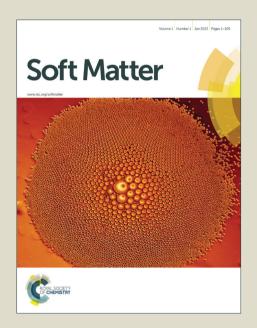
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Shear Banding in Entangled Polymers in Micron Scale Gap: a Confocal-Rheoscopic Study

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Pouyan E. Boukany, a Shi-Qing Wang, S. Ravindranath and L. James Lee

Recent shear experiments in well-entangled polymer solutions demonstrated that interfacial wall slip is the only source of shear rate loss and there is no evidence of shear banding in a micron scale gap. In this work, we experimentally elucidate how molecular parameters such as slip length, b, influence shear inhomogeneity of entangled polybutadiene (PBD solutions during shear in a small gap H \sim 50 μ m. Simultaneous rheometric and velocimetric measurements are performed on two PBD solutions with the same level of entanglements (Z = 54) in two PBD solvents with molecular weight of 1.5 kg/mol, and 10 kg/mol that possess different level of shear inhomogeneity ($2b_{max}/H = 17$ and 240). For the PBD solution, made with a low molecular weight PBD solvent of 1.5 kg/mol, wall slip is the dominant response within the accessification range of the shear rate, i.e., up to the nominal Weissenberg number (Wi) as high as 290. On the other hand, wall slip is minimized using a high molecular-weight PBD solvent of 10 kg/mol so that bulk shear banding is observed to take place of steady state for Wi > 100. Finally, these findings and previous result are in good agreement with our recently proposed phase diagram in the parameter space of apparent Wi versus $2b_{max}/H$ suggesting shear banding develops across the micron scale gap when imposed Wi exceeds $2b_{max}/H$ [Wang et al. Macromolecules 2011, 44, 183].

1 Introduction

Polymeric materials including DNA, actin filaments, plastics, textiles, rubbers and elastomers have emerged as a prominent class of soft matters, which can be found everywhere in nature and industry. Long macromolecules can be entangled in their disordered liquid state and display remarkable viscoelastic properties. Their sluggish macroscopic relaxation arises from chain uncrossability that constrains chains to perform "reptation" in the curvilinear one directional tube in quiescence. Hunder large fast deformation (when deformation rate exceeds the reciprocal of the reptation time), the intertwining chains pull on each other, resulting in molecular deformation, until the point of force imbalance, leading to chain disentanglement and yielding of the entanglement network. Whether chain disentanglement during large deformation produces a uniform shear field or not is a key issue in the nonlinear rheology of polymers.

Experimental knowledge about nonlinear rheological behavior of entangled polymers typically derives from a rotational shear rheometer where the sample thickness, H, is in the range of 1 mm. Recent experiments combined traditional rheometric measurements with particle-tracking velocimetric (PTV) characterization to obtain more insightful information about how chain entanglement responds to startup shear. At a high Weissenberg number $Wi = \dot{\gamma} \tau > 1$, defined as the product of the bulk

shear rate $\dot{\gamma}$ and the longest relaxation (or reptation) time τ , many entangled fluids exhibit wall slip and shear banding, including wormlike micelles, ⁸⁻¹² polybutadiene (PBD), ¹³⁻¹⁵ polyacrylamide, ^{16, 17} DNA, ¹⁸⁻²⁰ and F-actin solutions, ²¹ as well as polymer melts such as styrene-butadiene ²² and polyethylene-oxide. ²³ On the other hand, such shear banding can be avoided by replacing the sudden startup with gradual ramping up of the applied shear rate. ^{24, 25} Moreover shear banding and wall slip need not occur when the system is insufficiently entangled (level of entanglements per chain Z < 40) ^{1/2} or has a negligibly small extrapolation length b relative to the sample thickness H, i.e., when b/H << 1. ^{14, 28, 29}

Recent velocimetric measurements based on the confocal microscopy asserted that there was no bulk shear banding in entangled PBD solutions when the gap of the shear cell is reduced to tens of microns: $^{30, 31}$ Wall slip was the only discernible form of shear inhomogeneity, with linear velocity profiles across the gap for a high level of entanglement, i.e., Z = 56 entanglements per chain Such results were used to suggest that the previously observed shear banding $^{13, 14}$ involving conventional cone-plate or parallel-dictional device was due to the edge fracture: The absence of shear banding in a shear cell with a gap distance much lower than the conventional gap (e.g., by a factor of 20) was assumed to be due to the fact that there is negligible effect of edge fracture in the shear cell with 50 μ m gap.

Wall slip is a well-established phenomenon in both polymer melts and solutions. The polymer startup shear with Wi>1, entangled polymers show the first sign of shear inhomogeneity in the form owall slip by interfacial disentanglement, because polymer/wall interface is weaker than the cohesion of entangled networks. The intrinsic ability of the entangled solution to undergo slip can be estimated in terms of the slip length b. The magnitude of b of $(\eta/\eta_i)a$ relative to the sample thickness H determines how much the actual bulk shear rate $\dot{\gamma}_b$ is reduced from the nominal rate $\dot{\gamma}$, where a is the interfacial layer thickness, η and η_i are the bulk

^{a.} Department of Chemical Engineering, Delft University of Technology, Julianalaan 136, 2628 BL Delft, The Netherland.

E-mail: P.E.Boukany@tudelft.nl; Tel: +31-(0)15-27 89981

b Department of Polymer Science and Maurice Morton, Institute of Polymer Science, University of Akron, Akron, Ohio 44325, United States.

^{c.} Department of Chemical and Biomolecular Engineering, The Ohio State University, 174 West 18th Avenue, Columbus, Ohio 43210, United States.

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and interfacial viscosities respectively. The maximum value of b, denoted as b_{max} , corresponds to the full interfacial disentanglement when η_i reduces to the solvent viscosity η_s , i.e., $b_{\text{max}} = (\eta/\eta_s)a(\varphi)$. For polymer solutions, a would grow from its value in the melt l_{ent} upon dilution as: $a(\varphi)=l_{\text{ent}} \varphi^{-0.66}$, where φ is the polymer volume fraction.

Upon startup shear with Wi>1, wall slip will emerge as a consequence of interfacial yielding. Denoting the effective shear rate in the bulk as $\dot{\gamma}_b$, then the speed of the shearing wall is given in terms of the slip velocity V_s as

$$V = \dot{\gamma}_b H + 2V_s, \qquad (1a)$$

which can be rewritten as

$$\dot{\gamma} = (1 + 2b/H) \dot{\gamma}_h$$
, (1b)

where the nominal rate $\dot{\gamma}=V/{\rm H}$ and the slip length b has its kinematic meaning according to $b=V_s/\dot{\gamma}_b$, which is illustrated in Fiure 1. With increasing V or $\dot{\gamma}$, V_s and b grow towards their maximum values. Before the maximum slip velocity is reached, the bulk shear rate $\dot{\gamma}_b$ can be expected to remain at a critically low value around $1/\tau$. Correspondingly, the steady-shear stress does not appreciably increase with $\dot{\gamma}$. In other words, the value of $\dot{\gamma}$ can increase up to $\dot{\gamma}_{\rm wb-bnl}=(1+2b_{\rm max}/{\rm H})/\tau$ without forcing the bulk to leave the Newtonian regime whose upper-bound is given $1/\tau$.

In other words, there is a critical Weissenberg number $Wi_{\text{ws-bnl}}$, beyond which the bulk starts to enter the nonlinear response regime, given by

$$Wi_{ws-bnl} = (1+2b_{max}/H)$$
 (2)

When $Wi>Wi_{\text{ws-bnl}}$, even maximum wall slip cannot save the bulk from having $Wi_{\text{b}}=\dot{\gamma}_{\text{b}}\tau>1$. Here the subscript "ws-bnl" stands for a transition from wall slip (ws) to bulk nonlinear response (bnl). For well-entangled polymer solutions, $Wi_{\text{ws-bnl}}$ can be very large when H is reduced from a conventional gap distance of 1 mm to 50 μ m. This is a reason why Hayes et al. only reported wall slip as the source of shear rate loss for entangled PBD solutions.

In passing, we also note that the maximum value of $b_{\rm max}$ corresponds to the slip velocity $V_{\rm s}$ attaining its maximum at $Wi_{\rm ws-bnl}$ where the bulk shear rate $\dot{\gamma}_b \sim \tau^{-1}$. Thus, we have

$$V_{\rm s(max)} = b_{\rm max}/\dot{\gamma}_b \sim b_{\rm max}/\tau \tag{3}$$

In the current study, we show that the dominant wall slip characteristic of the previous reports $^{30,\ 31}$ is replaced by bulk shear banding when the extrapolation length b is reduced

using a polymeric solvent of sufficient high molecular weight. Specifically, one of our two 13 wt. % PBD solutions shows only wall slip, similar to one solution reported previously, 31 because of its high value for $b_{
m max}$, whereas the second solution displays bulk shear banding because of its lower value for b_{max} . Because the point of velocimetric observation in our setup is at least 3 mm away from the meniscus in a paralleldisk shear cell with H \sim 50 μ m, the aspect ratio is 60, no edge fracture and sample loss took place during shear. Finally, ou findings in micron scale gap are presented in terms of a phase diagram in the parameter space of apparent Wi versu $2b_{\text{max}}$ /H. We demonstrate that b_{max} is a key parameter for a fixed gap to control what type of velocity profile may occur fo a given Wi and bulk shear banding can develop when the applied Wi exceeds 2b_{max}/H. At sufficiently high Wi, linear velocity profile is recovered across the gap.

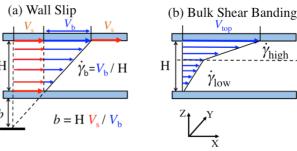


Fig. 1 Schematic diagram of the velocity profile within the gap of the shear geometry in presences of (left) wall slip, where $b = V_S/\dot{\gamma}_b$, and (right) bulk shear banding at the apparent shear rate.

3 Experimental

2.1. Materials and sample preparation. Our experiments are based on two well-entangled 1,4-polybutadiene (PBD) solutions made with the same parent high molecular weight PBD ($M_{\rm w} \sim 10^6 \, {\rm g/mol}$) at the same 13 wt. % concentration in polymeric butadiene (PBD) "solvents" (with molecular weights of 1.5 kg/mol and 10 kg/mol). In this work, these two solutions are labelled as 1M(13%)1.5K and 1M(13%)10K. The molecular characteristics of parent polymer a solvents are listed in Table 1. The parent PBD was first dissolved in excess of toluene to which PBD solvent was added and intimately mixed. For the particle tracking velocimetric (PTV) observations fluorescein isothiocyanate (FITC) labelled fluorescent melamine micro-beads with particle size of 1 μm (Sigma Aldrich, CAT no 90305) were dispersed in toluene and then added to the solution with the final loading of the particles around 600-800 ppm. Mosof the toluene was evaporated at room temperature under a hood for days, and the remaining was removed by applying vacuum unti the residual toluene is less than 0.5%.

Table 1. Molecular characteristics of parent 1MPBD, and 1.5KPBD and 10K PBD solvents.

Sample	M _n (g/mol)	M _w (g/mol)	$M_{\rm w}/M_{\rm n}$	η _s (Pa.s)	Source
1MPBD	1.01×10^{6}	1.05×10^{6}	1.03	n/a	Akron
1.5KPBD	1500	Not provided	Not provided	0.7	Sigma-Aldrich Cat No.200484
10KPBD	8900	10500	1.02	14	Bridgestone

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2.2. Rheometric and velocimetric measurements. In this work, we integrated a Bohlin-CVOR rheometer with a spin-disk confocal microscope to make the particle-tracking velocimetric (PVT) measurements at an unconventionally low gap distance of H = ca. 50 mm. The schematic representation of our confocal rheoscope is shown in Fig. 2 that involves an Olympus IX-81 inverted microscope. An EM-CCD camera (Hammamutsa) connected to the CFM was used to take two-dimensional (2D) movies in the XY plane through a piezo-mounted objective lens (60x, 1.4 NA). The field of view in our measurements is about 100 $\mu m \times 100 \mu m$ where the PTV observations are performed at distance of 3 mm from the meniscus so that the aspect ratio of the distance from the edge to the gap distance is ca. 60 (for H = 50 μ m). The lateral resolution, axial resolution, and optical slice thickness are 0.2, 0.5, and 1.34 μ m, respectively. The camera and spinning disk were synchronized, and the entire system was controlled using VoxCell software from Visitech International.

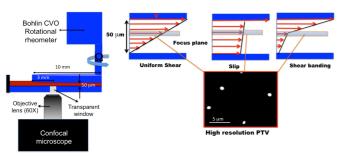


Fig. 2 (Left) Schematic illustration of rheo-confocal setup used for simultaneous rheometric and velocimetric measurements at room temperature with H = ca. 50 μ m. (Right) Sketch of the parallel-disk geometry with three different velocity profiles: Uniform flow, slip and shear banding. The velocity profiles were measured by tracking the fluorescent melamine micro-beads with size of 1 μ m.

A custom-made microscope stage was designed so that our rheometer (Bohlin CVOR) could integrate with the stage mounted onto the confocal fluorescence microscope (CFM) with three adjustable screws to ensure alignment. Initially, the adjustable platform allowed us to pre-align the rheometer on an optical table, on which is the CFM was placed. The rotating shaft has a short length of 2 cm to ensure good parallelism of the rotating disc to the bottom plate. To verify the alignment, the upper disc was first raised 5 μm above the stationary bottom plate and then spun to detect any misalignment. This setup has been previously employed to accurately conduct molecular imaging of entangled DNA solutions on the micron scale, 34 correlating interfacial slip with conformations of adsorbed DNA at wall.

All startup shear measurements were performed at room temperature around 25 °C, based on parallel-disk geometry with a radius R = 10 mm and H = ca. 50 μ m. Here all apparent shear rate values in the fluid sample are estimated as $\dot{\gamma}=\Omega R/H$, where Ω is the imposed angular velocity at R = 7 mm (at a radial distance of 3 mm from the edge). To determine the linear viscoelastic properties of these two entangled PBD solutions, small amplitude oscillatory shear (SAOS, strain amplitude γ = 5%) frequency sweep tests were conducted in a conventional parallel-plate shear cell with H = 1 mm. All startup shear tests were performed in the controlled rate mode at a narrow gap (H = ca. 50 μ m) under the confocal

microscope to capture the velocity profiles across the gap. The top and bottom plates were a glass slide (thickness 0.15-0.17 mm). The bottom plate was placed on the microscope stage, along with a circular plastic O-ring (inner radius 14 mm) to minimize meniscus instability and sample loss during high shear. The top moving a bottom stationary transparent plate were identified by scanning along the sample thickness direction to confirm the nominal gap is consistent with the true gap. In all startup shear experiments, 2°D images were captured every 2 to 4 microns across the sample thickness (with rate of 35 to 45 fps) to measure both transient and steady velocity profile across the gap. Typical error bars in the measured velocity are about 5 %, which was achieved by keeping track of sufficiently large displacements of the fluorescent particles

2.3. Extraction of slip velocity, slip length and local shear rates during shear. Experimental understanding of polymer rheology depends on simple shear rheometric measurements. Usually rheological properties of polymeric fluids are obtained based on the assumption that a uniform shear field with a constant shear rate ($\dot{\gamma} = V/H$) should prevail across the gap with no slip boundar, condition, where V is an imposed (apparent) velocity and H is a sample thickness sandwiched between two parallel plates.

At high shear rates, entangled fluids violate no-slip boundary condition and show strong wall slip during shear. The most effective way to quantify the slip is to introduce the slip length $b=V_{\rm S}/\gamma_b$. The magnitude of b relative to the sample thickness H determines how much the actual bulk shear rate $\dot{\gamma}_b$ is reduced from the apparent rate $\dot{\gamma}$. In this work, the slip velocity $V_{\rm S}$ and bulk rate $\dot{\gamma}_F$ are directly measured by confocal imaging to estimate the slip length, b, for both solutions. Specifically, to obtain accurate local shear rates, the velocity profiles with high spatial resolutions were constructed across the gap from PTV. Then, $\dot{\gamma}_b$ was evaluated from the velocity profile using ordinary least squares regression. The formation of two or more flow regimes with different local shear rates under the same imposed rate was defined from the best fits.

3 Results and Discussion

3.1. Conventional rheometric measurements. Fig. 3a should dynamic storage and loss moduli G' and G'' of the two 13 wt. % PBD solutions made with 1.5KPBD and 10KPBD respectively. The linear viscoelastic characteristics of these two samples are listed in Table 2, where the plateau modulus $G_{\rm pl}$ was determined from the value of G' at the frequency where G'' shows a minimum, and the longest relaxation time τ is estimated from the inverse of the crossov frequency ω_c where G' = G''. The similar value of $G_{\rm pl}$ confirms that the level of chain entanglement is the same in these two PBD solutions. The number of entanglements per chain can be estimated to be around 54 according to $Z = (M_w/M_e)\phi^{1.2}$, where M' is the molecular weight of the parent PBD, M_e the entanglement molecular weight for PBD melts, taken to be 1600 g/mol. The Rotelaxation time of two solutions are determined as $\tau_R = \tau/3Z$. Given $I_{\rm ent} = 3.8$ nm, $I_{\rm pos}^{35}$ we find $I_{\rm pos}^{35}$ to be ca. 15 nm at 13 wt% of 1MPBD

Table 2 lists the Wi_{ws-bnl} for the two polymer solutions by taking $\tau = 50~\mu m$. According to eq 2, to observe shear banding in the bulk we need to apply Wi in excess of either 17 or 240 respectively for the two solutions. By choosing two different solvents, we have estimated b_{max} to differ by a factor of ten as listed in Table 2. Here b_{max} is calculated based on the estimated values of η from Fig. 3.



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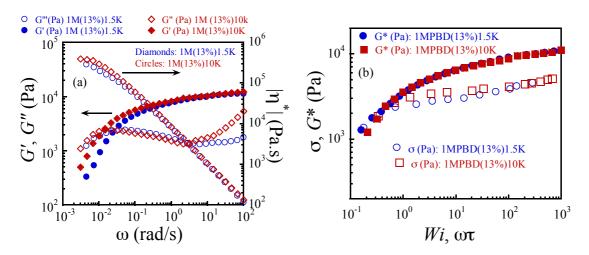


Fig. 3 (a): Small amplitude oscillatory shear (SAOS) measurement of two well-entangled PBD solutions. Dynamic storage, loss moduli and complex viscosity of 1M(13%)1.5K and 1M(13%)10K as a function of frequency using strain amplitude of 5% at room temperature (geometry: a 20 mm parallel-disk cell with separation of 1 mm). (b) Steady shear stress versus Wi (geometry: a 20 mm parallel disk with gap distance of ca. 50 μm), along with the oscillatory shear data of G^* versus the dimensionless oscillation frequency ($\omega \tau$) for two PBD solutions.

Table 2. Linear viscoelastic properties and slip characteristics

Sample	G _{pl} (kPa)	τ (s) ^a	<i>Z</i> (ф) ^b	$\tau_R(s)^{-c}$	η (kPa.s) ^d	а(ф) (nm) ^е	b _{max} (mm) ^f	Wi _{ws-b}
1M(13%)1.5K	9.7	36	54	0.22	288	15	6.0	2 0
1M(13%)10K	9.4	68	54	0.42	395	15	0.4	17

^a Terminal relaxation times are estimated as $\tau = \omega_c^{-1}$, where ω_c (in rad/s) is the crossover frequency in a frequency sweep test.

Next, we performed startup shear experiments to investigate the rheological responses at a narrow gap of H = ca. 50 μ m in the steady state. Fig. 2b displays the flow curves, showing steady shear stress against the nominal Wi, where the shear rate is given by WR/H, with W the angular velocity, R the disk radius. The two flow curves are very similar, showing the characteristic of stress plateau, both considerably below the curves of $|G^*|$ vs. $\omega\tau$. Because the parallel-disc setup was used to make these measurements, Fig. 3b only reflects an approximate shear stress vs. rate relationship.

3.2. Homogenous shear in Newtonian regime (Wi < 1.0). To check the reliability and performance of our confocal rheoscope, we

sheared 1M(13%)1.5K in the terminal regime (Wi < 1.0) where behaves like a Newtonian liquid. Fig. 4a shows that there is a stress overshoot at the low shear rate $\dot{\gamma} = 0.01~{\rm s}^{-1}$ (Wi = 0.36). Under this condition, the velocity profile is uniform across the sample thickness at all times, where the bulk shear rate ($\dot{\gamma}_b \sim 0.00.~{\rm s}^{-1}$) is close to the imposed shear rate. Small deviation from imposed shear rate indicates weak wall slip near both top and bottom plates occurs ($V_s \sim 0.03~{\rm \mu m/s}$). These results are consistent with previous reports^{18, 30} of homogenous shear in entangled polymer when Wi < 1.0.

^b Entanglement density, $Z(\phi)$ is calculated by $(M_w/M_e)\phi^{1.2}$, where M_e =1600 g/mol for 1,4 PBD melts.

 $^{^{\}rm c}$ Rouse times of two solutions are determined as $au_R = au/3Z$

 $^{^{\}rm d}\,$ The zero shear viscosity of the polymer solutions are estimated from figure 3.

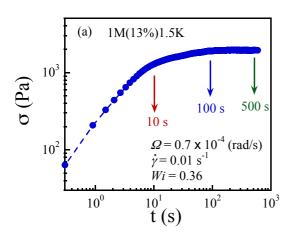
^e Interfacial layer thickness of polymer solutions are estimated as $a(\phi) = l_{ent} \phi^{-0.66}$, where $l_{ent} = 3.8$ nm for pure PBD melts and ϕ is the polymer volume fraction.

The theoretical maximum extrapolation length is estimated as $b_{\text{max}} = (\eta/\eta_s)a(\phi)$, where η_s for 1.5KPBD and 10KPBD is 0.7 and 14 Parespectively.

^g The critical Weissenberg number is estimated as $Wi_{ws-bnl} = 2b_{max}/H$, where H = 50 μ m.



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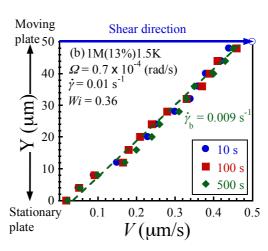
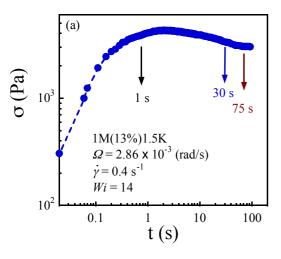


Fig. 4 (a) Shear stress response upon startup shear at rate of 0.01 s^{-1} as function of time. The arrows indicate the moments when the velocity profiles were measured and presented in (b). Linear velocity profiles prevail at different times at such a low shear rate (Wi = 0.36), involving the 20 mm-diameter parallel-disk with separation of 50 μ m. The open circle represents the velocity of upper plate, not PTV measurement.

3.2. Strong slip in 1M(13%)1.5K solution (1.0 < Wi \leq 288). At a shear rate of 0.4 s⁻¹ ($Wi \sim$ 14), the shear stress overshoot occurred during startup shear as shown in Fig. 5a, and the velocity profile is linear around t=1 s before stress overshoot and displays strong slip after the stress maximum as shown in Fig. 5b. The velocimetric measurement reveals that the bulk of the sample experiences a mere shear rate of 0.03 s⁻¹, which is comparable to the reciprocal of the terminal relaxation time ($\tau = 36$ s). At higher shear rates of 1.6,

3.0 and 8.0 s⁻¹ ($Wi = 57 \sim 288$,), apparent wall slip appears to be the only form of shear inhomogeneity near the steady state a shown in Fig. 6a-b. Accessing higher deformation rates (Wi > 296) to observe bulk shear banding across the gap is infeasible fo PBD1M(13%)1.5K because our PTV technique is limited to shear rates up to $10 \, \text{s}^{-1}$.



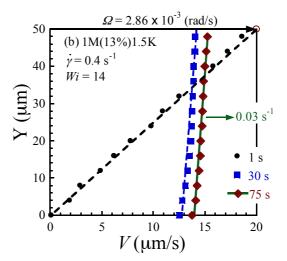


Fig. 5 (a) Shear stress response upon startup shear at rate of $0.4 \, s^{-1}$ (Wi = 14) for 1M(13%)1.5K. (b) The evolution of velocity profile at different times (t = 1, 30 and 75 s). Velocity profile is linear across the gap, before stress maximum then massive slip developed at long times, in the 20 mm-diameter parallel-disk shear cell with separation of 50 μ m. The open circle represents the velocity of upper plate, not PTV measurement.



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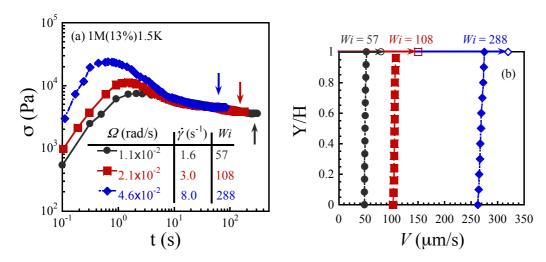
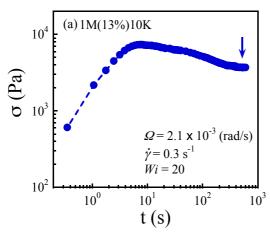
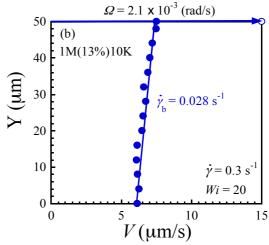


Fig. 6 (a) Shear stress response upon startup shear at different shear rates ($\dot{\gamma}$: 1.6, 3.0 and 8.0 s⁻¹) for 1M(13%)1.5K. (b) The linear velocity profiles in the bulk with strong slip at both surfaces at the moments indicated by the vertical arrows in (a), from the 20 mm-diameter parallel-disk shear cell with separation of 50 μm (at $\dot{\gamma}$ =1.6 and 3.0 s⁻¹) and 40 μm (at $\dot{\gamma}$ =8.0 s⁻¹). The rheometric velocities of upper plates are represented by open symbols.

3.3. Shear banding in 1M(13%)10K (100 \leq *Wi* \leq 408). The intrinsic ability to undergo wall slip can be considerably reduced by using a polymeric solvent with a sufficiently high molecular weight to increase the upper bound for the interfacial viscosity η_i . ²⁹ In this section, we only focus on steady-state velocity profiles at different shear rates in the stress plateau region. At low shear rate $\dot{\gamma} = 0.3 \text{ s}^{-1}$ ($Wi \sim 20$), this solution also violates the no-slip boundary condition at the top and bottom plates after stress maximum is reached, and strong slip prevails across the gap as shown in Fig. 7a-b. On the other hand, when Wi > 100, shear banding emerges across the small gap. The growth of shear stress for shear rates of 1.5, 3.0 and 6.0 s⁻¹ during startup shear is plotted in Fig. 8a. Fig. 8b shows that the velocity profile becomes nonlinear, characteristic of shear banding (with three different local shear rates of 0.15, 0.86 and

 $4.39 \, \text{s}^{-1}$) in steady state for the nominal shear rate of $1.5 \, \text{s}^{-1}$ Previous velocimetric measurements on polymer solutions have also reported the existence of multiple shear banding across the gap. For shear rates of $3.0 \, \text{and} \, 6.0 \, \text{s}^{-1}$, permanent shear banding persists across the gap even after hundreds of strain units, a shown in Fig. 8c. Accompanying the high shear band is also significant wall slip. For apparent shear rates of $1.5, \, 3.0 \, \text{and} \, 6.0 \, \text{s}^{-1}$ the local rate in the high shear band is $4.39, \, 5.67 \, \text{and} \, 14.48 \, \text{s}^{-1}$ respectively. As a function of the apparent shear rate, the local shear rate varies in each of the low, medium or high band, as shown in Fig. 8d. The local shear rate in the high band seems to increase exponentially with apparent shear rate.





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Fig. 7 (a) Shear stress response upon startup shear at a rate of 0.3 s⁻¹ (Wi = 20). (b) Steady-state linear velocity profile with apparent wall slip for 1M(13%)10K when $Wi < Wi_c$, obtained from the 20 mm-diameter parallel-disk shear cell with separation of 50 μ m. The open circle represents the velocity of upper plate, not PTV measurement.

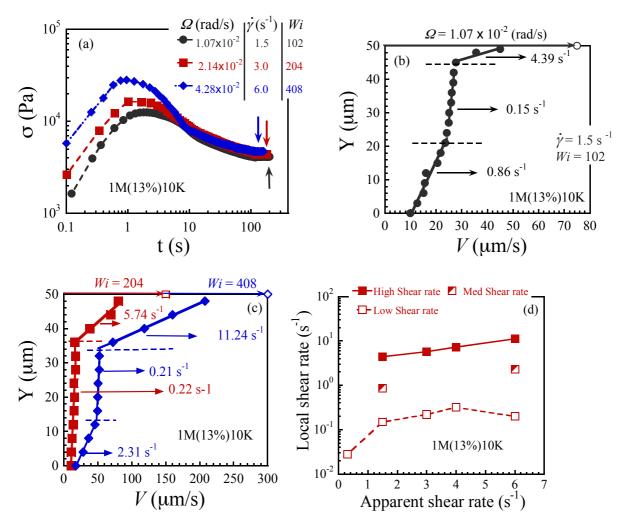


Fig. 8 (a) Shear stress response upon startup shear at different shear rates ($\dot{\gamma}$: 1.5, 3.0 and 6.0 s⁻¹) for 1M(13%)10K measured from the 20 mm-diameter parallel-disk shear cell with separation of 50 μ m. (b) Shear banded velocity profile with formation of three flow regimes (0.15, 0.86 and 4.39 s⁻¹) for apparent shear rate of 1.5 s⁻¹ in the steady state as indicated by the vertical arrow in (a). (c) Banded velocity profiles of 3.0 and 6.0 s⁻¹ in the steady state as indicated by the vertical arrow in (a). The rheometric velocities of upper plates are represented by open symbols in (b and c). (d) The local shear rates (obtained from PTV measurements) versus apparent shear rates for 1M(13%)10K.

3.4. Normalized steady state velocity profiles: slip vs. shear banding. Fig. 9a-b respectively present the normalized steady-state velocity profiles for the two solutions at different Wi. In Fig. 9a, the 1M(13%)1.5K solution shows nothing else but massive slip in the range of Wi from 14 to 288. In contrast, Fig. 9b shows that bulk shear banding develops across the gap in the range of Wi from 102 to 408 for 1M(13%)10K. Fig. 9c displays the steady state velocity profiles at comparable Wi = 288 and 272; $\dot{\gamma}\tau_R$ = 1.8 and 1.7, showing slip and bulk shear banding respectively of the two solutions.

Our PTV measurements allow us to examine how the wall slip grows in magnitude, i.e., how the slip velocity $V_{\rm s}$ increases with the applied rate $\dot{\gamma}$ toward its maximum. According to $V=2V_{\rm s}+\dot{\gamma}_b{\rm H},\,V_{\rm s}$ would change linearly with Wi as

$$Wi = (V/H) \tau = 2V_s/(H/\tau) + \tau \dot{\gamma}_b$$

if the bulk rate $\dot{\gamma}_b$ were to remain little changed with Wi. Fig. 9d plots V_s against Wi for both PBD solutions. With increasing Wi, the value of V_s grows linearly for 1M(13%)1.5K. Similar behavior is ai. observed for 1M(13%)10K up to 1.0 < Wi < 20. The slip velocity Vstarts to deviate from the linearity for Wi > 20, confirming that the shear rate $\dot{\gamma}_b$ remained unchanged up to Wi =20. The value V_s 1M(13%)-10K stays well below that of 1M(13%)1.5K for all values of Wi - noting the different scales used for the double-Y ax When the increase of V_s starts to deviate downward from linear growth with Wi, it has already reaches its maximum at 6 μm/c which coincides with the theoretical estimate of eq 3: $V_{s(max)}$ $b_{\text{max}}/\tau = 420/68 = 6.2 \,\mu\text{m/s}$. Because of the poor spatial resolution, the higher value of V_s observed at high Wi indicates apparent wal slip that involves a slip layer increasingly thicker than one monolayer. Fig. 8e shows the changes of the slip length $b = V_s/\dot{\gamma}_b$ is a function of Wi for the two solutions. The slip length b rang from 10 to \sim 1100 μm for 1M(13%)1.5K, which is one order of magnitude higher than slip length of 1M(13%)10K (maximum b

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 \sim 190 $\mu m). This can be estimated from the information in Table 1 showing that <math display="inline">\eta_s$ of PBD10K is 20 times as high as that of 1.5KPBD.

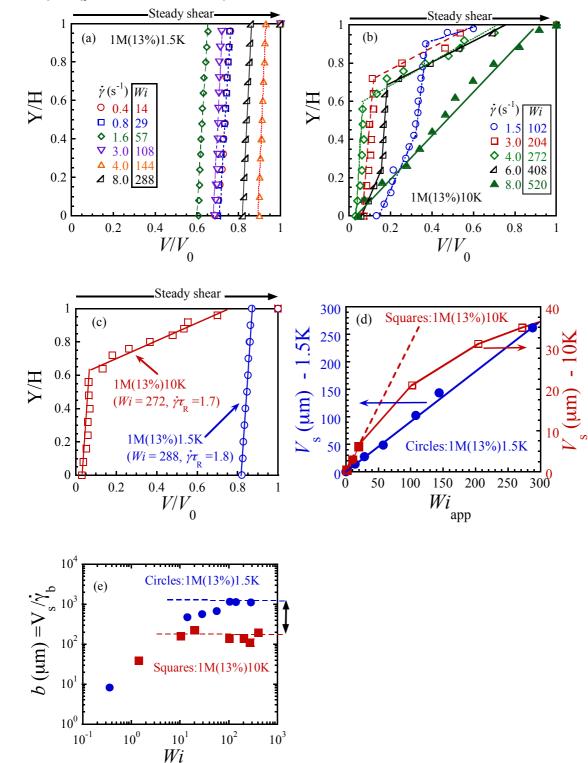


Fig. 9 Snap shots of velocity profiles in steady state for (a) 1M(13%)1.5K (slip-like behavior) and (b) 1M(13%)10K (bulk shear banding at $100 \le Wi \le 408$ and uniform shear at Wi = 520). (c) The normalized velocity profiles for the two PBD solutions at the Wi = 288 and 272; $\dot{\gamma}\tau_R = 1.8$ and 1.7, showing slip and shear banding respectively. (d) Slip velocity versus apparent Wi for the two PBD solutions where the vertical bar indicates the maximum difference. (e) Estimated slip length, b, versus apparent Wi for the two PBD solutions.



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3.5. Relationship between local and apparent Wi and comparison with previous work. Upon extracting the local, i.e., bulk, Weissenberg numbers from our velocimetric measurements, we show the relationship between the bulk Weissenberg number Wi_b and nominal Wi in Fig. 10. Here we compare our findings with the previous work obtained in a narrow-gap to address and discuss why only either linear velocity profile or wall slip was observed in the previous report. Hayes and coworkers³⁰ studied five different entangled solutions with different volume fractions ϕ based on two high molar mass PBD ($M_w = 0.7 \times 10^6$ g/mol, $M_w/M_n = 1.1$) and PBD ($M_w = 0.2 \times 10^6$ g/mol, $M_w/M_n = 1.05$) in an un-entangled PBD1K solvent ($M_w = 1 \times 10^3$ g/mol). These PBD solutions with a wide range

of level of entanglements ($8 \le Z \le 56$) were reported to show a linear velocity profile with some wall slip. We estimate the rheological properties and slip characteristics of five solutions as shown in Table 3. Among these five solutions, 0.2M(40%)1K 0.2M(60%)1K and 0.7M(20%)1K have a sufficiently high level of entanglements ($32 \le Z \le 56$) capable of producing shear banding across the gap at high values of Wi. We also note that only 0.7M(20%)1K was sheared at sufficiently high Wi ($9 \le Wi \le 114$). The two PBD solutions, based on the parent PBD 200K named 0.2M(40%)1K and 0.2M(60%)1K in our paper, were only explored in the Newtonian regime ($0.08 \le Wi \le 0.7$). It is well established that a linear velocity profile should be maintained across the gap when Wi < 1.0. 18,29

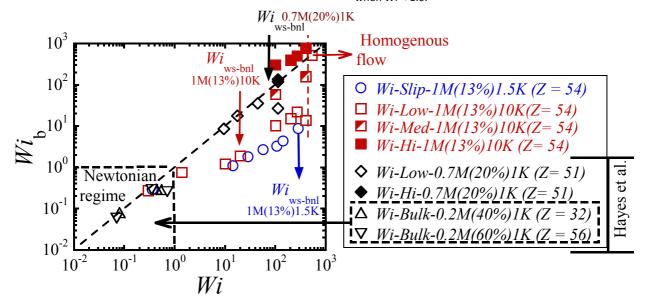


Fig. 10 Local Wi_b against apparent Wi for five PBD solutions with a sufficiently high level of entanglements ($32 \le Z \le 56$). Diamonds and triangles are extracted from the work of Hayes et~al. Both 0.2M(40%)1K and 0.2M(60%) were only sheared at low shear rate such that $Wi_b > 1.0$ (highlighted by dashed box in the Newtonian regime). At high $Wi_b > 100$, coexistence of high and low Wi_b appears across the microi scale gap for 1M(13%)10K, in contrast with apparent slip of 1M(13%)1.5K that keeps Wi_b low as indicated by the circles. For 0.7M(20%)1K, coexistence of high and low shear band has been reported by Hayes et~al at $Wi_b = 113$. Note that values of Wi_{ws-bnl} for 1M(13%)1.5K, 1M(13%)10K, and 0.7M(20%) are highlighted by vertical blue, red and black arrows respectively.

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Table 3. Composition and linear rheological properties of PBD solutions reported in the work of Hayes et al. 30

Sample	G _{pl} (kPa) ^a	τ (s)	<i>Ζ</i> (φ)	η(φ) ^d (kPas)	а(ф) (nm)	$b_{max} = (\eta/\eta_s)a(\phi)$ (mm) ^e	Wi _{ws-bnl} ∼ 2b _{max} /H ^f
0.7M(5%)1K	1.3	2.7	12 ^b , 8 ^c	3	27	0.02	0.5
0.7M(10%)1K	7.5	11	27 ^b , 20 ^c	67	17	0.26	7.4
0.7M(20%)1K	44	31.6	63 ^b , 51 ^c	1142	11	2.8	80
0.2M(40%)1K	220	0.8	41 ^b , 32 ^c	145	7	0.25	7.2
0.2M(60%)1K	511	1	68 ^b , 56 ^c	420	5	0.56	16

^a Plateau modulus of PBD samples were provided in PhD thesis of Keesha Hayes. ³

In general, at low shear rates (Wi < 1.0), the nominal and local Weissenberg numbers are the same, which is consistent with previous reports on entangled systems^{18, 30}. Besides, at Wi = 0.7 and 0.5 (closer to Wi = 1), both 0.2M (40%)1K and 0.2M(60%)1K suffered from some degree of wall slip,³⁰ as denoted by the triangles in Fig. 9. This is expected.

At higher Wi in the non-Newtonian regime (Wi > 1.0), we see that Wib remains the order of unity because of the dominant wall slip in 1M(13%)1.5K, except for last two points. In the explored range of apparent shear rates, the solution based on the 1.5K solvent has b equal to 1100 μm and shows interfacial slip or apparent wall slip only up to Wi = 288 ($\dot{\gamma}\tau_R\sim 1.8$). The PBD solution with PBD10K solvent shows coexistence of high and low shear bands, along with wall slip because its $b = 190 \mu m$. We note that beyond Wi = 100; $\dot{\gamma}\tau_R\sim 0.6$, there can be three bands of different local rates in the bulk for 1M(13%)10K. At In contrast, a linear velocity profile without wall slip was reported by Hayes et al. for their 0.7M(20%)1K (Z ~ 51) till Wi = 45. The lack of wall slip is at odds with their report of wall slip for the other solutions and in disagreement with our findings shown in Fig. 10. When Wi is increased to 113, the velocity profile began to deviate significantly from nominal Wi, displaying shear banding. This response can be consistent with our observation of shear banding, because shear banding should occur for 0.7M(20%)1K when $Wi > Wi_{ws-bnl} \sim 80$ (see diamonds in Fig. 10). However, Hayes et al. suggested that this behavior could be originated from secondary flows due to chain stretching and normal stresses at high shear rate. Since most of the reported values of Wi in Hayes et al.'s measurements are less than critical Wi_{ws-bnl} , except for one date point of 0.7M(20%)1K (at Wi =113), it is expected to observe linear velocity profile in their measurements. In this work since the point of PTV observation is so far away from the edge, it is implausible for our results to have anything to do with any edge instability. Thus we have proposed localized chain disentanglement as the origin of shear banding, more systematic studies are required to look for evidence of secondary flow phenomenon and effect of edge failure on the bulk velocity profile of well-entangled PBD solutions in such small-gap shear cells.

3.6. Suppression of edge effects at small gap. Edge fracture occurs frequently in well-entangled polymeric systems at high *Wi* in a conventional rheometric setup (with a gap size of 1 mm). ^{38, 39}T' phenomenon is attributed to the buildup of normal stresses. ^{38, 40} When edge fracture occurs, the sample may "leak out" at the meniscus during shear leading to a reduced stress response. It has been reported in the literature that a large decrease of the gap distance can minimize the edge effects during shear of entangled polymer solutions. ³⁰ We carry out SAOS to verify whether there is any sample loss during shear banding. Fig. 10 shows that dynamic oscillatory shear data are identical before and after shearing at shear rates of 1.5, 3.0 and 6.0 s⁻¹.

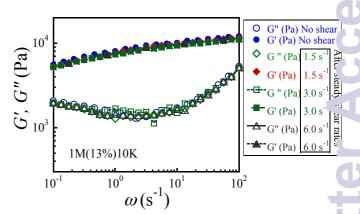


Fig. 11 Small amplitude oscillatory shear (SAOS) measurement before and after shear rates (with 650 s rest time for entanglement recovery after applying steady shear rates). Dynamic storage (closed symbols) and loss (open symbols) moduli of 1M(13%)10K a function of frequency using strain amplitude of 5% at room temperature.

Additionally, it is known that edge fracture would be more several thigh Wi, due to increased normal force. Fig. 12 shows that a higher Wi, a linear velocity profile is actually recovered in steady state. Specifically, at sufficiently high shear rate of 8.0 s⁻¹, the uniform shear is recovered (at t=77 s) after showing transient inhomogeneity (at t=7.7 s) across the gap. Therefore, we conclude that edge fracture has been minimized and sample loss negligible in our measurements, and our setup can be ideal for studying the non-linear response in entangled polymer at high Wi.

^b $Z(\phi)$ is estimated by $(M_w/M_e)\phi^{1.2}$, where $M_e = 1600$ g/mol for 1,4 PBD melts.

 $^{^{\}rm c}$ Z(ϕ) is reported by Hayes et al, where $M_{\rm e}$ is assumed to be around 2000 g/mol.

^d Bulk shear viscosity of polymer solutions are estimated as $\eta = \frac{\pi^2}{12} G_{pl} \tau$. ⁵

^e Maximum extrapolation length is estimated, where solvent viscosity (PBD1K, $M_n \sim 1000$ g/mol, Aldrich Inc.) is assumed to be around 4.0 Pas at room temperature.³⁷ The vinyl content of PBD1K (Aldrich 200417), is higher than PBD1.5K (Aldrich 200484) leading to lower T_g and higher viscosity.

 $^{^{}f}$ Wi_{ws-bnl} is estimated, where H = 35 μ m.

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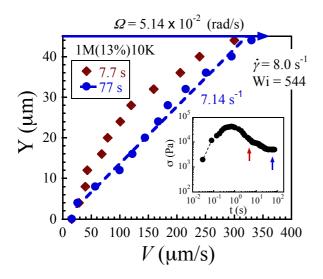


Fig. 12 Restoration of uniform velocity profile at high shear rate. Characterization of velocity profile at high shear rates = 8.0 s^{-1} (Wi = 544) at t = 7.7 and 77 s. The inset shows a shear stress response upon startup shear at rate of 8.0 s^{-1} .

3.7. The phase diagram. We can construct a "phase diagram" to summarize our findings in terms of Wi versus $2b_{\rm max}/H$, as shown in Fig. 13. Clearly, $b_{\rm max}$ is one of the key parameter to highlight when and what type of shear inhomogeneity may occur at different Wi for a fixed gap. For both 0.7M(20%)1K and 1.0M(13%)1.5K, much higher Wi is required to obtain shear banding, due to high value of slip length. We should emphasize that this phase diagram can only qualitatively describe whether shear banding should occur or not during shear for well-entangled systems (Z > 40).

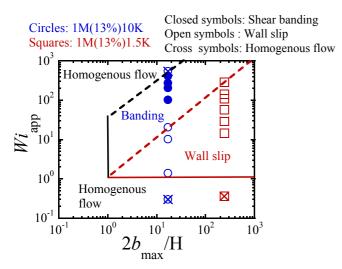


Fig. 13 Phase diagram in the parameter space of apparent Wi versus $2b_{\text{max}}/H$ for our findings at small gap for PBD solutions (Z = 54) in different PBD solvents.

4 Conclusions

In this study, two entangled PBD solutions with the same level or entanglement (Z = 54) have been subjected to various values o nominal shear rate $\dot{\gamma}$ to explore their nonlinear rheological responses in a shear cell with a small gap distance in the 50 microri range. Because the gap distance was unconventionally small, the PTV observations could be free of edge effects without implementation of cone-partitioned plate.^{39, 41-43} Using a confoca. microscope integrated with a rotational rheometer, we obtain simultaneous global rheology (apparent rheometric measurements and local velocity profiles. This setup allows us to probe when and what type of shear inhomogeneity (interfacial slip vs. shear banding) occurs across the gap. For the entangled PBD solution made with a low molecular weight PBD ($M_w = 1.5 \text{ kg/mol}$), only interfacial slip or apparent wall slip can be observed up to a shear rate of 8 s⁻¹. In contrast, the second solution, the higher molecula weight PBD ($M_w = 10 \text{ kg/mol}$) solvent reduces the magnitude of the slip length b so that apart from wall slip bulk shear banding can a take place at the experimentally accessible shear rates. The prevalence of interfacial slip in 1M(13%)1.5K is consistent with the findings of Hayes and coworkers. 30, 31 On the other hand, 1M(13%)10K exhibits shear banding despite a small gap distance of 50 μ m, when imposed Wi exceeds a critical value if Wi, i.e., $2b_{max}/H$. Finally, at sufficiently high Wi, shear homogeneity is restored acros the gap for 1M(13%)10K.

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