Chemical Science

Accepted Manuscript



This is an *Accepted Manuscript*, which has been through the Royal Society of Chemistry peer review process and has been accepted for publication.

Accepted Manuscripts are published online shortly after acceptance, before technical editing, formatting and proof reading. Using this free service, authors can make their results available to the community, in citable form, before we publish the edited article. We will replace this Accepted Manuscript with the edited and formatted Advance Article as soon as it is available.

You can find more information about *Accepted Manuscripts* in the **Information for Authors**.

Please note that technical editing may introduce minor changes to the text and/or graphics, which may alter content. The journal's standard <u>Terms & Conditions</u> and the <u>Ethical guidelines</u> still apply. In no event shall the Royal Society of Chemistry be held responsible for any errors or omissions in this *Accepted Manuscript* or any consequences arising from the use of any information it contains.



www.rsc.org/chemicalscience

ARTICLE TYPE

Tuning ESIPT Fluorophores into Dual Emitters^{\dagger}

Cloé Azarias^a, Simon Budzák^a, Adèle D. Laurent^a, Gilles Ulrich^b and Denis Jacquemin^{*a,c}

Received Xth XXXXXXXXX 20XX, Accepted Xth XXXXXXXX 20XX First published on the web Xth XXXXXXXX 200X DOI: 10.1039/b000000x

Dyes undergoing excited-state intramolecular proton transfer (ESIPT) are known to present large Stokes shifts as a result of the important geometrical reorganisation following photon absorption. When the ESIPT process is not quantitative, one can obtain dual emitters characterised by two distinct fluorescence bands, observed due to emissions from both the canonical and ESIPT isomers. However, dual emission generally requires to maintain a very specific balance, as the relative excited-state free energies of the two tautomers have to be within a narrow window to observe the phenomenon. Consequently, simple chemical intuition is insufficient to optimise dual emission. In the present contribution, we investigate, with the help of quantum-mechanical tools and more precisely, time-dependent density functional theory (TD-DFT) and algebraic diagrammatic construction (ADC), a wide panel of possible ESIPT/dual emitters with various substituents. The selected protocol is first shown to be very robust on a series of structures with known experimental behaviour, and next is applied to novel derivatives with various substituents located at different positions. This work encompasses the largest chemical library of potential ESIPT compounds studied to date. We pinpoint the most promising combinations for building dual emitters and highlight unexpected combination effects and rationalise the impact of the different auxochromes.

1 Introduction

Despite more than a century of history, dye chemistry remains a very active field of research. During the latest decades, the main developments in the field have been related to emission, and more specifically to fluorescence. Indeed fluorophores are extremely versatile and can be used in several devices, e.g., they can be employed to probe several analytes in various biological environments. To limit the possibility of absorption of the emitted photon by other dyes or by molecules present in the medium, it is highly desirable to obtain both redshifted emission and large Stokes shifts (Δ_{SS}). In that framework, molecules undergoing an excited-state intramolecular proton transfer (ESIPT) are particularly attractive. In these compounds (see Figure 1), the absorption takes place from the S_0 -stable enol (E) form while the emission occurs from the S_1 favored keto (K^*) isomer, implying large structural changes at the ES, and, consequently enhanced Stokes shifts.¹⁻⁸ ES-

IPT can be viewed as a very fast phototautomerisation process taking place along a strong intramolecular hydrogen bond between two atoms presenting acidities/basicities that are significantly tuned by an electronic excitation. ESIPT dyes have found applications in many fields, ^{9–14} and present the extra advantage to be very effective in solid-state, contrary to most fluorophores that are limited by fluorescence quenching in both films and crystals. If the ESIPT process is not quantitative, it is possible to obtain dual emission with fluorescence from both S_1 -enol (E^{*}) and S_1 -keto (K^{*}). Such phenomenon paves the way to the development of white organic light-emitting diodes (WOLED), if the positions and relative intensities of the two emissions can be adequately selected in the coulourimetric space.

Several series of compounds undergo ESIPT and they have been investigated with both experimental and theoretical approaches. Since the discovery of the phenomenon in methylsalicylate by Weller in 1956, ¹⁵ and the realistic interpretation by Otterstedt¹⁶ and Kasha,¹⁷ many works have been reported. A non exhaustive list of studies includes works focussed on salicylic acid, ^{18–22} methyl salicylate, ^{23–28} salicyli-deneaniline, ^{29–32} hydroxy-acetophenones, ^{26,28,33} hydroxyindanone, 20-22,26 hydroxy flavones,^{17,34–41} (pyridyl)pyrroles, -pyrazoles and -indoles, 42-49 fluorescent protein chromogens, ^{50,51} hydroxy-benzofluorenone, 52 phenylphenol,⁵³ hydroxyphenyl-oxazole (HO),²⁸ hydroxyphenylbenzoxazoles (HBO), ^{54–69} hydroxybenzofuran-benzoxazoles (HBBO),⁷⁰ hydroxyphenyl-benzothiazole (HBT)^{54,61,62,71-80}

^a CEISAM, UMR CNRS 6230, BP 92208, Université de Nantes, 2, Rue de la Houssinière, 44322 Nantes, Cedex 3, France. Tel: +33-2-51-12-55-64; E-mail: Denis.Jacquemin@univ-nantes.fr

^b Institut de Chimie et Procédés pour l'Energie, l'Environnement et la Santé (ICPEES) UMR7515 CNRS Université de Strasbourg, 25 rue Becquerel, 67087 Strasbourg Cedex 02 (France)

^c Institut Universitaire de France, 1, rue Descartes, F-75005 Paris Cedex 05, France.

[†] Electronic Supplementary Information (ESI) available: (1) extra examples of potential energy surface/IRC; (2) comparison between TD-DFT and experimental values for the compounds of Tables 1 and 4; (3) density difference plots for selected compounds; (4) relative E^*/K^* free energies for substituted compounds and barrier for proton transfer when dual emission is foreseen.



Fig. 1 Representation of a typical ESIPT process in a typical dye.

and hydroxyphenyl-benzimidazoles (HBI). ^{56,60–62,77,81–88} The typical HBO and HBI structures, two of the most popular ESIPT cores, are displayed in Figure 2.



Fig. 2 ESIPT compounds studied herein. The X=O, X=NH and X=CH₂ structures are respectively named hydroxyphenyl-benzoxazole (HBO), -benzimidazole (HBI) and [3H]-indole (HI), respectively. $R_{1,2,3,4}$ indicate the substitution position used in this work.

ESIPT, as many excited-state processes, is difficult to rationalise using intuitive organic chemistry concepts. Indeed, the excited-state acidities and basicities governing ESIPT are related to $pK_{a/b}^{\star}$ values that cannot be easily inferred but for trivial cases. In that framework, the use of quantum theories able to treat electronically excited-states often allows to take the inner track to efficient analysis and predictions of ESIPT. Without surprise, numerous theoretical works have appeared to deal with ESIPT compounds. For tiny model molecules, advanced excited-state post-Hartree-Fock methods, e.g., equation-of-motion coupled cluster, configuration interaction and multiconfigurational self-consistent field theories, can be used, ^{20,21,53,89-92} but for "real-life" cases, density functional theory (DFT) and its time-dependent version (TD-DFT), are generally selected, ^{20,21,30,52,65,69,70,89,93–97} a choice justified by several benchmark studies demonstrating the adequacy of TD-DFT for ESIPT.^{20,21,89} The second-order Algebraic Diagrammatic Construction [ADC(2)] method was also shown to provide a valuable compromise for medium-sized molecules.^{53,68,90,98} Recently, we have used a TD-DFT protocol accounting for solvent effects to tackle two HBO⁶⁹ and seven HBBO dyes,⁷⁰ in order to rationalise why dual emission was observed only in certain compounds. For the former, we could explain the appearance of dual fluorescence upon substitution with two dialkylamino groups and obtain an estimate of the relative quantum yields of E* and K* through calculations of the vibronic couplings.⁶⁹ For the latter HBBO dyes, the relative free energies of the E* and K* computed with TD-DFT correlated almost perfectly with the emission ratio obtained experimentally.⁷⁰ In two other cases, this same level of theory allowed us to prove beyond reasonable doubts that ESIPT was not taking place, contrary to former experimental analysis.^{97,99}

Whilst there exists, as discussed above, a very large panel of experimental and theoretical studies for a vast variety of ESIPT systems, much less investigations tackled the impact of chemical substitutions on the ESIPT properties, and these works mainly focused on HBO, HBT, HBI and HBBO derivatives. 59-62,66,70,75 For HBO, the data are summarised in Table 1 (see Section 4) and two main conclusions emerge: i) adding a strong donor, e.g., NAlk₂, on the phenol side favours emission from E^* ; ii) adding strong acceptors on the benzoxazole side also yields more intense emissions from E^* . However, it should be noted that all these experimental studies typically considered only a few (ca. 1-3) derivatives, generally differing by several groups. Clearly a systematic investigation on a very large set of compounds would be welcome to obtain accurate design rules. The present contribution aims to fill this gap by using theoretical tools, shown to be effective for existing molecules, to provide a throughout investigations of substituent effects on ESIPT and dual emitters.

This paper is organised as follows: in the next Sections we briefly describe our original computational procedure combining TD-DFT and ADC(2), and detail the results for a test case for which the reaction paths were investigated. In Section 4, we provide extensive comparisons with experiments for HBO dyes before investigating numerous mono- and di-substituted compounds in Section 5. In Section 6, HBI and HI compounds are investigated before concluding.

2 Methods

Here, the structures and vibrational frequencies have been obtained with TD-DFT, the total and transition energies with ADC(2) and the solvent effects with the Polarisable Continuum Model (PCM).¹⁰⁰ The different properties (P, e.g., the fluorescence energies and the free energies) were obtained as,

$$P = P(\text{Gas}, \text{ADC}) + P(\text{PCM}, \text{TD}) - P(\text{Gas}, \text{TD}). \quad (1)$$

For all TD-DFT calculations, we have used the latest revision of the Gaussian09 program,¹⁰¹ applying default thresholds and algorithms, except when noted below. These calculations relied on the M06-2X hybrid exchange-correlation functional,¹⁰² a choice justified by previous benchmarks demonstrating the accuracy of this functional for determining both vertical and adiabatic transition energies as well as for predicting band shapes and proton transfer in HBO compounds.^{69,102–108} Here, we have applied a recently proposed approach for ESIPT⁶⁹ which is to determine the geometrical and vibrational parameters with the 6-31G(d) atomic basis set, whereas the total and transition energies are corrected with a much more extended atomic basis set, namely 6-311+G(2d,p). This combination leads nearly basis set converged values at the TD-DFT level. To achieve numerically-stable and accurate values, we have tightened self-consistent field (10^{-10} a.u.) and geometry optimisation (10^{-5} a.u.) convergence thresholds, as well as used a (99,590) pruned integration grid (so-called ultrafine grid). For each molecule, both the enol and keto ES have been fully optimised using TD-DFT analytical gradients. We have also determined the corresponding transition states on the ES potential energy surface for all experimentally available compounds and a selection of new compounds (see below). TD-DFT Hessian calculations were performed to confirm the nature of all ES structures and to determine the free energies (G).

Environmental effects (here cyclohexane, except when noted) have been accounted for using the well-known PCM.¹⁰⁰ as implemented in Gaussian09.¹⁰¹ While TD-DFT geometry optimisations, Hessian calculations, enthalpies and entropies (and hence G) have been performed with the popular linear-response PCM approach, the transition energies have been evaluated using the more accurate corrected linearresponse scheme.¹⁰⁹ This latter scheme allows to correct the cavity polarisation in the ES by accounting for the change of electron density upon electronic transition. Therefore, it allows to more accurately estimate the emission wavelengths, while remaining computationally affordable. Of course, while we applied the equilibrium PCM limit for optimisation and vibrational TD-DFT calculations (slow phenomena), fluorescence wavelengths are corrected for non-equilibrium effects (fast phenomena).

The gas phase ADC(2) total and transition energies determined on the TD-DFT structures have been obtained with the Turbomole code.¹¹⁰ These ADC(2) calculations relied on the so-called ADC(2)-s formalism¹¹¹ and used the resolution of identity technique.^{112,113} Wavefunction approaches being more sensitive to basis set effects than TD-DFT, the very extended *aug*-cc-pVTZ atomic basis set was used for all ADC(2) calculations.

3 Shape of the potential energy surfaces

To set the scope of this study, a typical shape of the energy change along the reaction coordinate is depicted in Figure 3 (see also Figure S1 in the ESI) for the $R_3=NEt_2$ ($R_{1,2,4}=H$) HBO dye (7 in Table 1).



Fig. 3 Results obtained for the HBO dye **7**. (a) Density difference plot (isovalue=0.0018 a.u.). The red/blue zones indicate an increase/decrease of the electronic density upon absorption of light. (b) Energy profile for proton transfer along the ground, excited state IRC. Energy scale is relative to the ground state enol form and is calculated at the M062X/6-31G(d) level.¹¹⁴ Bond lengths are in Å, reaction coordinate is defined in mass weighted coordinates (Bohr \sqrt{AMU}^{-1}).

We determined the intrinsic reaction coordinate (IRC) connecting the enol and keto forms through transition state in both ground and excited states using local quadratic approximation (LQA) technique.¹¹⁵ In the ground state the activation energy to go from E to K is too high and the back-reaction is nearly barrier-less, both factors confirming the presence of the enol form only, before photon absorption, a completely usual outcome for HBO structures. After excitation the molecule reaches the ES (S_1) surface, where the barrier for proton transfer is significantly smaller and K^* is now a stable isomer. However, both the difference of free energy between the K^* and E^{\star} isomers (ΔG^{ES} , see Figure 3b) and the height of the free energy barrier for ESIPT ($\Delta G^{\text{ES}\#}$, see Figure 3b) are positive and relatively large which favours emission from E^* as was also experimentally observed (see next Section). The change of electron density upon excitation can be seen on Figure 3a. The most important features are, one the one hand, the gain of density of the nitrogen atom (in red), which is connected with the stabilisation of K* form and, on the other hand, the relatively small (blue) lobe on the OH group, indicating a small change of density. For some compounds in which K^{*} is more stable than E^* , e.g., for the non-substituted structure, the density loss in the OH area can be much larger (see Figure S4 in the ESI). In Figure 3, the activation energies for both states are in accordance with Hammond postulate, i.e., GS proton transfer from K to E goes through an early TS (NH distance in TS is only 0.05 Å longer than in the optimal K geometry) which indicates very small activation energy. In contrast the geometry of TS for ESIPT supports comparable activation energies for both direct and backward reactions at the selected level of theory. We underline that the geometries of the GS and ES transition states are different. As a consequence computing only single point energies on the top of ground state IRC leads to large errors in estimating the reaction parameters (see Figure S2 in the ESI) and should be discouraged. On the other hand, 6-311+G(2d,p) ES single-point calculations obtained on the ES 6-31G(d) IRC nicely follows the path of the smaller basis set, which supports our protocol (see Figure S3 in the ESI).

4 Comparisons with experiments

In Table 1, we compare the theoretical and measured results for a series of HBO compounds, some in different media, for a total of twenty-seven cases. First, we underline that all the theoretical values reported in that Table are obtained through Eq. (1), that is, include an ADC(2) correction to the TD-DFT energies. The uncorrected TD-DFT values can be found in the ESI (Table S2). It turns out that: (i) TD-DFT tends to provide too small emission wavelengths, an effect that we relate to the selection of the M06-2X functional that yields consistent but too large transition energies;¹⁰⁴ (ii) both the TD-DFT's ΔG^{ES} and $\Delta G^{ES\#}$ are larger than their ADC(2) counterparts, indicating that TD-M06-2X tends to overestimate the stability of the E^{*} isomer in most cases – **26** being a notable exception to this general trend. As a consequence, TD-DFT provides inaccurate predictions for a series of cases, e.g., **9**, **18** and **27**, for which Eq. (1) gives reliable estimates. Consequently, we do not further discuss the "raw" TD-DFT estimate in the following.

Let us now turn towards the emission wavelengths (λ_{fl} in Table 1). First, one notes that there are serious discrepancies between experimental values obtained by different groups. For instance, for 9, the emission of E^* in dichloromethane was reported to occur at 376 nm⁶² and 390 nm,¹²⁰ a sizeable difference (0.12 eV). The two values reported for 7 in chloroform, 382 nm⁵⁹ and 451 nm,⁶⁶ are also in so strong disagreement (0.50 eV) that invoking apparatus differences or the presence of small share of impurities is not satisfying. The emission wavelength reported for the K* of 23, 656 nm, was also extracted from an oversaturated spectrum,⁶⁶ and should be considered cautiously as well. If one removes from the set the data measured in the puzzling Ref. 66, we note that the theoretical emission wavelengths are in reasonable match with experiment, a statement holding for both tautomers. Indeed, for E^* the absolute errors range from 0.04 to 0.51 eV, with an average of 0.19 eV, whereas for K^* the deviations are slightly smaller (from 0.01 to 0.16 eV with an average of 0.08 eV). These deviations are in the expected range at this level of theory.^{111,125} We note that we obtain a theory-experiment linear correlation coefficient of 0.96 for the emission energies, further justifying the selected level of theory.

For the ΔG^{ES} and $\Delta G^{\text{ES}\#}$ (see Figure 3), there are of course, no available experimental values allowing direct comparisons. However, one can see from the data listed in Table 1 that the computed free energies can nicely explain the experimental outcomes. Indeed, when a positive ΔG^{ES} is calculated, indicating that ESIPT is not a thermodynamically favoured process, only E* emission is experimentally observed. By contrast, significantly negative ΔG^{ES} (in the -0.20 to -0.30 eV range), corresponding to a strong driving force for the proton transfer, are computed for cases in which only the K^* emission was obtained experimentally. The intermediate situations (- $0.20 \text{ eV} < \Delta G^{\text{ES}} < 0.00 \text{ eV}$) are related either to dual emission or to E^{*} emission. In these intermediate cases, it was expected that relatively small ESIPT barriers, $\Delta G^{\text{ES}\#}$, would favour K^{*} emission whereas large $\Delta G^{\text{ES}\#}$ would indicate a dominating E^{*} emission. However, the number of experimental data available is too limited to provide reliable boundaries for $\Delta G^{\text{ES#}}$. Despite these interesting trends, we note some disagreements: (i) for 23 theory foresees a strongly favoured E^* , whereas experiment finds both E^{*} and K^{*} emission bands,⁶⁶ though the latter is questionable (see above); (ii) for 19, a dominating K^{*} band is observed in dichloromethane¹²³ although the computed ΔG^{ES} is positive – for the same compound in the less polar solvent (18) the trend is however correctly given by theory; (iii) for both 14 and 26 a strong K* band is observed ^{122,124} which is not reproduced by the calculations, though theory

Table 1 Available experimental values compared to theoretical simulations for HBO-ESIPT dyes. All emission wavelengths are expressed in nm, whereas the relative Gibbs energies are given in eV (see Figure 3), a negative value indicating a more stable K^* . We summarise the experimental observations, giving the approximated relative E^{*} and K^{*} intensities in the emission spectra, w and vw standing for weak and very weak contributions from the minority tautomer. CH, CHL, DCM, DIOX, HEP and 3MP stand for cyclohexane, chloroform, dichloromethane, 1,4-dioxane, *n*-heptane and 3-methylpentane, respectively.¹¹⁶

		Structu	ires			Expe	riment					Theory	
	R1	R ₂	R ₃	R4	Solv.	Observations	$\lambda_{ m fl}^{ m E^{\star}}$	$\lambda_{\mathrm{fl}}^{\mathrm{K}^{\star}}$	Ref.	$\lambda_{\mathrm{fl}}^{\mathrm{E}^{\star}}$	$\lambda_{ m fl}^{ m K^{\star}}$	ΔG^{ES}	$\Delta G^{\text{ES#}}$
ine 1	Н	Н	Н	Н	3MP	Keto		ca.480	55	_	492	-0.315	-0.146 ^a
2	Н	Н	Н	Н	CH	Keto	_	ca.490	117	-	491	-0.314	-0.144
3	Н	Η	Н	Н	CHL	Keto	—	ca.489	59	-	482	-0.303	-0.119
4	Н	Н	Н	NH_2	DCM	Keto $(4/5)$ + Enol $(1/5)$	442	565	62	460	593	-0.078	-0.079
						Keto	_	551	118				
5	Н	Н	Н	CHO	CHL	Keto + vw Enol	ca.405	474	119	352	455	-0.280	-0.072
6	Н	Н	Н	CHO	DIOX	Keto	_	483	119	-	463	-0.292	-0.091
7	Н	Н	NEt ₂	Н	CHL	Enol	382		59	377	—	0.087	0.176
						Enol	451		66				
8	Н	Н	NEt ₂	Н	DIOX	Enol	471		66	373	—	0.023	0.159
9	Н	Н	NH ₂	Н	DCM	Keto (7/8) + Enol (1/8)	376	467	62	359	458	-0.055	0.072
						Keto (3/5) + Enol (2/5)	390	460	120				
10	Н	Н	NH_2	Н	CHL	Keto $(3/4)$ + Enol $(1/4)$	390	460	120	357	464	-0.086	0.054
11	Н	Н	NH_2	Н	DIOX	Keto $(3/4)$ + Enol $(1/4)$	415	487	121	354	478	-0.150	0.019
12	Н	Н	OMe	Н	CHL	Keto + vw Enol	ca. 375	ca. 467	59	351	488	-0.241	-0.019
13	Н	Н	Me	Н	3MP	Keto	_	ca.480	55	-	505	-0.297	-0.125
14	Н	$C=C(CN)_2$	Н	Н	CH	Keto + w Enol	ca. 425	ca. 550	122	408	586	0.083	0.074
15	Н	$C=C(CN)_2$	Н	Н	CHL	Keto + Enol	ca. 450	ca. 625	122	425	642	-0.032	0.173
16	Н	CHO	Н	Н	CHL	Keto	_	ca. 517	59	-	500	-0.202	-0.082
17	Н	COOEt	Н	Н	CHL	Keto	_	ca. 495	59	-	497	-0.254	-0.100
18	Η	NH ₂	Н	Н	HEP	Keto + vw Enol	390	500	123	376	481	-0.065	0.012
19	Н	NH ₂	Н	Н	DCM	Keto (9/10) + Enol (1/10)	420	485	123	399	468	0.037	0.085 <
20	Н	COOEt	NEt ₂	Н	CHL	Enol	421		59	401	_	0.188	0.245
21	Η	COOEt	OMe	Н	CHL	Keto + vw Enol	ca. 375	ca. 482	59	365	505	-0.202	0.012
22	Η	NH ₂	NEt ₂	Н	DIOX	Enol	460	_	66	389	_	0.146	0.201
23	Н	NO_2	NEt ₂	Н	DIOX	Keto + Enol	476	656	66	434	550	0.327	0.353
24	NH_2	Н	NEt ₂	Н	DIOX	Enol	440		66	389	_	0.129	0.216
25	NO_2	Н	NEt ₂	Н	DIOX	Enol	440		66	435	_	0.356	0.297
26	NH_2	Н	Н	Н	HEP	Keto (9/10) + Enol (1/10)	400	500	124	406	488	0.054	0.182
27	NH ₂	Н	Н	Н	DCM	Enol + vw Keto	450	ca. 480	124	432	474	0.076	0.197

Chemical Science Accepted Manuscript

^aA negative barrier indicates a barrierless process on the free energy surface. The transition states can nevertheless be found on the energy surface.

again provides the correct results in other media (15 and 27). At this stage, we can logically attribute the latter problems to the limitations of the PCM solvation approach, rather than to the inadequacy of the electronic structure description. To further improve the accuracy of the ΔG^{ES} , one would therefore probably need to explicitly model solvent molecules, a task beyond our scope here. We recall that we have selected only non-protic solvents to be within the range of applicability of the PCM model. In addition, there is an overall high degree of correlation between the estimated theoretical free energies and the experimental observations, but for a few exceptions

(ca. 15% of the cases). Consistently with one of our previous work devoted to HBBO,⁷⁰ we note that dual emission can only be obtained in a narrow energetic window, as the E* and K* energies should only differ by ca. 0.00 to -0.20 eV. This hints that only subtle and well-thought chemical substitutions should be used.

In short, this investigation demonstrated the robustness of the proposed protocol: the theoretical emission wavelengths present the expected accuracy at the selected level of theory, whereas the computed relative excited-state free energies allow predicting the experimental outcome (enol, keto or dual emission) in the vast majority (85%) of cases.

5 Substitution effects

In this Section, we investigate the impact of 6 auxochromic groups, CN, CF₃, F, OMe, NH₂ and NMe₂ [a set that was selected to contain both electron-donating groups (EDG) and electron-withdrawing groups (EWG) of different strengths and natures] considering various substitution positions (R₁, R₂, R₃ and/or R₄, see Fig. 2). First, a systematic investigation of singly-substituted HBO derivatives is performed to unravel the impact of each substituent. Next, we assess combination effects by tackling doubly-substituted HBO with substituents at both R₁ and R₃ positions. To have a clearer view of the substituent effects, we report in the body of the text the relative free energies contribution [$\Delta(\Delta G_{R_x})$, x=1, 2, 3 and/or 4] with respect to the non-substituted case,

$$\Delta(\Delta G_{R_x}^{ES}) = \Delta G_{R_x}^{ES} - \Delta G_{non-substituted}^{ES}$$
(2)

The interested reader can find the $\Delta G_{R_x}^{ES}$ in the ESI (Table S2).

5.1 Singly-substituted

In Table 2, we list the energetic contributions to the relative stability of both forms and the computed emission wavelengths for the emissive species. A negative (positive) value indicates that the K^{*} form is relatively stabilised (unstabilised) by the substitution compared to the non-substituted HBO dye. Let us first discuss the impact of EWG. When located on the benzoxazole side, acceptor groups systematically decrease the stability of the keto isomer. Indeed, such substitution decreases the electronic density on the nitrogen atom, and hence its basicity (see Figure S4 and associated comments in the ESI). At the R₂ para position, the largest effect is obtained with the mesomeric cyano substitutent, whereas at the R₁ meta position, the strongest impact is obtained with the inductive trifluoromethyl group. In contrast, adding a EWG on the phenol side can favour both the E^* and K^* tautomers. At the *para* position (R_4), both CF₃ and CN stabilises the K^{*} form. whereas the fluoro substitution surprisingly yields the reverse trend. At the *meta* position (R_3) , the mesomeric CN group stabilises E^* , whereas inductive EWG yield the opposite effect. Whilst some EWG reduce the energetic difference between the two isomers, their effect is too limited to change the trend obtained for the unsubstituted HBO compound, and only K^{*} emission is predicted in all cases (red background in Table 2).

Let us now turn to EDG. One first notes that, irrespective of their position, donor groups systematically stabilise the E^* form, and consequently, tend to yield dual or sole E^* emission. The magnitude of this stabilisation is (much) larger than for the EWG and follows the logical OMe $< NH_2 <$

6 |

Table 2 Theoretical results for HBO dyes in cyclohexane. Top: relative Gibbs energy differences with respect to the non-substituted HBO, $\Delta(\Delta G_{R_x}^{ES})$ in eV, a negative value indicating that substitution relatively favours the K* form (see Table S2 in the ESI for $\Delta G_{R_x}^{ES}$ that can be obtained by adding -0.314 eV to the value reported here). Bottom: E*/K* emission wavelengths ($\lambda_{fl}^{E^*} / \lambda_{fl}^{K^*}$ in nm) for the isomers that are predicted to be present. The background colour indicates the predicted emission based on the $\Delta G_{R_x}^{E_x}$: red/green/white background corresponding to sole K*/sole E*/dual fluorescence.

$\Delta(\Delta G_{\rm Rx}^{\rm ES})$	R ₁	R ₂	R ₃	R ₄
CN	0.038	0.068	0.053	-0.009
CF ₃	0.061	0.029	-0.035	-0.036
F	0.039	0.029	-0.022	0.060
Н	0.000	0.000	0.000	0.000
OMe	0.150	0.130	0.127	0.110
NH ₂	0.370	0.257	0.153	0.313
NMe ₂	0.540	0.405	0.318	0.364
$\lambda_{ m fl}^{ m E^{\star}}$ / $\lambda_{ m fl}^{ m K^{\star}}$	R ₁	R ₂	R ₃	R ₄
ine CN	<i>— /</i> 506	— <i>/</i> 513	<i>— </i> 494	<i>— </i> 479
CF ₃	<i>— /</i> 502	— / 505	<i>— </i> 498	<i>— </i> 491
F	<i>— /</i> 496	<i>— /</i> 492	— <i>/</i> 469	<i>— /</i> 510
Н	— <i>/</i> 491	<i>— </i> 491	<i>— </i> 491	— <i>/</i> 491
OMe	364 / 488	361 / 483	349 / 452	406 / 582
NH ₂	407 / —	377 / 480	354 / 480	441 / 579

NMe2 ranking. Of course, for substitutions on the phenol side, these results were expected, i.e., adding EDG increases the ES electron density on the hydroxyl and consequently reduces its acidity, the effect being larger for the para than meta positions (see the ESI). More surprising is the fact that EDG yield a similar effect when substituting on the benzoxazole moiety, the magnitude of the E^{*} stabilisation being even larger. Indeed, chemical intuition would have led to foresee that EDG would increase the basicity of the nitrogen centre and hence strengthen the ESIPT process. In Figure S4 in the ESI, the density difference plots allow to explain the unexpected outcome: EDG at R1 and R2 actually decrease the acidity of the phenol (in the excited-state) by localising the excited-state on the benzoxazole side, the change of density on the hydroxyl after absorption becoming too small to favour ESIPT. One also notices that this impact is slightly larger at R_1 than R_2 positions, consistently with the values of Table 2. With EDG, two different emission patterns can be obtained: (i) pure E^* emission for the strongest stabilisation (e.g., NMe₂ group at R_1 , R_2 , and R_4 position); (ii) dual emission with groups that present an intermediate contribution to the E* stabilisation, enabling to obtain a ΔG^{ES} in the energetic window determined in Section 4 (-0.20 - 0.00 eV). For these latter cases, we systematically computed the energetic barrier separating the E* to K^{*}, $\Delta G^{\text{ES}\#}$. The values are listed in the ESI (Table S2) and do not exceed 0.129 eV, indicating that proton transfer can actually take place. Indeed, this value is smaller than the barrier

obtained in Section 4 for compound **15** ($\Delta G^{\text{ES#}}=0.173 \text{ eV}$) that experimentally displays dual emission.

As discussed in Section 1, another attractive feature of ES-IPT dyes is the possibility to redshift the emission due to the strong geometrical reorganisation following absorption. Of course, designing such compounds first requires that emission from the K^{*} form is actually possible. For example, while the most red-shifted emission predicted by theory was obtained with the NMe₂ EDG at R₄, this dye is inadequate as only the E^{*} tautomer emits, as explained above. Amongst the derivatives displaying an emissive keto isomer, the most red-shifted bands (ca. 580 nm, a rather long wavelength for compact compounds) are obtained for HBO presenting a OMe or NH₂ group at R₄.

5.2 Doubly-substituted

We investigate in this Section, the combination of substitutions at both R₁ and R₃ positions, these two position being selected as they yield diverse outcomes (see Table 2). Our data are reported in Table 3. To facilitate the discussion, we have also reported in the ESI (Table S3) the additive contributions, $\Delta(\Delta G_{R_1,R_3}^{ES})_{add}$, that have been obtained by summing the single contributions, $\Delta(\Delta G_{R_3}^{ES})$ reported in Table 2.

When comparing the results in Tables 3 and S3, one first observes a similar prediction in the emission profile, i.e., the same background colour patterns are found, hinting a qualitatively additive trend. Other conclusions emerge: (i) combining two EWG only slightly tunes the relative energies, and only K* emission is obtained; (ii) inserting EDG that strongly stabilise E* (NH₂ at R₁ and NMe₂ at both R₁ or R₃) yields a sole E* emission, irrespective of the second substituent, that is unable to counterbalance the effect; (iii) for the remaining cases, e.g., R₃=OMe or NH₂ with EWG at R₁, dual emission is likely to occur. For these latter compounds, the ESIPT barrier, $\Delta G^{\text{ES#}}$, was computed and the results are listed in Table S4 in the ESI. As in the singly-substituted group, all barriers are relatively small (< 0.14 eV).

Despite the qualitative parallelism between the results of Tables 2 and 3, a quantitatively additive pattern is clearly not obtained. Indeed, the absolute differences between the computed and additive energetic contributions, show both a large spread (from 0.002 to 0.291 eV) and a non-negligible average (0.067 eV). We found that substantial discrepancies are obtained for the series presenting a NH₂ or a NMe₂ group at R₁, with deviations from additivity ranging from 0.059 to 0.291 eV; largest difference being obtained for dye bearing two NMe₂ groups. For the other compounds, the maximal discrepancy only attains 0.074 eV (with an average of 0.026 eV) but changes of sign between the computed and additive contributions are obtained for dyes presenting a calculated negative $\Delta(\Delta G_{R_1,R_3}^{ES})$ – the additive approach systematically

providing positive values for this parameter. For instance, the R₁=CF₃,R₃=F dye presents a $\Delta(\Delta G_{R_1,R_3}^{ES})$ of -0.012 eV whereas simple addition of substituent effects foresees a free energy difference of 0.039 eV compared to the unsubstituted HBO.

Regarding the emission wavelengths, one notes that the most redshifted values are obtained for the HBO derivatives presenting a strong EWG (CN or CF₃) at R_1 combined to another active group at R_3 . The redshift is nevertheless smaller than in the HBO dye substituted by a single OMe or NH₂ group at R_4 (see previous Section). This result is related to the fact that HBO dyes developing a strong push-pull character, known to yield bathochromic shifts, are not subject to ESIPT and do not show K^{*} emission.

6 Impact of the heteroatom

In this Section, we investigate the impact of the core on both the relative stabilities and spectra of the enol and keto forms by replacing the heteroatom (X=O atom in Figure 2) by X=NH or X=CH₂. The same two-step methodology as in Section 5 is applied: (i) we first compare the theoretical and measured results for experimentally available data; (ii) we perform a systematic study of the impact of single-substitution using the same auxochromes in the same solvent as above.

6.1 Benzimidazoles

As in Section 4, let us first compare the available experimental data to ADC(2)-corrected theoretical results for a series of HBI compounds (see Table 4). The TD-DFT values can be found in the ESI (Table S1) and as for HBO series, it turns out that TD-DFT overestimates both the transition energies (too small emission wavelengths) and the stability of the E^* isomer $(\Delta G^{\text{ES}} \text{ and } \Delta G^{\text{ES}\#} \text{ being too large compared to the ADC(2)}$ values). The theoretical emission wavelengths are in good agreement with experiments except for 37 for which the error attains 0.72 eV. However, one can wonder if the attribution of the emission band to E*, suggested in Ref. 62, is valid. Indeed, while the theoretical $\lambda_{fl}^{E^{\star}}$ (at 354 nm) clearly does not match the observed band peaking at 445 nm, the calculated emission wavelength for the K^{*} isomer at 440 nm perfectly fits the measurement. Except for this case, the absolute errors for the E^{\star} form (from 0.02 to 0.47 eV) and the K^{\star} tautomer (from 0.03 to 0.14 eV) are rather similar to those obtained for HBO derivatives. The average error for emission energies for the data reported in Table 2 is 0.10 eV.

Comparing the experimental emission profiles with the computed relative stabilities of the tautomers, we found the same energetic criteria as for the HBO structure: (i) an unique K^* emission band is observed when the Gibbs energy difference in the ES is strongly negative (in the -0.20 to -0.40 eV);

Chemical Science Accepted Manuscript

				$\Delta(\Delta G_{\mathbf{R}_1,\mathbf{R}_3}^{\mathbf{ES}})$				
$R_1 \downarrow \backslash R_3 \rightarrow$	CN	CF ₃	F	H H	OMe	NH ₂	NMe ₂	
CN	0.071	-0.027	-0.014	0.038	0.154	0.180	0.350	
CF ₃	0.071	0.002	-0.012	0.061	0.164	0.206	0.333	
F	0.090	-0.006	0.023	0.039	0.176	0.198	0.371	
Н	0.053	-0.035	-0.022	0.000	0.127	0.153	0.318	
OMe	0.272	0.189	0.183	0.150	0.273	0.289	0.409	
NH ₂	0.522	0.469	0.407	0.370	0.397	0.345	0.440	
NMe ₂	0.742	0.672	0.584	0.540	0.552	0.520	0.567	
	$\lambda_{\mathrm{fl}}^{\mathrm{E}^\star}$ / $\lambda_{\mathrm{fl}}^{\mathrm{K}^\star}$							
				$\lambda_{\rm fl}^{\rm E^{\circ}} / \lambda_{\rm fl}^{\rm K^{\circ}}$				
$R_1 \setminus R_3$	CN	CF ₃	F	$\lambda_{\rm fl}^{\rm E^{*}} / \lambda_{\rm fl}^{\rm K^{*}}$	OMe	NH ₂	NMe ₂	
$\frac{R_1 \setminus R_3}{CN}$	CN —/504	CF ₃ —/513	F —/485		OMe 350/467	NH ₂ 356/502	NMe ₂ 312/—	
		5	-	Н		2	2	
CN	/504	<u> </u>	/485	Н —/506	350/467	356/502	312/—	
CN CF ₃	—/504 —/500	/513 /508	/485 /480	H —/506 —/502	350/467 349/462	356/502 354/496	312/— 369/—	
CN CF ₃ F	—/504 —/500 —/498	—/513 —/508 —/504	—/485 —/480 —/474	H —/506 —/502 —/496	350/467 349/462 353/457	356/502 354/496 359/487	312/— 369/— 372/—	
CN CF ₃ F H	—/504 —/500 —/498 —/494	—/513 —/508 —/504 —/498	—/485 —/480 —/474 —/469	H —/506 —/502 —/496 —/491	350/467 349/462 353/457 349/452	356/502 354/496 359/487 354/480	312/— 369/— 372/— 367/—	

Table 3 Theoretical results for doubly-substituted HBO dyes in cyclohexane. See caption of Table 2 for more details.

Table 4 Available experimental values compared to theoretical simulations for HBI-ESIPT dyes. See caption of Table 1 for more details.

		S	tructures			-	Experimen	t]	Theory	
	R ₁	R ₂	R ₃	R ₄	Solv.	Observations	$\lambda_{ m fl}^{ m E^{\star}}$	$\lambda_{ m fl}^{ m K^\star}$	Ref.	$\lambda_{\mathrm{fl}}^{\mathrm{E}^{\star}}$	$\lambda_{ m fl}^{ m K^{\star}}$	ΔG^{ES}	$\Delta G^{\text{ES#}}$
28	Н	Н	Н	Н	CH	Keto		470	117	-	479	-0.388	-0.127
						Keto	_	ca. 470	77				
29	Н	Η	Н	Н	DIOX	Keto + vwEnol	350	468	81	345	473	-0.393	-0.125
30	Н	Η	Н	NH ₂	DCM	Keto	_	539	118	-	571	-0.213	-0.144
						Keto + vwEnol	414	544	62				
31	Н	Η	Н	NH_2	DIOX	Keto + Enol	414	568	81	428	564	-0.158	-0.125
32	Н	Н	Н	OMe	DIOX	Keto + vwEnol	368	530	81	395	560	-0.345	-0.123
33	Н	Η	Н	OH	DIOX	Keto + vwEnol	358	525	81	388	537	-0.319	-0.170
34	Н	Η	Н	Me	DIOX	Keto + vwEnol	352	489	81	354	501	-0.353	-0.114
35	Н	Η	Н	Cl	DIOX	Keto	_	474	81	-	489	-0.379	-0.129
36	Н	Η	Н	F	DIOX	Keto + vwEnol	350	486	81	361	497	-0.362	-0.166
37	Н	Н	NH_2	Н	DCM	Enol ^a	445		62	354	440	-0.170	-0.083
38	Н	Н	NEt ₂	Н	CH	Keto + wEnol	ca. 370	ca. 453	82	368	460	-0.072	0.067
39	Н	Н	NEt ₂	Н	DIOX	Enol	386	_	84	368	_	-0.079	0.131
40	Н	NH_2	NEt ₂	Н	DIOX	Enol	431	_	84	382	_	0.054	0.115
41	Н	NO_2	NEt ₂	Н	DIOX	Keto + vwEnol	_	531	84	-	489	-0.214	-0.244

^a We report the form that is *probably* emitting according to Ref. 62

(ii) a positive ΔG^{ES} indicates that the enol isomer is the only emissive species; (iii) an intermediate situation, -0.20 eV < ΔG^{ES} < 0.00 eV, is observed for both **31** and **38** that actually display dual emission. However, one notes a disagreement for **39** in 1,4-dioxane, that also presents an intermediate ΔG^{ES} though only emission from E^{*} is observed. As in Section 4, we highlight that the correct trend is obtained for the same compound in cyclohexane, so that this discrepancy can be attributed to the limitation of the continuum environmental model. Overall, theoretical results are consistent with the

experimental outcomes for 12 out of 13 cases (> 90 % of the cases) which confirms here again the robustness of the computational protocol.

We now compare the experimental observations for similar HBO (see Table 1) and HBI (see Table 4) derivatives considered in the same solvent, i.e., 2 / 28, 7 / 39 and 4 / 30. The two former display the same emission profile but for the latter couple, a substantial dual emission (4/5 K^{*} + 1/5 E^{*}) is obtained with X=O whereas the spectrum of the compound with X=NH displays a negligible E^{*} band. Consequently, re-

placing the benzoxazole with a benzimidazole core tends to stabilise K^{*} and hence to favour the ESIPT process, a fact that is confirmed theoretically. Indeed, for the three couples cited above, but also for all the singly-substituted derivatives, the ΔG^{ES} values are systematically more negative for the HBI structures than for their HBO counterparts (see Table S2 in the ESI). For instance, for the non-substituted compounds, we computed a ΔG^{ES} of -0.314 eV and -0.388 eV for HBO and HBI, respectively.

In Table 5, the counterpart of Table 2, we report the emission wavelengths of the emissive species and the relative contributions of each substituent for HBI dyes. The $\Delta G_{R_x}^{ES}$ values are reported in the ESI (Table S2). Let us first discuss acceptor groups. When located on the benzimidazole side, EWG slightly decrease the relative stability of the keto isomer (similarly to the benzoxazoles), except for R_2 =CF₃ that yields a reverse trend, that is, a negative contribution corresponding to a K^{*} stabilisation. With respect to HBO, the impact of the CF₃ group at R₁ is reduced in HBI whereas those of the CN and F groups are similar. At the R_2 para position to the nitrogen atom involved in the ESIPT process, the impact of all EWG is smaller than in the corresponding HBO structure, though the largest effect being still obtained with the strong mesomeric cyano group. For the phenol substitution, a stabilisation of the keto isomer is obtained for both the mesomeric CN group at the R₄ para position and the strong inductive CF₃ group at both R₃ and R₄, the latter auxochrome having a large quantitative impact. The other substitution patterns tend to decrease the stabilisation of the keto isomer. However, like in the HBO series, the impacts of EWG remain too limited to significantly tune the tautomeric equilibrium and the same emission profile as for the non-substituted compound is systematically predicted.

Similarly to the HBO series, EDG systematically decrease the stability of the K^{*} isomer with a magnitude in line with their donating strength, that is, OMe < NH₂ < NMe₂, the effect being stronger when substituting the benzimidazole side. Dual emission is likely to occur for intermediate auxochromic contributions (in the 0.188 - 0.388 eV range), i.e. for NH₂ at R₁, R₂ and R₄ positions and for NMe₂ on both positions of the phenol ring. As the K^{*} form is more stabilised in the unsubstituted HBI than HBO derivative, it is well-understandable that donor groups with a stronger impact have to be selected to reach dual emission with the former core.

In Table 5, the most red-shifted fluorescence wavelength (604 nm) is obtained for the K^{*} fluorescence of the R₄=NMe₂ derivative. This substitution, that likely yields dual emission, indeed provides the most red-shifted emission of all HBO and HBI compounds investigated and therefore stands as a valuable candidate for synthesis.

Table 5 Theoretical results for a series of HBI dyes in cyclohexane: substituent effects. See caption of Table 2 for more details. The $\Delta G^{\rm ES}$ of the unsubstituted HBI is -0.388 eV, and this value should be added to the $\Delta (\Delta G^{\rm ES}_{R_x}$ reported at the top to obtain the $\Delta G^{\rm ES}_{R_x}$ (see also Table S2 in the ESI).

$\Delta(\Delta G_{\rm Rx}^{\rm ES})$	R ₁	R ₂	R ₃	R ₄
CN	0.035	0.038	0.032	-0.010
CF ₃	0.014	-0.011	-0.029	-0.064
F	0.044	0.014	0.027	0.026
Н	0.000	0.000	0.000	0.000
OMe	0.150	0.120	0.128	0.042
NH ₂	0.378	0.236	0.169	0.231
NMe ₂	0.528	0.417	0.377	0.262
$\lambda_{\mathrm{fl}}^{\mathrm{E}^{\star}}$ / $\lambda_{\mathrm{fl}}^{\mathrm{K}^{\star}}$	R ₁	R ₂	R ₃	R ₄
$\lambda_{\rm fl}^{\rm E^{\star}} / \lambda_{\rm fl}^{\rm K^{\star}}$ ine CN	R ₁ — / 499	R ₂ — / 497	R ₃ — / 482	R ₄ — / 459
		-	5	
ine CN	/ 499	/497	— / 4 82	— <i>/</i> 459
ine CN CF ₃	— / 499 — / 487	— / 497 — / 488	— / 482 — / 481	— / 459 — / 469
ine CN CF ₃ F	— / 499 — / 487 — / 483	— / 497 — / 488 — / 475	— / 482 — / 481 — / 458	— / 459 — / 469 — / 498
ine CN CF ₃ F H	-/499 -/487 -/483 -/479	/ 497 / 488 / 475 / 479	/ 482 / 481 / 458 / 479	/ 459 / 469 / 498 / 479

6.2 3H-indoles

We finally describe the impact of substitution on HI and compare the results to the two preceding series. To the best of our knowledge, they are no experimentally available data for HI (X=CH₂ in Figure 2) derivatives. In Table 6, we report the computed emission wavelengths and the relative free energies contributions for these compounds. One notices that the values in that Table are systematically more negative for HI than for both HBO and HBI compounds. This effect is far from negligible, e.g., the free energy difference of the non-substituted HI is -0.463 eV whereas the computed ΔG^{ES} are -0.314 eV and -0.388 eV for HBO and HBI, respectively. Therefore the use of 3H-indole tends to strongly favour ESIPT and hence the emission from the K^{*} isomer.

We note that the impact of EWG on HI dyes is slightly smaller than in HBO and of the same order of magnitude as in HBI. Like above, EWG on the 3H-indole side favours the enol, whereas substitution on phenol moiety can induce E^* or K^* stabilisation. For all EWG-substituted HI, theory predicts a sole emission from the K^* tautomer, which is consistent with their relatively weak absolute effect. Adding EDG provides larger changes, with a magnitude that can be smaller (e.g., at R_1) or larger (e.g., at R_4) than in HBI derivatives. To reach dual emission, it is mandatory to add strong amino donor groups, that yield a significant stabilisation of E^* . However, in contrast with HBI, a R_3 =NMe₂ substitution is not sufficient to significantly counter the ESIPT trend. Interestingly, all HI compounds display significantly redshifted emission compared to the other series. The fluorescence wavelengths deter-

Table 6 Theoretical results for a series of HI dyes in cyclohexane. To determine the nature of the emission, we used the same energetic windows as for both HBO and HBI. See caption of Table 2 for more details. The ΔG^{ES} of the unsubstituted HBI is -0.463 eV, and this value should be added to the $\Delta (\Delta G^{\text{ES}}_{R_x}$ reported at the top to obtain the $\Delta G^{\text{ES}}_{R_x}$ (see also Table S2 in the ESI).

$\Delta(\Delta G_{\rm Rx}^{\rm ES})$	R ₁	R ₂	R ₃	R4
CN	0.024	0.060	0.038	-0.009
CF ₃	0.042	0.014	-0.021	-0.022
F	0.034	0.029	0.009	0.036
Н	0.000	0.000	0.000	0.000
OMe	0.144	0.165	0.151	0.115
NH ₂	0.281	0.280	0.127	0.320
NMe ₂	0.437	0.455	0.238	0.292
$\lambda_{\mathrm{fl}}^{\mathrm{E}^{\star}}$ / $\lambda_{\mathrm{fl}}^{\mathrm{K}^{\star}}$	R ₁	R ₂	R ₃	R4
$\lambda_{\rm fl}^{\rm E^{\star}} / \lambda_{\rm fl}^{\rm K^{\star}}$ ine CN	R ₁ -/ 570	R ₂ -/ 557	R ₃ -/527	R ₄ -/ 526
		-	5	
ine CN	-/570	-/ 557	-/ 527	-/ 526
ine CN CF ₃	/ 570 / 567	-/ 557 -/ 553	- / 527 - / 547	- / 526 - / 547
ine CN CF ₃ F	- / 570 - / 567 - / 562	-/ 557 -/ 553 -/ 562	- / 527 - / 547 - / 527	- / 526 - / 547 - / 552
ine CN CF ₃ F H	- / 570 - / 567 - / 562 - / 555	-/ 557 -/ 553 -/ 562 -/ 555	- / 527 - / 547 - / 527 - / 555	- / 526 - / 547 - / 552 - / 555

mined for the OMe, NH_2 and NMe_2 groups at R_4 now attain 643, 624 and 680 nm, respectively. Therefore, starting from a dye core strongly favouring ESIPT, but frustrating the proton transfer through the addition of very strong donor groups, allows reaching both dual emission and strong bathochromic shifts in the same molecule. To our knowledge, such strategy was not extensively considered previously.

7 Conclusions and Outlook

We have investigated a large number (> 110) of potential ES-IPT dyes belonging to the HBO, HBI and HI families with a focus on the impact of chemical substitutions. To reach reliable ab initio predictions, we used an advanced computational protocol in which the structures and vibrational parameters are determined with TD-DFT, the total and transition energies with ADC(2) and the environmental effects with PCM. First, by comparing experimental and theoretical values for more than 40 cases for which fluorescence spectra have been measured, we found that theory was able to deliver reasonably accurate fluorescence wavelengths, and more importantly, allows to predict the experimental spectroscopic outcome (enol, keto or dual emission) with a very good consistency. Indeed, the relative free energies of the two tautomers at the excitedstate provides the correct prediction in more than 85% of the cases, the remaining discrepancies being mostly attributable to the limitations of continuum solvation approaches. Second, we defined an energetic window corresponding to dual emission and found that is was quite narrow for this family of compounds (K^* more stable than E^* , by 0.00 to -0.20 eV), indicating that subtle substitutions patterns need to be found. Third, we showed that going from HBO to HBI and next HI core induces systematic stabilisation of K* tautomer compared to E^* form, and does not significantly perturb the effect of the substituents. Fourth, it turns out that adding acceptor groups yields relatively limited variations, and a stabilisation of the K^* or the E^* isomer can be obtained depending on the substitution side. In contrast, adding donor groups systematically favours E* form, and hence limits ESIPT, irrespective of the substitution side. This unexpected result was explained by examining the localisation of the excited-state given by density difference plots. Fifth, we have also shown that combining two substituents does not give simple additive effects. Notably when a strong pushing group is present, adding a second donor has a rather limited impact on the tautomeric equilibrium.

Going across Tables 2, 3, 5 and 6, we found 32 relatively simple compounds (single or double substitutions) that are predicted to display a dual emission behaviour. In Table 2, one notices that the methoxy substituent is predicted to yield dual emission in HBO irrespective of its position, and we can relate this finding to the fact that HBBO derivatives, that can be viewed as extended HBO with an additional oxygen atom are known to show dual emission.⁷⁰ At this stage, we can therefore recommend these compounds for synthesis, experimental spectroscopic characterisations and feedback. One also finds a few (4) compounds with predicted emission wavelengths larger than 600 nm, a remarkably high value for relatively compact molecules. For instance, the R_4 =NMe₂ X=CH₂ derivative, dual emission are predicted at 540 and 680 nm, which seems promising to design a ratiometric probe in a biological environment.

Finally, let us comment on environmental effects. First, the extreme sensitivity of several dyes to the used solvent (see the results of Table 1) makes these compounds particularly appealing for applications as probes, but also extremely challenging for theoretical modelling. It is rather clear that more advanced solvation model, including the consideration of dynamical effects and the explicit characterisation of hydrogen bonds, will have to be used in the future to obtain accurate theoretical insights regarding the specific solvatochromic effects. Secondly, one further theoretical challenge to be tackled is the estimation of possible (dual-)emission in the solidstate.¹⁴ While there are experimental examples of efficient solid-state ESIPT-based dual emitters,⁷⁰ the modelling of the crystal-packing effects on the emission of these derivatives remains to be performed. We note that first simulations, devoted to absorption, already appeared, ³⁰ but more would certainly be necessary in the framework of optimising actual devices.

Acknowledgement

C.A. acknowledges the support of the Agence National de La Recherche (ANR - EMA grant) for her PhD grant. S.B.. acknowledges the support of the European Research Council (ERC - Marches 278845 grant) for his post-doctoral grant. D.J. acknowledges the ERC for financial support in the framework of Starting Grant (Marches - 278845). The authors thank the *Région des Pays de la Loire* for the LUMOMAT RFI project. This research used resources of the GENCI-CINES/IDRIS, of the CCIPL (*Centre de Calcul Intensif des Pays de Loire*) and of a local Troy cluster.

References

- 1 A. Heller and D. L. Williams, J. Phys. Chem., 1970, 74, 4473–4480.
- 2 J. Wu, W. Liu, J. Ge, H. Zhang and P. Wang, *Chem. Soc. Rev.*, 2011, **40**, 3483–3495.
- 3 O. K. Abou-Zied, R. Jimenez, E. H. Z. Thompson, D. P. Millar and F. E. Romesberg, *J. Phys. Chem. A*, 2002, **106**, 3665–3672.
- 4 W.-H. Chen and Y. Pang, Tetrahedron Lett., 2010, 51, 1914–1918.
- 5 J. Zhao, S. Ji, Y. Chen, H. Guo and P. Yang, *Phys. Chem. Chem. Phys.*, 2012, **14**, 8803–8817.
- 6 T. Mutai, H. Sawatani, T. Shida, H. Shono and K. Araki, J. Org. Chem., 2013, 78, 2482–2489.
- 7 N. Suzuki, A. Fukazawa, K. Nagura, S. Saito, H. Kitoh-Nishioka, D. Yokogawa, S. Irle and S. Yamaguchi, *Angew. Chem. Int. Ed.*, 2014, 53, 8231–8235.
- 8 W. Zhang, Y. Yan, J. Gu, J. Yao and Y. S. Zhao, Angew. Chem. Int. Ed., 2015, 54, 7125–7129.
- 9 S. Park, O.-H. Kwon, S. Kim, S. Park, M.-G. Choi, M. Cha, S. Y. Park and D.-J. Jang, J. Am. Chem. Soc., 2005, 127, 10070–10074.
- 10 M. J. Paterson, M. A. Robb, L. Blancafort and A. D. DeBellis, J. Phys. Chem. A, 2005, 109, 7527–7537.
- 11 K. I. Sakai, T. Tsuzuki, Y. Itoh, M. Ichikawa and Y. Taniguchi, *Appl. Phys. Lett.*, 2005, **86**, 081103.
- 12 W. Chen, B. D. Wright and Y. Pang, Chem. Commun., 2012, 48, 3824– 3826.
- 13 V. S. Patil, V. S. Padalkar, A. B. Tathe and N. Sekar, *Dyes Pigm.*, 2013, 98, 507 – 517.
- 14 V. S. Padalkar and S. Seki, Chem. Soc. Rev., 2016, 45, 169-202.
- 15 A. Weller, Z.Elektrochem., 1956, 60, 1144–1147.
- 16 J. E. A. Otterstedt, J. Chem. Phys., 1973, 58, 5716-5725.
- 17 P. K. Sengupta and M. Kasha, Chem. Phys. Lett., 1979, 68, 382-385.
- 18 P. B. Bisht, H. Petek, K. Yoshihara and U. Nagashima, J. Chem. Phys., 1995, 103, 5290–5307.
- 19 F. Lahmani and A. Zehnacker-Rentien, J. Phys. Chem. A, 1997, 101, 6141–6147.
- 20 A. J. A. Aquino, H. Lischka and C. Hattig, J. Phys. Chem. A, 2005, 109, 3201–3208.
- 21 A. J. A. Aquino, F. Plasser, M. Barbatti and H. Lischka, Croat. Chem. Acta, 2009, 82, 105–114.
- 22 A. L. Sobolewski, D. Shemesh and W. Domcke, J. Phys. Chem. A, 2009, 113, 542–550.
- 23 L. A. Heimbrook, J. E. Kenny, B. E. Kohler and G. W. Scott, J. Chem. Phys., 1981, 75, 5201–5203.
- 24 P. M. Felker, W. R. Lambert and A. H. Zewail, J. Chem. Phys., 1982, 77, 1603–1605.
- 25 L. Heimbrook, J. E. Kenny, B. E. Kohler and G. W. Scott, J. Phys. Chem., 1983, 87, 280–289.

- 26 T. Nishiya, S. Yamauchi, N. Hirota, M. Baba and I. Hanazaki, J. Phys. Chem., 1986, 90, 5730–5735.
- 27 J. L. Herek, S. Pedersen, L. Banares and A. H. Zewail, J. Chem. Phys., 1992, 97, 9046–9061.
- 28 A. Douhal, F. Lahmani and A. H. Zewail, *Chem. Phys.*, 1996, 207, 477– 498.
- 29 C. Randino, M. Ziolek, R. Gelabert, J. A. Organero, M. Gil, M. Moreno, J. M. Lluch and A. Douhal, *Phys. Chem. Chem. Phys.*, 2011, **13**, 14960– 14972.
- 30 D. Presti, F. Labat, A. Pedone, M. J. Frisch, H. P. Hratchian, I. Ciofini, M. C. Menziani and C. Adamo, J. Chem. Theory Comput., 2014, 10, 5577–5585.
- 31 J. Jankowska, M. F. Rode, J. Sadlej and A. L. Sobolewski, *ChemPhysChem*, 2014, 15, 1643–1652.
- 32 J. Jankowska, J. Sadlej and A. L. Sobolewski, *Phys. Chem. Chem. Phys.*, 2015, **17**, 14484–14488.
- 33 C. Su, J.-Y. Lin, R.-M. R. Hsieh and P.-Y. Cheng, J. Phys. Chem. A, 2002, 106, 11997–12001.
- 34 M. Itoh, K. Tokumura, Y. Tanimoto, Y. Okada, H. Takeuchi, K. Obi and I. Tanaka, J. Am. Chem. Soc., 1982, 104, 4146–4150.
- 35 M. Itoh and Y. Fujiwara, J. Phys. Chem., 1983, 87, 4558–4560.
- 36 D. McMorrow and M. Kasha, Proc. Natl. Acad. Sci. USA, 1984, 81, 3375–3378.
- 37 P. T. Chou, M. L. Martinez and J. H. Clements, J. Phys. Chem., 1993, 97, 2618–2622.
- 38 V. V. Shynkar, Y. Mely, G. Duportail, E. Piemont, A. S. Klymchenko and A. P. Demchenko, J. Phys. Chem. A, 2003, 107, 9522–9529.
- 39 A. N. Bader, V. G. Pivovarenko, A. P. Demchenko, F. Ariese and C. Gooijer, J. Phys. Chem. B, 2004, 108, 10589–10595.
- 40 X. Poteau, G. Saroja, C. Spies and R. G. Brown, J. Photochem. Photobiol. A: Chem., 2004, 162, 431–439.
- 41 S. Ash, S. De, S. Pyne and A. Misra, J. Mol. Mod., 2010, 16, 831–839.
- 42 W.-S. Yu, C.-C. Cheng, Y.-M. Cheng, P.-C. Wu, Y.-H. Song, Y. Chi and P.-T. Chou, *J. Am. Chem. Soc.*, 2003, **125**, 10800–10801.
- 43 J. Waluk, Acc. Chem. Res., 2003, 36, 832–838.
- 44 M. Kijak, Y. Nosenko, A. Singh, R. P. Thummel and J. Waluk, J. Am. Chem. Soc., 2007, 129, 2738–2739.
- 45 Y. Nosenko, G. Wiosna-Sałyga, M. Kunitski, I. Petkova, A. Singh, W. Buma, R. Thummel, B. Brutschy and J. Waluk, *Angew. Chem. Int. Ed.*, 2008, **47**, 6037–6040.
- 46 P. J. Morgan, A. J. Fleisher, V. Vaquero-Vara, D. W. Pratt, R. P. Thummel, M. Kijak and J. Waluk, J. Phys. Chem. Lett., 2011, 2, 2114–2117.
- 47 T.-Y. Lin, K.-C. Tang, S.-H. Yang, J.-Y. Shen, Y.-M. Cheng, H.-A. Pan, Y. Chi and P.-T. Chou, *J. Phys. Chem. A*, 2012, **116**, 4438–4444.
- 48 L. Spörkel, G. Cui, A. Koslowski and W. Thiel, J. Phys. Chem. A, 2014, 118, 152–157.
- 49 P. O. Hubin, A. D. Laurent, D. P. Vercauteren and D. Jacquemin, *Phys. Chem. Chem. Phys.*, 2014, **16**, 25288–25295.
- 50 K.-Y. Chen, Y.-M. Cheng, C.-H. Lai, C.-C. Hsu, M.-L. Ho, G.-H. Lee and P.-T. Chou, J. Am. Chem. Soc., 2007, 129, 4534–4535.
- 51 X. Fang, Y. Wang, D. Wang, G. Zhao, W. Zhang, A. Ren, H. Wang, J. Xu, B.-R. Gao and W. Yang, *J. Phys. Chem. Lett.*, 2014, **5**, 92–98.
- 52 M. Zhang, D. Yang, B. Ren and D. Wang, J. Fluoresc., 2013, 23, 761– 766.
- 53 S.-H. Xia, B.-B. Xie, Q. Fang, G. Cui and W. Thiel, *Phys. Chem. Chem. Phys.*, 2015, **17**, 9687–9697.
- 54 M. D. Cohen and S. Flavian, J. Chem. Soc. B, 1967, 317-321.
- 55 W. Al-Soufi, K. H. Grellmann and B. Nickel, J. Phys. Chem., 1991, 95, 10503–10509.
- 56 K. Das, N. Sarkar, A. K. Ghosh, D. Majumdar, D. N. Nath and K. Bhattacharyya, J. Phys. Chem., 1994, 98, 9126–9132.
- 57 A. Muhlpfordt, U. Even and N. Ernsting, *Chem. Phys. Lett.*, 1996, 263, 178–184.

- 58 A. Fernandez-Ramos, J. Rodriguez-Otero, M. A. Rios and J. Soto, J. Mol. Struct., 1999, 489, 255–262.
- 59 J. Seo, S. Kim, S. Park and S. Y. Park, Bull. Korean. Chem. Soc., 2005, 26, 1706–1710.
- 60 F. S. Rodembusch, F. P. Leusin, L. B. Bordignon, M. R. Gallas and V. Stefani, J. Photochem. Photobiol. A: Chem., 2005, 173, 81–92.
- 61 F. S. Rodembusch, F. P. Leusin, L. F. da Costa Medina, A. Brandelli and V. Stefani, *Photochem. Photobiol. Sci.*, 2005, 4, 254–259.
- 62 F. S. Rodembusch, F. P. Leusin, L. F. Campo and V. Stefani, *J. Luminesc.*, 2007, **126**, 728–734.
- 63 I. S. Irgibaeva, D. A. Birilzhaniva and N. N. Barashkov, Int. J. Quantum Chem., 2008, 108, 2700–2710.
- 64 J. Massue, G. Ulrich and R. Ziessel, Eur. J. Org. Chem., 2013, 2013, 5701–5709.
- 65 Y. Syetov, J. Fluoresc., 2013, 23, 689-696.
- 66 V. S. Padalkar, P. Ramasami and N. Sekar, J. Luminesc., 2014, 146, 527– 538.
- 67 H. Roohi, F. Hejazi, N. Mohtamedifar and M. Jahantab, *SpectroChim. Acta A*, 2013, **118**, 228–238.
- 68 R. Daengngern and N. Kungwan, Chem. Phys. Lett., 2014, 609, 147– 154.
- 69 Y. Houari, A. Charaf-Eddin, A. D. Laurent, J. Massue, R. Ziessel, G. Ulrich and D. Jacquemin, *Phys. Chem. Chem. Phys.*, 2014, 16, 1319–1321.
- 70 K. Benelhadj, W. Muzuzu, J. Massue, P. Retailleau, A. Charaf-Eddin, A. D. Laurent, D. Jacquemin, G. Ulrich and R. Ziessel, *Chem. Eur. J.*, 2014, **20**, 12843–12857.
- 71 F. Laermer, T. Elsaesser and W. Kaiser, Chem. Phys. Lett., 1988, 148, 119–124.
- 72 W. Al-Soufi, K. H. Grellmann and B. Nickel, *Chem. Phys. Lett.*, 1990, **174**, 609–616.
- 73 S. Lochbrunner, A. J. Wurzer and E. Riedle, J. Phys. Chem. A, 2003, 107, 10580–10590.
- 74 R. de Vivie-Riedle, V. De Waele, L. Kurtz and E. Riedle, J. Phys. Chem. A, 2003, 107, 10591–10599.
- 75 R. Wang, D. Liu, K. Xu and J. Li, J. Photochem. Photobiol. A: Chem., 2009, 205, 61–69.
- 76 V. Padalkar, P. Ramasami and N. Sekar, Proc. Comput. Sci., 2013, 18, 797–805.
- 77 F. A. S. Chipem and G. Krishnamoorthy, J. Phys. Chem. B, 2013, 117, 14079–14088.
- 78 S. Luber, K. Adamczyk, E. T. J. Nibbering and V. S. Batista, J. Phys. Chem. A, 2013, 117, 5269–5279.
- 79 K. J. Chen, A. D. Laurent and D. Jacquemin, *J. Phys. Chem. C*, 2014, **118**, 4334–4345.
- 80 L. Wilbraham, M. Savarese, N. Rega, C. Adamo and I. Ciofini, J. Phys. Chem. B., 2015, 119, 2459–2466.
- 81 A. Douhal, F. Amat-Guerri, M. Lillo and A. Acuña, J. Photochem. Photobiol. A: Chem., 1994, 78, 127–138.
- 82 S. R. Vazquez, M. C. R. Rodriguez, M. Mosquera and F. Rodriguez-Prieto, J. Phys. Chem. A, 2008, 112, 376–387.
- 83 H.-H. G. Tsai, H.-L. S. Sun and C.-J. Tan, J. Phys. Chem. A, 2010, 114, 4065–4079.
- 84 V. S. Padalkar, P. Ramasami and N. Sekar, J. Fluoresc., 2013, 23, 839– 851.
- 85 V. S. Patil, V. S. Padalkar, A. B. Tathe, V. D. Gupta and N. Sekar, J. Fluoresc., 2013, 23, 1019–1029.
- 86 A. I. Ciuciu, L. Flamigni, K. Skonieczny and D. T. Gryko, *Phys. Chem. Chem. Phys.*, 2013, **15**, 16907–16916.
- 87 K. Benelhadj, J. Massue, P. Retailleau, G. Ulrich and R. Ziessel, Org. Lett., 2013, 15, 2918–2921.
- 88 Y. Houari, S. Chibani, D. Jacquemin and A. D. Laurent, J. Phys. Chem. B, 2015, 119, 2180–2192.

- 89 A. L. Sobolewski and W. Domcke, *Phys. Chem. Chem. Phys.*, 1999, 1, 3065–3072.
- 90 F. Plasser, M. Barbatti, A. J. A. Aquino and H. Lischka, J. Phys. Chem. A, 2009, 113, 8490–8499.
- 91 V. Vetokhina, K. Dobek, M. Kijak, I. I. Kaminska, K. Muller, W. R. Thiel, J. Waluk and J. Herbich, *ChemPhysChem*, 2012, **13**, 3661–3671.
- 92 C. G. Triandafillou and S. Matsika, J. Phys. Chem. A, 2013, 117, 12165– 12174.
- 93 M. Savarese, P. A. Netti, C. Adamo, N. Rega and I. Ciofini, J. Phys. Chem. B, 2013, 117, 16165–16173.
- 94 N. Minezawa, J. Chem. Phys., 2013, 138, 244101.
- 95 J.-S. Chen, P.-W. Zhou, L. Zhao and T.-S. Chu, *RSC Adv.*, 2014, 4, 254– 259.
- 96 M. Savarese, P. A. Netti, N. Rega, C. Adamo and I. Ciofini, *Phys. Chem. Chem. Phys.*, 2014, 16, 8661–8666.
- 97 A. D. Laurent, Y. Houari, P. H. P. R. Carvalho, B. A. D. Neto and D. Jacquemin, *RSC Adv.*, 2014, 4, 14189–14192.
- 98 L. Du and Z. Lan, J. Chem. Theory Comput., 2015, 11, 1360–1374.
- 99 A. Laurent and D. Jacquemin, Sc. China Chem., 2014, 57, 1363–1368.
- 100 J. Tomasi, B. Mennucci and R. Cammi, *Chem. Rev.*, 2005, **105**, 2999– 3094.
- M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, G. Scalmani, V. Barone, B. Mennucci, G. A. Petersson, H. Nakatsuji, M. Caricato, X. Li, H. P. Hratchian, A. F. Izmaylov, J. Bloino, G. Zheng, J. L. Sonnenberg, M. Hada, M. Ehara, K. Toyota, R. Fukuda, J. Hasegawa, M. Ishida, T. Nakajima, Y. Honda, O. Kitao, H. Nakai, T. Vreven, J. A. Montgomery, Jr., J. E. Peralta, F. Ogliaro, M. Bearpark, J. J. Heyd, E. Brothers, K. N. Kudin, V. N. Staroverov, R. Kobayashi, J. Normand, K. Raghavachari, A. Rendell, J. C. Burant, S. S. Iyengar, J. Tomasi, M. Cossi, N. Rega, J. M. Millam, M. Klene, J. E. Knox, J. B. Cross, V. Bakken, C. Adamo, J. Jaramillo, R. Gomperts, R. E. Stratmann, O. Yazyev, A. J. Austin, R. Cammi, C. Pomelli, J. W. Ochterski, R. L. Martin, K. Morokuma, V. G. Zakrzewski, G. A. Voth, P. Salvador, J. J. Dannenberg, S. Dapprich, A. D. Daniels, O. Farkas, J. B. Foresman, J. V. Ortiz, J. Cioslowski and D. J. Fox, *Gaussian 09 Revision D.01*, 2009, Gaussian Inc. Wallingford CT.
- 102 Y. Zhao and D. G. Truhlar, Theor. Chem. Acc., 2008, 120, 215-241.
- 103 R. Li, J. Zheng and D. G. Truhlar, Phys. Chem. Chem. Phys., 2010, 12, 12697–12701.
- 104 D. Jacquemin, A. Planchat, C. Adamo and B. Mennucci, J. Chem. Theory Comput., 2012, 8, 2359–2372.
- 105 M. Isegawa, R. Peverati and D. G. Truhlar, J. Chem. Phys., 2012, 137, 244104.
- 106 S. S. Leang, F. Zahariev and M. S. Gordon, J. Chem. Phys., 2012, 136, 104101.
- 107 A. Charaf-Eddin, A. Planchat, B. Mennucci, C. Adamo and D. Jacquemin, J. Chem. Theory Comput., 2013, 9, 2749–2760.
- 108 A. D. Laurent and D. Jacquemin, Int. J. Quantum Chem., 2013, 113, 2019–2039.
- 109 M. Caricato, B. Mennucci, J. Tomasi, F. Ingrosso, R. Cammi, S. Corni and G. Scalmani, J. Chem. Phys., 2006, 124, 124520.
- 110 TURBOMOLE V6.6 2014, a development of University of Karlsruhe and Forschungszentrum Karlsruhe GmbH, 1989-2007, TURBOMOLE GmbH, since 2007; available from http://www.turbomole.com.
- 111 A. Dreuw and M. Wormit, WIREs Comput. Mol. Sci., 2015, 5, 82-95.
- 112 C. Hättig and F. Weigend, J. Chem. Phys., 2000, 113, 5154–5161.
- 113 C. Hattig, Phys. Chem. Chem. Phys., 2005, 7, 59-66.
- 114 Note that in the specific case selected, the relative energies of the tautomers on the excited-state surfaces are reversed by applying ADC(2) corrections.
- 115 M. Page and J. W. McIver, J. Chem. Phys., 1988, 88, 922-935.
- 116 Note that 3MP is not defined in Gaussian09 and we used 2methylpentane instead during the calculations.

12 |

- 117 O. K. Abou-Zied, RSC Adv., 2013, 3, 8747-8755.
- 118 M. G. Holler, L. F. Campo, A. Brandelli and V. Stefani, J. Photochem. Photobiol. A: Chem., 2002, 149, 217–225.
- 119 R. F. Affeldt, A. C. de Amorim Borges, D. Russowsky and F. Severo Rodembusch, *New J. Chem.*, 2014, **38**, 4607–4614.
- 120 N. Jiang, C. Yang, X. Dong, X. Sun, D. Zhang and C. Liu, Org. Biomol. Chem., 2014, 12, 5250–5259.
- 121 M. Gutierrez, N. Alarcos, M. Liras, F. Sánchez and A. Douhal, *J. Phys. Chem. B*, 2015, **119**, 552–562.
- 122 J. Seo, S. Kim and S. Y. Park, J. Am. Chem. Soc., 2004, 126, 11154–11155.
- 123 N. Alarcos, M. Gutiérrez, M. Liras, F. ánchez and A. Douhal, *Phys. Chem. Chem. Phys.*, 2015, **17**, 16257–16269.
- 124 N. Alarcos, M. Gutiérrez, M. Liras, F. Sánchez, M. Moreno and A. Douhal, *Phys. Chem. Chem. Phys.*, 2015, **17**, 14569–14581.
- 125 P. H. P. Harbach, M. Wormit and A. Dreuw, J. Chem. Phys., 2014, 141, 064113.

Graphical Abstract

