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*Acquisition of time-frequency localized mechanical properties of
biofilms and single cells with high spatial resolution*

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24

25 **Abstract**

26 Biofilms are a cluster of bacteria embedded in extracellular polymeric substances (EPS) that contain a
27 complex composition of polysaccharides, proteins, and extracellular DNA (eDNA). Desirable mechanical
28 properties of the biofilms are critical for their survival, propagation, and dispersal, and the response of
29 mechanical properties to different treatment conditions also sheds light on biofilm control and eradication
30 *in vivo* and on engineering surfaces. However, it is challenging yet important to interrogate mechanical
31 behaviors of biofilms with a high spatial resolution because biofilms are very heterogeneous. Moreover,
32 biofilms are viscoelastic, and their time-dependent mechanical behavior is difficult to capture. Herein, we
33 developed a powerful technique that combines the high spatial resolution of the atomic force microscope
34 (AFM) with a rigorous history-dependent viscoelastic analysis to deliver highly spatial-localized biofilm
35 properties within a wide time-frequency window. By exploiting the use of static force spectroscopy in
36 combination with an appropriate viscoelastic framework, we highlight the intensive amount of time-
37 dependent information experimentally available that has been largely overlooked. It is shown that this
38 technique provides a detailed nanorheological signature of the biofilms even at the single-cell level. We
39 share the computational routines that would allow any user to perform the analysis from experimental raw
40 data. The detailed localization of mechanical properties in space and in time-frequency domain provides
41 insights on the understanding of biofilm stability, cohesiveness, dispersal, and control.

42

43 *Keywords:* biofilms, atomic force microscopy, viscoelasticity, biofilm nanomechanics, single-cell
44 mechanics, nanorheology.

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46

47 I. INTRODUCTION

48 Biofilms that propagate in human organs and tissues and biomedical devices¹ are one of the leading causes
49 of infectious diseases. Biofilms are also problematic in the food industry by disseminating on food
50 processors, utensils, and packages, ultimately causing foodborne diseases or disease outbreaks².
51 Moreover, biofilms are naturally abundant and undesirable in drinking water distribution pipes where they
52 support the survival and accumulation of pathogens, increasing the risk of waterborne diseases³. Biofilms
53 are consortia of microorganisms embedded in a self-produced matrix of extracellular polymeric
54 substances (EPS) that hold the cells together and attach them to surfaces. The EPS are responsible for
55 biofilm mechanical sturdiness by providing biofilms with high cohesion and adhesion stability^{4,5}. Besides
56 the important mechanical stability, EPS are also recognized to enhance antimicrobial and antibiotic
57 resistance of the biofilms⁶.

58 Eradicating biofilms via mechanical failure, either adhesive or cohesive, demands detailed knowledge
59 of biofilm mechanical properties⁵. Specifically, biofilm mechanical properties have been widely
60 recognized to be history-dependent (i.e., viscoelastic). Viscoelasticity refers to the distinct behavior that
61 some materials such as biofilms have, of simultaneously storing and dissipating energy when deformed.
62 This behavior gives rise to the material appearing to be ‘softer or stiffer’ and ‘less or more dissipative’
63 depending on the rate at which it is probed, fact that adds more complexity to its appropriate analysis.
64 Importantly, this viscoelastic behavior is believed to be responsible for biofilm persistence against
65 mechanical and chemical threats⁷⁻⁹ (e.g., antibiotics). This belief is supported by observations in polymer
66 physics where it has been shown that adhesion and cohesion failure is a rate dependent phenomenon linked
67 to the polymer viscoelastic properties¹⁰⁻¹². These observations should be applicable to biofilms where the
68 EPS matrix is regarded as responsible for their outstanding cohesion and adhesion. Despite of its
69 importance, evaluating the mechanics of such a highly heterogeneous and complex system is very

70 challenging, which has made it impossible to attain a consensus on biofilm mechanical properties¹³. This
71 lack of consensus may have (at least) two distinct roots: *i*) various length scales at which biofilms have
72 been studied (from bulk rheological measurements to micro and nanoscale measurements)¹⁴, and *ii*)
73 whether the studies include or neglect viscoelastic effects.

74 Within the various length scales, measurements at the nanoscale deserve a special interest due to the
75 high spatial heterogeneity that biofilms display, even at the microscale. Moreover, it is important to
76 understand the underlying mechanisms governing biofilm adhesion and cohesion, which are of nanoscale
77 nature (e.g., intermolecular forces between biofilm components). To achieve this goal, the atomic force
78 microscope (AFM) has shown its capability to probe biological systems with nanoscale spatial resolution
79 and high force sensitivity (piconewton)¹⁵⁻¹⁹. However, the few studies on biofilm nanomechanics
80 available in the literature generally rely on material inversion methods that neglect viscoelastic effects
81 (e.g., Hertzian elastic analysis)^{18, 20, 21}. That approach (a first order approximation) has allowed important
82 observations and conclusions, however, to make further advances it is necessary to study in detail the
83 biofilm viscoelastic properties.

84 The goal of this study is to provide a method that addresses the viscoelastic nature of biofilms, while
85 exploiting the high spatial resolution offered by the AFM. The analysis here offered demonstrates the
86 feasibility of localizing mechanical properties spatially and in the time-frequency domain by employing a
87 rigorous framework that considers their history-dependent nature. This technique is of a great interest for
88 understanding in detail the *nanoscale viscoelastic properties* of biofilms, which are understood to be
89 closely related to biofilm stability and cohesiveness, as well as eradication and control. We demonstrate
90 that this method can measure viscoelastic properties with high spatial localization even at the single-
91 bacterium level. Lastly, it is appropriate to mention that our selection of AFM static force spectroscopy in
92 this study over AFM dynamic methods obeys practical convenience for the retrieval of viscoelastic

93 properties. Since viscoelasticity is a history-dependent phenomenon, it is of utmost importance to have
94 information on the force/displacement history, as the constitutive equations (convolution integrals)
95 demand this information. This loading-indentation history is readily available in a force spectroscopy
96 experiment. On the other hand, in dynamic methods this detailed information is not available, making it
97 very difficult to establish relationships between observables and viscoelastic parameters. For this reason,
98 we propose performing the analysis through static force spectroscopy, although further developments
99 appropriate for dynamic methods are highly encouraged.

100

101 **II. EXPERIMENTAL**

102 **Sample Preparation**

103 *Staphylococcus epidermidis* (*S. epidermidis*) biofilms were grown over silicon wafers as follows. *S.*
104 *epidermidis* was cultured in tryptic soy broth (TSB) at 37 °C under mixing conditions overnight and
105 subsequently harvested by centrifugation. Then, bacteria were resuspended in a phosphate buffered saline
106 (PBS) solution and silicon wafers were completely submerged in 2 ml of the bacterial suspension
107 ($OD_{600}=0.5$) in a sterile six-well plate. The system was incubated at 37 °C for 24 h with no stirring to
108 promote bacterial attachment to the silicon wafers. Then, the suspension was evacuated by aspiration, and
109 10-fold diluted TSB solution was added to submerge the silicon wafers. Last, the wafers were incubated
110 at 37 °C for 3 days with a mixing rate of 80 rpm and daily nutrient replacement of 10-fold diluted TSB
111 solution. Before the AFM experiments, silicon wafers with biofilms were gently rinsed three times by
112 autoclaved ultrapure water and placed in a vacuum dryer overnight at room temperature.

113

114 **Atomic force microscopy (AFM) experiments**

115 Tapping mode and static force spectroscopy AFM techniques were performed to obtain high spatial
116 topographical images and high sensitivity force spectroscopy analysis, respectively. In all experiments
117 presented here we have used commercial AFM cantilevers (Olympus AC200TS R3) with a force constant
118 of approximately 1.1 N/m. We have used a commercial AFM for our measurements (Cypher equipped
119 with an ARC2 controller, Asylum Research).

120 For morphological characterization of the biofilms we used tapping mode AFM. In this popular low
121 invasive technique, the probe is dynamically excited with a sinusoidal signal whose frequency is typically
122 close to the cantilever's first mode resonance frequency²², and the tapping amplitude is a fraction of the
123 free oscillating amplitude (~50 % in our experiments).

124 For mechanical characterization we employ static force spectroscopy AFM where the cantilever is
125 approached towards the sample at rates far from the probe's resonance frequency (quasi-static regime)²³,
126 ²⁴. This mode of operation is very popular for material property calculation because it allows to obtain a
127 force-displacement curve that describes the tip-sample interaction force as a function of the probe position.
128 Consequently, from these force-distance curves material properties are often calculated by employing
129 specific contact mechanic models^{17, 25-27}. However, obtaining a force-distance curve requires doing
130 certain assumptions because the AFM does not directly measure force and indentation depth²⁸. Instead,
131 it measures values of cantilever deflection, $d(t)$, (in Volts) as a function of the cantilever relative position
132 (also called z-sensor position, $z(t)$). As a result, it is necessary to define unambiguously some reference
133 points (or offsets) during the postprocessing of the raw signals, especially if an automated approach is
134 needed for analyzing multiple force-distance curves as in the present study. This affair is usually not
135 discussed in the literature, although fortunately a couple of reviews on this matter are available^{28, 29}. For
136 self-containment purposes, we summarize some key points relevant to our analysis. First, we need to
137 convert the raw signal of deflection (recorded in Volts) to length units through the photodetector

138 sensitivity calibration (with a hard substrate) which yields the deflection history, $d(t)$. Then, we need to
 139 capture the point of zero-indentation (d_0, z_0) which in this study was assumed to occur at the value of
 140 maximum negative deflection (jump to contact point). Note, that this might not be true for highly adhesive
 141 interactions (e.g., Johnson-Kendall-Roberts model JKR³⁰, Maugis-Dugdale MD³¹) where at the point of
 142 contact the indentation can be negative. After defining this point, we can estimate the indentation history,
 143 $h(t)$, with the following relationship:

$$h(t) = (z(t) - z_0) - (d(t) - d_0) \quad (1)$$

144 In static force spectroscopy, the deflection of the cantilever is directly linked to the tip-sample
 145 interaction force. However, prior to multiplying the deflection by the cantilever spring constant (k_c) to
 146 obtain force, it is needed to subtract a deflection offset (d_1) that often appears in the raw signal collected.
 147 This offset corresponds to the deflection value in the noncontact region, where the tip-sample interaction
 148 force is zero. We calculate d_1 by averaging the range of d values over the noncontact region (values of
 149 deflection far from the jump-to-contact point). With the appropriate offset subtraction, we can then
 150 calculate the tip-sample interaction force, $p(t)$:

$$p(t) = k_c(d(t) - d_1) \quad (2)$$

151 where the cantilever's stiffness, k_c , was calculated through the standard thermal noise method³².

152

153 **Elastic Analysis**

154 In the first portion of the results section we extract an "apparent stiffness" on the basis of Derjaguin-
 155 Muller-Topolov (DMT) theory that combines Hertzian contact mechanics with the inclusion of attractive
 156 probe-sample interactions attributed to Van de Waals forces (prominent at the nanoscale)³³. For the
 157 repulsive portion of the interaction, the relationship between tip-sample force, p , and sample penetration,
 158 h , (accessible quantities through the static force spectroscopy experiments) is:

$$p = \frac{4\sqrt{R}}{3} \frac{E}{1-\nu^2} h^{3/2} - 4\pi R\gamma \quad (3)$$

159 where R , E , ν , and γ are the tip radius, sample Young's modulus, sample Poisson's ratio, and the work of
 160 adhesion, respectively. We summarize the parameters accompanying the deformation as: $\beta = \frac{4\sqrt{R}}{3} \frac{E}{1-\nu^2}$,
 161 which is proportional to the Young's modulus. For the measurements in this study we extracted this
 162 parameter β (instead of the Young's modulus) to avoid making further assumptions about tip geometry
 163 (radius of curvature of the apex, R) which is hard to characterize for sharp AFM tips. Afterwards, we
 164 normalized the value of stiffness β by dividing all measurements by the largest stiffness measurement
 165 within the data analyzed. As a result, the values reported range from zero to one (from 'softer' to 'stiffer').
 166 The factor $4\pi R\gamma$ in Equation 3 corresponds to the adhesion force during contact (assumed to be constant
 167 in DMT theory) dictated by the work of adhesion between the AFM tip and the biofilm (γ). The adhesion
 168 force was calculated by the minimum tip-sample force located at the jump-to-contact point. Moreover, the
 169 AFM tip is assumed to experience no deformation (hard indenter), but instead only the sample is
 170 considered to be indented^{34,35}. As the accuracy of mechanical property determination with AFM depends
 171 on the assumption of maintaining a constant tip geometry, we tracked the probe's resonance frequency
 172 throughout the experiments to assess changes in the tip mass, and detected no significant changes.

173

174 **Viscoelastic analysis**

175 The main portion of the viscoelastic analysis (which is the main subject of this study) is presented in the
 176 results and discussion section. Here, we show some auxiliary functions that are specifically relevant to
 177 our analysis routines. We model the viscoelastic retardance, $U(t)$, with a Prony series to consider the
 178 presence of multiple characteristic times³⁶. We should emphasize that the approach outlined in this study
 179 is general to other viscoelastic models such as Power law models, fractional models, ladder models, etc.

180 We have found the use of Prony series to be especially advantageous for the automated analysis demanded
 181 in this context. The Prony series can be physically represented in terms of rheological models comprised
 182 by springs and dashpots (as we have used in previous studies³⁷⁻³⁹). Specifically, they may be represented
 183 with the generalized Voigt model or the generalized Maxwell model, which are mechanical analogs that
 184 display identical behaviors upon appropriate selection of parameters⁴⁰. Choosing one over the other obeys
 185 algebraical convenience, depending on whether stress/force or strain/displacement are regarded as the
 186 input. In the context of AFM force spectroscopy, where loading history is approximately linear²⁵, the
 187 generalized Voigt model is mathematically convenient (i.e., leads to more compact close-form
 188 solutions³⁹). Specifically, the viscoelastic retardance of the generalized Voigt model (Figure 1) is given
 189 by

$$U(t) = J_g + \sum_n J_n / \tau_n \exp(-t/\tau_n) + \{\phi_f\} \quad (4)$$

190 where J_g is the ‘glassy’ compliance and refers to the material’s response at infinitely short time-scales. ϕ_f
 191 is the steady-state fluidity in the case where the material is regarded as rheodictic (i.e., it can sustain
 192 steady-state flow), otherwise if the term is disregarded, and the material is considered arrheodictic. J_n and
 193 τ_n refer to the compliance and retardation time of the n^{th} Voigt unit in the generalized Voigt model⁴⁰. In
 194 this work, for convenience in the automated data analysis, the Prony Series in Equation 4 has been
 195 truncated to the first term (i.e., the standard linear solid model), although the code provided can be easily
 196 adjusted to incorporate more terms in the series as needed in the user’s specific application.

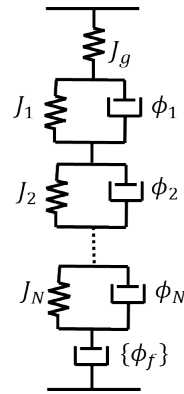


Figure 1 The generalized Voigt model consists of an arbitrary large number, N , of springs and dashpots. The elastic compliance of each spring J_n describes how ‘soft’ the spring is (inverse of stiffness). The fluidity of each dashpot (ϕ_n) describes how (inversely) viscous the damper is (i.e., how dissipative the dashpot is). This set of springs and dashpots accounts for the simultaneous energy storage and dissipation occurring when a biofilm is deformed. Each spring-dashpot pair in parallel corresponds to a distinct retardation time ($\tau_n = J_n/\phi_n$), i.e., the characteristic time at which rearrangements in the biofilm’s structure occur when a deformation is imposed. The (strain) response of this model to an impulsive (stress) excitation is given in terms of a Prony series as shown in Equation 4.

197

198 In Figure 3 and Figure 4 the inverse of the viscoelastic stiffness was also normalized to be shown as a
 199 value ranging from zero to one (from ‘softer’ to stiffer’). This also obeys practical purposes of avoiding
 200 further assumptions about tip geometry (hard to characterize with certainty for a sharp AFM tip). Avoiding
 201 assumptions about tip geometry we obtained values of normalized retardance ($U_N(t) = 3/[16\sqrt{R}]U(t)$)
 202 from which we obtained values of normalized compliance ($J_N(t) = 3/[16\sqrt{R}]J(t)$). Then in Figure 3 and

203 Figure 4 the normalized values of inverse of stiffness ($1/J_N(t)$) were divided by the maximum value
204 within the data analyzed, resulting in reported values ranging from zero to one.

205 III. RESULTS AND DISCUSSION

206 3.1 Elastic analysis of biofilms: addressing the spatial heterogeneity

207 In this section we show how the AFM can be exploited to obtain mechanical maps of biofilms with
208 nanoscale spatial resolution. We started by employing the common strategy (in AFM studies) of assuming
209 the material to be purely elastic. It is our intention to show that this simplified strategy (although
210 convenient for its simplicity) has significant shortcomings when analyzing a sample that is viscoelastic.

211 Figure 2 shows the results of performing a mechanical analysis on the biofilm over a scanned
212 image of $5 \mu m$. Figure 2(a) shows the topographical image acquired with tapping mode AFM where the
213 biofilm structure, comprised by closely packed bacterium cells, is clearly seen. Then we performed force
214 spectroscopy AFM experiments (see Experimental section for details) to interrogate the mechanical
215 properties of the biofilm on a 64×64 pixel grid (higher resolution may be obtained at the expense of a
216 longer experimental time) over the same area shown in Figure 2(a). Specifically, two force spectroscopy
217 maps were acquired at distinct cantilever approach velocities (1.02 and $14.6 \mu m/s$). Each force map was
218 then postprocessed by assuming that the sample is elastic (see details in Elastic Analysis subsection of the
219 Experimental section) and a relative stiffness map was then derived for each distinct approach velocity
220 (Figure 2(b) and (c)). These analyses are quite straightforward and provide a quick understanding of the
221 mechanical map of the material with high spatial resolution. However, for viscoelastic materials (such as
222 biofilms) the values of apparent stiffness depend on the probing rate, as evidenced by the differences in
223 the maps between Figure 2(b) and (c). Intuitively, viscoelastic materials rearrange stresses when
224 deformed, through processes involving energy dissipation. Therefore, their apparent stiffness depends on

225 the timescale at which they are probed. If the probing timescale is long, the material may rearrange stresses
 226 and appear to be ‘softer’ than if probed at high velocities.

227 The immediate consequence of the elastic simplification is that inconsistent mechanical maps are
 228 obtained when probing a viscoelastic material at different velocities (Figure 2(b) and (c)). This
 229 inconsistency causes the stiffness map in Figure 2(b) to display larger bright-color areas, indicating a
 230 general apparent stiffer behavior compared to the map in Figure 2(c). This is further evidenced in the
 231 summarized statistical analysis in Figure 2(d) where the histogram for the approach velocity of $14.6 \mu\text{m/s}$
 232 shows significantly larger counts in the higher stiffness range (0.5-1.0) compared to the $1.02 \mu\text{m/s}$
 233 velocity map. The boxplots in Figure 2(d) also support this observation, showing that the distribution of
 234 stiffness shifts to higher values for the case of the $14.6 \mu\text{m/s}$ approach velocity map. These inconsistencies
 235 happen because biofilms have rate-dependent mechanical properties, and therefore their analysis demands
 236 using an appropriate method that considers their viscoelastic behavior.

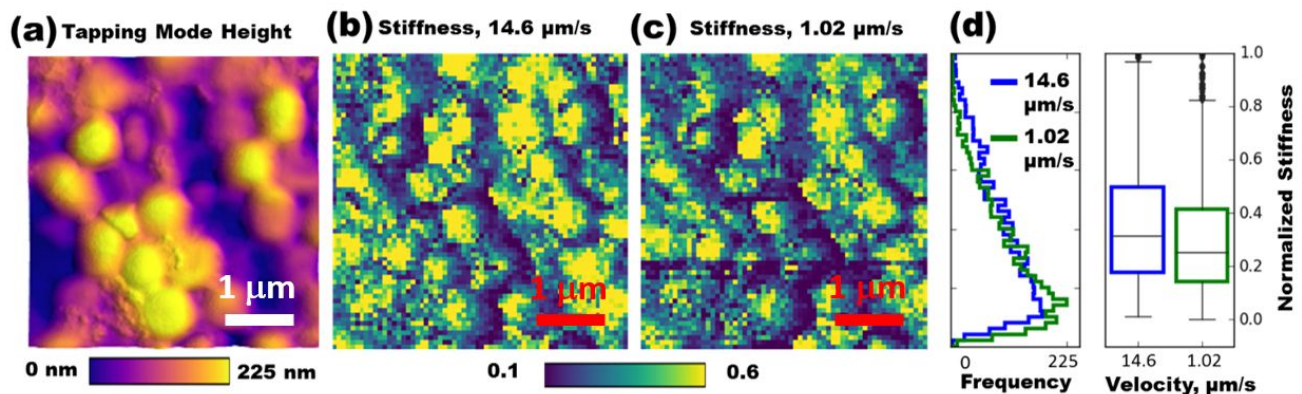


Figure 2 Illustration of spatial heterogeneity and velocity dependence of apparent Young’s modulus of biofilms. (a) Tapping mode topography of the biofilm over a $5 \mu\text{m}$ size image. (b) and (c) correspond to maps of apparent relative stiffness at two distinct cantilever approach velocities: 14.6 and $1.02 \mu\text{m/s}$, respectively. These stiffness maps

correspond approximately to the area of the tapping mode image in (a). The relative stiffness (proportional to the apparent Young's modulus) ranges between 0 and 1, from softer to stiffer (see Experimental section for details). (d) Horizontal histogram (left-hand-side) and boxplots (right-hand-side) sharing common vertical axis and legends, for the stiffness data shown in (b) and (c).

237

238 **3.2 Viscoelastic analysis: addressing the time and spatial heterogeneity simultaneously**

239 **3.2.1 Time-frequency localized mechanical maps of biofilms**

240 As stated in the previous section, the simplified elastic analysis has shortcomings when analyzing
241 viscoelastic materials like biofilms. In this case we should analyze the AFM data in the light of an
242 appropriate theoretical framework that considers the history-dependent nature of biofilms. This distinct
243 nature can be approximately captured by rheological models comprised by (elastic) springs and (viscous)
244 dashpots^{39, 40}. The springs reproduce the elastic response of the specimen, whereas the dashpots consider
245 the energy dissipated through the mechanical deformation. The dashpot can be visualized as a piston-
246 cylinder device whose mechanical (stress) response is proportional to the (input) strain-rate and the
247 viscosity of the fluid contained in the cylinder. These spring-dashpot models range from very simple sets
248 comprised by one spring and one dashpot (e.g., Maxwell and Kelvin-Voigt models) to more sophisticated
249 representations that contain multiple characteristic times (e.g., Generalized Voigt model as in Figure 1)^{39,}
250 ⁴⁰. The specific model selection obeys practical aspects concerning the time-scale studied, the level of the
251 approximation, the amount of noise in the measurement, etc. However, regardless of the model chosen,
252 viscoelastic materials display general behaviors such as a distinct apparent stiffness and distinct levels of
253 energy dissipation, depending on the rate at which they are deformed. A direct consequence of this rate-
254 dependent behavior was discussed in the previous section with respect to the differences in the apparent

255 elastic maps shown in Figure 2(b) and (c). Consequently, viscoelastic materials cannot be described by
256 elastic constants but instead their deformation is captured by time and frequency dependent functions (i.e.,
257 the standard viscoelastic responses). For this analysis we chose two distinct standard responses, the loss
258 angle $\theta(\omega)$ and the creep compliance $J(t)$. The creep compliance, $J(t)$, describes how a viscoelastic material
259 deforms in time when a constant stress (force per unit area) is applied ³⁶. We interpret its inverse, $1/J(t)$,
260 as an effective time-localized stiffness (i.e., instantaneous stiffness) for reasons that are mathematically
261 justified in a later subsection.

262 Figure 3 (a) shows this localized stiffness that we calculate within a finite time window for the
263 same location of the biofilms shown in Figure 2(a). Unlike the elastic analysis of the previous section, in
264 this viscoelastic analysis we are able to capture a time-varying stiffness by exploiting an appropriate
265 mathematical framework that considers the viscoelastic behavior of biofilms. Details on the retrieval of
266 the viscoelastic properties are provided in the following subsection. It is evident that, in general, the
267 stiffness in the biofilms evolves from a stiffer to a softer behavior (see scale bar in Figure 3(a)). This
268 observation obeys the fact that at short time scales (fast deformations) viscoelastic materials tend to be
269 stiff-elastic, which is known as the glassy response. Intuitively this happens because, upon imposition of
270 fast deformations, the materials do not have enough time to accommodate the internal stresses and behaves
271 as if they were purely elastic. On the other extreme, at very large time-scales (slow deformations) the
272 material totally rearranges and behaves in a soft-elastic manner, which is known as the rubbery elastic
273 response. The left-hand-side and right-hand-side maps in Figure 3(a) lay in between these two (elastic)
274 extrema in a regime where energy dissipation occurs: the viscoelastic regime. For this analysis we have
275 used the same AFM force spectroscopy raw data used to generate the elastic map in Figure 2(b). Although,
276 in this case instead of retrieving a single map, we obtain a time-localized stiffness that may be plotted with
277 an arbitrary number of frames within the experimental time window. In other words, we can

278 simultaneously localize mechanical properties in space and time. The mathematical details of the analysis
 279 are provided in the next subsection.

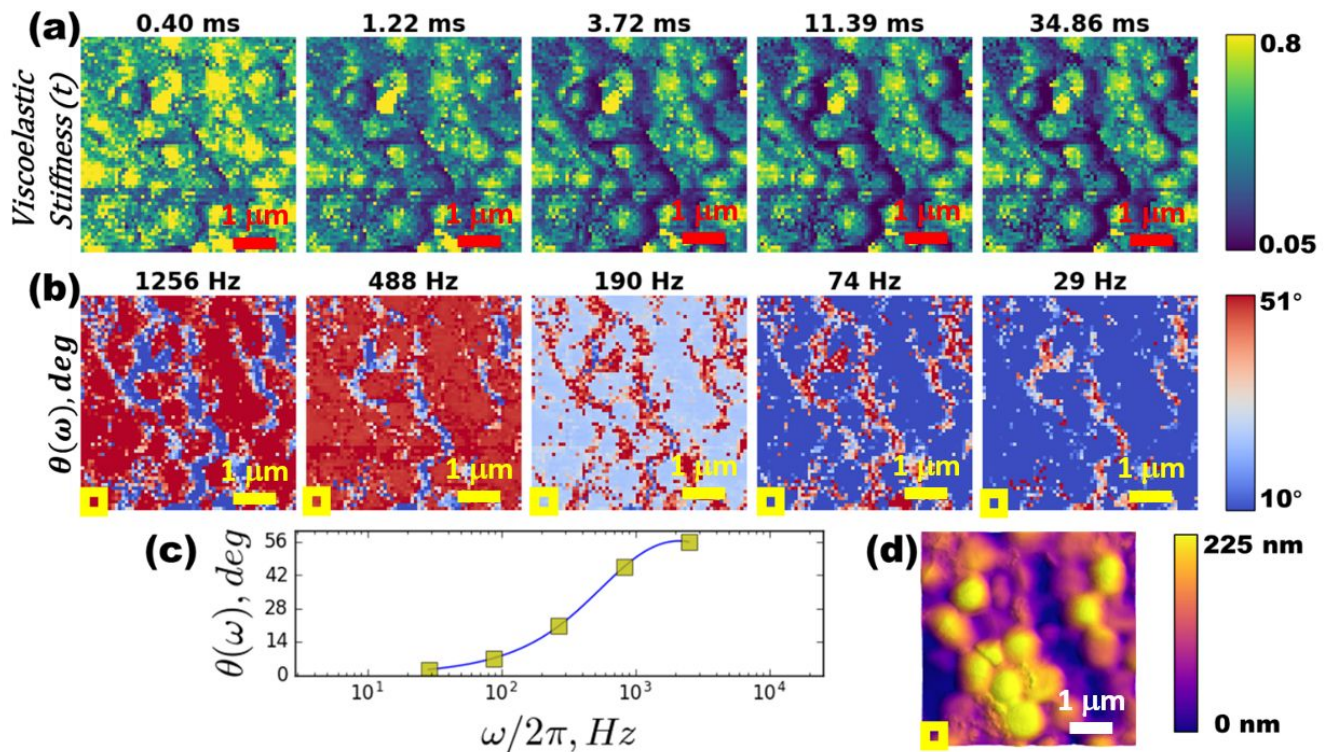


Figure 3 Representation of the simultaneous spatial and time-frequency localization of mechanical (viscoelastic) properties of biofilms obtained in a single force spectroscopy AFM map. (d) Tapping mode topography of the 5 μm image where, approximately, the force spectroscopy map was performed. (a) and (b) highlight the time and frequency localization of mechanical properties, respectively, obtained by the method explained in the next subsection: Mathematical foundation of the viscoelastic analysis. Specifically, we show the localization of mechanical properties in time and frequency, in terms of the inverse of viscoelastic compliance, $1/J(t)$, and the loss angle, $\theta(\omega)$, respectively. The time-frequency localization in (a) and (b) is shown from short timescale mechanical behavior (left) to longer timescale behavior (right). The scale bar

in (a) shows a value of relative stiffness between 0 and 1, with values closer to 1 being an indication of stiffer behavior (details are explained in the Experimental section). The units in the scale bar of (b) are degrees and span between 0° and 90° , lower values indicating the sample being closely elastic and higher values more viscous. (c) Loss angle $\theta(\omega)$ for the (0,0) spatial pixel, then 5 points equally spaced (in logarithmic frequency scale) are selected to generate frequency-localized maps of loss angle. The calculation of the limits in the time-frequency window is explained in the subsection: Finite time-frequency window of the viscoelastic analysis.

280

281 Besides the retrieved time-varying stiffness, the present analysis allows us to retrieve another
282 meaningful viscoelastic property: the loss angle $\theta(\omega)$, whose value spans from zero when the material is
283 purely elastic to ninety when the material is purely viscous. For example, when a biofilm is harmonically
284 deformed with a specific frequency ω (i.e., a sinusoidal input) it dissipates and stores energy with a certain
285 ratio that depends on the value of ω . When the frequency ω is high (fast deformations) a viscoelastic
286 material tends to its glassy-like behavior, whereas at low excitation frequencies (long time scales) the
287 viscoelastic material tends to behave in a rubber-elastic fashion, as previously discussed. We plot $\theta(\omega)$ in
288 Figure 3(b) and it is interesting to observe the complementary information that this quantity offers and
289 how it can further aid in the identification of specific material phases at the surface of the biofilm. In this
290 case, the most abundant phase shows a high viscous behavior at short time scales (high frequencies) while
291 a more elastic-like behavior at long time scales (low frequencies), probably associated with a rubbery
292 response (consistent with the previous discussion). Here, the frequency window is again finite and defined
293 by the experimental time scale (details provided in the Experimental Section).

294 Figure 3(c) shows as an example the loss angle $\theta(\omega)$ retrieved for the (0,0) pixel corresponding to
295 (approximately) the biofilm area marked by the yellow square in Figure 3(d). Once we retrieve this
296 function, we proceed to choose (arbitrarily) five points equally localized in the logarithmic scale (marked
297 by the yellow squares in Figure 3(c)). By locating these values, we can map them to two-dimensional grids
298 in distinct frames (each frame corresponding to a distinct frequency). By repeating this process for each
299 pixel, we can generate the visualization plotted in Figure 3(b). An analogous process is performed to
300 retrieve the visualization shown in Figure 3(a) showing the instantaneous stiffness. For convenience this
301 process is fully automated, and the analysis is shared in an open-access repository ⁴¹.

302 To demonstrate that this technique can be exploited even at the single-cell scale, we show its
303 applicability in a small scanned area of 500 nm located on top of a single bacterium in the biofilm. These
304 results are shown in Figure 4 and the same explanations used for Figure 3 apply here. As a result of these
305 analyses, we are able to localize viscoelastic properties in the time-frequency domain with the high spatial
306 resolution afforded by the AFM. This is a very relevant step forward when compared with the often used
307 Hertzian analysis that only allows extraction of a map of apparent stiffness, without any time-frequency
308 localization (e.g., Figure 4(d)). By the additional channels that the proposed technique offers, and the time-
309 frequency localization afforded by the viscoelastic analysis, we can better discriminate between the
310 components of the materials.

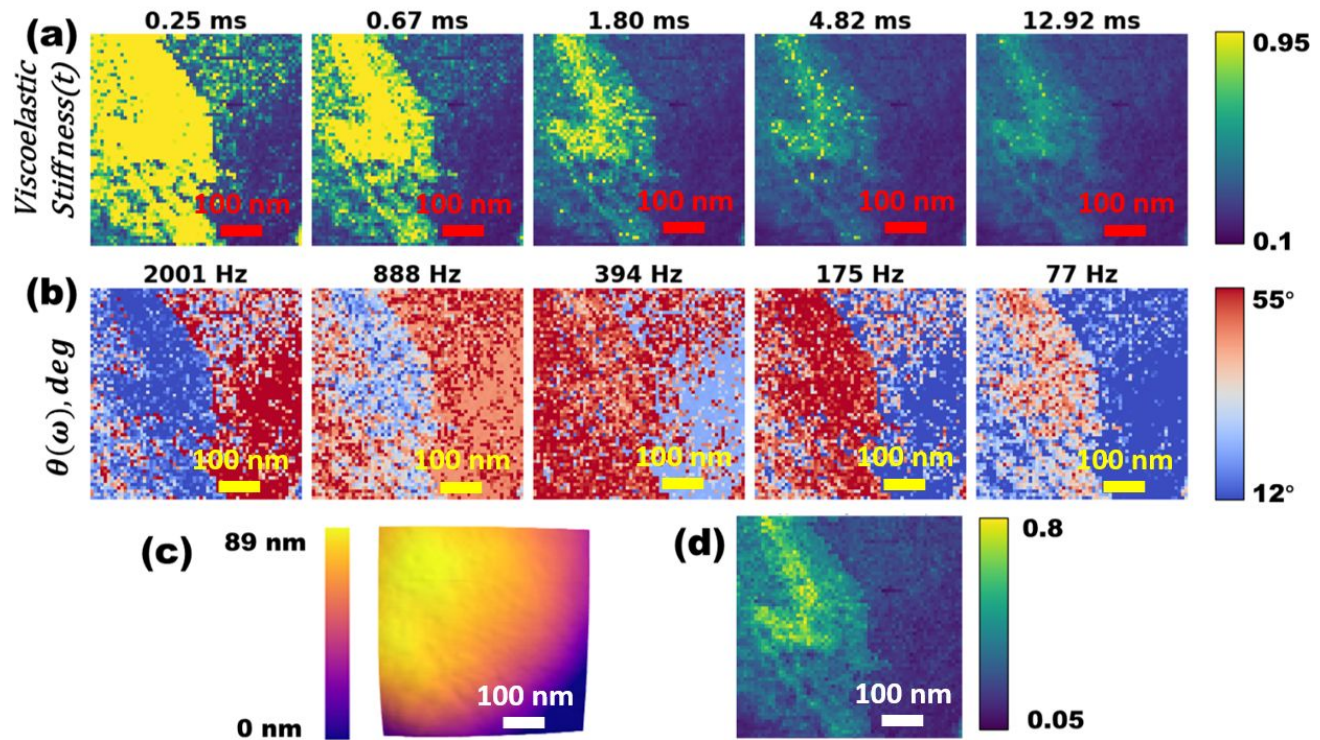


Figure 4 Same analysis as the one shown in Figure 3 but applied to a 500 nm image size on top of a single bacterial cell. (c) Tapping mode topography of the bacterial cell. (a) and (b) highlight the time and frequency localization of mechanical properties, respectively. We show the localization of mechanical properties in time and frequency in terms of the inverse of viscoelastic compliance, $1/J(t)$, and the loss angle, $\theta(\omega)$, respectively. The time-frequency localization in (a) and (b) is shown from short timescale mechanical behavior (left) to longer timescale behavior (right). The scale bar in (a) shows a value of relative stiffness between 0 and 1, ranging from softer to stiffer (details are explained in the Experimental section). The units in the scale bar of (b) are degrees and span between 0° and 90° , lower values indicating the sample being closely elastic and higher values indicating it is more viscous. (d) ‘Apparent stiffness’ map when assuming the

sample is purely elastic (i.e., using Hertzian analysis), within this framework the time-frequency localization of mechanical properties is not available.

311

312

313 **3.2.2 Mathematical foundation of the viscoelastic analysis**

314 After the qualitative description, we proceed with a brief mathematical description of the viscoelastic
 315 analysis that is used to extract meaningful mechanical information of the biofilm. To gain mechanical
 316 information with high spatial resolution, we used a sharp probe with a nanoscale tip that interacted with
 317 the sample. Regardless of the rheological model used, when our AFM tip indents a viscoelastic biofilm,
 318 the relationship between the loading history, $p(t)$, and indentation, $h(t)$, is given by^{39, 42-46}:

$$\frac{16\sqrt{R}}{3}h(t)^{3/2} = \int_0^t U(t - \zeta)p(\zeta)d\zeta \quad (5)$$

319 where R is the tip radius, $U(t)$ the retardance (i.e., the (shear) strain response to a unit (shear) stress impulse
 320 ⁴⁰), t refers to instantaneous time and ζ is a dummy variable of integration. In this relationship the
 321 viscoelastic retardance $U(t)$ is convolved with the history of loads $p(t)$ applied to the biofilm during the
 322 AFM indentation, which underlines the history-dependent nature of the biofilm mechanical model.
 323 Equation 5 has assumed the biofilm to be incompressible (Poisson's ratio $\nu = 0.5$), a common assumption
 324 in biological models^{47, 48}. In a force spectroscopy experiment we can access the indentation and load
 325 history ($p(t)$, and $h(t)$) in Equation 5, from which we can (in principle) find a suitable integration kernel,
 326 $U(t)$, that satisfies the relationship. Nonetheless, this is a mathematically challenging problem (a first kind
 327 Volterra integral equation) that is inherently ill-posed^{49, 50}. This issue can be alleviated if assuming we
 328 know in advance the general shape of $U(t)$, hence the need of employing specific rheological models (e.g.,
 329 set of springs and dashpots). In this study we employ the generalized Voigt model³⁹ (see Figure 1),

330 although the theory outlined here is general and other representations could be employed (e.g., power law
 331 models^{51,52}, fractional models^{53,54}, ladder models⁴⁰, Kelvin-Voigt model^{16,55}).

332 Once we calculate the retardance, $U(t)$, we can easily obtain the so-called creep compliance $J(t)$ ⁴⁰:

$$J(t) = \int_0^t U(\zeta) d\zeta \quad (6)$$

333 and the dynamic compliance (also called complex compliance) $J^*(\omega)$ ⁴⁰:

$$J^*(\omega) = \int_{-\infty}^{\infty} U(t) e^{-i\omega t} dt \quad (7)$$

334 which has real and imaginary components: $J^*(\omega) = J'(\omega) + iJ''(\omega)$, that correspond to the storage $J'(\omega)$
 335 and loss compliance $J''(\omega)$ respectively. Also, the loss angle, $\theta(\omega)$, can be deduced from the ratio of these
 336 quantities:

$$\theta(\omega) = \tan^{-1} \left(\frac{J''(\omega)}{J'(\omega)} \right) \quad (8)$$

337 This viscoelastic analysis can be performed in a pixel by pixel manner (as illustrated in Figure 5)
 338 when the AFM probes specific points in the biofilm, while collecting a force spectroscopy map (see
 339 Experimental section for details). This map of viscoelastic functions is analogous to the map of stiffness
 340 shown in Figure 2(b) and (c), although in this case it is a map of time-dependent or frequency-dependent
 341 functions (as shown in Figure 3). Figure 5(b) and (c) show the result of the non-linear square (NLS)
 342 optimization process to retrieve the retardance $U(t)$ for a specific pixel. In Figure 5(b) the solid lines follow
 343 the experimental traces collected by the AFM (i.e., left-hand side of Equation 5) while the dashed lines
 344 correspond to the convolution between $U(t)$ (obtained through the NLS fitting process), and the
 345 experimental load history, $p(t)$ (i.e., the right-hand side of Equation 5). The results shown correspond to
 346 two distinct cantilever approach velocities, as described in the figure legends. Figure 5(c) shows analogous
 347 data as that of Figure 5(b), but in terms of a conventional force-distance curve, a common representation
 348 in AFM force spectroscopy.

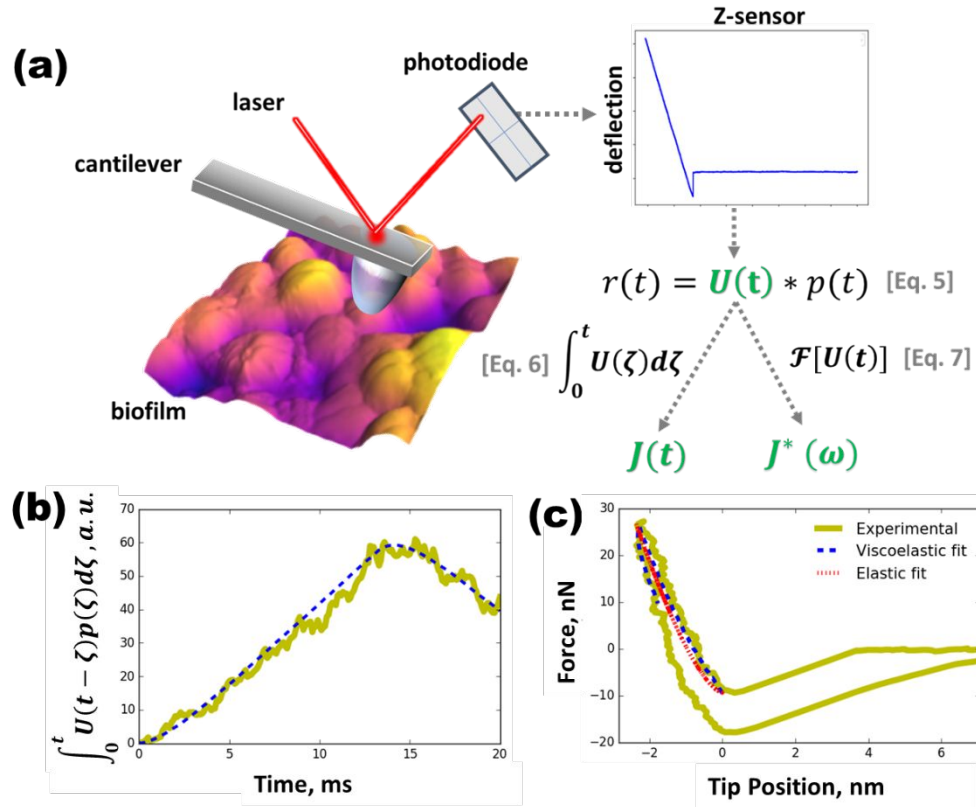


Figure 5 Pixel by pixel evaluation of biofilm viscoelastic properties. (a) General schematics of the experimental procedure and analysis to extract the viscoelastic properties. Briefly, the viscoelastic characterization centers on finding a suitable convolution kernel (the viscoelastic retardance, $U(t)$) in Equation 5 through a non-linear least square optimization (here $r(t)$ summarizes the left hand side of Equation 5). Once the retardance is found, other viscoelastic quantities can be derived from it following Equations 6 - 8. (b) Result of the fitting performed to the force spectroscopy observables in a single pixel. The continuous lines represent the experimental observables (left hand side of Equation 5) while the blue dashed line is the non-linear viscoelastic fit (right hand side of Equation 5). (c) The same results as in (b) but plotted in terms of the more intuitive

typical force-distance curve. The elastic fit is also given in the red dashed line for reference.

349

350 **3.2.3 Why we interpret the inverse of creep compliance ($1/J(t)$) as a measurement of time-localized** 351 **stiffness**

352 The relation between load (p) and indentation (h) described in Equation 5 can be equivalently written in
353 its more popular form in terms of the creep compliance function $J(t)$ ⁴²:

$$\frac{16\sqrt{R}}{3}h(t)^{3/2} = \int_0^t J(t-\zeta) \frac{dp(\zeta)}{d\zeta} d\zeta \quad (9)$$

354

355 During static force spectroscopy AFM, the tip-sample interaction force (load) approximately grows
356 linearly in time: $p \approx \dot{p}t$ ^{25, 26}. Which reduces the previous equations to³⁹:

$$\frac{16\sqrt{R}}{3}h(t)^{3/2} = \dot{p} \left[\int_0^t J(\zeta) d\zeta \right] = \dot{p}[\chi(t)] \quad (10)$$

357 where the term in brackets, $\chi(t)$, refers to the sample's fluidity, the strain response to a unit stress ramp (
358 $\sigma(t) = \dot{\sigma}t$)⁴⁰. Differentiating with respect to time yields:

$$\frac{16\sqrt{R}dh(t)^{3/2}}{3 dt} = \dot{p}J(t) \quad (11)$$

359 Now, substituting $\dot{p} = \frac{dp}{dt}$ and rearranging, we obtain:

$$\frac{dp}{dh(t)^{3/2}} = \frac{16\sqrt{R}}{3} \frac{1}{J(t)} \quad (12)$$

360 We may compare the above with the elastic case (parabolic hard indenter penetrating an elastic surface)

361 ^{34, 35}

$$\frac{dp}{dh^{3/2}} = \frac{16\sqrt{R}}{3} G \quad (13)$$

362 where G is the elastic shear modulus, and the material has been assumed to be incompressible (Poisson's
363 ratio, $\nu = 0.5$). The viscoelastic relationship only differs from the elastic one by the factor $\frac{1}{J(t)}$ in place of

364 G . This interesting observation demonstrates that the inverse of the shear creep compliance ($1/J(t)$) is the
365 viscoelastic analog to the elastic shear modulus in a force spectroscopy experiment ⁵⁶, therefore we use it
366 as a measurement of time-localized (viscoelastic) stiffness in Figure 3 and Figure 4. Recall that the shear
367 modulus (G) and Young's modulus (E) are proportional: $E = 2G(1 + \nu)$.

368

369 ***3.2.4 Finite time-frequency window of the viscoelastic analysis***

370 In this section we discuss some technical yet critical details about the limits in time and frequency where
371 the viscoelastic functions retrieved remain valid. For example, it is desirable to know how dissipative the
372 biofilm is (value of $\theta(\omega)$) for a wide range of harmonic frequencies ω , to know how it will respond to a
373 wide variety of mechanical stimuli. However, our experiment has a limited time-frequency window where
374 our viscoelastic functions calculated are meaningful. In Figure 3 and Figure 4 we have clearly laid out
375 these specific time-frequency windows where the calculations are accurate (from the first to the fifth
376 frame), however the justification and calculation of these windows have not been explained yet.

377 To clearly understand this point, it is important to focus our attention on Equation 5, which contains
378 the viscoelastic source function (the retardance, $U(t)$) from which the other functions are derived
379 (Equations 6 - 8). This integration kernel $U(t)$ in Equation 5 is the system's response of the material to an
380 impulsive excitation. Any linear theory regards knowledge of this function as highly desirable since it
381 fully characterizes the system ^{57, 58}. Therefore, it is tempting to believe that obtaining a suitable
382 approximation of $U(t)$ (by means of Equation 5) would give us information about the material's
383 viscoelastic properties in the whole time and frequency domains. This concept of course is flawed, because
384 we only have a finite time resolution of the retrieved $U(t)$. Specifically, we can only access
385 (experimentally) this quantity with a certain degree of certainty within a specific 'region of interest'
386 dictated by the experimental timescale. This 'region of interest' is bound by the limits in which the

387 experimental observables (in this case load and displacement) are above certain level of signal to noise
388 ratio (SNR), i.e., the regions where the quantities deliver meaningful information. For example, if we
389 probe a material at three different speeds (see Figure 6(a)) the retrieved $U(t)$ will have different ‘regions
390 of interest’ for each approach velocity. Only within this ‘region of interest’ is it correct to describe the
391 derived mechanical properties. This concept is illustrated in Figure 6(c) and Figure 6(d) where we have
392 delimited with solid lines the regions where the calculations are appropriate. In the ‘signal to noise ratio’
393 (SNR) calculation we made an *a posteriori* estimation, assuming that noise is of stochastic nature (details
394 can be found in Czesla et al.⁵⁹). This assumption is compatible with the type of noise arising from thermal
395 fluctuations of the AFM cantilever⁶⁰. Once noise is calculated, we calculated the minimum time when the
396 deflection signal surpasses the noise level by 10 times (SNR=10) and defined this as the lower limit of the
397 time window (t_{min}). The upper limit in the time window (t_{max}) is given by the total experimental time
398 during tip-sample contact in the force spectroscopy experiment. The lower limit in the frequency window
399 is the inverse of the total experimental time ($f_{min} = 1/t_{max}$). The upper limit of the frequency window is
400 the Nyquist frequency ($f_{max} = 1/2 f_s$),⁶¹ where f_s is the sampling frequency, which for the viscoelastic
401 retardance $U(t)$ is $1/t_{min}$, thus $f_{max} = 1/[2 t_{min}]$.

402 With the dashed lines we highlight the dangers of extrapolating the results to frequency windows
403 beyond the ‘region of interest’. In other words, we underline that certain model parameters are only
404 appropriate within a time-frequency window. For this reason, we avoid the practice of reporting specific
405 rheological parameter values and instead focus on discussing standard viscoelastic responses (e.g., $J(t)$
406 , $\theta(\omega)$) and the time-frequency regions where they are valid.

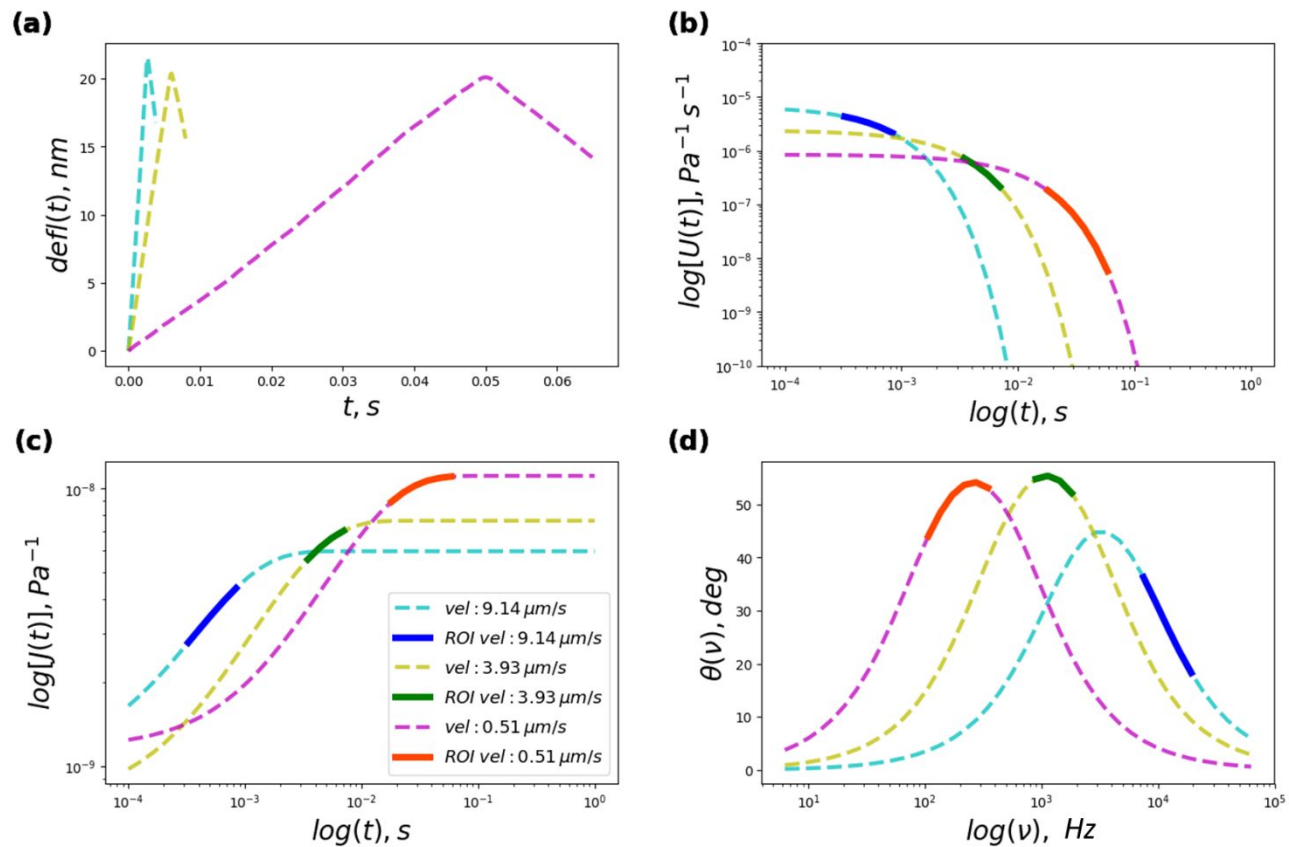


Figure 6 Results of viscoelastic analysis related to force spectroscopy experiments performed at three different velocities (as indicated in the figure legends) over approximately the same area (single-pixel) of the biofilm. This figure illustrates the complementary viscoelastic information gained when probing at different speeds. (a) Load histories for three different force spectroscopy experiments. (b)-(d) Calculated viscoelastic quantities: retardance, creep compliance, and loss angle, respectively, with their ‘regions of interested (ROI)’ delimited within a finite time-frequency window. These viscoelastic quantities were calculated with Equations 5, 6, and 8, respectively. The figure legends shown in (c) are applicable for all subplots. Details on the estimation of the time-frequency window’s limits are provided in the main text.

408 ***3.2.4 Implications of the viscoelastic measurements on biofilm removal***

409 The viscoelastic properties of biofilms, especially of the EPS matrix are believed to confer high structural
410 stability to the system. Therefore, a detailed understanding of the viscoelastic signature is highly desirable.
411 Specifically, it is believed that EPS closely relates to the high cohesiveness of the biofilms. Mechanical
412 properties such as shear modulus have been proved to be directly linked to cohesiveness in the context of
413 synthetic polymers. It is logical to extrapolate this observation to biofilms where biopolymers are the main
414 component of the EPS matrix. As has been discussed for the results of Figure 3 and Figure 4, the shear
415 modulus of biofilms is time-dependent (viscoelastic), therefore its apparent value depends on the time
416 scale of the deformation. For example, the time-dependent shear modulus may display a stiff-elastic
417 behavior at fast deformations or soft-elastic behavior at slow deformations. This concept is further
418 illustrated in Figure 7.

419 For this reason, a viscoelastic framework such as the one discussed here is crucial in order to have
420 a better picture of how biofilms behave at different rates of deformation. This thorough knowledge has
421 direct implications on understanding and envisioning effective techniques for biofilm removal. For
422 example, knowing at which deformation rates the material is less dissipative can give effective guidelines
423 for mechanical removal through time-dependent inputs that can effectively transfer the energy to cohesive
424 fracture mechanisms. This would also help to avoid deformation rates at which the mechanical input for
425 removal would be wasted through energy dissipation (i.e., viscoelastic dissipation).

426 The limited time-frequency window in which the biofilm's mechanical properties are evaluated
427 can be conveniently expanded within the framework given in this study (as discussed in the previous
428 subsection, see Figure 6) to higher frequencies up to the kHz regime. This is achieved with the appropriate
429 selection of experimental parameters (e.g., probing velocity, cantilever resonance frequency), which
430 results in obtaining the mechanical response of the biofilm in the ultrasonic regime. This has direct

431 implications in the context of treating biofilm infections in hospital patients, as has been shown that
 432 antimicrobial activity can be enhanced when ultrasound waves are propagated to the specimen. In other
 433 words, knowing specifically the nanomechanical response of the biofilm in the ultrasonic regime can
 434 provide a better understanding on specific frequencies at which the biofilm can become more susceptible
 435 to chemical stimuli (e.g., antimicrobial and antibiotic activities). To summarize, the analysis technique
 436 presented here allows the acquisition of a very thorough viscoelastic picture with high spatial resolution,
 437 having explicit practical implications regarding effective mechanisms for biofilm eradication.

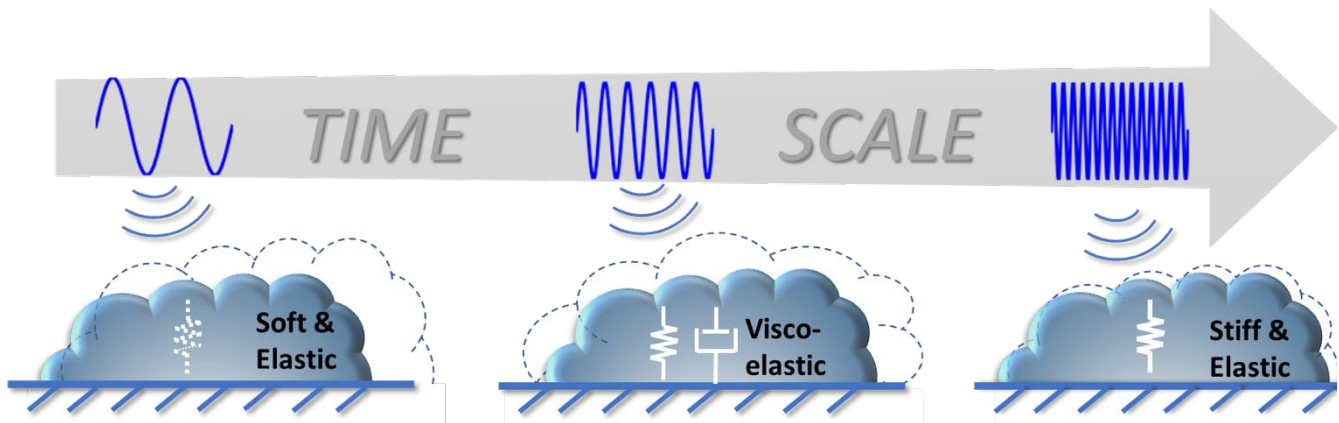


Figure 7 Illustrative concept of the viscoelastic properties of biofilms. The conceptual sketch shows that the mechanical behavior of biofilms depends on the timescale of the deformation, showing that at certain deformation rates they may display a *near elastic* behavior, whereas at other rates they may be more *dissipative*.

438

439 IV. CONCLUSION

440 We have presented a powerful technique to extract viscoelastic properties of nanoscale materials in a
 441 localized manner. We have shown that this technique is especially beneficial for highly heterogeneous
 442 systems, such as biofilms. In this powerful technique the mechanical properties are localized in the time-
 443 frequency domain, giving specific information on how the material behaves at different deformation time

444 scales. The amount of information obtained is very intensive when compared with the frequently used
445 Hertzian analysis, which neglects viscoelastic effects. It has been shown that the proposed technique can
446 provide thorough mechanical information in a wide time-frequency window up to the kHz regime. We
447 have also discussed the practical implications that the insights provided by this technique may have with
448 respect to designing effective strategies for biofilm eradication. Additionally, the technique requires little
449 sample preparation and is compatible with biofilm native environments (e.g., liquids), while providing a
450 high spatial resolution, even at the single-cell level. We expect this type of analysis to also be beneficial
451 to study other biological (e.g., human cells and tissues) viscoelastic systems that would be better described
452 by the theoretical framework on which this technique relies (compared to the conventional Hertzian
453 analysis).

454

455 **V. CONFLICTS OF INTEREST**

456 There are no conflicts to declare.

457

458 **VI. ACKNOWLEDGEMENTS**

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460

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462 **VII. REFERENCES**

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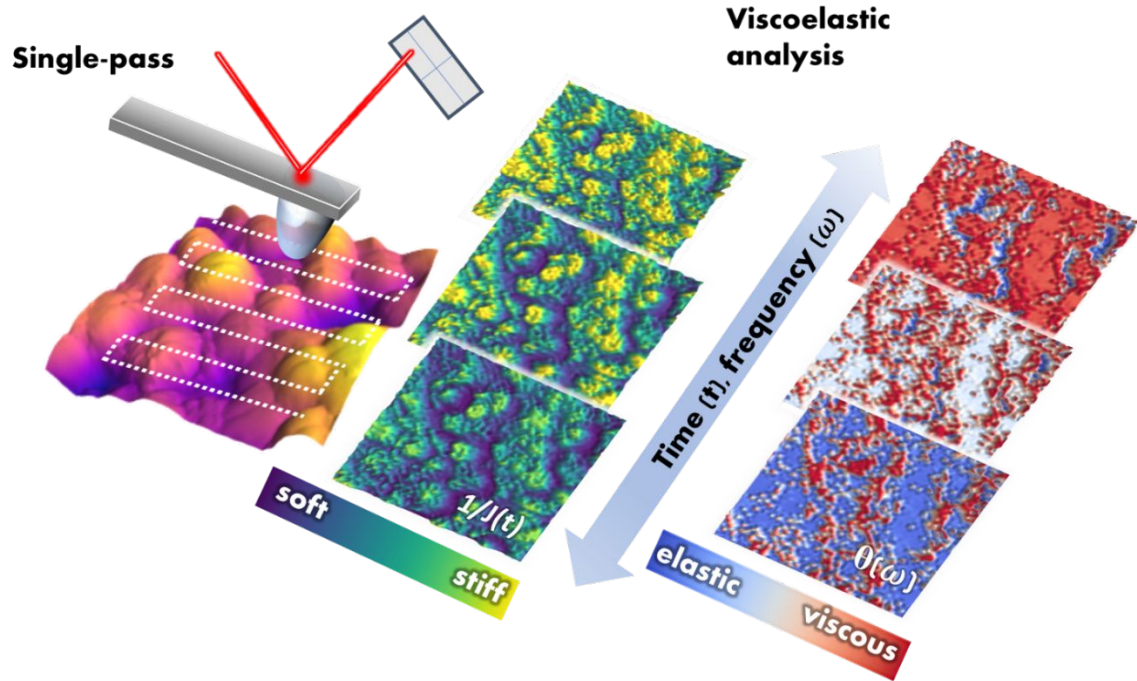
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Table of Contents



History-dependent viscoelastic analysis by atomic force microscopy delivers highly spatial-localized biofilm properties within a wide time-frequency window.