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1 Precise, Contactless Measurements of  
2 the Surface Tension of Picolitre Aerosol Droplets

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29 **ABSTRACT**

30           The surface composition and surface tension of aqueous droplets can influence key aerosol  
31 characteristics and processes including the critical supersaturation required for activation to form cloud  
32 droplets in the atmosphere. Despite its fundamental importance, surface tension measurements on droplets  
33 represent a considerable challenge owing to their small volumes. In this work, we utilize holographic optical  
34 tweezers to study the damped surface oscillations of a suspended droplet ( $<10\ \mu\text{m}$  radius) following the  
35 controlled coalescence of a pair of droplets and report the first contactless measurements of the surface  
36 tension and viscosity of droplets containing only 1 – 4 pL of material. An advantage of performing the  
37 measurement in aerosol is that supersaturated solute states (common in atmospheric aerosol) may be  
38 accessed. For pairs of droplets starting at their equilibrium surface composition, surface tensions and  
39 viscosities are consistent with bulk equilibrium values, indicating that droplet surfaces respond to changes in  
40 surface area on microsecond timescales and suggesting that equilibrium values can be assumed for growing  
41 atmospheric droplets. Furthermore, droplet surfaces are shown to be rapidly modified by trace species  
42 thereby altering their surface tension. This equilibration of droplet surface tension to the local environmental  
43 conditions is illustrated for unknown contaminants in laboratory air and also for droplets exposed to gas  
44 passing through a water-ethanol solution. This approach enables precise measurements of surface tension  
45 and viscosity over long time periods, properties that currently are poorly constrained.

46 **INTRODUCTION**

47           The surface tension and viscosity of droplets are crucial properties that must be understood and  
48 quantified in a range of disciplines, ranging from the evaporation and drying of sprays,<sup>1</sup> the deposition of  
49 droplets on surfaces in inkjet printing,<sup>2</sup> digital microfluidics/micromachinery,<sup>3</sup> and cloud droplet activation  
50 in the atmosphere.<sup>4</sup> Although readily probed in bulk phases, direct measurements of these properties for  
51 droplets are challenging. Reconciling bulk phase data with the high surface-to-volume ratios characteristic of  
52 dispersed droplet systems is difficult, particularly in highly dynamic systems where the transfer of volatile  
53 components across gas-liquid surfaces must be considered. Additionally, states exhibited by droplets may  
54 differ markedly from the (equilibrium) phase behaviour of bulk solutions, accessing metastable  
55 supersaturated states with solute concentrations above the solubility limit,<sup>5</sup> amorphous or glassy states,<sup>6,7</sup> and  
56 liquid-liquid phase separated structures.<sup>8</sup> Measurements on timescales relevant to dispersed droplet systems  
57 may be similarly inaccessible through bulk measurements, as values of the surface tension and viscosity are  
58 often required for surface ages (i.e. the time since the surface was first generated) as short as a millisecond.  
59 Finally, conventional techniques require substantial amounts of sample, often precluding measurements on  
60 systems where the sample is limited (for example, in the collection of atmospheric aerosol samples).

61           In particular, the surface tension of aerosols and growing cloud droplets represents a critical  
62 uncertainty in determining the effect of aerosols on climate.<sup>9</sup> Atmospheric aerosols are chemically diverse  
63 containing a myriad of organic species, and surface tension depression has been observed in aqueous aerosol  
64 extracts.<sup>10,11</sup> In the absence of direct measurements, however, there has been considerable debate for many  
65 years as to the composition of particle surfaces and the magnitude of surface tensions for atmospheric  
66 aerosols and cloud droplets.<sup>12</sup> The equilibrium size of an aerosol particle at a particular relative humidity  
67 (RH) is governed by an interplay between a bulk solute effect and surface curvature and is treated by Köhler  
68 theory.<sup>13</sup> The former effect allows for stable particle sizes under sub-saturated RH conditions while the latter  
69 governs the magnitude of the characteristic thermodynamic barrier that must be overcome for an aerosol  
70 particle to “activate”, spontaneously growing by water condensation to form a cloud droplet. This barrier can  
71 only be overcome under supersaturated conditions with respect to gaseous water ( $RH > 100\%$ ), and  
72 estimating this critical supersaturation is central to predicting the fraction of aerosol particles that are  
73 activated to form cloud droplets, impacting on cloud droplet number and size, cloud albedo and persistence,  
74 and therefore radiative forcing. The fraction of the aerosol population that can act as cloud condensation

75 nuclei (CCN) is also important for “cloud invigoration” effects, where a larger number of CCN prolong  
76 cloud development and lifetime.<sup>14</sup> Some studies suggest that a surface tension equivalent to that of pure  
77 water may be appropriate for representing an activating CCN and for determining the critical super-  
78 saturation from Köhler theory.<sup>15</sup> However, this assumption directly contravenes expectations for droplets  
79 containing organic solutes, the interplay between bulk and surface partitioning of organic components, and  
80 the dependence on droplet size.<sup>16, 17</sup> More recently, studies have suggested that organics species, which can  
81 contribute to more than half of the mass growth of nanoparticles,<sup>18</sup> may reduce nanoparticle surface tension,  
82 thereby reducing the energy barrier to further growth by vapour condensation.<sup>19</sup> Additionally, surface tension  
83 may play a crucial role in determining the thermodynamic state of nucleation mode aerosol, highlighting the  
84 need for reliable surface tension data for solute solutions at supersaturated concentrations.<sup>20</sup>

85 Organic surface coatings on aerosols have been observed by a number of indirect methods. Surface  
86 coatings on aerosol have been shown to play a significant role in controlling the mass transport kinetics of  
87 volatile components, such as in the transport of water across the droplet surface<sup>20, 21</sup> or in heterogeneous  
88 reaction rates with gas-phase species (e.g. N<sub>2</sub>O<sub>5</sub> and O<sub>3</sub>) that must similarly pass into the bulk.<sup>22</sup> Indeed, even  
89 substantial discrepancies between measurements of water condensation kinetics on droplets with fresh or  
90 aged surfaces have been attributed to contamination by organic species, which may form highly ordered  
91 surface films.<sup>21</sup> Hygroscopicity studies have inferred surface tension through measurements of critical  
92 particle radii for activation and have observed surface tension depression on the order of 10% relative to  
93 water due to uptake of the small surface-active molecules methylglyoxal and acetaldehyde.<sup>23</sup> Indirect  
94 inference of surface tension in this manner, however, only provides averaged values over large particle  
95 ensembles and requires solute and curvature effects to be separable. Direct and unambiguous measurements  
96 of droplet surface tensions are crucial to refine our understanding of CCN activation, the growth of cloud  
97 droplets, and the interactions that occur across gas-liquid surfaces in the atmosphere.

98 Two approaches have been taken to determine droplet surface tensions. One approach is the  
99 oscillating droplet method, which has been used to infer surface tension and viscosity for droplets consisting  
100 of Newtonian and non-Newtonian fluids primarily in falling droplet chains.<sup>2, 24, 25</sup> The damped oscillatory  
101 motion of a droplet following generation can be compared with the expected natural oscillation modes of a  
102 droplet initially described by Rayleigh<sup>26</sup> and extended to include viscous damping by Lamb.<sup>27</sup> Using this  
103 approach, Yang et al. have recently shown that surface tensions inferred from measurements of the

104 oscillation frequencies of droplets several  $\mu\text{L}$  down to  $\sim 100$  pL in volume over 10s of ms can be reconciled  
105 with dynamic surface tension measurements made on bulk samples.<sup>2</sup> Over the short timescale of these  
106 measurements, droplet composition is necessarily limited to sub-saturated solutions and the interaction with  
107 the surrounding gas-phase (crucial to determine aerosol surface properties) is minimal. Another approach  
108 adopted by Morris et al. uses atomic force microscopy (AFM) to probe the surfaces of aerosol particles  
109 sampled and deposited on a substrate by relating the probe tip retention force to the surface tension.<sup>28</sup> This  
110 approach allows equilibrium surface tension measurements on the same droplet with varying RH (solute  
111 concentration). The benefit of this approach is that measurements are performed on individual particles  
112 deposited onto a substrate. However, this approach is necessarily more invasive as it requires contact of the  
113 AFM probe tip to the droplet, which can result in crystallization on the tip and impact the quality of the  
114 measurement.

115 In this work, we present contactless, non-invasive measurements of the surface tensions and  
116 viscosities of aqueous solution droplets with volumes typically 1 – 4 picolitres. We show that the surface  
117 tension and viscosity of a droplet can be determined with accuracies better than  $\pm 1$   $\text{mN}\cdot\text{m}^{-1}$  and  $\pm 1 \times 10^{-3}$   $\text{Pa}\cdot\text{s}$ ,  
118 respectively, a consequence of the extremely high accuracy with which droplet size ( $\pm 2$  nm) and refractive  
119 index (RI,  $\pm 0.0005$ ) are determined.<sup>29</sup> The excitation and damping of oscillatory modes are observed for the  
120 smallest droplets to date (radii down to 6  $\mu\text{m}$ ) and approaching the fundamental hydrodynamic limit as  
121 determined by Chandrasekhar.<sup>30</sup> This approach has the additional advantage that the composition is known at  
122 the moment of measurement (by virtue of the precise RI determination). Further, measurements can be made  
123 over a wide range in surface age extending from seconds to hours with the exposure of the droplet to varying  
124 gas phase conditions (for example, RH) permitting direct investigation of the dependence of surface tension  
125 and viscosity on particle composition. Performing such measurements on trapped, airborne droplets allows  
126 access to supersaturated solute states that are characteristic of aerosol. We show that surface tensions  
127 measured on picolitre droplets agree well with bulk measurements of sub-saturated solutions. Additionally,  
128 we find that that droplet surfaces become contaminated on timescales of minutes unless the most stringent  
129 precautions are taken to control the purity of the local gas phase environment of the droplet. Finally, we  
130 show that the response of droplet surface tension to changes in its local gas phase environment (resulting in  
131 small changes to droplet chemical composition) can be monitored by this approach. Combined, these results  
132 describe a versatile new technique to study a crucial aerosol property that currently is poorly constrained.

133

134 **EXPERIMENTAL SECTION**135 **Holographic Optical Trapping and Controllable Coalescence of Aerosol Droplets**

136 The basic optical tweezers approach used here has been described previously<sup>5,31</sup> and a schematic of  
137 the apparatus is shown in Fig. S1 of the Electronic Supplementary Information (ESI). Briefly, the optical  
138 tweezers are configured in the standard inverted microscope geometry. To form multiple steerable optical  
139 traps, the phase front of a continuous wave 532 nm laser (Laser Quantum, Opus 3W) is dynamically shaped  
140 using a liquid crystal on silicon spatial light modulator (LCOS-SLM, Hamamatsu X10468). The beam is  
141 expanded to fill the SLM display, which is conjugated to the back focal plane of a high numerical aperture  
142 microscope objective (Olympus ACH, 100×/1.25, oil) by a pair of condensing 4*f* telescopes. A pre-calculated  
143 sequence of kinoforms provides a simple and reproducible method by which the trapping positions can be  
144 reconfigured. Upon initiation of the user, the trap separation is varied leading to eventual droplet  
145 coalescence. The capture and relative position of trapped droplets is monitored by a camera (Dalsa Genie  
146 HM 640, CMOS). Brightfield contrast is provided by widefield illumination with a high power LED  
147 (Thorlabs, 470 nm). Similar to previous studies,<sup>5,31</sup> backscattered Raman light is imaged onto the entrance  
148 slit of a 0.5 m focal length spectrograph (Princeton Instruments, Action Spectra Prop SP-2500), dispersed by  
149 a 1200 line pairs/mm grating onto a cooled CCD camera. The resulting Raman spectrum from a spherical  
150 droplet consists of a broad underlying Stokes band with superimposed resonant structure at wavelengths  
151 commensurate with whispering gallery modes (WGMs), from which the radius, RI, and dispersion can be  
152 determined with accuracies better than ±2 nm, ±0.0005 and ±3×10<sup>-8</sup> cm respectively.<sup>29</sup> The intensity of the  
153 elastically scattered component is measured using a silicon photodetector (Thorlabs, DET 110) and recorded  
154 using a low-load, high bit-rate oscilloscope (LeCroy, HDO 6034-MS). The signal is sampled with a  
155 bandwidth >100 MHz, typically > 3 orders of magnitude higher than the oscillation frequency. A high frame  
156 rate camera (Vision Research, Phantom v. 7.3) is used to obtain the images shown in Fig. 1a, which have a  
157 time resolution around 8 μs. The camera acquisition is synchronized to the trigger of the oscilloscope to  
158 capture the coalescence on the camera buffer.

159 To isolate trapped droplets and allow environmental control, the objective focuses the beams through  
160 a coverslip (Chance Glass, #0 thickness) into a custom built trapping chamber. To populate the optical traps  
161 a fine mist of aerosol is produced using an ultrasonic nebulizer (Omron NE U22) from an aqueous solution

162 containing involatile (or very low volatility) solutes. All chemicals are used without further purification  
163 (sodium chloride, Sigma Aldrich, 99.9999%; glutaric acid, Acros Chemicals, 99%) and dissolved in  
164 ultrapure water. The RH in the trapping cell can be controlled by varying the relative flow rates of dry and  
165 humidified nitrogen (BOC, 99.998%, 2 ppm THC max), using paired mass flow controllers (Bronkhorst),  
166 allowing fine control over the water activity of the solution droplet and control over the solute  
167 concentrations. The initial concentration of a trapped droplet has been shown to be comparable to that of the  
168 nebulized solution,<sup>32</sup> which provides a coarser method for tuning the solute concentration.

169

### 170 **Determination of Droplet Composition and Density**

171 Fitting of the wavelengths of the WGMs in the droplet Raman spectra to Mie theory provides a  
172 precise determination of droplet radius and RI. RI is then related to solute concentration, droplet density,  
173 expected surface tension, and expected viscosity through different parametrizations. For NaCl, these  
174 parametrizations were obtained through polynomial fits of RI to concentration and then from concentration  
175 to density, surface tension, and viscosity across the entire range of water activity using the Aerosol Diameter  
176 Dependent Equilibrium Model (ADDEM)<sup>33, 34</sup> and the Aerosol Inorganics Model (E-AIM).<sup>35</sup> For glutaric  
177 acid, thermodynamic data are not available, so these parametrizations were based on the relationship  
178 between measured RI (at 589 nm, Misco Digital Refractometer PA203) and solution concentration and  
179 measured RI, dispersion, and solution density (Mettler Toledo, Densito 30PX) for a range of subsaturated  
180 solutions. Parametrizations used are available in ESI.

181

### 182 **Bulk Tensiometry and Viscometry**

183 The surface tension of bulk aqueous solutions of sodium chloride and glutaric acid are also reported  
184 for the same solutions studied by optical tweezers. For sodium chloride, bulk measurements of surface  
185 tension allow comparison to both the optical tweezers method and calculated E-AIM results. For glutaric  
186 acid, no thermodynamic model results are available and (as discussed later) existing parametrizations of  
187 concentration to surface tension span a relatively wide range for a given solution concentration. Therefore,  
188 the surface tensions of subsaturated glutaric acid solutions were experimentally determined to more directly  
189 compare to the results of the optical tweezers approach. The surface tensions of all solutions were measured  
190 using a Wilhelmy plate tensiometer (Krüss K100).



191 The concentration dependence of the viscosity of glutaric acid solutions has not been reported in  
192 detail, and we report here measurements for subsaturated glutaric acid solutions measured by capillary  
193 viscometry using a Cannon-Fenske routine 200 viscometer (psl-Rheotek).

194

## 195 **RESULTS AND DISCUSSION**

### 196 **Direct Observation of Oscillatory Modes from Coalescing Droplets**

197 The coalescence of two liquid droplets,  $\sim 5\text{-}10\ \mu\text{m}$  in radius, yields an initially dumbbell-shaped  
198 particle, which undergoes relaxation in shape via damped surface oscillations to a single sphere. This shape  
199 relaxation is driven by capillary forces and the minimization of surface free energy. Above some critical  
200 value of viscosity,  $\eta_{\text{crit}}$  (typically  $10\text{-}20\ \text{mPa}\cdot\text{s}$  for the droplet sizes considered here), the surface relaxation is  
201 so efficiently damped that purely aperiodic behaviour is observed. Previously we have shown that  
202 measurement of characteristic relaxation times spanning from  $\mu\text{s}$  to days provides a probe of the bulk  
203 properties of metastable solution droplets with viscosities spanning from  $0.01$  to  $10^9\ \text{Pa}\cdot\text{s}$ , a range of 11  
204 orders of magnitude.<sup>5, 31</sup> Here we consider in detail the relaxation dynamics of droplets with viscosities  
205 below  $\eta_{\text{crit}}$  within the underdamped regime, demonstrating that accurate measurements of surface tension and  
206 viscosity can be made.

207 Following coalescence the large initial distortion leads to the excitation of many oscillatory surface  
208 modes, with those of highest order damped over  $<10\ \mu\text{s}$  and the longest-lived over  $\sim 100\ \mu\text{s}$ . A sequence of  
209 high frame rate images of the oscillating particle recorded with a time-resolution of  $8\ \mu\text{s}$  is shown in Fig. 1a.  
210 These images show a dilute sodium chloride droplet doped with the surfactant sodium dodecyl sulphate  
211 following coalescence. The composite droplet is axially situated just below the objective focal plane due to  
212 reduced buoyancy when trapping in air<sup>36</sup> and laterally at the centre-of-mass of the coalescing pair. Due to the  
213 comparably weak optical forces confining the particle when compared with capillary forces,<sup>37</sup> the optical  
214 forces have no influence on the relaxation dynamics and the composite particle is only drawn back into an  
215 optical trap over much longer times ( $>1\ \text{ms}$ ).<sup>38, 39</sup> Even after only a few  $\mu\text{s}$ , the symmetry of the oscillation  
216 appears to be consistent with only the lowest order ( $l = 2$ ) mode for an incompressible droplet. After about  
217  $50\ \mu\text{s}$ , the amplitude of the oscillation has diminished significantly. The images capture the approximate  
218 turning points in the oscillations clearly, as these are the geometries at which the sinusoidally oscillating  
219 droplet spends most time. The damping time can be readily estimated from the maxima in the droplet aspect

220 ratio. The main uncertainty in determining the damping time from the droplet image aspect ratios arises from  
221 the camera frame rate being of similar order to the droplet oscillation frequency, so the moment of maximum  
222 shape distortion is not known with high precision relative to the oscillation period. The time-dependence of  
223 the ratio of the two droplet axes (the aspect ratio,  $a_y/a_x$ ) is shown in Fig. 1b. The decay in the oscillation  
224 amplitude with time is evident. From the treatment of Lamb, the characteristic damping time for the  $l$ -th  
225 order mode ( $\tau_l$ ) is related to the dynamic viscosity ( $\eta$ ), radius ( $a$ ), and density ( $\rho$ ) of the droplet by the  
226 expression:<sup>27</sup>

$$227 \quad \tau_l = \frac{a^2 \rho}{(l-1)(2l+1)\eta} \quad (1)$$

228 For a droplet where  $a = 10 \mu\text{m}$ ,  $\rho = 1000 \text{ kg}\cdot\text{m}^{-3}$ , and  $\eta = 1 \text{ mPa}\cdot\text{s}$ , the second order mode has a characteristic  
229 damping time of  $20 \mu\text{s}$ , broadly consistent with the timescale of damping shown in Fig. 1b.

230 The natural angular oscillation frequencies ( $\omega_l$ ) of the mode of order  $l$  can be expressed as:<sup>26</sup>

$$231 \quad \omega_l^2 = \frac{l(l-1)(l+2)\sigma}{a^3 \rho} \quad (2)$$

232 where  $\sigma$  is the surface tension. For a droplet of the size and density considered above and with  $\sigma = 75 \text{ mN}\cdot\text{m}^{-1}$   
233 the expected linear oscillation frequency ( $\omega/2\pi$ ) for the  $l = 2$  mode is  $\sim 100 \text{ kHz}$ , equivalent to a period of  
234  $\sim 10 \mu\text{s}$ . Even with the highest frame rate accessible in the experiment, the imaging bandwidth imposes a  
235 Nyquist-limited resolution of  $\sim 50 \text{ kHz}$ . Therefore, a more accurate method to measure oscillation frequency  
236 and infer surface tension utilising elastic backscattered light is described below.

237 Figure 1b also shows the time dependence of the light intensity backscattered from the coalescing  
238 droplet shown in the images. A correspondence is immediately apparent between the distortions in shape  
239 apparent in the images (quantified by the aspect ratio) and the oscillations in backscattered intensity. A  
240 damping time can be estimated from the backscattered light by fitting an exponential to the peaks in the  
241 signal. The backscattered light measurement gives a damping time of  $31 \pm 3 \mu\text{s}$ . The origin of the  
242 backscattered light signal can be considered analogous to the variation in reflected intensity from a dielectric  
243 slab of variable thickness. As the path length of the light through the droplet changes with the distortion in  
244 shape, the interference of light reflected from the front and back face of the droplet leads to a modulation of  
245 the backscattered light amplitude at the modal oscillation frequencies. A Fast Fourier Transform (FFT) of the  
246 backscattered light signal allows the frequency components of the oscillation to be determined. The FFT of

247 the backscattered light signal in Fig. 1b is shown in Fig 1c. A single (linear) oscillation frequency  
248 corresponding to the  $l = 2$  mode ( $\omega_{l=2}/2\pi$ ) is evident at  $59.6 \pm 0.3$  kHz. The linewidth of the resonance peak is  
249 a consequence of the damping rate of the oscillator. From this frequency it is possible to determine  
250 experimentally the droplet surface tension using Eq. (2). However, first we validate our interpretation of the  
251 backscattered light signal using a heuristic model to demonstrate that the form of the light scattering signal  
252 and its corresponding frequency spectrum result from the geometries accessed by the oscillating droplet and  
253 the optical fields that confine it.

254

### 255 **Modelling the Intensity of Scattered Light from Oscillating Droplets**

256 Semi-analytical T-matrix calculations have been performed to give insight into the origin of the  
257 detected signal. Full details of the model are provided in ESI. It is assumed that the signal derives primarily  
258 from the  $l = 2$  mode and that the centre-of-mass of the composite droplet remains stationary over the course  
259 of the measurement,<sup>38</sup> centred between the propagation axes of the two beams, which are separated by a  
260 distance equivalent to the radii of the initial droplets. This understanding of the position of the composite  
261 droplet relative to the trapping beams, made possible by the high frame rate images, is the key advance that  
262 enables more accurate light scatter simulations relative to our previous work.<sup>5</sup> Since the optical and inertial  
263 forces are negligible, the droplet has a symmetry axis that is directed between the centres of the droplets  
264 prior to coalescence. In the model, the axis of rotational symmetry coincides with the x-axis, and the beams  
265 propagate along the z axis (out of the page). The separation between the beam axes is equivalent to the  
266 diameter of the initial droplets, i.e. the beams pass through the points on the x-axis at  $y = +(a/2)^{1/3}$  and  $y = -$   
267  $(a/2)^{1/3}$ , where  $a$  is the radius of the combined droplet.

268 Figure 2a shows the droplet shape for a series of relative amplitudes,  $A_l/a$ , of the  $l = 2$  mode. For  
269  $A_2/a = \pm 0.5$ , the droplet shape resembles a dumbbell. For  $A_2/a = 0$ , the droplet shape is spherical (i.e. the  
270 shape oscillation has no amplitude so no shape deformation occurs). For  $A_2/a = \pm 0.25$ , the droplet has an  
271 elliptical shape, corresponding to an intermediate deformation between the two extremes. Figure 2b shows  
272 the change in the integrated backscatter with variation in  $A_2/a$  for an assumed droplet radius of  $5.621 \mu\text{m}$   
273 with  $\sigma = 74.5 \text{ mN}\cdot\text{m}^{-1}$ ,  $\rho = 1059 \text{ kg}\cdot\text{m}^{-3}$ , and  $\eta = 1.28 \text{ mPa}\cdot\text{s}$ . For comparison, integrated backscatter for two  
274 additional droplet radii are included: one where the radius is larger by  $\lambda/4$ , where  $\lambda$  is the wavelength of the  
275 trapping beam (532 nm), and another where the radius is smaller by  $\lambda/4$ . The inclusion of these two

276 additional droplet sizes illustrates the sensitivity in the light scatter signal to relatively small ( $\sim 2\%$ ) changes  
277 in droplet radius. From this figure it is clear that at positive relative amplitudes ( $A_2/a > 0$ ) the intensity of the  
278 backscatter is much larger than the backscatter at negative relative amplitudes ( $A_2/a < 0$ ). The difference  
279 results directly from the position of the trapping beams relative to the composite droplet: when  $A_2/a > 0$  the  
280 composite droplet intercepts the trapping beams while it does not when  $A_2/a < 0$ .

281 The time resolved signal (shown in Fig. 2c) is determined by considering the evolution of  $A_2/a$ ,  
282 governed by the damped oscillation of the surface.<sup>5, 31</sup> Again, the three radii were considered. The result is a  
283 backscattered light signal with additional features superimposed on an underlying oscillating signal. These  
284 features are broadly similar to those observed in the experiment (compare to Fig. 1b). The dominant  
285 influence on the signal amplitude arises from the extent to which the beams intercept the oscillating droplet  
286 surface. Higher frequency features superimposed on the underlying structure arise from the Fabry-Perot type  
287 resonance caused by optical path length changes through the droplet and the concomitant interference fringes  
288 expected in reflected light. Moreover, for the three droplet radii shown, although there are differences in the  
289 intensities of various higher frequency features, the general form of the signal is consistent, indicating that  
290 these higher frequency features should not complicate the interpretation of the experimental results.

291 Figure 2d shows the corresponding FFTs of the simulated signals. Again, the dominant feature is a  
292 single resonance peak at the frequency corresponding to the  $l = 2$  mode (calculated from the input  
293 parameters). Clearly, small changes in the droplet radius lead to resolvable shifts in the resonance peaks,  
294 highlighting the need for highly accurate particle size measurements. Such differences are readily resolvable  
295 in our measurements.

296

### 297 **Measurements of Droplet Viscosity and Surface Tension**

298 Inferring the droplet surface tension from the modal frequencies estimated from the FFT of the  
299 elastic light scattering signal requires an accurate determination of the radius of the droplet and the density,  
300 apparent from Eq. (2). We have shown previously that the radius and RI can be determined with high  
301 accuracy from the fingerprint of WGMs apparent in the Raman spectrum.<sup>29</sup> Once the RI is known, the  
302 droplet composition can be inferred and the density estimated. The relationship between density, RI, and  
303 mass fraction of solute can be treated by the molar refraction mixing rule.<sup>40, 41</sup> We now return to consider the  
304 oscillation frequency measured for the FFT shown in Fig. 1d.

305 When viscous damping is significant ( $\eta > \sim 1 \times 10^{-3}$  Pa·s for the droplet sizes considered here), the  
306 influence of this dissipation on the natural oscillation frequencies is non-negligible and the measured  
307 oscillation frequency ( $\omega_l^*$ ) is lower than that predicted using Eq. (2) and is more accurately given by:<sup>27</sup>

$$308 \quad \omega_l^* = \sqrt{\omega_l^2 - \tau_l^{-2}} \quad (3)$$

309 With the signal dominated by the  $l = 2$  mode of oscillation, the characteristic damping time  $\tau_{l=2}$  (and  
310 consequently viscosity) can be determined from the exponentially decaying light scatter signal. Once  $\tau_{l=2}$  is  
311 determined, the frequency and surface tension can be determined in the non-dissipative limit. While  
312 neglecting the influence of damping may be increasingly valid as the particle size increases, for the particles  
313 sizes investigated here this can lead to systematically low values for the inferred surface tension, which may  
314 be as large as  $4 \text{ mN}\cdot\text{m}^{-1}$  for the smallest, most viscous droplets studied. Note that if the viscosity is larger  
315 than the critical viscosity ( $\eta_{\text{crit}} \geq 0.76 \times (a\sigma\rho)^{1/2}$ ), then surface oscillations are so efficiently damped that only  
316 aperiodic relaxation is observed, i.e. a slow merging of two droplets.<sup>30</sup> In this limit, the surface tension  
317 cannot be obtained by this method.

318 The viscosity of aqueous organic aerosols is less well understood than for inorganic components.  
319 Numerous studies suggest that organic aerosols may exist in a highly viscous state.<sup>6, 7, 42, 43</sup> The viscosities for  
320 glutaric acid droplets inferred from the damping times are reported in Fig. 3 and compared with bulk phase  
321 measurements. To determine the viscosity, the maxima in the backscattered light signal were fit to an  
322 exponential decay to determine the damping time. Note that whereas initially the backscattered light does not  
323 follow an exponential decay, at later times it does (see Fig. 1b). Therefore, the number of maxima included  
324 in the fit was systematically varied to produce the fit most consistent with the later portion of the backscatter  
325 signal. The damping times and additional droplet parameters ( $a$ ,  $\rho$ ) were then used to determine  $\eta$  from Eq.  
326 (1). As shown in Fig. 3, the agreement between the optical tweezers approach and bulk measurements of  
327 solution viscosity is very good.

328 Strictly, the linear theory of Rayleigh is valid only for small amplitude oscillations. Non-linear  
329 effects including mode coupling and frequency modulation may dominate when the distortion of the droplet  
330 exceeds 10% of the unperturbed droplet radius.<sup>44, 45</sup> The shape distortion is increasingly dominated by the  $l =$   
331 2 mode as the amplitude of surface oscillations decreases; the oscillation frequency then asymptotically

332 approaches the values predicted by the linear theory. Thus, the oscillation frequency is determined in this  
333 asymptotic limit to exclude possible hydrodynamic non-linearities (see Fig. S2 in ESI).

334 Droplet surface tensions inferred from the coalescence measurements are shown in Fig. 4 for  
335 droplets containing sodium chloride (Fig. 4a) or glutaric acid (Fig. 4b). Both sodium chloride and glutaric  
336 acid are atmospherically relevant compounds. Sodium chloride makes up a significant fraction of  
337 atmospheric aerosol, generated by mechanical processes at the marine surface.<sup>46</sup> Similarly, the dicarboxylic  
338 acids are atmospherically prevalent and glutaric acid is often chosen as a surrogate for water soluble,  
339 surface-active organic aerosol.

340 In Fig. 4, the lower x-axis shows solute concentration, which is then used to infer water activity,  $a_w$   
341 (shown on the upper x-axis). The relationship between concentration and  $a_w$  can be determined directly from  
342 E-AIM calculations for sodium chloride. For glutaric acid,  $a_w$  was determined through parametrizations of  
343 bulk concentration and density coupled with E-AIM calculations to determine the solute mass fraction as a  
344 function of RH. For the optical tweezers results, individual measurements are aggregated into 0.2 M  
345 concentration bins. Uncertainties reported on the x- and y-axes are the standard deviation of the  
346 measurements in any given bin. If no uncertainty is provided, then only one data point fell into that specific  
347 concentration bin.

348 In Fig. 4a, surface tensions of sodium chloride droplets obtained by the optical tweezers approach  
349 are compared with bulk tensiometry measurements and E-AIM model predictions. Additionally, results from  
350 a recent study of the surface tension of submicron aerosol by AFM are included.<sup>28</sup> Overall, there is very good  
351 agreement between the optical tweezers measurements and the other measurements, validating the  
352 experimental approach. The solubility limit of NaCl is approximately 6 M, so the optical tweezers results  
353 extend into the supersaturated solute regime and appear to agree well with expected values (from E-AIM).

354 In Fig. 4b, surface tensions of glutaric acid droplets obtained by the optical tweezers approach are  
355 compared with bulk tensiometry measurements and a number of different parametrizations of surface tension  
356 and concentration. These parametrizations come from several independent measurements<sup>47-51</sup> but we use the  
357 parameters of the Szyszkowski equation for each that are summarized in Lee and Hildemann.<sup>49</sup> In addition,  
358 we show results from the AFM approach only for  $a_w$  close to the saturation limit, which is closest to our  
359 measured concentrations. Overall, our experimental results agree very well with bulk measurements. Among  
360 the various parametrizations, our measurements agree best with the parametrization of Gaman et al.<sup>48</sup> and

361 appear to be consistent with the AFM results at high  $a_w$ . Overall, the precision of the optical tweezers  
362 measurements typically is  $< 1 \text{ mN}\cdot\text{m}^{-1}$ . Notably, the inorganic salt and organic dicarboxylic acid show the  
363 anticipated increase<sup>52</sup> and decrease in surface tension, respectively, relative to water ( $72.6 \text{ mN}\cdot\text{m}^{-1}$  at 294 K).

364 A related parameter encountered in surface science is the dynamic surface tension. When forming  
365 new surface area, diffusion to the interface is non-instantaneous resulting in a surface age dependent surface  
366 tension. This phenomenon is readily observed in macroscopic measurements but also in oscillating droplets.  
367 Using the falling droplet approach, Yang et al. found that for droplets with volumes of 100s of picolitres and  
368 surface ages on the order of 10 – 100  $\mu\text{s}$ , the surface tensions of droplets were considerably higher than  
369 expected based on equilibrium values.<sup>2</sup> This observation is consistent with an expectation that a surfactant  
370 film (depending on surface excess and concentration) achieves an equilibrium composition on a timescale  
371 considerably longer than the surface age in such measurements, typically  $\sim 20 \text{ ms}$ . No such effect is seen here  
372 despite the extremely short surface ages during droplet oscillation. However, it should be noted that the  
373 relevant timescale governing the surface compositions of the two droplets is the time frame prior to  
374 coalescence when they can be assumed to reach their equilibrium values.

375 During the relaxation process, the surface-to-volume ratio must relax by a factor of 1.26 with initial  
376 oscillations that approach a change of this order. Over one period of oscillation in surface area ( $\sim 10 \mu\text{s}$ ), a  
377 typical solute with a diffusion constant of  $2 \times 10^{-9} \text{ m}^2\cdot\text{s}^{-1}$  may diffuse over  $\sim 200 \text{ nm}$ . Thus, the expansion and  
378 contraction of the surface area remains sufficiently slow that the near-surface concentration gradients  
379 established by the inorganic salt double layer and the surface excess for the organic component can rapidly  
380 compensate, maintaining a near-surface equilibrium distribution of solute molecules throughout the  
381 relaxation process. Such an observation may provide insight into the value of the surface tension during  
382 water condensation and CCN activation in the atmosphere.<sup>53, 54</sup> Moreover, turbulent mixing is avoided under  
383 the low Reynolds number conditions encountered here, similarly maintaining the radial concentration  
384 gradients that exist in the pre-coalescence pair.<sup>55</sup> In fact, the essentially static values of surface tension  
385 measured are more comparable with those of Yamada et al. for coalescence under large shear deformations<sup>25</sup>  
386 and Apfel et al. for super-deformed droplets under microgravity,<sup>24</sup> where static values of the surface tension  
387 are observed for oscillating droplets. Thus, the surface tensions inferred from these measurements match the  
388 expected equilibrium values and provide a robust method for determining the surface tension of  
389 atmospherically relevant droplet compositions.

390

391 **The Contamination of Droplet Surfaces**

392 It has long been assumed that liquid surfaces can become contaminated through adsorption of trace  
393 impurities in the gas phase and this can have consequences, in particular, for understanding mass transfer  
394 rates across the surface of liquid droplets.<sup>21</sup> Despite this presumption, direct confirmation has not been  
395 possible. Using the droplet coalescence approach it is possible to directly explore the possible time-  
396 dependent contamination of liquid surfaces. Up to this point, coalescence has been induced within 10 s of  
397 droplet capture. To study surface adsorption from the gas-phase, pairs of sodium chloride droplets are  
398 retained in the optical traps for well-defined times ranging from 10 s to > 7000 s and representing more than  
399 2 orders of magnitude in surface age.

400 In Fig. 5, we report the surface tension depression recorded for variably surface aged droplet pairs. A  
401 clear decrease in surface tension is observed with surface age, converging to  $\sim 30 \text{ mN}\cdot\text{m}^{-1}$  when pairs of  
402 droplets were captured and held in the trapping chamber opened to laboratory air (no gas flow introduced  
403 into the cell). The time scale for the decrease in surface tension is characteristic of adsorption from the gas-  
404 phase rather than the surface partitioning of organic impurities from the droplet bulk, which would be very  
405 rapidly salted out under conditions of high ionic strength. In addition, time dependencies of two different  
406 starting salt concentrations (0.7 and 5.1 M) were found to be similar, which would not be expected if the  
407 bulk solution concentration of impurities were increased by a factor of 7.5. The bulk surface tension data  
408 recorded using a tensiometer corroborates this interpretation. It should be stressed that the level of  
409 contamination may remain very small: forming a complete monolayer would require  $\sim 10^{10}$  molecules or  $10^{-14}$   
410 moles. Droplet surface tension relaxes to an approximately constant value around  $30 \text{ mN}\cdot\text{m}^{-1}$  after about  
411 2000 s in the trap. This timescale for equilibration ( $\tau_\sigma$ ) can be related to a Henry's law constant ( $H$ ) for the  
412 condensing species if its molar mass ( $M$ ) and accommodation coefficient ( $\alpha$ ) are known, where  $a$  is the  
413 droplet radius,  $R$  is the gas constant, and  $T$  is temperature:

$$414 \quad \tau_\sigma = \frac{r \times H \sqrt{2\pi MRT}}{3\alpha} \quad (4)$$

415 Accommodation coefficients can vary widely for different compounds but are frequently reported in  
416 the range of 0.01-1.0. Assuming a compound with molar mass of  $100 \text{ g}\cdot\text{mol}^{-1}$  condenses on an  $8 \mu\text{m}$  radius  
417 droplet, the Henry's law constant would be expected to be in the range from  $10^4$  to  $10^6 \text{ M}\cdot\text{atm}^{-1}$ , depending



418 on the assumed value of  $\alpha$ . Such a range for the Henry's law constant could be consistent with absorption  
419 and contamination of the droplet surface by variety of ambient species including glyoxal and oxalic acid.  
420 Absorption and dissolution would be clearly evident in the fingerprint region ( $500 - 3000 \text{ cm}^{-1}$ ,  $550 - 625$   
421 nm) of the Raman spectrum if the particle were to attain an appreciable bulk concentration of organics. Such  
422 a change is not observed here, indicating a change in composition below the Raman detection limit (typically  
423  $\sim 100 \text{ mM}$ ).

424 Further evidence that the depression in surface tension can be attributed to adsorption from the gas  
425 phase is obtained by generating droplets from a bulk solution intentionally doped with an ionic surfactant  
426 (sodium dodecyl sulphate). In each case, coalescence was induced quickly following capture ( $< 10 \text{ s}$ ). In  
427 contrast to the data in Fig. 5, a marked depression of the inferred surface tension is immediately apparent (to  
428  $60 \pm 4 \text{ mN} \cdot \text{m}^{-1}$  over 8 individual measurements). (The range of measured surface tensions for the surfactant-  
429 doped droplets is larger than for the single component droplets due to the variability in the absolute quantity  
430 of surfactant in the droplet for each coalescence event.) Sodium chloride remains in a 100:1 excess and the  
431 amount of surfactant in the droplet is insufficient to form a full surface monolayer, typically containing  $10^7 -$   
432  $10^8$  molecules, assuming the stoichiometry of the solute components in the droplet remains the same as in the  
433 bulk.

434 Also shown in Fig. 5 are the results of two other experiments where we examine the response of  
435 droplet surface tension to the environmental conditions. Initially we use a cylinder of ultrapure nitrogen,  
436 which shows only a minor improvement over laboratory air in terms of the time required for the surface  
437 tension depression. Using the boil-off from a liquid nitrogen dewar is the most reliable way of avoiding the  
438 presence of trace quantities of contaminants in the gas phase. In this case, suppression of droplet surface  
439 tension over many thousands of seconds becomes possible.

440

#### 441 **Time-Dependent Observations of the Adsorption of a Water Soluble Organic and the Change in** 442 **Surface Tension**

443 We have demonstrated that the experimental approach is capable of performing precise  
444 measurements of droplet surface tension and that it is possible to control the local environment surrounding  
445 the trapped droplets such that undesired contamination of the droplet surface is minimized over long time  
446 periods. As a next step a gas phase "contaminant" is intentionally introduced and the response of droplet

447 surface tension explored; that is, the response of droplet surface tension to changes in the gas phase is  
448 monitored. This process has relevance to atmospheric aerosol microphysics where aerosol chemical  
449 composition can change substantially, likely impacting surface tension. A proof-of-concept example of such  
450 an experiment is shown in Fig. 6. In this experiment, aqueous sodium chloride droplets were trapped in the  
451 cell and subjected to a vapour flow from air bubbled through a solution of water and ethanol (97.5%/2.5%  
452 volume/volume). The salt concentration in the droplets was approximately 1 M.

453 In the upper panel of Fig. 6, we report the change in droplet surface tension as a function of time  
454 exposed to the vapour flow. Droplet surface tension at time  $t = 0$  s (i.e. a purely aqueous NaCl droplet) is  
455 about  $73 \text{ mN}\cdot\text{m}^{-1}$ . By comparison, a surface tension of  $74 \text{ mN}\cdot\text{m}^{-1}$  was measured for a bulk 1 M aqueous  
456 NaCl solution (dotted line in the figure), in close agreement with the droplet measurements (where salt  
457 concentration is not precisely controlled but can be inferred from measurements of RI). As the droplet  
458 equilibrates to the vapour flow, the surface tension decreases and after  $\sim 200$  s stabilizes around a value of  
459  $\sim 63 \text{ mN}\cdot\text{m}^{-1}$ . If the liquid reservoir from which the vapour flow arises is converted into a 1 M NaCl solution  
460 (i.e. 1 M NaCl in 97.5% water, 2.5% ethanol by volume), bulk measurements of surface tension yield a value  
461 of  $64 \text{ mN}\cdot\text{m}^{-1}$  (dotted line in the figure), corresponding well with the droplet measurements and indicating  
462 that the droplet has equilibrated with the vapour flow.

463 Although the change in surface tension is substantial ( $\sim 15\%$ ), such a change only corresponds to a  
464 very minor change in droplet bulk composition. The lower panel of Fig. 6 shows the accompanying change  
465 in Raman CH/OH band ratio. The CH/OH ratio can provide a quantitative measure of ethanol uptake. The  
466 CH/OH band ratio changes on the same timescale as droplet surface tension, confirming that the change in  
467 surface tension is indeed coming from a change in the droplet composition due to absorption of ethanol.  
468 Further, the change in droplet composition is very small and barely resolvable from the change in Raman  
469 intensity. In short, this proof-of-concept experiment demonstrates that our experimental approach is capable  
470 of resolving changes in droplet surface tension for very small changes in droplet chemical composition and  
471 promises to allow us to quantitatively resolve the impact of atmospherically relevant chemistry on droplet  
472 surface tension.

473

474 **CONCLUSIONS**

475 We have demonstrated for the first time that contactless measurements of surface tension can be  
476 made on micrometre-sized droplets containing only 1 – 4 pL of material. Holographic optical tweezers  
477 provide a versatile platform for conditioning aerosol, controllably inducing coalescence and probing the  
478 dynamics of the subsequent relaxation in shape via damped oscillations. By freeing the droplet from contact  
479 with a substrate or external probe and in concert with spectroscopic measurements of particle size and RI,  
480 this platform can be utilised as an all optical tensiometer. We demonstrated that measurements of surface  
481 tension can be made on simple organic/inorganic solute droplets with a comparable level of accuracy ( $\pm 1$   
482  $\text{mN}\cdot\text{m}^{-1}$ ) to bulk phase measurements. Additionally, measurements of the droplet viscosity are also possible  
483 and agree well with bulk values, essentially enabling a simultaneous determination of both surface tension  
484 and viscosity in one measurement. Therefore, this approach allows for a full exploration of the relaxation  
485 dynamics following droplet coalescence and provides complementary data to previous studies of aerosol  
486 viscosity.

487 Measurement of the droplet surface tension is limited to droplets with viscosities below the critical  
488 value, above which surface oscillations become overdamped (generally 10-20  $\text{mPa}\cdot\text{s}$  for droplet radii studied  
489 here). However, droplet surface tension is key to the activation of aerosol to cloud droplets, which occurs at  
490 high water activities. As a result, activating droplets would be expected to have substantial water content and  
491 viscosities below this critical value. Droplets analyzed by this approach are typically between 5-10  $\mu\text{m}$   
492 radius, larger than the typical diameter of a CCN at activation ( $\sim 1 \mu\text{m}$ ), but allowing direct measurements of  
493 comparably sized droplets for the first time. In principle, surface tension measurements over the typical  
494 range accessible to aqueous droplets are measurable by this approach.

495 Light scattering simulations reproduce the form of the oscillatory light scattering signal,  
496 simultaneously confirming our interpretation of the data and providing an experimental validation of models  
497 used to describe light scattering from non-spherical dielectric objects. Surface tension measurements are  
498 performed on microsecond timescales (the period during which the droplet shape is oscillating). Since these  
499 measurements agree well with bulk values, the agreement suggests that equilibrium is retained in the surface  
500 composition during shape relaxation when starting from droplets with pre-equilibrated composition. Such a  
501 result has implications for activating aerosol growing into cloud droplets from an equilibrium state, as the  
502 surface tension at any given point along the growth can be taken as its equilibrium value.

503 Building on the ability to measure precisely both surface tension and viscosity, we have explored the  
504 contamination of droplets due to adsorption of organics from the gas-phase, which represents a key  
505 mechanism by which droplets may obtain a surfactant coating. Recent studies have suggested the possibility  
506 of co-condensation of organic vapours during hygroscopic growth as a route to enhanced cloud droplet  
507 number concentrations.<sup>56</sup> The surface tension of aqueous droplets was observed to decrease, tending towards  
508 a value for a saturated surfactant coated surface over a timescale of minutes to hours. These data have a  
509 significant implication for the assumed surface tension values of aqueous droplets in any environment and,  
510 more specifically, on the assumed value in atmospheric models of cloud droplet number. Although further  
511 studies are necessary to explore the contamination of droplet surfaces under tropospherically relevant  
512 conditions, this study suggests that assuming a surface tension of a surfactant coated surface ( $\sim 30 \text{ mN}\cdot\text{m}^{-1}$ )  
513 may be appropriate. Moreover, we show that we are able to control the local environment and monitor the  
514 response of droplet surface tension. Previous studies on aerosol extracts have shown that the organic fraction  
515 of aerosol certainly contains surfactants and a surface tension depression on the order of  $\sim 60\%$  could  
516 correspond to an increase in cloud droplet number concentration as large as  $\sim 40\%$ .<sup>10</sup> Regardless, we have  
517 shown that surface partitioning and adsorption from the gas-phase can be probed in micrometre sized aerosol  
518 droplets which should provide fertile ground for further studies aiming to disentangle the various  
519 contributors to aerosol activation and the effect of aerosol on climate.

520

## 521 **ELECTRONIC SUPPLEMENTARY INFORMATION**

522 Electronic supplementary information (ESI) available: parametrizations used to infer concentration, density,  
523 viscosity, and surface tension from refractive index for sodium chloride and glutaric acid; description of the  
524 semi-analytical T-matrix calculations; Figs. S1-S2. See DOI: 10.1039/XXXXXX.

525

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629

630 **FIGURE CAPTIONS**

631 **Figure 1:** Coalescence of an aqueous  $\sim 1$  M NaCl droplet doped with the surfactant sodium dodecyl sulphate.

632 a) High frame rate images of the composite droplet for the first several microseconds after  
633 coalescence. Time ranges underneath each image provide the time period during which the image was  
634 taken. b) Backscattered light collected after coalescence (left axis, time  $t = 0$   $\mu\text{s}$  corresponds with the  
635 moment of coalescence) and droplet aspect ratios ( $a_y/a_x$ ) determined from the high frame rate imaging  
636 (right axis). c) Fast Fourier Transform of the backscattered light gives the frequency of the shape  
637 oscillation.

638 **Figure 2:** Computational modeling of droplet coalescence with the following composite droplet properties:  $a$

639  $= 5.621$   $\mu\text{m}$ ,  $\sigma = 74.5$   $\text{mN}\cdot\text{m}^{-1}$ ,  $\rho = 1059$   $\text{kg}\cdot\text{m}^{-3}$ , and  $\eta = 1.28$   $\text{mPa}\cdot\text{s}$ . a) droplet shapes at various  $l = 2$   
640 distortion amplitudes ( $A_2$ ). The trapping beams are perpendicular to the plane of the page and pass  
641 through the points on the x-axis at  $y = +(a/2)^{1/3}$  and  $y = -(a/2)^{1/3}$ . b) intensity of the integrated  
642 backscatter as a function of relative amplitude ( $A_2/a$ ). c) Simulated time-resolved backscattered light  
643 for three droplet radii (offset for clarity). d) Fast Fourier Transform of the time-resolved  
644 backscattered light in part c) to give the frequency of the shape oscillation. Colors in c) and d) follow  
645 the legend in b).

646 **Figure 3:** Viscosity of glutaric acid as a function of molar concentration. Symbols give measurements on

647 droplets using the optical tweezers approach. The line corresponds to bulk capillary viscometry  
648 measurements over the same concentration range. The upper axis gives water activity ( $a_w$ ), which is  
649 inferred from the solute concentration.

650 **Figure 4:** Surface tension measurements on two atmospherically relevant systems: a) sodium chloride and b)

651 glutaric acid. Also included are bulk tensiometry measurements, E-AIM modeling (sodium chloride),  
652 surface tension parametrizations performed by others (glutaric acid),<sup>47-50</sup> and measurements on  
653 submicron aerosol using atomic force microscopy.<sup>28</sup> The upper axis gives water activity ( $a_w$ ), which is  
654 inferred from the solute concentration.



655 **Figure 5:** Surface tension of dilute sodium chloride droplets held in the trapping cell for varying lengths of  
656 time. Red circles correspond to measurements where no gas flow was introduced to the cell. Green  
657 circles correspond to a gas flow at  $80 \text{ mL}\cdot\text{min}^{-1}$  using a high purity  $\text{N}_2$  cylinder. Blue circles  
658 correspond to a gas flow at the same flow rate but using the boiloff flow from a liquid  $\text{N}_2$  dewar.

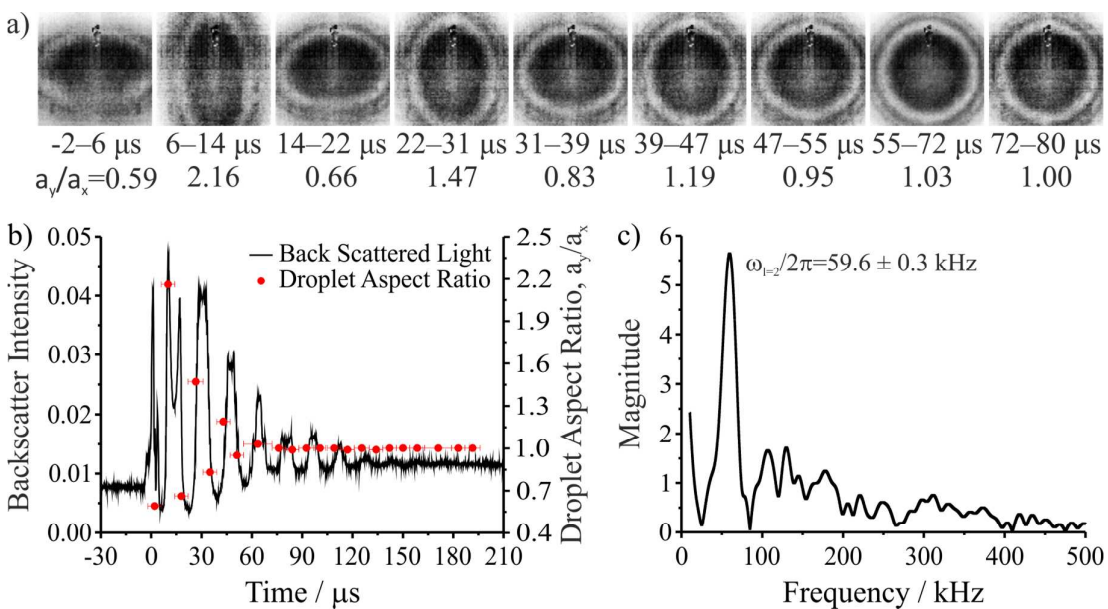
659 **Figure 6:** Exposure of aqueous sodium chloride to a gas flow bubbled through a 2.5% ethanol/97.5% water  
660 (volume/volume) solution. In the upper panel, symbols give measured surface tension with an  
661 assigned  $\pm 1 \text{ mN}\cdot\text{m}^{-1}$  uncertainty. Dotted lines correspond to a 1 M aqueous NaCl solution ( $74 \text{ mN}\cdot\text{m}^{-1}$ )  
662 and a 1 M 2.5% ethanol solution ( $64 \text{ mN}\cdot\text{m}^{-1}$ ). The lower panel gives the Raman CH/OH band  
663 ratio. Uncertainty bars correspond to the standard deviation of the ratio obtained from the spectra  
664 over the 20-50 seconds after coalescence.

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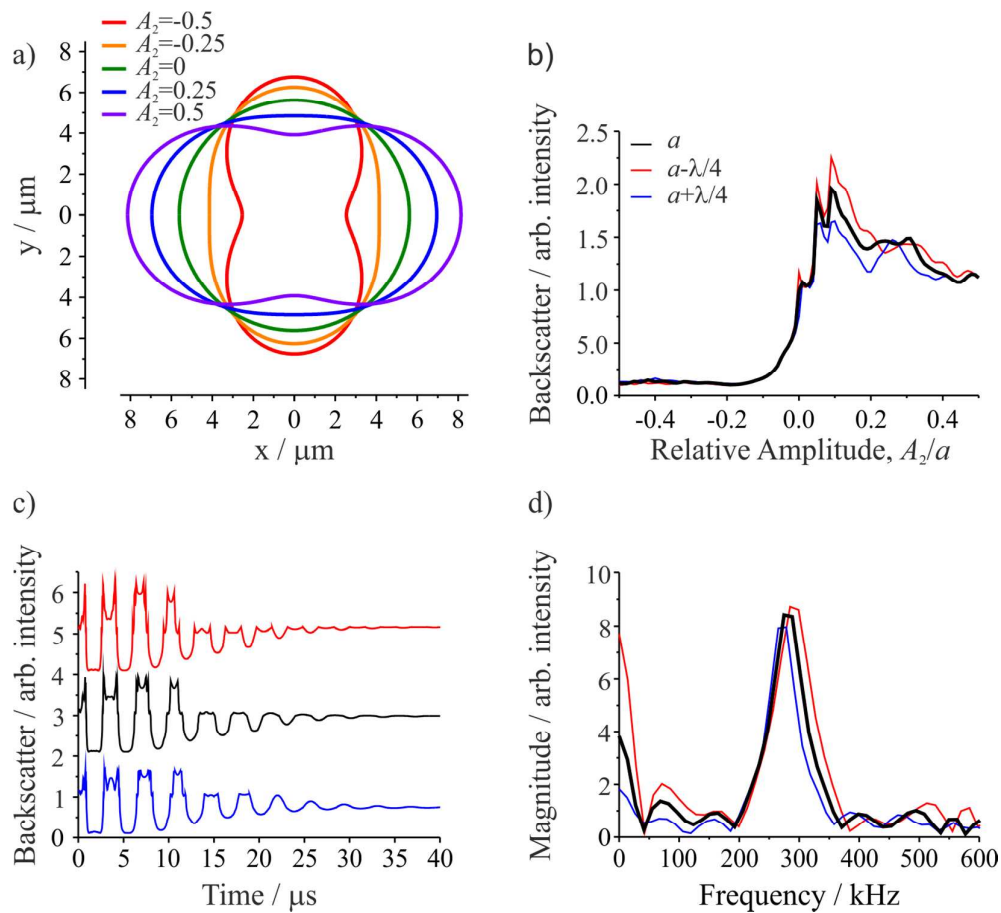
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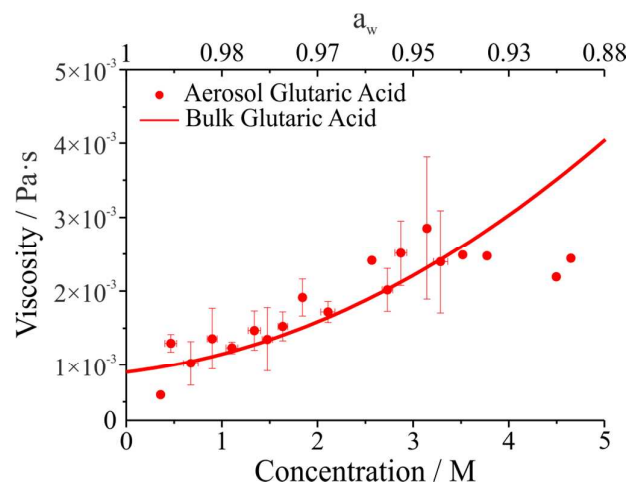
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**Figure 1**

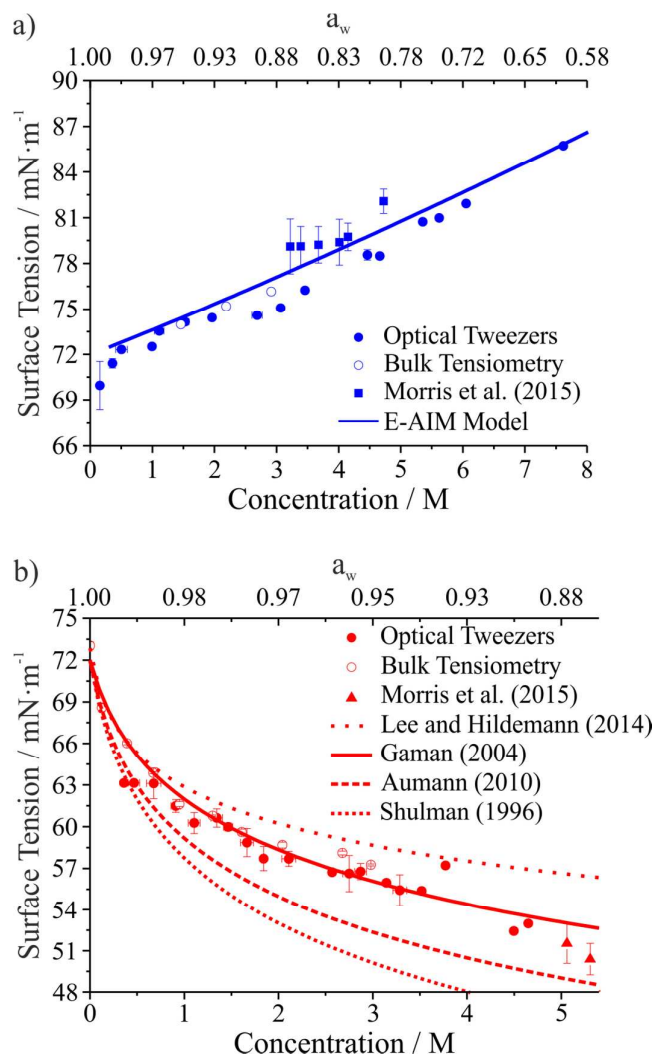
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670 **Figure 2**

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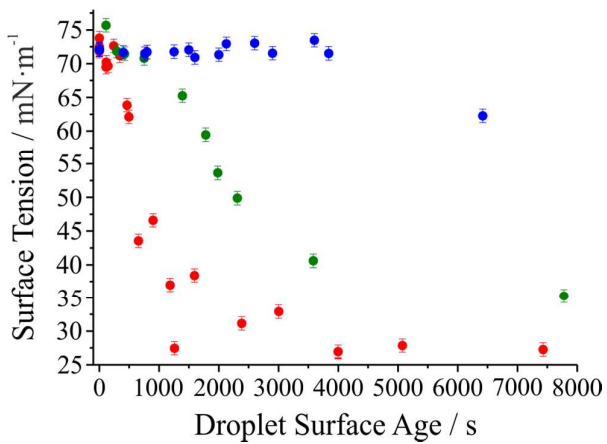
672 **Figure 3**

673

674 **Figure 4**

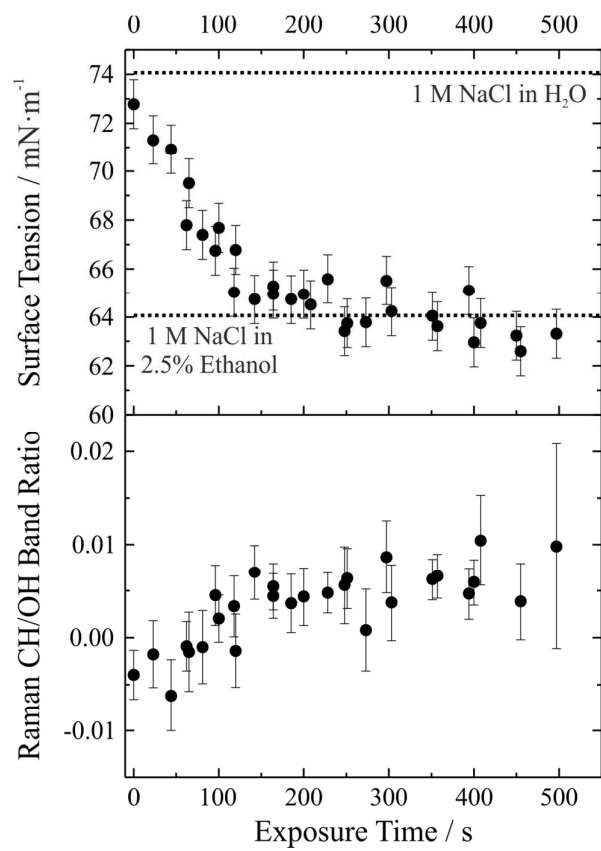
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677 **Figure 5**

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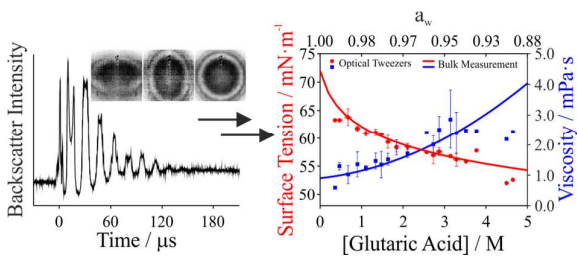
679

680 **Figure 6**

681

682

## 683 Table of Contents Entry



684

685 **Descriptive Statement:** Precise measurements of the surface tension and viscosity of airborne picolitre

686 droplets can be accomplished using holographic optical tweezers.