure $p_0 = 1$ atm, obtaining an initial

state equilibrium volume $v_0 = 0.568 \text{ cm}^3/\text{g}$ and density $\rho_0 = 1.76 \text{ g/cm}^3$ (in a good agreement with the 1.806 g/cm^3 experimental density of neat RDX).

Then we use ReaxFF to predict the final state in which complete reaction products are calculated from a long cook-off holding the system at a prescribed temperature that leads to stable products (H_2O , CO_2 , N_2 , CO etc.). We find that this requires $\sim 250 \text{ ps}$ for the energetic materials being considered here.

Figure 1 illustrates one example for RDX at $T=2700 \text{ K}$ and $V=0.85V_0$. We observe the gradual approach to equilibrium for the the potential energy, as well as the stable compositions of the final products (inset of figure), indicating that steady state convergence is reached after 200 ps. Consequently, we average the properties of the trajectories over the last 100 of the 350 ps total trajectory. In the earlier energy releasing period within the first 250 ps, the Hugoniot and potential energy curve trend downward, indicating the dominance of exothermic chemical reactions.

To validate that 350 ps was sufficient to reach equilibrium, we extended one case for RDX decomposition up to 550 ps and calculated the averages of thermal properties and the main reaction products from 200 ps to 550 ps. The potential energy of $-1.127 \pm 0.014 \text{ kcal/g}$ for the last 100 ps of the 550 ps simulation agrees with the previous value of $-1.130 \pm 0.014 \text{ kcal/g}$ averaged between 200 and 300 ps. The product distributions were also the same as shown in Fig.S2 of the Supporting Information.

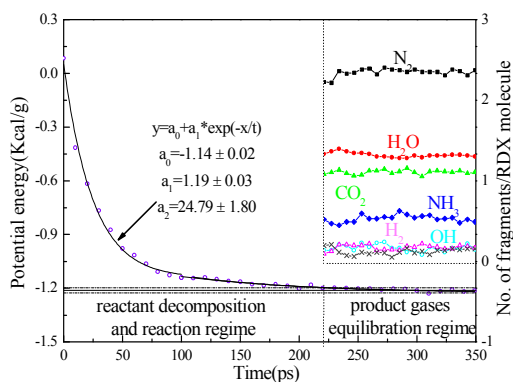


Fig. 1. Time evolution of the potential energy per unit mass and reaction products (inset for the last 100ps of NVT simulation) for RDX at $T=2700 \text{ K}$ and $V/V_0=0.85$. The solid horizontal line shows an average over the final 100 ps of simulation while the dashed lines mark the standard deviation above and below the average values from five independent simulations. The corresponding plots for PETN and HMX are included in the Supplemental Information.

For each specific temperature we obtain a family of Hugoniot function values by changing the density (volume) of the material. From these curves we find the $H_g=0$ points that determine the Crussard curve. We determine five $H_g=0$ points to describe the Crussard curve accurately. Each $H_g=0$ point corresponds to a specific temperature. For each temperature, we do at least three different compression ratios to bracket the $H_g=0$ case, as shown in Figure 2. The compression volume ratios at the intersection between

Hugoniot function for a fixed temperature and the $H_g=0$ axis provides the location of one point in the Crussard curve of Figure 3a.

We examined the points obtained from Figure 2 at each temperature and found that their Hugoniot values remain quite close to 0. Thus these points provide an accurate description of the Crussard curve. Then, as shown in Figure 3a, we fit the pressure versus V/V_0 to a quadratic polynomial that expresses the evolution of pressure as a function of the volume compression. The temperature is expressed in the same way, as shown in Figure 3b.

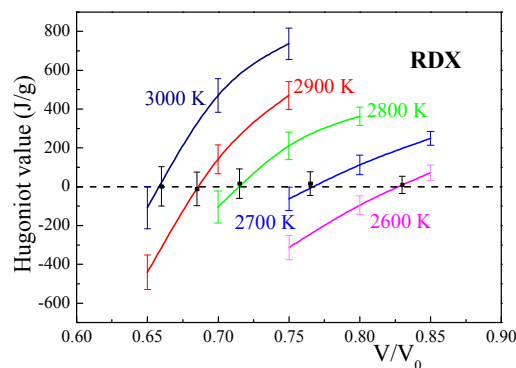


Fig. 2. The family of isotherms (spline fitted) for RDX at compression ratios from 0.60 to 0.85 for five different temperatures. For each temperature we did five independent calculations to estimate the standard deviation error bars. The intersection of these curves with the $H=0$ line provides five points along the Crussard isentrope that are plotted in Fig. 3: $V/V_0=0.660$ at 3000 K, 0.685 at 2900 K, 0.715 at 2800 K, 0.760 at 2700 K, and 0.830 at 2600 K. The corresponding plots for PETN and HMX are included in the Supplemental Information.

Once we have determined the Crussard curve as in Fig. 3, we can determine the CJ point. The CJ point is the tangent point between the Rayleigh line and the Crussard curve, as illustrated in Figure 3. Thus, at the CJ point, the derivative of the pressure along the Crussard curve with respect to the volume is given by the slope of the Rayleigh line. We represent the Crussard curve and Rayleigh line as:

$$P = a_0 + a_1n + a_2n^2 \quad (5)$$

$$P = an + b \quad (6)$$

where $n = V/V_0$.

Here, as the shock wave starts from the undisturbed material, the Rayleigh line starts from the point at (1, 0). As a result, the Rayleigh line can be expressed as:

$$P = an - a \quad (7).$$

For the Rayleigh line that is a tangent line to the Crussard curve, we obtain:

$$a = a_1 + 2a_2n \quad (8).$$

The variables P and a can be eliminated from Eq. (5) using Eqs. (7) and Eqs. (8) to obtain the CJ point volume compression ratio as:

$$n_{CJ} = 1 - \sqrt{1 + \frac{a_1 + a_0}{a_2}} \quad (9).$$

From here, we obtain the CJ temperature by substituting n_{CJ} into the temperature-compression ratio curve.

We denote this method as the ReaxFF RMD to CJ point method (Rx2CJ). From the calculated P_{CJ} and n_{CJ} , we calculate the detonation velocity D_{CJ} , using the following equation derived from the Hugoniot relations:

$$D_{CJ} = \sqrt{\frac{P_{CJ} - P_0}{\rho_0(1 - n_{CJ})}} \quad (10).$$

This predicted detonation velocity is important because it can be measured directly from experiments, providing an overall validation of the entire computational process of predicting the CJ state parameters from atomistic simulations.

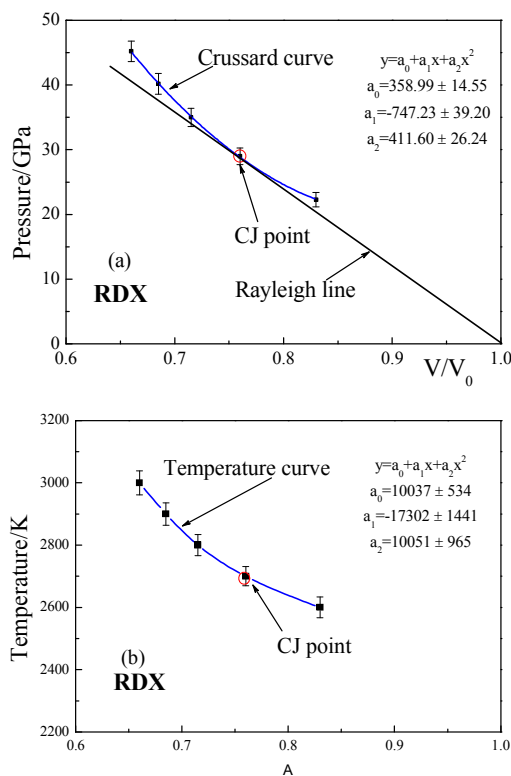


Fig. 3. Calculation of the CJ state parameters by fitting the Crussard curve to a series of equilibrium states simulated by the ReaxFF RMD method (Rx2CJ). (a) The CJ point is the tangent point of the Rayleigh line to the Crussard curve fitted with a quadratic polynomial. This fitting provides the CJ point with compression ratio $V/V_0=0.76$ and pressure $P_{CJ} = 28.62$ GPa for RDX. (b) Equilibrium temperatures for the various points along the Crussard curve, fitted to a quadratic polynomial. The predicted CJ temperature for RDX^{30,31} is 2700 K, as indicated by the circle. The corresponding plots for PETN and HMX are included in the Supplemental Information.

3. Results and Discussions

We applied the Rx2CJ protocol to predict the Crussard curve and CJ state parameters for 4 systems:

- An RDX supercell containing 96 molecules (or 2016 atoms) at constant temperature $T_0 = 300$ K and pressure $p_0 = 1$ atm, obtaining an initial state equilibrium volume $v_0 = 0.568$ cm³/g and density $\rho_0 = 1.76$ g/cm³, (in good agreement with the 1.806 g/cm³ experimental density of neat RDX.). This leads to $D = 8266 \pm 198$ m/s for RDX, which is 4.7% below the experimental values of 8639 ± 41 m/s and 8700 m/s;
- A β -HMX supercell containing 2688 molecules (or 96 atoms) at constant temperature $T_0 = 300$ K and pressure $p_0 = 1$ atm, obtaining an initial state equilibrium volume $v_0 = 0.538$ cm³/g and density $\rho_0 = 1.86$ g/cm³, (in good agreement with the 1.90 g/cm³ experimental density of neat β -HMX). This leads to $D = 8401 \pm 217$ m/s for β -HMX which is 4.5% below the experimental values of 8740 m/s and 8880 m/s.
- A PETN supercell containing 72 molecules (or 2088 atoms) at constant temperature $T_0 = 300$ K and pressure $p_0 = 1$ atm, obtaining an initial state equilibrium volume $v_0 = 0.581$ cm³/g and density $\rho_0 = 1.72$ g/cm³, (in good agreement with the 1.77 g/cm³ experimental density of neat PETN). This leads to $D = 7440 \pm 209$ m/s for PETN, which is 7.1% below with the experimental values of 7975 m/s and 8260 m/s;
- The decomposition of a model mixture of 27 H₂ and 27 O₂ molecules using the same ReaxFF parameters started an initial density of 0.09 g/cm³ at an initial temperature of 123 K. This leads to a CJ temperature of 2600 K and a detonation velocity of 2538 ± 377 m/s, which is 9.3% below the experimental values, which range from 2800 to 3000 m/s³² (see more details in Supporting Information).

The predicted CJ parameters are in reasonable agreement with experiment, but they are slightly below the experimental values. We believe that this is because the products evolution shown in Fig. 1 on the timescale up to 350 ps still contains carbonaceous products (0.47 mol/mol for RDX, 0.52 mol/mol for PETN 0.48 mol/mol for β -HMX). Under experimental conditions in which the reaction zone persists for microseconds, much of this carbonaceous material may burn off to form additional gases and hence a higher velocity. We consider that these results validate the Rx2CJ method for first principles based predictions of performance properties for new propellants and explosive materials, where the systematic underestimate of the experimental velocity will still provide a valid measure of performance.

Sewell and co-workers^{33,34} suggested that quantum nuclear vibrational effects ignored in classical MD, lead to an underestimate of the temperature along the Hugoniot curve for weak to medium shocks (<1 km/sec). Moreover, Goldman et al³⁵ suggest that such problems with classical MD could explain the discrepancy of their QM simulations with experiments. The quantum nuclear vibrational effects might slightly affect the calculated pressure and temperature at the CJ conditions.³⁶ The quantum effects will enhance the chemical reactivity of the

system, allowing it to approach chemical equilibrium more rapidly³⁶.

The predicted properties at CJ state for the three materials are collected in Table 1.

Along with these detonation parameters, we can extract from our simulations detailed distribution of chemical products at the CJ states. We do this using a bond order based molecular fragment analysis on the RMD simulation trajectory (tabulated in Supporting Information), leading to the results shown in Table 2. These results are averaged over 3 independent trajectories and over the last 100 ps of the 350 ps simulation.

For example, for each mole of the PETN explosive we find that the main products at the CJ state are

- 1.81 moles of N₂ (2.00 experimental),
- 3.00 moles of H₂O (3.50 experimental),
- 2.37 moles of CO₂ (3.39 experimental),
- 0.18 moles of CO (1.69 experimental) and
- carbonaceous clusters with an overall composition of C_{3.3}H_{0.6}N_{0.3}O_{2.6} containing approximately 49% of the original C, 32% of the original O and 8% of the original H atoms (these clusters are not characterized experimentally at the CJ state).

We also found small amounts of other molecules, such as 0.20 moles of NH₃, 0.20 moles of OH and 0.27 moles of H₂.

The total number of N₂, H₂ and H₂O molecules agrees well with calorimeter bomb experiment³⁷; but the prediction for CO₂ from PETN are 30% lower than observed experimentally, while that of CO is 89% lower. This is because the products in calorimetric experiments are formed over a timescale of seconds, allowing further expansion along the Crussard isentrope and cooling down into the gas phase at normal conditions. However our constant-volume simulations measure the product composition at the CJ state for thermodynamic conditions in the hot compressed material. Thus we end up in a state with temperature of 2000-4000 K and pressure of 20-50 GPa. As a result, our simulations show an additional number of carbon and oxygen atoms remaining agglomerated in small carbon containing clusters. Although this may affect slightly the resulting product distribution and the total energy release over the 350 ps timescale of our simulations it should allow accurate comparisons in performance of various materials.

We estimated the mass percentage of carbon clusters, final products, and other small isolated molecules at the CJ state conditions for RDX, as shown in Fig. 4(a). About 29% mass of the system is in the form of clusters containing C, O, N, and H.

Table 1. Detonation parameters calculated by the Rx2CJ method, compared with experimental data³⁸⁻⁴¹.

	RDX			PETN			HMX		
	ReaxFF	Exp1 ³⁸	Exp2 ³⁹	ReaxFF	Exp1 ⁴⁰	Exp2 ³⁹	ReaxFF	Exp1 ⁴¹	Exp2 ⁴¹
Density (g/cm ³)	1.76	1.767	1.77	1.72	1.67	1.76	1.86	1.832	1.875
P _{CJ} (GPa)	28.62 ± 4.77			22.47 ± 3.09			32.68 ± 3.43		
T _{CJ} (K)	2700 ± 56			2460 ± 40			2680 ± 58		
V _{CJ} (cm ³ /g)	0.433 ± 0.019			0.445 ± 0.013			0.404 ± 0.021		
D _{CJ} (m/s)	8266 ± 198	8639 ± 41	8700	7440 ± 209	7975	8260	8401 ± 223	8740	8880

To determine the stability and evolution of these clusters in expanding gases, we applied the “linear volume expansion” procedure²⁴ using variable-volume RMD simulations: here the system volume V₀ is increased very slowly at a linear rate within 100 ps until it expands to 8V₀. The evolution of carbon clusters, CO₂ and CO molecules during the expansion are shown in Figure 4(b). As expected, many agglomerates continue to decompose,

producing additional CO₂ and CO products. Indeed we saw exactly same result in our previous expanded-volume RMD simulations of RDX¹⁶ as well as for HMX and TATB²⁴. We expect that this after-burning of carbonaceous clusters would affect the predicted product compositions in expanded gases, bringing it closer to experiment.

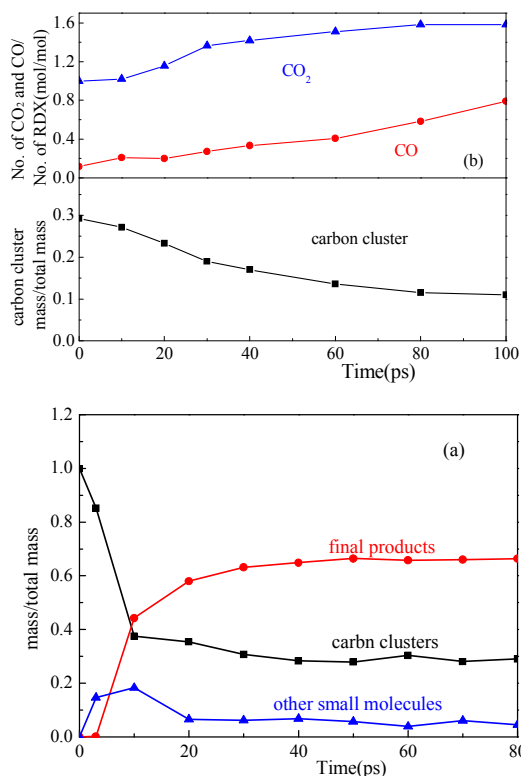


Fig. 4. Evolution of the products with time for RDX RMD simulation as the volume is expanded linearly by a factor of 8 from the 250 ps point over an additional 100 ps: (a) the mass percentage of carbon clusters (with more than 2 carbon atoms per cluster), final products, and other small isolated molecules for RDX during NVT (at CJ point thermodynamic conditions). (b) Evolution of mass percentage of carbon clusters and the number of CO₂ and CO molecules normalized by the initial number of RDX molecules during the “linear volume expansion” simulation.

To estimate the additional energy release from carbonaceous cluster decomposition induced by the expansion simulation of 100 ps, we recompressed the expanded system back to the CJ volume and temperature over an additional 50 ps (see Fig. 5). We found that the potential energy release increased about 2.4% and the pressure increased about 2.1%, leading to a detonation velocity of 8314 m/s, which is ~0.6% higher than the previous results (8266 m/s).

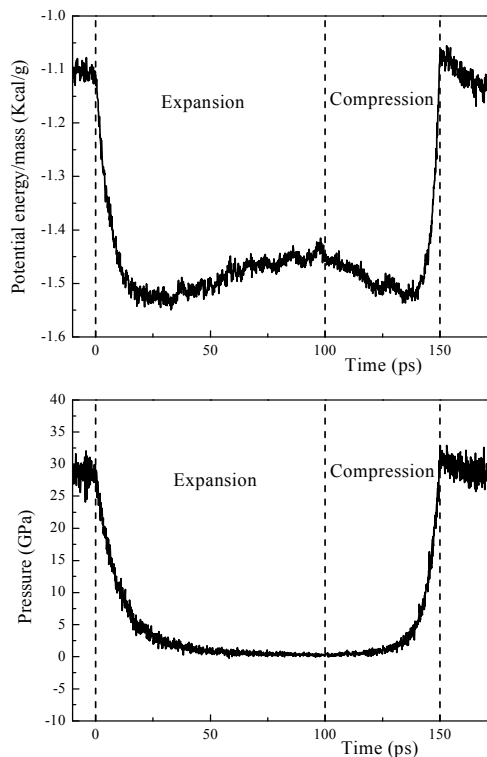


Fig. 5. Evolution of the potential energy and pressure during constant temperature simulation of 8 times volume expansion over 100 ps and the volume recompression over 50 ps back to the initial volume, followed by additional 25 ps of NVT equilibration constant volume.

Some of the minor discrepancies between Rx2CJ prediction and experiment may reflect inaccuracy in the ReaxFF description and some may arise from imperfections in the experiments (e.g. nonuniform detonation front conditions and difficulties in precise measurements of detonation temperature and pressure).

Previous studies aimed at predicting the CJ state parameters were based on the use of simple nonreactive potentials for intermolecular interactions^{3,9} and involved Monte Carlo estimates of statistical ensembles with a predefined set of the reactions over a small set of molecules (RxMC)²⁷⁻²⁹. Thus these previous approaches depend strongly on defining an *ad hoc* set of the final products and their reactions for an assumed chemical equilibrium of their mixture. In contrast, our Rx2CJ approach predicts the detonation products at the CJ state without any assumption about their composition. It does this directly from the ReaxFF RMD simulation of the complex chemical reactions, starting from the initial neat reactant to obtain the CJ state thermodynamic conditions. A similar approach employing MD simulations with the generic reactive AB-potential¹⁰ was recently applied to calculate the CJ state properties as well as complex cellular structure of the detonation front for an AB-model of a diatomic explosive⁴².

Table 2. Detonation Products predicted at the CJ state in RDX, PETN, and HMX, compared to calorimeter bomb experiment^{37,43}

		RDX		PETN		HMX	
		Experiment confined (gas phase)	ReaxFF (condensed)	Experiment confined (gas phase)	ReaxFF (condensed)	Experiment confined (gas phase)	ReaxFF (condensed)
Density(g/cm ³)		1.76	1.76	1.73-1.74	1.72	1.89	1.86
$\Delta H(\text{cal/g})$		1452 ± 15	1458 ± 12	1370	1331 ± 15	1479 ± 12	1520 ± 19
Products (mol/mol)	N ₂	2.80	2.38 ± 0.04	2.00	1.81 ± 0.02	3.68	3.13 ± 0.03
	H ₂ O	2.34	1.50 ± 0.05	3.50	3.00 ± 0.03	3.18	2.45 ± 0.04
	HO		0.24 ± 0.05		0.20 ± 0.06		0.25 ± 0.05
	CO ₂	1.39	1.14 ± 0.03	3.39	2.37 ± 0.06	1.92	1.29 ± 0.03
	CO	1.10	0.23 ± 0.02	1.69	0.18 ± 0.01	1.06	0.24 ± 0.02
	C(s)	0.44				0.97	
	H ₂	0.34	0.43 ± 0.01	0.45	0.27 ± 0.01	0.30	0.41 ± 0.01
	NH ₃	0.028	0.46 ± 0.03	0.038	0.20 ± 0.02	0.39	0.43 ± 0.02
	HCN	0.029				0.008	
	CH ₄	0.041		0.003		0.039	
Material recovery (%) ^a							
	C	85.5	45.67	101.5	51.00	75.6	42.5
	H	94	91.33	100.1	91.75	104	90.75
	N	94.2	87.00	100.8	95.50	97.1	83.63
	O	104	66.50	99.7	67.67	101	72.38
(mol/mol)	Carbon clusters ^b		0.47		0.52		0.48
	Cluster composition		C _{2.3} H _{0.7} N _{1.0} O _{2.5}		C _{3.3} H _{0.6} N _{0.3} O _{2.6}		C _{2.3} H _{0.7} N _{1.3} O _{2.2}
	Total molecules		96		72		96

^a Number of atoms (% of system total) included in the above products. ^b Some small aggregates still exist at such high temperature and pressure conditions in the CJ state.

4. Summary and Conclusions

We propose the first-principles based ReaxFF Reactive Dynamics to CJ state protocol (Rx2CJ) to predict the thermochemical parameters at the CJ state characterizing a self-sustaining detonation wave in an energetic material. We applied Rx2CJ to three well-studied explosives (RDX, PETN and HMX) and to an H₂/O₂ mixture.

The predicted CJ detonation velocities are in good agreement with available experimental data: for RDX, HMX, and PETN, but systematically low by 4% to 7%. We consider that part of this modest error may arise because even after ~250 ps of the system evolution in the NVT simulation, a significant

number of carbon and oxygen atoms remains agglomerated in small carbonaceous clusters (0.47 mol/mol for RDX, 0.52 mol/mol for PETN, 0.48 mol/mol for β -HMX), while the typical reaction zone in detonation experiment is thought to be considerably longer (from nano- to microseconds). Thus, the carbon clusters may continue to burn off to form additional gases, leading to additional energy release hence a higher velocity.

Indeed, allowing the RDX system volume to expand isoentropically by a factor of 8 over an additional 100 ps, we observed the formation of additional CO and CO₂ gases.

We consider that these results validate the Rx2CJ method for first principles based predictions of performance properties for new propellants and explosive materials.

This Rx2CJ first principle based protocol for predicting the CJ point provides the matching point between first principles based atomistic reaction dynamics simulations and the macroscopic properties of detonation. Thus Rx2CJ can now be used for *in silico* predictions of the CJ state parameters as a measure of performance for *in silico* design of new materials, using it to assess proposed new high energy materials prior to the difficult task of their synthesis and characterization. This can be used to discover new higher performance energetic materials that might optimize energy release, sensitivity, and environmental impact.

Our Rx2CJ calculations also provide the detailed properties and products at the CJ point that could be used as input into for macroscale continuum simulations of explosives and propellants.

ACKNOWLEDGMENTS

This work was supported by the U.S. ONR ((N00014-12-1-0538, Dr. Cliff Bedford). It was also supported by the National Natural Science Foundation of China (Grant No. 11172044 and 11221202).

Notes and references

^a State Key Laboratory of Explosion Science and Technology, Beijing Institute of Technology, Beijing 100081, People's Republic of China.

^b Materials and Process Simulation Center, 139-74, California Institute of Technology, Pasadena, California 91125, USA.

* Corresponding author: email: wag@wag.caltech.edu.

1. P. J. Kortbeek, C. A. Ten Seldam and J. A. Schouten, *Mol. Phys.*, 1990, 69, 1001-1009.
2. Z. Duan, N. Møller and J. H. Weare, *Geochim. Cosmochim. Acta*, 1996, 60, 1209-1216.
3. B. M. Rice, W. Mattson, J. Grosh and S. F. Trevino, *Phys. Rev. E*, 1996, 53, 611-622.
4. M. Ross, *J. Chem. Phys.*, 1979, 71, 1567-1571.
5. G. Zerah and J. P. Hansen, *J. Chem. Phys.*, 1986, 84, 2336-2343.
6. L. E. Fried and W. M. Howard, *J. Chem. Phys.*, 1998, 109, 7338-7348.
7. J. H. Batteh and J. D. Powell, *Phys. Rev. B*, 1979, 20, 1398-1409.
8. B. L. Holian, W. G. Hoover, B. Moran and G. K. Straub, *Phys. Rev. A*, 1980, 22, 2798-2808.
9. J. J. Erpenbeck, *Phys. Rev. A*, 1992, 46, 6406-6416.
10. D. W. Brenner, D. H. Robertson, M. L. Elert and C. T. White, *Phys. Rev. Lett.*, 1993, 70, 2174-2177.
11. J. B. Maillet, M. Mareschal, L. Soulard, R. Ravelo, P. S. Lomdahl, T. C. Germann and B. L. Holian, *Phys. Rev. E*, 2000, 63, 016121.
12. J. D. Kress, S. Mazevet, L. A. Collins and W. W. Wood, *Phys. Rev. B*, 2000, 63, 024203.
13. A. K. Rappe, C. J. Casewit, K. S. Colwell, W. A. Goddard III and W. M. Skiff, *J. Amer. Chem. Soc.*, 1992, 114, 10024-10035.
14. W. Liu, S. V. Zybin, S. Dasgupta, T. M. Klapötke and W. A. Goddard III, *J. Amer. Chem. Soc.*, 2009, 131, 7490-7491.
15. Q. An, W. A. Goddard, III and T. Cheng, *Phys. Rev. Lett.*, 2014, 113, 095501.
16. A. Strachan, E. M. Kober, A. C. T. van Duin, J. Oxgaard and W. A. Goddard III, *J. Chem. Phys.*, 2005, 122, 054502.
17. A. C. T. van Duin, S. Dasgupta, F. Lorant and W. A. Goddard III, *J. Phys. Chem. A*, 2001, 105, 9396-9409.
18. L. Liu, Y. Liu, S. V. Zybin, H. Sun and W. A. Goddard III, *J. Phys. Chem. A*, 2011, 115, 11016-11022.
19. Q. An, S. V. Zybin, W. A. Goddard III, A. Jaramillo-Botero, M. Blanco and S. Luo, *Phys. Rev. B*, 2011, 84, 220101.
20. Q. An, W. A. Goddard III, S. V. Zybin, A. Jaramillo-Botero and T. Zhou, *J. Phys. Chem. C*, 2013, 117, 26551-26561.
21. D. Guo, Q. An, W. A. Goddard III, S. V. Zybin and F. Huang, *J. Phys. Chem. C*, 2014, 118, 30202-30208.
22. D. Guo, Q. An, S. V. Zybin, W. A. Goddard III, F. Huang and B. Tang, *J. Mater. Chem.*, 2015, 3, 5409-5419.
23. A. Strachan, A. C. T. van Duin, D. Chakraborty, S. Dasgupta and W. A. Goddard III, *Phys. Rev. Lett.*, 2003, 91, 098301.
24. L. Zhang, S. V. Zybin, A. C. T. van Duin, S. Dasgupta, W. A. Goddard III and E. M. Kober, *J. Phys. Chem. A*, 2009, 113, 10619-10640.
25. T. Zhou, H. Song, Y. Liu and F. Huang, *Phys. Chem. Chem. Phys.*, 2014, 16, 13914-13931.
26. T. Zhou, L. Liu, W. A. Goddard III, S. V. Zybin and F. Huang, *Phys. Chem. Chem. Phys.*, 2014, 16, 23779-23791.
27. J. K. Brennan and B. M. Rice, *Phys. Rev. E*, 2002, 66, 021105.
28. E. Bourasseau, V. Dubois, N. Desbiens and J. B. Maillet, *J. Chem. Phys.*, 2007, 127, 084513.
29. E. Bourasseau, J. B. Maillet, N. Desbiens and G. Stoltz, *J. Phys. Chem. A*, 2011, 115, 10729-10737.
30. L. E. Finger M, Helm FH, Hayes B, Hornig H, McGuire R, Kahara M, Guidry M presented in part at the 6th Syrup (International) on Detonation, Washington, DC 710, 1980.
31. C. L. Mader, ed. C. Press, University of California Press, Baca Raton London New York, 1979.
32. R. Zitoun, D. Desbordes, C. Gueraud and B. Deshaies, *Shock Waves*, 1995, 4, 331-337.
33. A. Piryatinski, S. Tretiak, T. Sewell, and S. McGrane, *Phys.*

Journal Name

34. *Rev. B* 2007, 75, 214306
R. Dawes, A. Haghighi, T. Sewell, and D. Thompson, *J. Chem. Phys.* 2009, 131, 224513
35. N. Goldman, E. Reed and L. Fried, *J. Chem. Phys.*, 2009, 131, 204103
36. T. Qi and E. Reed, *J. Phys. Chem. A*, 2012, 116, 10451-10459
37. D. L. Ornellas, ed. U. o. C. Lawrence Livermore Laboratory, Livermore, California, 1982, p. 39.
38. W. E. Deal, *J. Chem. Phys.*, 1957, 27, 796-800.
39. W. M. Evans, *Proc. R. Soc. London*, 1951, 204A, 12-17.
40. W. C. Davis, B. G. Craig and J. B. Ramsay, *Phys. Fluids*, 1965, 8, 2169-2182.
41. J. Kurrle, "HMX Detonation vs Density", Report OSAO No. 4148, SANL No. 901-003, 1971
42. V.V. Zhakhovsky, M. M. Budzevich, A.C. Landerville, I.I. Oleynik, and C. T.White, *Phys. Rev. E*, 2014, 90, 03331234.
43. Dobratz, B. M. Crawford, P. C. Lawrence Livermore National Laboratory: Livermore, CA, 1985.

Table of Contents

