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# A Comparative Computational Study on the Hydrogen Adsorption on the $\text{Ag}^+$ , $\text{Cu}^+$ , $\text{Mg}^{2+}$ , $\text{Cd}^{2+}$ , and $\text{Zn}^{2+}$ Cationic Sites in Zeolites<sup>†</sup>

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In this article the interaction between  $\text{H}_2$  and  $\text{Ag}^+$ ,  $\text{Cu}^+$ ,  $\text{Mg}^{2+}$ ,  $\text{Cd}^{2+}$ , and  $\text{Zn}^{2+}$  cations in cluster models of several sizes has been studied computationally. Depending on the changes imposed by the adsorption process on  $\text{H}_2$  molecule the activation can vary in wide range – from only slight weakening of H-H bond to complete dissociation of  $\text{H}_2$  molecule. The NOCV (Natural Orbitals for Chemical Valence) analysis allowed for decomposition of the electron density distortion into contributions easier for interpretation. Three essential factors have been identified (*i-iii*). In the case of bare cation the main contribution is a donation from  $\sigma_{\text{H}_2}$  to the cation (*i*). When zeolite framework surrounding the cation is introduced, it hinders  $\sigma$ -donation and enhances  $\pi$ -backdonation from the cation to antibonding orbital of the molecule (*ii*). For Cu(I) and Ag(I) sites  $\pi$ -backdonation becomes dominant while for Mg(II), Cd(II), and Zn(II) cations the  $\sigma$ -donation, albeit diminished, still remains a dominant contribution. Calculation showed that the localization and coordination of the Zn(II) have crucial influence on its interaction with  $\text{H}_2$ . We identified a  $\text{Zn}^{2+}$  position for which  $\text{H}_2$  molecule dissociates – here the interaction between  $\text{H}_2$  and oxygen framework (*iii*) plays crucial role. Based on the calculations the mechanism of  $\text{H}_2$  transformations has been proposed. Upon heterolytic dissociation of  $\text{H}_2$  the  $\text{Zn}^0$  moiety and two OH groups can be formed. Eventually, in two elementary steps  $\text{H}_2$  molecule can be restored. In this case, the ability of the site to activate/dissociate hydrogen is caused by low coordination number of zinc cation and the geometry of the site which allows positively charged  $\text{H}_2$  to interact with framework oxygen – it enhances formation of OH and  $\text{Z}-\text{O}-(\text{ZnH})^+$  groups.

## 1 Introduction

Hydrogen adsorption and activation are important for catalytic hydrogenation and other reactions involving hydrogen transfer, and, as such, are crucial for research concerning fuel cells or hydrogen storage,<sup>1-3</sup> to recall just a few processes. The zeolite cationic sites are known for activation of  $\pi$ -bonds<sup>4-12</sup> and also of  $\sigma$ -bonds, in, *i.e.*,  $\text{H}_2$ . Depending on the cationic site in MeMFI the adsorption energy and the  $\text{H}_2$  activation extent, measured by stretching red-shift, can vary in a wide range – from only slight weakening of H-H bond to the dissociation of  $\text{H}_2$  molecule. The MeMFI systems are also active in alkane/arene involving processes like dehydrogenation<sup>13</sup> and aromatization of light alkanes,<sup>14-17</sup> and also in alkylation processes.<sup>18</sup>

The low interaction energy (3 to 5 kcal/mol) between  $\text{H}_2$  and the zeolitic sites (*e.g.*,  $\text{Li}^+$ ,  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Mg}^{2+}$ ,  $\text{Ca}^{2+}$ ) drew attention of several scientific groups in the field of hydrogen storage.<sup>19-29</sup> However, hydrogen concentration in high-silica zeolites are much lower than the values acceptable for commercial use (*ca.* 6 % mass).

The aim of this article was to study the H-H activation properties of the sequence of cationic zeolite systems, and further study of the most active, which was found to be ZnMFI, and whose activity was also confirmed experimentally.<sup>16,30</sup> Besides  $\text{Zn}^{2+}$ , three other cations with  $d^{10}$  electron configuration,  $\text{Ag}^+$ ,  $\text{Cu}^+$ , and  $\text{Cd}^{2+}$ , have been chosen for the case study while  $\text{Mg}^{2+}$ , a non-transition cation, was used as the reference. In spite of the same configuration of the valence shell, the cations behave/interact with hydrogen in different ways. Although hydrogen is unusually strongly activated by CuMFI, it does not dissociate.<sup>27,31,32</sup> The process of hydrogen activation by the cation sites was studied by means of the ETS-NOCV analysis and the energetic contributions were obtained – donation, backdonation, and covalent, constituted a novel “geometric” descriptor,  $\Delta r_{\text{HH}}^{\text{NOCV}}$ , which was further correlated to the geometric parameter,  $\Delta r_{\text{HH}}$  (see *Results and discussion* section).

<sup>†</sup> Electronic Supplementary Information (ESI) available: [details of any supplementary information available should be included here]. See DOI: 10.1039/b000000x/

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In this context the H-H bond activation resembles that of C-H; indeed, the ZnMFI catalyst is also active toward methane or other alkanes.<sup>31,33–36</sup> The mono-<sup>37</sup> and dinuclear<sup>38,39</sup> zinc sites were considered to be active towards hydrogen molecule. In the work of Kazansky *et al.*<sup>40</sup> the heterolytic nature of two-site H<sub>2</sub> dissociation into cationic H<sup>+</sup> – O<sub>zeolite</sub> and anionic H<sup>–</sup> – Zn(II) is emphasised.

Zinc cation can coordinate to zeolite framework at various sites. Calculation showed that localization and coordination of the cation have crucial influence on the interaction between the cation and H<sub>2</sub> and at some sites H<sub>2</sub> dissociates upon adsorption.<sup>41</sup> Even though the localisation of copper and zinc cations in the MFI framework is similar, the H<sub>2</sub> activation properties are different. Shubin *et al.*<sup>42</sup> have considered the site for which the barrier for hydrogen dissociation is 10.5 kcal/mol, however, the experimental data<sup>43</sup> shows that H<sub>2</sub> dissociate spontaneously. We have considered the zinc sites which are active in spontaneous dissociation of hydrogen. According to the results of Shubin *et al.* the hydrogen atom is labile and can migrate in the zeolite framework easily, however, in the raised temperature the hydrogen atom bound to Zn<sup>2+</sup> ion can also migrate forming a second OH group.

In the present paper the mechanism for both spontaneous dissociation as well as for formation of Zn<sup>0</sup> and hydrogen desorption, being in good agreement with the model suggested by Oda<sup>43</sup>, is proposed. Surprisingly, even though the redox potential is positive for Cu and negative for Zn, the activation of hydrogen molecule on Zn site is much deeper (eventually leads to H<sub>2</sub> dissociation) rather than on Cu site. The pivotal issue of this article was to elucidate this phenomenon and thus to complement the article of Oda *et al.*<sup>43</sup> by qualitative justification of the hydrogen transformation in ZnMFI.

## Methodology

### Models

As models of cationic sites we used bare cations of copper(I), silver(I), magnesium(II), cadmium(II), and zinc(II) as well as these cations coordinated to [Al(OH<sub>4</sub>)]<sup>–</sup> anion (T1), or M7 frameworks, the latter composed of seven silica tetrahedra. Hydrogen molecule is bound side-on both with bare cations and with cation sites (see Fig. 1). For divalent exchanged cations the T8 and T11 (see Fig. 1 in the Supporting Information to recall the naming convention) positions of Al atoms was used, labelled S2 by Oda *et al.*,<sup>43</sup> whereas for monovalent cations one Al was introduced in the T7 position so that all the models are electrostatically neutral. The S2 model was chosen based on the conclusion<sup>43</sup> of higher energy barrier for H-H dissociation for S3 (attributed to the longer distance between Al atoms in S3 model compared to S2, which makes dissociation a less concerted and thus more energetically hindered process) and also the larger discrepancies between calculated and experimental wavenumbers. The S1 and S4 models were discriminated due to the closer distance between two Al atoms which causes excessive charge build-up repulsing the divalent zinc ion.

The hydrogen atoms of the terminating OH groups were placed along the O-T' bond (where T' is the next T site, replaced by H atom in this model) but at the distances of 0.9666 Å and 0.9628 Å in silicon or aluminium T site, respectively. The positions of these hydrogen atoms have been fixed to preserve the structure of the zeolite framework.

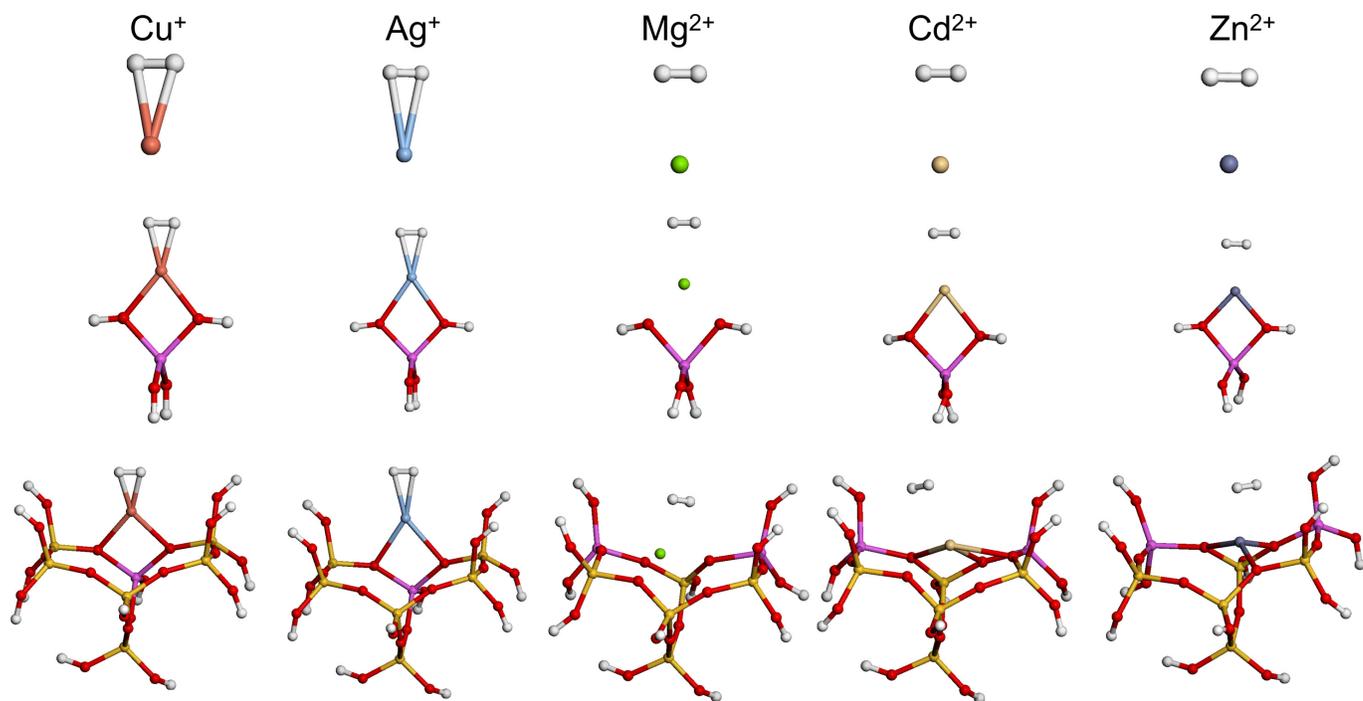


Fig. 1 Qualitative view of the discussed models.

### Computational details

Geometry optimization and vibrational analysis have been done with Turbomole package on the DFT B3LYP level of theory with def2-TZVP basis set.<sup>44</sup>

Even though the inclusion of dispersion interactions can improve the total SCF energy values it is not necessarily the case when the relative energies (*i.e.*, for barriers) are studied. In fact, Lochan *et al.*<sup>45</sup> discuss the importance of the contributions to the total binding energies (electrostatic, dispersion, and orbital interactions) for the H-storage materials like MOFs, dehydrated Prussian blue analogues or others. They emphasise that in the studied systems it is the orbital energy that plays the decisive role in the selection of the elementary steps. To verify the applicability of that statement in the system studied in this article the DFT+D<sup>46</sup> computations were redone and it was concluded that even though the total ESCF indeed changed significantly (a few tens of kcal/mol), the binding and barrier energies changed only by  $\leq 4$  and  $\leq 0.4$  kcal/mol, respectively, upon inclusion of the dispersion forces, even though the full geometry re-optimisation was performed. However, to be able to compare our results to those obtained by Oda the non-D energies are presented hereafter. The set of DFT+D *vs.* DFT energies for the first 7 structures (5 minima and two TS) are summarised in the ESI.

The difference between electron density of the composed system and the sum of densities of non-interacting fragments in the geometries of the complex (deformation density  $\Delta\rho$ ) is represented by deformation density matrix  $\Delta\mathbf{P}$ . The Natural Orbitals for Chemical Valence (NOCV) are defined as the eigenvectors,  $\psi_i$  (expressed in the orthogonalized basis set of  $N$  fragment molecular orbitals  $\phi_j$ ), diagonalizing deformation density matrix,  $\Delta\mathbf{P}$ :  $\Delta\mathbf{P}\mathbf{C}_i = \lambda_i\mathbf{C}_i$ , where  $\mathbf{C}_i$  is a vector of the coefficients in the basis  $\phi_j$ , and  $\lambda_i$  is the  $i$ -th eigenvalue, a descriptor for the number of electrons transferred along selected channel. Deformation density can be expressed as a sum of pairs of ordered complementary orbitals ( $\lambda_{-k}$ ,  $\lambda_k$ ) corresponding to eigenvalues equal to the absolute value, but with opposite signs<sup>47-50</sup> defining independent density transfer channels ( $\Delta\rho_k$ ):

$$\Delta\rho(r) = \sum_{k=1}^{N/2} \lambda_k [-\psi_{-k}^2(r) + \psi_k^2(r)] = \sum_{k=1}^{N/2} \Delta\rho_k(r) \quad (1)$$

The NOCV decomposition of the differential density given by Eq. 1 may be linked to Ziegler-Rauk energy decomposition approach (Extended-Transition-State, ETS).<sup>51</sup> Total interaction energy between two fragments may be decomposed, according to ETS, into the following terms:  $\Delta E_{\text{total}} = \Delta E_{\text{dist}} + \Delta E_{\text{Pauli}} + \Delta E_{\text{elstat}} + \Delta E_{\text{orb}}$ . The distortion energy,  $\Delta E_{\text{dist}}$ , is the energy needed

to change the geometry of non-interacting fragments to that in the complex. The Pauli term,  $\Delta E_{\text{Pauli}}$ , is associated with repulsion of closed shells of fragments. The electrostatic component,  $\Delta E_{\text{elstat}}$ , is an energy of interaction between electron densities on both fragments (promolecules). The orbital term,  $\Delta E_{\text{orb}}$ , is an orbital interaction energy of the fragments, including inter- and intrafragment polarization. By applying ETS-NOCV method the last term ( $\Delta E_{\text{orb}}$ ), describing the part of adsorption energy due to direct electronic interactions, was decomposed into contributions corresponding to independent electron transfer channels spanning deformation electron density. The ETS-NOCV analysis has been performed with partition of the system into two fragments: the hydrogen molecule, and the rest of the system, a free or embedded cation.

Additionally, for zinc site the conceivable paths of hydrogen transformation were analysed. The optimized zinc sites, however, turned out to be inactive toward hydrogen dissociation hence the dissociation product structure ( $Z - O - (\text{ZnH})^+$  and  $Z - \text{OH}$  groups) was optimised instead. After having moved H atoms together the resultant  $\text{H}_2$  departed the system leaving the  $\text{Zn}^{2+}$  cation in the position where it was active in  $\text{H}_2$  decomposition.

Since it was experimentally showed that at raised temperature the  $Z - O - (\text{ZnH})^+$  and  $Z - \text{OH}$  groups transform into two  $Z - \text{OH}$  groups and  $\text{Zn}^0$ , and at even higher temperature the restoration of  $\text{H}_2$  is observed,<sup>43</sup> the direct process of H-H association was studied by bringing H atoms (of  $Z - \text{OH}$  groups) together but in such scheme the  $\text{H}_2$  molecule was not restored but rather one of H atoms formed a bond with  $\text{Zn}^0$ . The different scheme, commenced by the restoration of  $Z - O - (\text{ZnH})^+$  and  $Z - \text{OH}$  groups, lead, however, to forming the  $\text{H}_2$  molecule. It can be rationalised by the opposite partial charges accumulated on H atoms. It was not the case for the previous mechanism, where both H atoms in OH groups were positively charged, and hence the restoration of  $\text{H}_2$  was not feasible.

The forming/breaking bond in the elementary steps was scanned by means of the routine LST/QST (own extension to the QMPot code<sup>52,53</sup>) procedure and the resulting TS guess was optimised (Powell update of the Hessian) with constrained proper Hessian curvature. The optimised TS was eventually verified by the harmonic vibrational analysis.

## Results and discussion

### Hydrogen activation on bare cations, and T1 and M7 sites

The values of H-H bond elongation and stretching frequency red-shift, with respect to the gas phase hydrogen molecule, are given in Fig. 1 as the measures of the extent of activation. Bond length is related to calculated value for free molecule (0.744 Å, while experimental values is 0.741 Å<sup>54</sup>). The red-shifts are calculated as the differences between the calculated harmonic frequency for  $\text{H}_2$  of 4418  $\text{cm}^{-1}$ , close to the experimental harmonic frequency of 4401  $\text{cm}^{-1}$ .<sup>54</sup> Experimental frequency value for para- $\text{H}_2$  (4161  $\text{cm}^{-1}$ ) is taken as the reference for experimental shifts.<sup>55</sup> Hydrogen molecule adsorbed on Brønsted acid or sodium sites exhibit red-shift of *ca.* 60  $\text{cm}^{-1}$ <sup>37,56</sup> while the values for hydrogen interacting with free silver and copper cations are 8-10 times higher.<sup>37,57</sup>

**Table 1** The measures of H-H bond activation –  $\Delta r_{\text{HH}}$ ,  $\Delta\nu$ , and  $\Delta E_{\text{total}}$ .

Model label	Model	Coord number	$r_{\text{MH}}$ /Å	$\Delta r_{\text{HH}}$ /pm	$\Delta\nu$ / $\text{cm}^{-1}$	$\Delta E_{\text{total}}$ / $\text{kcal} \cdot \text{mol}^{-1}$
a	$[\text{AgH}_2]^+$	0	2.04	3.1	–442	–10.0
b	$[(\text{T1})\text{AgH}_2]^0$	2	1.77	5.1	–769	–11.3
c	$[(\text{M7})\text{AgH}_2]^0$	2	1.93	3.6	–506	–6.4
d	$[\text{CuH}_2]^+$	0	1.77	4.2	–600	–22.6
e	$[(\text{T1})\text{CuH}_2]^0$	2	1.61	7.7	–1133	–23.8
f	$[(\text{M7})\text{CuH}_2]^0$	2	1.65	6.1	–502	–13.9
g	$[\text{MgH}_2]^{2+}$	0	2.04	3.7	–484	–24.6
h	$[(\text{T1})\text{MgH}_2]^+$	2	2.12	1.5	–197	–10.2
i	$[(\text{M7})\text{MgH}_2]^+$	2	2.03	1.1	–149	–4.1
j	$[\text{CdH}_2]^{2+}$	0	2.14	3.2	–407	–26.2
k	$[(\text{T1})\text{CdH}_2]^+$	2	2.10	3.0	–421	–11.5
l	$[(\text{M7})\text{CdH}_2]^+$	3	2.29, 2.44	2.2	–350	–4.9
m	$[\text{ZnH}_2]^{2+}$	0	1.88	7.8	–967	–44.1
n	$[(\text{T1})\text{ZnH}_2]^+$	2	1.89	3.3	–454	–16.7
o	$[(\text{M7})\text{ZnH}_2]^+$	4	2.14	1.3	–182	–3.6
p	$[(\text{M7})\text{ZnH}_2]^0$	3	2.03, 2.14	2.5	–373	–4.5

Both  $\Delta r_{\text{HH}}$  and  $\Delta\nu_{\text{HH}}$  vary significantly among the hydrogen molecules interacting with discussed cations (Table 1). Calculated red-shifts and H-H bond elongations are well correlated (Fig. 2). The slope of linear fit equals to  $-132 \pm 5 \text{ cm}^{-1} \cdot \text{pm}^{-1}$ . Experimental wavenumbers are easier to measure than bond length thus the dependence of  $\Delta\nu_{\text{HH}}$  vs.  $\Delta r_{\text{HH}}$  allows for a quick estimation of the calculated hydrogen activation measure in case where IR data are available. It is especially useful for evaluating large models where vibrational analysis becomes prohibitively time consuming. It could also be potentially used for estimation of CO wavenumber as for some acidic and hard cationic zeolite sites the red-shift for  $\text{H}_2$  is a doubled value for CO:  $\Delta\nu_{\text{HH}} \approx 2\Delta\nu_{\text{CO}}$ .<sup>55,58</sup>

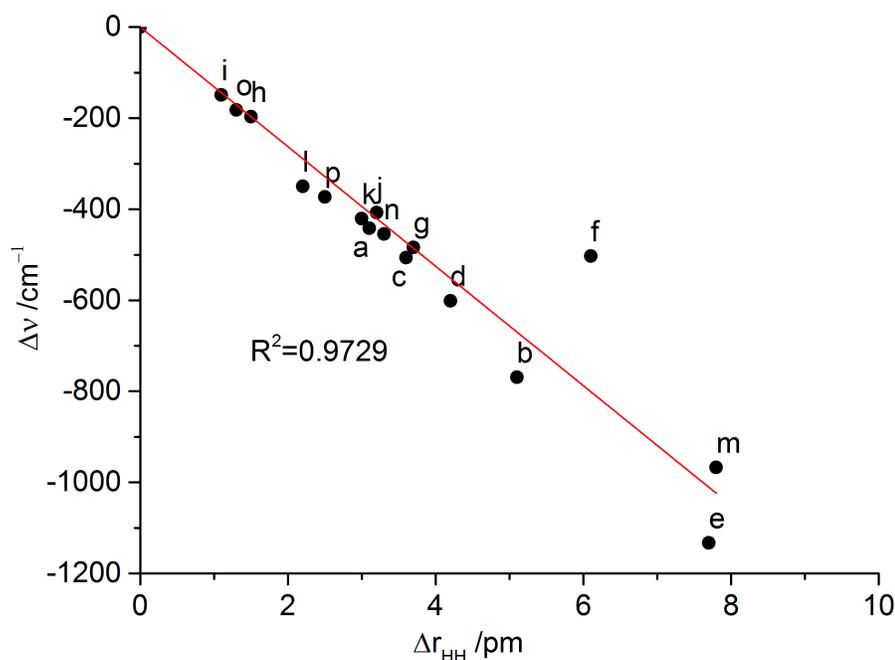


Fig. 2 Correlation between H-H bond elongation ( $\Delta r_{\text{HH}}$ ) and IR red-shift ( $\Delta \nu_{\text{HH}}$ ) cationic MFI sites. Labelling refers to Table 1.

The IR red-shift of H-H bond resulting from the interaction between hydrogen molecule and studied cation sites are in relatively wide range – from  $-149 \text{ cm}^{-1}$  for magnesium site to  $-1133 \text{ cm}^{-1}$  for copper site. Comparing the activation effect for bare cations and those surrounded by zeolite framework it can be concluded that for Ag(I) and Cu(I) the zeolite framework enhances the activation while for Mg(II), Cd(II), and Zn(II) is conversely. Calculated interaction energy ( $\Delta E_{\text{total}}$ ) is a measure of the strength of the hydrogen molecule bonding. However, it does not refer directly to the activation process. Indeed, for Mg(II), Cd(II), and Zn(II) the stronger interaction leads to the more efficient activation but it does not hold always. Contrary to  $\Delta E_{\text{total}}$ , the orbital interaction energy of the systems,  $\Delta E_{\text{orb}}$ , is well correlated with elongation of H-H bond (see Fig. 2). It implies that the activation is mainly determined by populating or depopulating the hydrogen molecule orbitals. It has also been previously stated<sup>45</sup> that in the case of hydrogen the orbital interaction energy, rather than electrostatic or dispersion contributions, is crucial for reproducing the substantial part of energy of interaction with host materials. In the copper containing zeolites some  $\text{Cu}^{2+}$  cations undergo autoreduction forming  $\text{Cu}^+$  cations while the rest of them remain in the original oxidation state and both constitute adsorption centres for hydrogen. For that reason, even though the  $\text{Cu}^{2+}$  cation, having  $d^9$  configuration, is the open-shell system, contrary to those discussed in this article, we have performed analogous computation (see SI). For the  $\text{Cu}^{2+}$  cation, despite it having unpaired electron, the spin density does not change upon interaction with hydrogen molecule and this interaction resembles that for Mg(II), Cd(II), and Zn(II).

**Table 2** Elongation of H-H bond ( $\Delta r_{\text{HH}}$ ), orbital interaction energy ( $\Delta E_{\text{orb}}$ ), its contributions:  $\sigma$ -donation ( $\Delta E_{\text{orb}}^{\text{don}}$ ), covalent component ( $\Delta E_{\text{orb}}^{\text{coval}}$ ),  $\pi$ -backdonation ( $\Delta E_{\text{orb}}^{\text{bdon}}$ ), and respective NOCV charge transfer estimates ( $\lambda^i$ ). Empty cells denote negligible values.

Model	Coordinate number	$\Delta r_{\text{HH}}/\text{pm}$	$\Delta E_{\text{orb}}/\text{kcal} \cdot \text{mol}^{-1}$	$\sigma$ -donation		Covalent component	$\lambda^{\text{coval}}$	$\pi$ -backdonation	
				$\Delta E_{\text{orb}}^{\text{don}}$	$\lambda^{\text{don}}$			$\Delta E_{\text{orb}}^{\text{bdon}}$	$\lambda^{\text{bdon}}$
[AgH <sub>2</sub> ] <sup>+</sup>	0	3.1	-15.3	-10.7	0.27	-2.7	0.11	-1.4	0.09
[(T1)AgH <sub>2</sub> ] <sup>0</sup>	2	5.1	-29.9	-8.7	0.25	-8.6	0.18	-10.8	0.28
[(M7)AgH <sub>2</sub> ] <sup>0</sup>	2	3.6	-15.5	-5.6	0.20	-5.1	0.15	-3.8	0.16
[CuH <sub>2</sub> ] <sup>+</sup>	0	4.2	-27.3	-16.0	0.36	-7.2	0.19	-3.7	0.16
[(T1)CuH <sub>2</sub> ] <sup>0</sup>	2	7.7	-37.2	-11.4	0.29	-9.9	0.21	-14.6	0.33
[(M7)CuH <sub>2</sub> ] <sup>0</sup>	2	6.1	-28.8	-9.6	0.26	-8.7	0.19	-10.0	0.27
[MgH <sub>2</sub> ] <sup>2+</sup>	0	3.7	-25.7	-25.6	0.37				
[(T1)MgH <sub>2</sub> ] <sup>+</sup>	2	1.5	-11.2	-9.8	0.23				
[(M7)MgH <sub>2</sub> ] <sup>+</sup>	2	1.1	-7.4	-6.1	0.18				
[CdH <sub>2</sub> ] <sup>2+</sup>	0	3.2	-28.4	-27.4	0.42				
[(T1)CdH <sub>2</sub> ] <sup>+</sup>	2	3.0	-11.2	-11.6	0.29				
[(M7)CdH <sub>2</sub> ] <sup>+</sup>	3	2.2	-11.6	-10.4	0.26				
[ZnH <sub>2</sub> ] <sup>2+</sup>	0	7.8	-46.9	-44.4	0.52	-4.0	0.05		
[(T1)ZnH <sub>2</sub> ] <sup>+</sup>	2	3.3	-21.9	-15.6 -1.0*	0.33 0.08*			-5.3	0.08
[(M7)ZnH <sub>2</sub> ] <sup>0</sup>	3	2.5	-15.7			-12.7 <sup>#</sup>	0.30		

\* –  $\sigma$ -backdonation

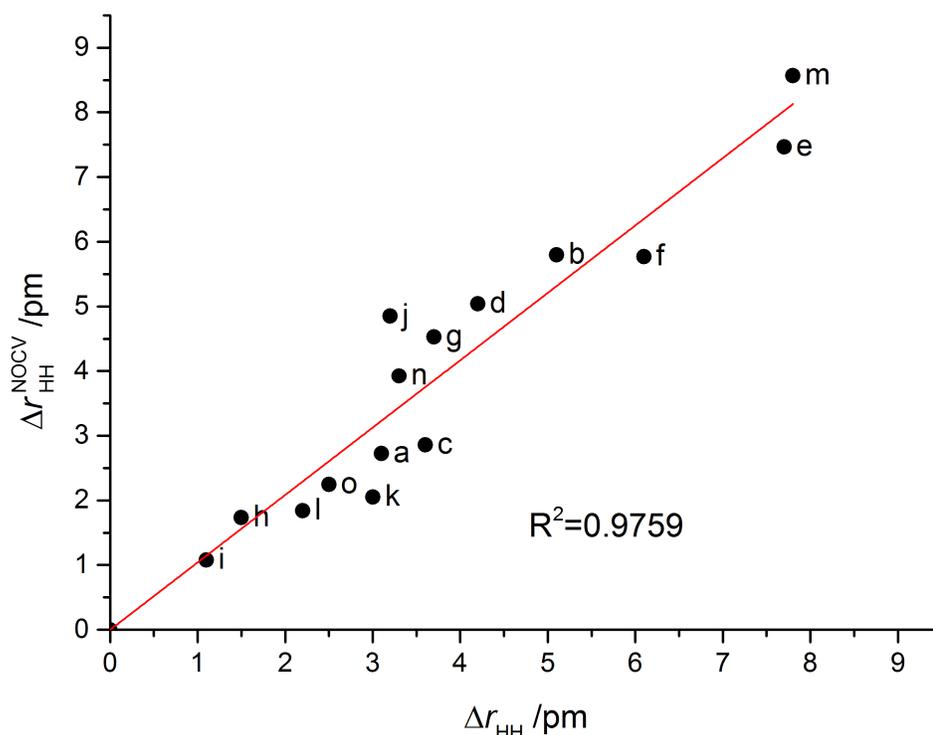
<sup>#</sup> – with admixture of interaction between framework oxygen and H<sub>2</sub> molecule, see Fig. 6.

Much more detailed information on the interaction between H<sub>2</sub> and cation sites is delivered by the NOCV analysis. Using it the deformation density ( $\Delta\rho$ ) is decomposed into a few contributions,  $\Delta\rho_k$ , which are easier for interpretation. The eigenvalues  $\lambda^i$  estimate the number of electrons transferred in the channels  $\Delta\rho_k$ . Moreover, the ETS-NOCV analysis delivers components of orbital interaction energy,  $\Delta E_{\text{orb}}^i$ , relevant for electron density transfer channels  $\Delta\rho_k$ . These values give the information on the importance of each contribution to the deformation density. In all cases the significant contribution can be attributed to one of three channels: (i) donation from  $\sigma(\text{H-H})$  to s orbital of the cation ( $\Delta E_{\text{orb}}^{\text{don}}$ ), (ii) polarization toward the bonding region (donation to bonding H<sub>2</sub> – M space with depopulation of  $\sigma_{\text{H}_2}$  and  $d_{z^2}$  orbitals),  $\Delta E_{\text{orb}}^{\text{coval}}$ , (iii) backdonation from  $d_{\pi}$  orbitals to  $\sigma_{\text{H}_2}^*$  antibonding orbital,  $\Delta E_{\text{orb}}^{\text{bdon}}$ . All the contribution weaken the H-H bond and the second term, (ii), is also responsible for valence bonding between the hydrogen and the site. The (i) and (ii) contributions represent depopulation of the bonding orbitals while the (iii) contribution represents population of antibonding orbitals. The Analogous analysis for Cu<sup>+</sup> and Na<sup>+</sup> has been done by X. Solans-Monfort *et al.* by selectively deleting fragment virtual orbitals.<sup>26</sup> The authors also report the effect of favouring the charge transfer from Cu<sup>+</sup> ( $3d_{\pi}$ ) orbital to the H<sub>2</sub> ( $\sigma^*$ ). However, the NOCV method reveals even stronger influence of zeolite on backdonation. Thus in the next step we focused on the semi-quantitative analysis of the impact of each contribution to orbital interaction energy on hydrogen activation.

Having  $\Delta E_{\text{orb}}$  decomposed, it is possible to determine the importance of particular contribution to hydrogen activation. The following equation has been optimized to reproduce calculated elongation of H-H bond:

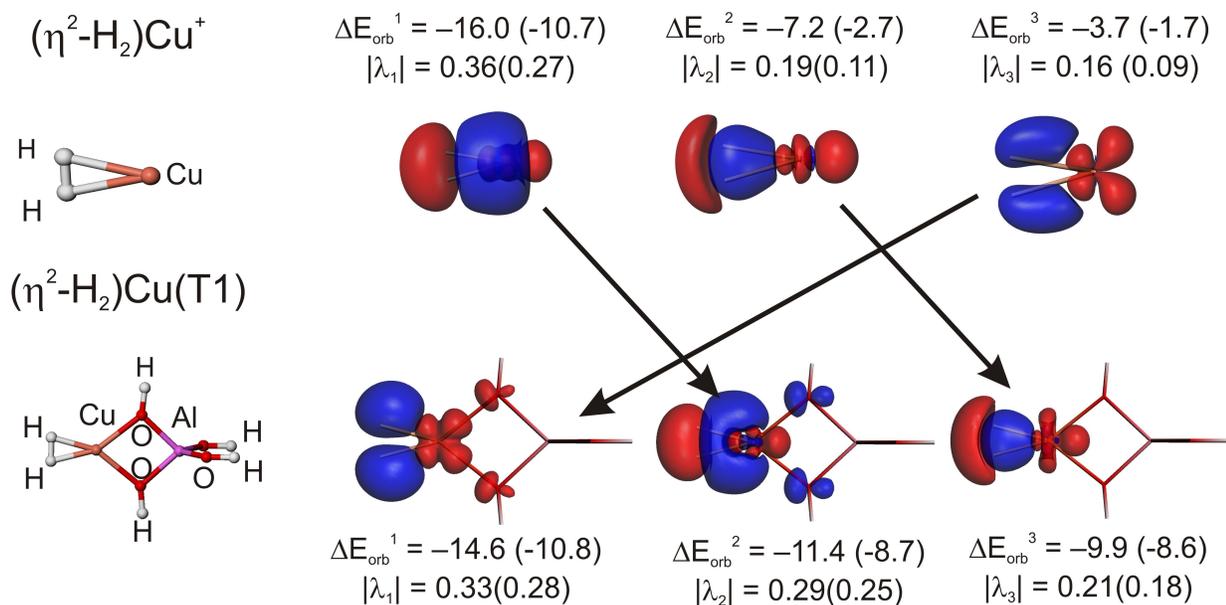
$$\Delta r_{\text{HH}}^{\text{NOCV}} = c \left[ \alpha \cdot \Delta E_{\text{orb}}^{\text{bdon}} + (1 - \alpha) \left( \Delta E_{\text{orb}}^{\text{don}} + \Delta E_{\text{orb}}^{\text{coval}} \right) \right] \quad (2)$$

The contributions to orbital interaction energy, taken with optimized coefficients  $c$  and  $\alpha$ , reproduced calculated H-H bond elongation well (Fig. 3). The coefficient  $\alpha = 0.59$  indicates that backdonation processes have stronger impact on the adsorbed hydrogen molecule than those connected with depopulation of bonding orbitals ( $1 - \alpha = 0.41$ ) — the ratio between the respective values is approximately like 3 to 2. Despite the fact that the contributions to orbital interaction energy vary in a wide range (often some of them are absent), the linear dependency is preserved what confirms that orbital interaction is an important factor in the process of the hydrogen molecule activation. It can be also inferred that the  $\alpha$  coefficient is relatively universal (at least for a given molecule).

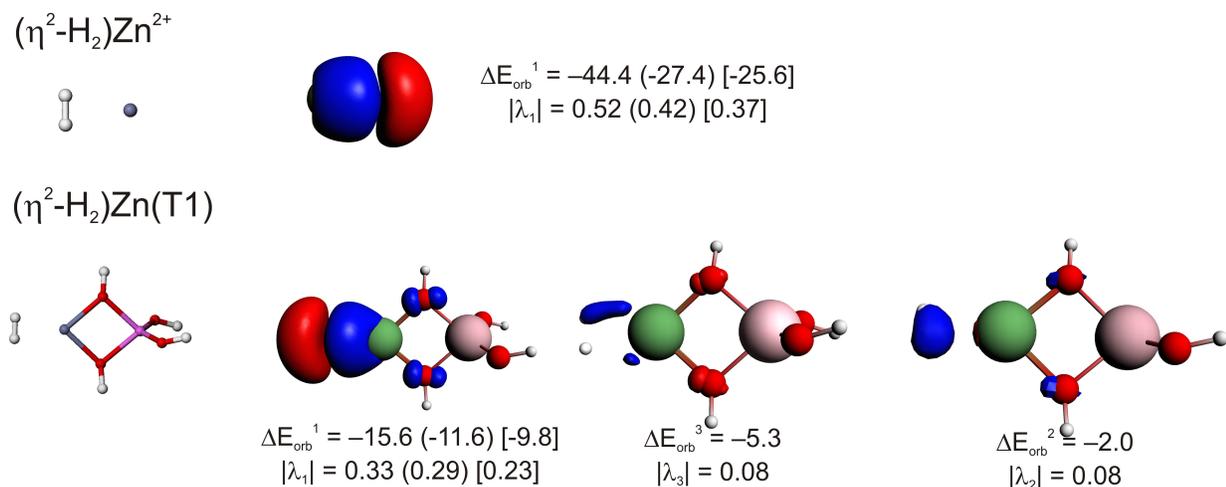


**Fig. 3** H-H bond elongation calculated from contributions to orbital interaction energy ( $\Delta r_{\text{HH}}^{\text{NOCV}}$ ) vs. calculated wave numbers ( $\Delta r$ ). Labelling refers to 1.

The influence of the zeolite oxygen atoms can be elucidated from the results obtained for the systems with or without zeolite framework. When the cation is surrounded by the zeolite framework, the latter opposes  $\sigma$ -donation and enhances  $\pi$ -backdonation from the cation to antibonding orbital of the molecule. It holds for all cases studied and is apparently the result of interaction between the cations and free electron pairs of framework oxygen atoms. The less positively charged cations have lower ability to accept electrons while they are more efficient donors. Although cations are partially neutralized, only some of them exhibit significant ability as  $\pi$ -donors. These are Cu(I) and Ag(I) sites for which  $\pi$ -backdonation becomes dominating (see Fig. 4), while for Mg(II), Cd(II) and Zn(II)  $\sigma$ -donation, although diminished, still remains a dominant contribution (Fig. 5). Depending on the cation, for symmetric site-on adsorption, one of the channels determines the activation – either  $\pi$ -backdonation or  $\sigma$ -donation.



**Fig. 4** Contribution to deformation electron density for  $[(\text{T1})\text{CuH}_2]^0$  together with the corresponding orbital interaction energy contributions ( $\Delta E_{\text{orb}}^i/\text{kcal} \cdot \text{mol}^{-1}$ ) and NOCV charge transfer estimates ( $\lambda_i$ ). Data in parentheses for  $\text{Ag}^+$ , red (light grey) – density outflow, blue (dark grey) – density inflow (contour value 0.001 a.u., colour figures on-line).

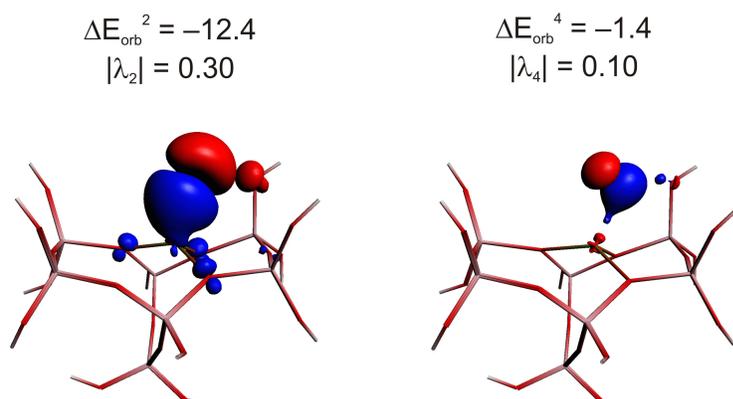


**Fig. 5** Contribution to deformation electron density for  $[(\text{T1})\text{ZnH}_2]^+$  together with the corresponding orbital interaction energy contributions ( $\Delta E_{\text{orb}}^i/\text{kcal} \cdot \text{mol}^{-1}$ ) and NOCV charge transfer estimates ( $\lambda_i$ ). Data in parentheses for  $\text{Cd}^{2+}$ , data in square brackets for  $\text{Mg}^{2+}$ , red (light grey) – density outflow, blue (dark grey) – density inflow (contour value 0.001 a.u., colour figures on-line).

In the models described above the zeolite framework binds the cations, delivers electrons to them, but does not interact with hydrogen molecule directly. Expanding the model to M7 the modes of adsorption remain the same for all systems but  $[(\text{M7})\text{ZnH}_2]^0$  and  $[(\text{M7})\text{CdH}_2]^0$ , in which hydrogen molecule is not adsorbed symmetrically – the distance between the cation and hydrogen atoms are different. It is caused by the interaction between positively charged hydrogen and framework oxygen atoms in its vicinity what is visible in the Fig. 6. Electron density flows mainly from  $\sigma$ -orbital of  $\text{H}_2$  molecule to bonding area between  $\text{Zn}^{2+}$  cation and the adsorbed molecule. Moreover, framework oxygen donates electrons from its lone pair. As a

result, the H<sub>2</sub> molecule is polarized and it is reflected in the second contribution to deformation density. The H<sub>2</sub> molecule is not dissociated and H atoms are not equivalent – one is in its half way to form Zn-H bond and the second is to form the OH group. The whole system adapts a transition state-like geometry.

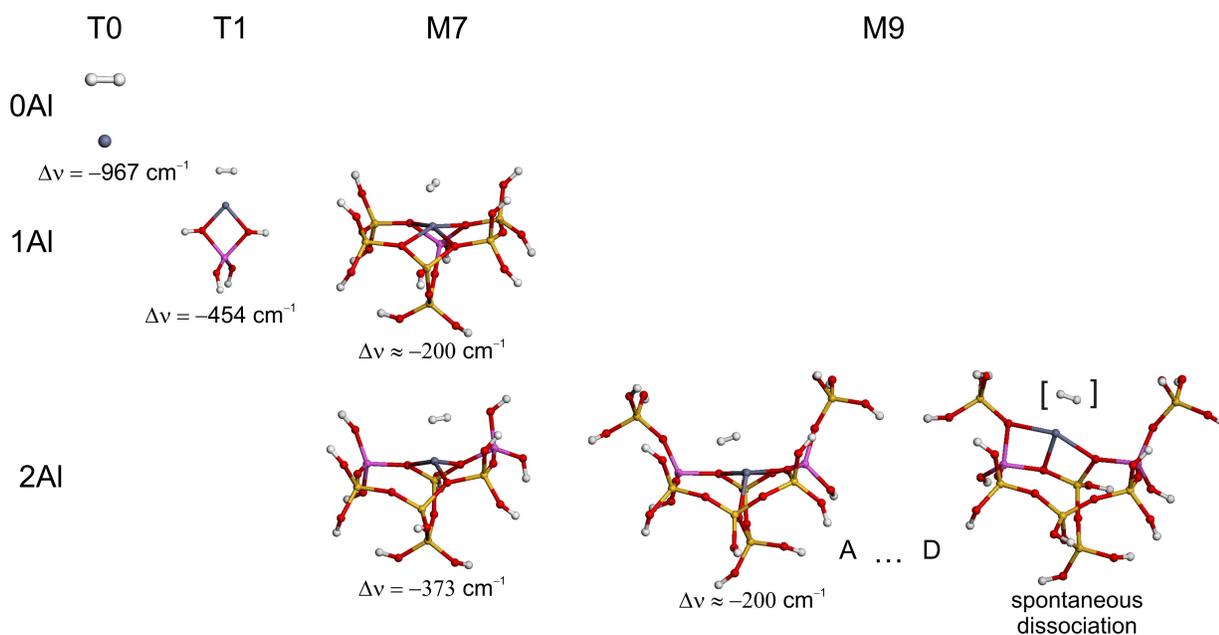
Even though the M7 model brought fruitful observation on how hydrogen interacts with the zinc site, further extension of the model by additional two tetrahedra was necessary (M9 model) having realised that the crucial oxygen atom is linked to hydrogen terminating model.



**Fig. 6** Contribution to deformation electron density for [(M7)ZnH<sub>2</sub>]<sup>0</sup> together with the corresponding orbital interaction energy contributions ( $\Delta E_{\text{orb}}^i/\text{kcal} \cdot \text{mol}^{-1}$ ) and NOCV charge transfer estimates ( $\lambda_i$ ). Red (light grey) – density outflow, blue (dark grey) – density inflow (contour value 0.001 a.u., colour figures on-line).

### Transformation of hydrogen on Zn<sup>2+</sup> zeolite sites

Concerning zinc sites several models of the certain range of size and for 0 to 2 aluminium atoms (Fig. 7) were studied. Even in the same model zinc cation can form differently coordinated sites in the zeolite framework. In the Table 3 the models for zinc site are listed with relative energy, elongation of H-H bond, and population analysis.



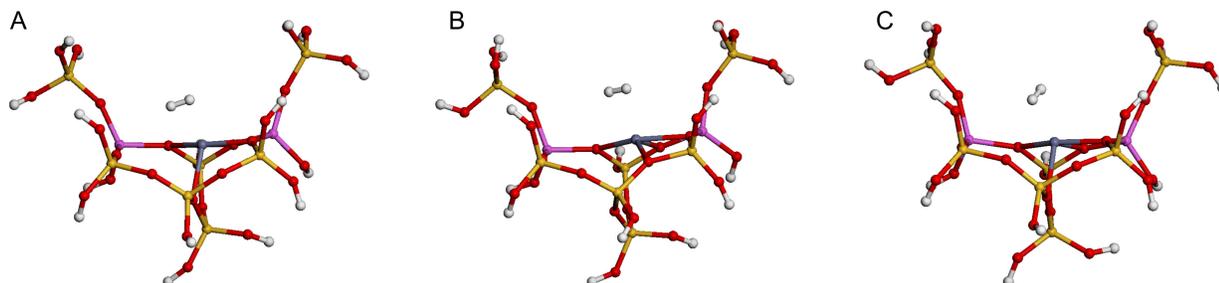
**Fig. 7** IR peak shifts for studied models.

**Table 3** Adsorption energies ( $\Delta E_{\text{ads}}$ ), H-H bond elongation ( $\Delta r_{\text{HH}}$ ) and Mulliken population analysis for hydrogen on Zn site models

Model	$\Delta E_{\text{ads}} /$ ( $\text{kcal} \cdot \text{mol}^{-1}$ )	$r_{\text{MH}} / \text{\AA}$	$r_{\text{MO}} / \text{\AA}$	$\Delta r_{\text{HH}} /$ pm	$q_{\text{Zn}} /  e $	$q_{\text{H}_A} /  e $	$q_{\text{H}_B} /  e $	$q_{\text{Z}} /  e $
$[\text{ZnH}_2]^{2+}$	-44.1	1.88	–	7.8	1.50	0.25	0.25	–
$[(\text{T1})\text{ZnH}_2]^+$	-16.7	1.89	1.87; 1.87	3.3	0.75	0.15	0.15	-0.05
$[(\text{M7})\text{ZnH}_2]^+$	-3.6	2.14	2.06; 2.06; 2.19; 2.23	1.3	0.80	0.08	0.06	+0.06
$[(\text{M7})\text{ZnH}_2]^0$	-4.5	2.03; 2.14	2.02; 2.07; 2.09	2.5	0.80	0.03	0.14	-0.97
$[(\text{M9})\text{ZnH}_2]$ A	-4.0	2.12	2.03; 2.05; 2.14; 2.18	1.4	0.86	0.08	0.05	-0.99
$[(\text{M9})\text{ZnH}_2]$ B	-5.1	2.12	2.03; 2.03; 2.15; 2.18	1.4	0.91	0.09	0.04	-0.94
$[(\text{M9})\text{ZnH}_2]$ C	-3.3	2.12	2.07; 2.12; 2.13; 2.21	1.4	0.88	0.12	0.04	-1.04
$[(\text{M9})\text{ZnH}_2]$ D *	-41.4	1.53	1.90	dissoc.	0.46	0.31	-0.05	-0.72

\* – structure labelled as **2** in the further part of the text

Among bare cations, zinc activates the H-H bond to the largest extent,  $\Delta\nu = -967 \text{ cm}^{-1}$ . Indeed, the contribution to orbital interaction energy attributed to  $\sigma$ -donation is  $-44 \text{ kcal} \cdot \text{mol}^{-1}$  – the zinc cation has the greatest acceptor properties among analysed ones and the Mulliken population analysis indicates its withdrawal of 0.5 e from hydrogen molecule. Upon coordination by alumina tetrahedron (T1) the  $\sigma$ -donation channel is diminished and also hydrogen activation is weaker. The Mulliken analysis shows that in this case 0.3 e is transferred from hydrogen molecule to zinc site which is additionally partly neutralised by T1 – it gains a total of 0.95 e. For M7 cluster with one aluminium atom the zinc cation is four-fold coordinated and the red-shift is as low as  $-182 \text{ cm}^{-1}$  and only 0.14 |e| is taken from hydrogen. The extent of the activation is strongly correlated with coordination number as for M7 cluster with two aluminium atoms zinc cation is coordinated to three oxygen atoms and the red-shift falls between those for two-fold and four-fold coordinated zinc cations. For M7 cluster with two aluminium atoms the hydrogens are in different distance from zinc cation presenting the distorted side-on mode of adsorption. As the result, the hydrogen molecule is polarized – one H atom has charge  $q/|e| = +0.03$  while the other has  $q/|e| = +0.14$  – see also Fig. 6. It is caused by the interaction between positively charged hydrogen and framework oxygen atom. This oxygen atom is linked to terminating hydrogen of the M7 cluster and hence is poorly represented in the relatively small M7 structure. Thus the system has been extended by another two tetrahedra, as mentioned above, yielding the larger cluster, M9, for which two stable zinc cation localizations were found. On the more stable site in M9, not active toward hydrogen dissociation, three modes of adsorption were found (Fig. 8). The analogous modes, with geometries and red-shifts very close to ours, have been studied by Shubin *et al.*,<sup>42</sup> who found the dissociation and diffusion pathway with energy barriers of  $\sim 10 \text{ kcal} \cdot \text{mol}^{-1}$ , relatively very small comparing to the hydrogen dissociation energy of  $104 \text{ kcal} \cdot \text{mol}^{-1}$ .<sup>54</sup>

**Fig. 8** Modes of  $\text{H}_2$  adsorption on ZnM9 site.

In all these modes the H-H bond is elongated by only 1.4 pm and the red-shifts remain in the range of  $-196 \text{ cm}^{-1}$  to

$-201\text{ cm}^{-1}$  thus only slight activation is observed. However, the  $\text{H}_2$  molecule dissociates spontaneously on the second type of zinc site. According to EXAFS experiment,<sup>43</sup> zinc cation in such active site is three-fold coordinated. On the basis of calculations, we found two active, almost equivalent, zinc positions – structures **1** and **8** presented in Fig. 9. Calculations confirmed the activity of these zinc sites toward spontaneous hydrogen dissociation. The mechanism of  $\text{H}_2$  transformation has been proposed in Fig. 9. The IR measurements identified absorption bands corresponding to  $(\text{ZnH})^+$  stretching mode at  $1933\text{ cm}^{-1}$  and the OH group band at  $3615\text{ cm}^{-1}$ .<sup>43</sup> The structure **2** shows the product of hydrogen molecule dissociation upon adsorption on the site **1**. Vibrational analysis for the former structure gives the wavenumbers of  $1907\text{ cm}^{-1}$  and  $3570\text{ cm}^{-1}$  which reasonably match the experimental ones and also the computational results of Oda *et al.* (*op. cit.*),  $1922\text{ cm}^{-1}$  and  $3656\text{ cm}^{-1}$ , respectively. The Mulliken population analysis gives the charge  $q/|e| = +0.31$  for one hydrogen, the value typical for OH groups, while for the other  $q/|e| = -0.05$ , what indicates the slight hydride type of that hydrogen.

Upon heterolytic dissociation of  $\text{H}_2$  the  $\text{Zn}^0$  moiety can be formed together with two OH groups (structure **4**). Calculated wavenumbers for these OH groups are equal to  $3287\text{ cm}^{-1}$  and  $3580\text{ cm}^{-1}$ . It is observed experimentally as increasing of IR band intensity at  $3615\text{ cm}^{-1}$  and also by DRIFT UV spectroscopy (absorption peaks in the range of  $42000\text{ cm}^{-1}$  and  $47000\text{ cm}^{-1}$  are assigned to  $\text{Zn}^0$ ).<sup>43</sup> The Mulliken charges are consistent with this interpretation yielding  $q/|e| = +0.01$  for Zn, which is indeed at zero valence state, and  $q/|e| = +0.26$  and  $q/|e| = +0.32$  for hydrogen atoms forming OH groups. From the experiment it is known that at  $600\text{ }^\circ\text{C}$  hydrogen desorbs and zinc site is restored. According to our calculation this process runs in two elementary steps. The H atoms (of OH groups), approaching each other, do not form a molecule as they are both positively charged — one of them rather tends to form the Zn-H bond — so the first step of hydrogen desorption is again the formation of OH group and  $\text{Z}-\text{O}-(\text{ZnH})^+$ . Depending on which OH bond is cleaved the reaction can proceed forward (to structure **6**) or backward (to structure **2**). As the structure **6** is similar to the structure **2**, the corresponding wavenumbers are close to each other, namely  $1940\text{ cm}^{-1}$  for ZnH bond and  $3692\text{ cm}^{-1}$  for OH group, respectively. For the structure **6** hydrogen atom bound to zinc ion has slightly negative Mulliken charge ( $q/|e| = -0.02$ ), while the other is positively charged ( $q/|e| = +0.34$ ). In the last step, leading to **8**, the  $\text{H}_2$  molecule is restored. Obviously, the structure **8** is also active in hydrogen dissociation. According to computational results, there is virtually no barrier between structure **8** and structure **6** (upper bound of  $0.5\text{ kcal}\cdot\text{mol}^{-1}$ ). Thus the hydrogen adsorption on the site **8** can lead to structure **6** or can proceed through the analogous, “mirrored”, steps according to the path presented in Fig. 10.

**Table 4** Energy changes between given elementary step and the first one ( $\Delta E$ , 3rd column) or between given elementary step and the previous step ( $\Delta E'$ , 4th column). The energies in 4th column are:  $E_{\text{SCF}}$ ;  $\Delta G^\ominus(200\text{ }^\circ\text{C})$ ;  $\Delta G^\ominus(400\text{ }^\circ\text{C})$ ;  $\Delta G^\ominus(600\text{ }^\circ\text{C})$ , respectively.

Structure	Label, $n$	$\Delta E = E_n - E_1 / (\text{kcal}\cdot\text{mol}^{-1})$	$\Delta E' = E_n - E_{n-1} / (\text{kcal}\cdot\text{mol}^{-1})$
$[(\text{M9})\text{Zn}]^* + \text{H}_2$	<b>1</b>	0	—
$[(\text{M9})\text{ZnH}_2]$	<b>2</b>	-41.4	-41.4 ; -22.3 ; -15.6 ; -9.1
$\text{TS}_{2,4}$	<b>3</b>	-6.5	35.0 ; 36.0 ; 39.1 ; 42.4
$[(\text{M9})\text{ZnHH}]$	<b>4</b>	-14.2	-7.8 ; -7.4 ; -10.0 ; -12.3
$\text{TS}_{4,6}$	<b>5</b>	5.8	20.1 ; 17.9 ; 17.6 ; 17.3
$[(\text{M9})\text{HZnH}]$	<b>6</b>	-48.1	-53.9 ; -53.1 ; -53.1 ; -53.0
$\text{TS}_{6,8}$	<b>7</b>	-2.0	46.1 ; 30.0 ; 24.3 ; 18.1 *
$[(\text{M9})\text{Zn}]^* + \text{H}_2$	<b>8</b>	-2.5	**

\* -  $E_8 - E_6$ ; \*\* - negligible value; see text

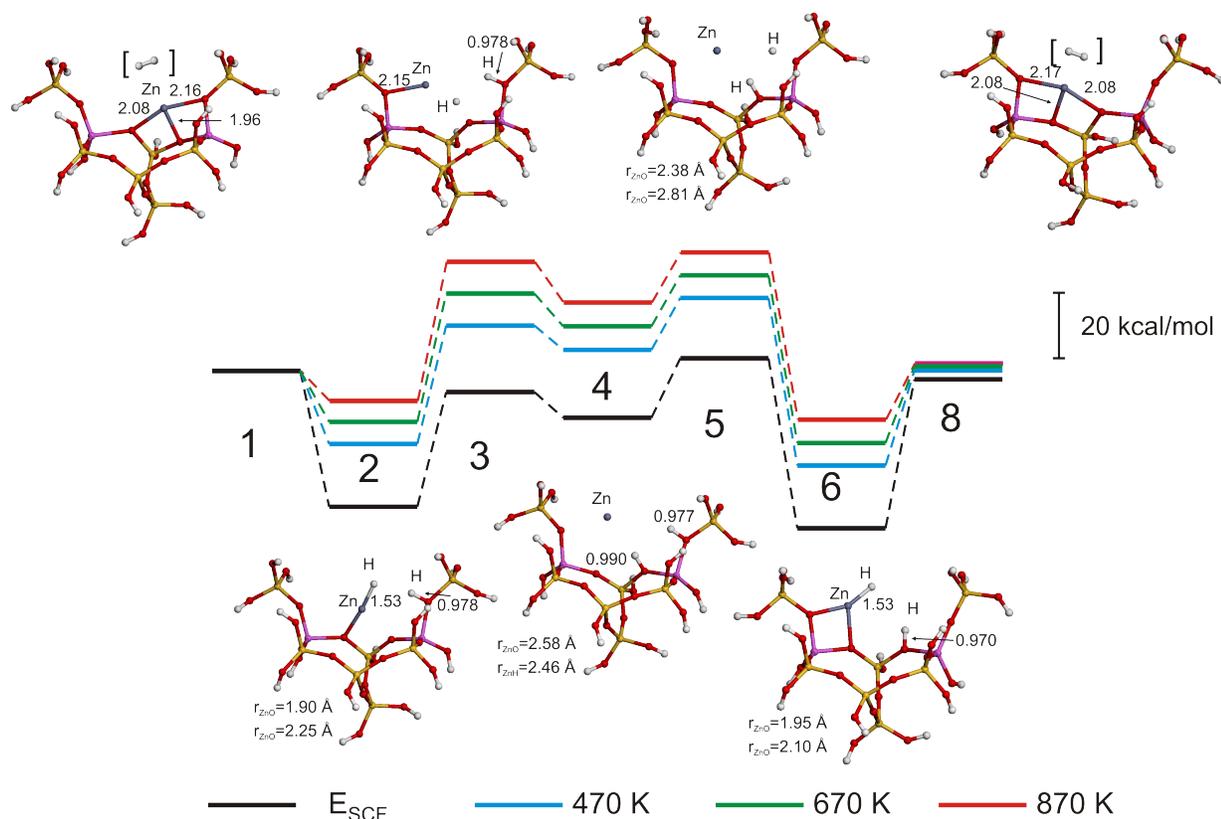
The energy and the wavenumbers calculated for the structures **9**, **10**, **11** are very close to analogous structures **2**, **4**, **6**. For the structure **9** the wavenumbers for Zn-H and O-H bond are  $1905\text{ cm}^{-1}$  and  $3613\text{ cm}^{-1}$ , respectively. The wavenumbers for OH groups in the structure **10** are  $3472\text{ cm}^{-1}$  and  $3678\text{ cm}^{-1}$ . Moreover, the Mulliken population analysis for structures **9**, **10**, **11** also gives the values strictly resembling those for structures **2**, **4**, **6** – see Table 5. At the end of the transformation the structure **1** is formed – the cycle of hydrogen transformation is closed and the zinc site is restored. However, in the process of adsorption and desorption of hydrogen, zinc can get displaced (**1**  $\rightarrow$  **8** or **8**  $\rightarrow$  **1**) or return to the same position (**1**  $\rightarrow$  **2**  $\rightarrow$  **4**  $\rightarrow$  **2**  $\rightarrow$  **1** or **8**  $\rightarrow$  **9**  $\rightarrow$  **10**  $\rightarrow$  **9**  $\rightarrow$  **8**).

**Table 5** Mulliken population analysis for the stable intermediates of H<sub>2</sub> on M9 model.

	$q_{Zn}/ e $	$q_{H_A}/ e $	$q_{H_B}/ e $	$q_Z/ e $
<b>2</b>	0.46	0.31	-0.05	-0.72
<b>4</b>	0.01	0.26	0.32	-0.59
<b>6</b>	0.33	-0.02	0.34	-0.65
<b>9</b>	0.48	0.32	-0.07	-0.78
<b>10</b>	0.05	0.29	0.35	-0.69
<b>11</b>	0.33	-0.02	0.33	-0.64

Calculation showed that localisation and coordination of the Zn cation have essential influence on the interaction of the cation with H<sub>2</sub>. As far as hydrogen molecule does not interact with framework oxygen atoms, the higher coordination number implies the less positive zinc cation and the weaker hydrogen activation ( $\Delta r_{HH}$ ). Moreover, even strong symmetric activation cannot lead to dissociation as easily as when the interaction with framework oxygen atoms is present.

The vibrational analysis allows for studying the influence of temperature on the rate constants of elementary steps. As can be derived from Fig. 9, the temperature raise destabilises the structures comprising/including the gas phase moieties. This is due to the dominant contribution of the translational and rotational entropy comparing to the frustrated rotations the translation and rotation degrees of freedom are converted to upon adsorption.



**Fig. 9** Reaction path for hydrogen adsorption without (SCF energy, black) and with temperature correction at various temperatures (free energies as blue, green, and red lines), bond lengths are given in Å; part 1.

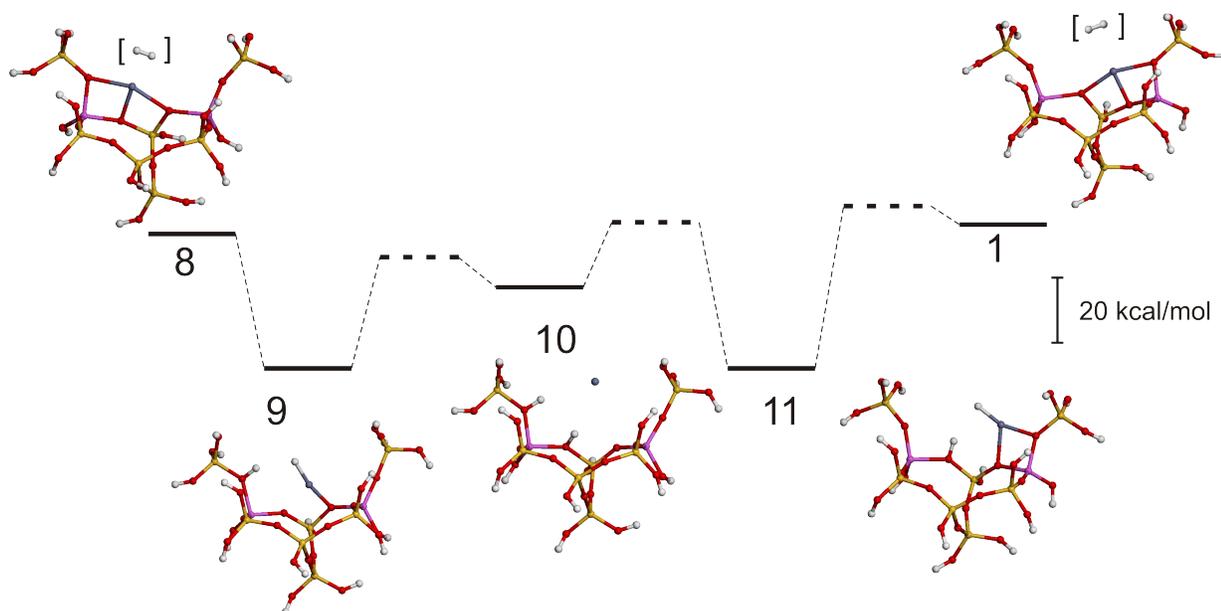


Fig. 10 Reaction path for hydrogen adsorption on active Zn site, part 2.

## Conclusions

Depending on the cation and the surrounding framework the hydrogen activation can vary in a wide range – from only slight weakening of the H-H bond to utter dissociation of  $\text{H}_2$  molecule. The results obtained for the interaction between  $\text{H}_2$  and cations  $\text{Ag}^+$ ,  $\text{Cu}^+$ ,  $\text{Mg}^{2+}$ ,  $\text{Cd}^{2+}$ ,  $\text{Zn}^{2+}$  in cluster model of several sizes indicate that there are three main factors determining hydrogen activation:  $\sigma$ -donation from  $\sigma_{\text{H}_2}$  to the cation,  $\pi$ -backdonation from the cation to antibonding  $\sigma_{\text{H}_2}^*$  orbitals, and interaction between  $\text{H}_2$  molecule and framework oxygen atoms. First two of them are described by orbital interaction and are, in general, characterized by orbital interaction energy,  $\Delta E_{\text{orb}}$ , which includes the components of donation and backdonation processes depending strongly on the cation. For one group of cations, *e.g.*  $\text{Ag}^+$  and  $\text{Cu}^+$ , the backdonation is more efficient, while for the others the  $\sigma$ -donation is privileged. These processes can be moderated by the surrounding zeolite framework, which hinders the  $\sigma$ -donation and enhances the  $\pi$ -backdonation. The coordination number of the cation correlates positively with the significance of the zeolite framework influence. The NOCV analysis allowed to elucidate the components for individual channels of the activation process and also to conclude that the backdonation is more efficient in weakening the H-H bond than the donation channels. The third factor of H-H activation is the distance between the approaching hydrogen molecule and framework oxygen atom combined with the charge accumulated on the molecule. It varies dramatically from one cation localisation to another; it is, however, important that the place stable for one cation is not necessarily stable for the other. Zinc cation can coordinate to zeolite framework in many conformations and the localisation of  $\text{Zn}^{2+}$  for which the  $\text{H}_2$  molecule dissociates was identified. In other localisation, even more stable by 32 – 35 kcal/mol, zinc site activates H-H bond only slightly ( $\Delta v \approx -200 \text{ cm}^{-1}$ ). Thus the geometry of the site, larger than the first coordination sphere, determines the ability of the site to activate (or even dissociate) adsorbed molecule. In the case of Zn-MFI the low coordination number of  $\text{Zn}^{2+}$  corresponds to the geometry which allows for the interaction of positively charged  $\text{H}_2$  with framework oxygen atom and enhances the formation of OH group and  $\text{Z}-\text{O}-(\text{ZnH})^+$  cation. Based on the calculations, the mechanism of  $\text{H}_2$  transformations has been proposed and it points out a possibility of an analogous C-H bond activation. Upon heterolytic dissociation the  $\text{Zn}^0$  moiety can be formed together with two OH groups. Eventually, in two elementary steps the  $\text{H}_2$  molecule can be restored.

## Acknowledgement

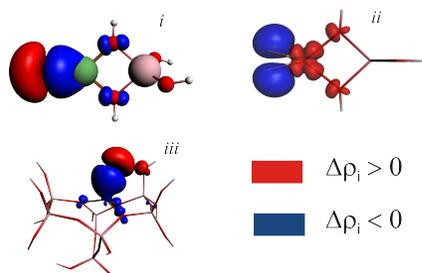
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### Abstract

Three essential factors have been identified (*i-iii*) for the interaction between  $\text{H}_2$  and  $\text{Ag}^+$ ,  $\text{Cu}^+$ ,  $\text{Mg}^{2+}$ ,  $\text{Cd}^{2+}$ , and  $\text{Zn}^{2+}$  sites in zeolites. In the case of bare cation the main contribution is a donation from  $\sigma_{\text{H}_2}$  to the cation (*i*). When zeolite framework surrounding the cation is introduced, it hinders  $\sigma$ -donation and enhances  $\pi$ -backdonation from the cation to antibonding orbital of the molecule (*ii*). For the  $\text{Zn}^{2+}$  position for which  $\text{H}_2$  molecule dissociates, the interaction between  $\text{H}_2$  and oxygen framework (*iii*) plays crucial role. Based on the calculations the mechanism of  $\text{H}_2$  transformations has been proposed.