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# Ionic strength and molecular weight effects on floc formation and growth in Taylor-Couette flows

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26 Keywords: flocculation, Taylor-Couette flows, aqueous colloidal suspensions, mixing, radial  
27 fluid injection, bentonite, polyelectrolytes

28

29 Abstract

30

31 Polyelectrolyte-driven flocculation of suspended particulate in solution is an important process in  
32 a variety of industrial processes such as drinking water treatment and composite material  
33 synthesis. Flocculation depends on a wide variety of physicochemical and hydrodynamic  
34 properties, which affects floc size, growth rate, and morphology. Floc formation and growth  
35 behavior is explored here using two different molecular weights of a cationic polyacrylamide  
36 flocculant and anisotropic Na-bentonite clay particles under a variety of solution ionic strengths.  
37 A Taylor-Couette cell with radial injection capabilities was used to study the effects of solution  
38 ionic strength and polyelectrolyte molecular weight on floc size, growth rate, and morphology  
39 during the flocculation process with a constant global velocity gradient. The floc size generally  
40 decreased with increasing ionic strength whereas the floc growth rate initially increased then  
41 decreased. This likely occurred due to charge screening effects, where increased bentonite  
42 aggregate size and a less expanded polyelectrolyte conformation at higher ionic strengths results  
43 in a decreased ability for the polyelectrolyte to bridge multiple bentonite aggregates. The  
44 densification of bentonite aggregates at higher ionic strengths resulted in floc morphologies that  
45 were more resistant to shear-induced breakage. With the exceptions of optimal dose  
46 concentration and dispersion coefficients, there were no clear differences in the floc growth rate  
47 behaviors for the two molecular weights studied. This work contributes to an improved  
48 understanding of the physicochemical complexities of polyelectrolyte-driven flocculation that  
49 can inform dosing requirements for more efficient industrial operations.

50 Introduction

51

52 Polyelectrolytes, or polymers with charged functional groups, are used in a variety of  
53 applications such as drag reduction, enhanced oil recovery, paper manufacturing, and  
54 flocculation in drinking water treatment.<sup>1-5</sup> In flocculation, polyelectrolytes are added to a  
55 particulate-laden suspension so that they adsorb to multiple suspended particulates, forming  
56 structures known as flocs that can be readily separated from solution. Rapid floc growth occurs  
57 during mixing by orthokinetic aggregation, where the particulates with adsorbed polyelectrolyte  
58 collide and grow due to the shear gradients present in the flow.<sup>6-8</sup> The variation in chemical  
59 composition of the aqueous solutions along with the complexity of the hydrodynamics involved  
60 in mixing make understanding the process of flocculation difficult to understand. This results in  
61 reliance of highly empirical methods to determine polyelectrolyte flocculant dosing amounts in  
62 applications like drinking water treatment.

63 The particulate of interest in this study is bentonite, a clay particle commonly found in  
64 surface waters that has been used in prior flocculation studies.<sup>9-12</sup> Bentonite itself is an aggregate  
65 of many thin sheets, where the basal planes consist of permanent negative charges, and the edges  
66 consist of hydroxyl groups where the charge can vary with pH.<sup>13,14</sup> Due to these surface charges,  
67 the morphology of the bentonite aggregate is susceptible to changes in solution ionic strength or  
68 pH. An increase in solution ionic strength results in a change in the bentonite structure from a  
69 more porous morphology to a denser morphology. This change in aggregate structure has been  
70 indirectly confirmed with rheological measurements and confocal microscopy and directly  
71 confirmed with scanning electron microscopy.<sup>15-22</sup> Changes in solution ionic strength also have  
72 consequences for bentonite aggregate size. A previous study by Wilkinson et al.<sup>21</sup> showed that an

73 increase in solution ionic strength resulted in an increase by two orders of magnitude of the  
74 initial bentonite aggregate size, which is attributed to the decrease in Debye length between  
75 bentonite sheets. This allows aggregation of the bentonite sheets to form denser, face-face  
76 morphologies and larger bentonite aggregates in solution.<sup>7,23</sup>

77 The variations in bentonite aggregate surface morphology and aggregate size due to  
78 changes in solution ionic strength result in different adsorption capacities and interaction  
79 potentials with the polyelectrolyte flocculant that is added to a bentonite-laden suspension, thus  
80 increasing the complexity of fundamentally understanding flocculation.<sup>24</sup> In addition to charge  
81 screening affecting the aggregate structure of the bentonite, the polyelectrolyte present in  
82 solution will also change conformation depending on the ionic strength of the solution. At lower  
83 ionic strengths, the charged moieties along the polymer backbone are not sufficiently screened,  
84 and the polymer chains adopt an expanded conformation, resulting in larger persistence lengths.  
85 At higher ionic strengths, the charged moieties are now screened, and the polymer chains adopt a  
86 coil-like conformation, resulting in smaller persistence lengths.<sup>3,25,26</sup>

87 The mixing environment also influences the flocculation behavior. One method to test  
88 for flocculation performance is with jar tests, which replicate scaled-down industrial mixing  
89 tanks for flocculation. Jar tests are a relatively rapid, easy technique to obtain a lot of information  
90 about flocculation processes, but they lack homogeneous spatial and temporal flow features and  
91 possess un-controlled shear stresses, thus making it difficult to attribute certain floc properties to  
92 a specific flow features.<sup>27,28</sup> Instead, Taylor-Couette (TC) cells, which consists of two concentric  
93 cylinders with a specified gap width, can be used as they can generate a controlled variety of  
94 laminar and turbulent flow states as a function of cylinder speed.<sup>18,29-33</sup> Prior flocculation studies  
95 using a TC cell were limited in that the flocs had to be pre-formed outside of the cell.<sup>34-36</sup> A TC

96 cell with a glass outer cylinder for imaging and an inner cylinder modified for radial injection  
97 was recently constructed to directly inject the polymer flocculant into the annulus, so that the full  
98 flocculation process can be studied *in-situ*.<sup>37,38</sup> This unique TC cell was used previously by the  
99 authors in Metaxas et al.<sup>39</sup> to test the effects of initial mixing speed, which corresponds to a  
100 specific vortex type in the TC cell, on the flocculation of bentonite with a cationic  
101 polyacrylamide flocculant. It was found that an increase in the early mixing speed results in an  
102 increased floc growth rate, but the maximum floc sizes were similar in size.

103 While *in-situ* bentonite-polyelectrolyte flocculation work by Metaxas et al.<sup>39</sup> enabled a  
104 first study of flocculation in varying TC flows, the influence of changes in solution chemical  
105 composition was not examined as the ionic strength of the suspension, the polyelectrolyte  
106 molecular weight, and the concentration of polyelectrolyte were constant. However, the known  
107 ionic strength-dependence of size and morphology of the bentonite aggregate as well as the ionic  
108 strength-dependence of polyelectrolyte persistence length and conformation adds an important  
109 additional complexity to understanding flocculation dynamics. The ionic strength-induced  
110 changes in polyelectrolyte chain conformation will modify the extent that extensional forces  
111 present in the flow field around the polymer act to stretch the polyelectrolyte chains and enhance  
112 the bridging capability of the polyelectrolyte.<sup>40,41</sup> In this work, we vary ionic strength and  
113 molecular weight to understand the effects of these properties on the flocculation process,  
114 specifically the floc size, floc growth rate, and floc morphology, in well-controlled flow  
115 conditions.

116 1 Materials and Methods

117

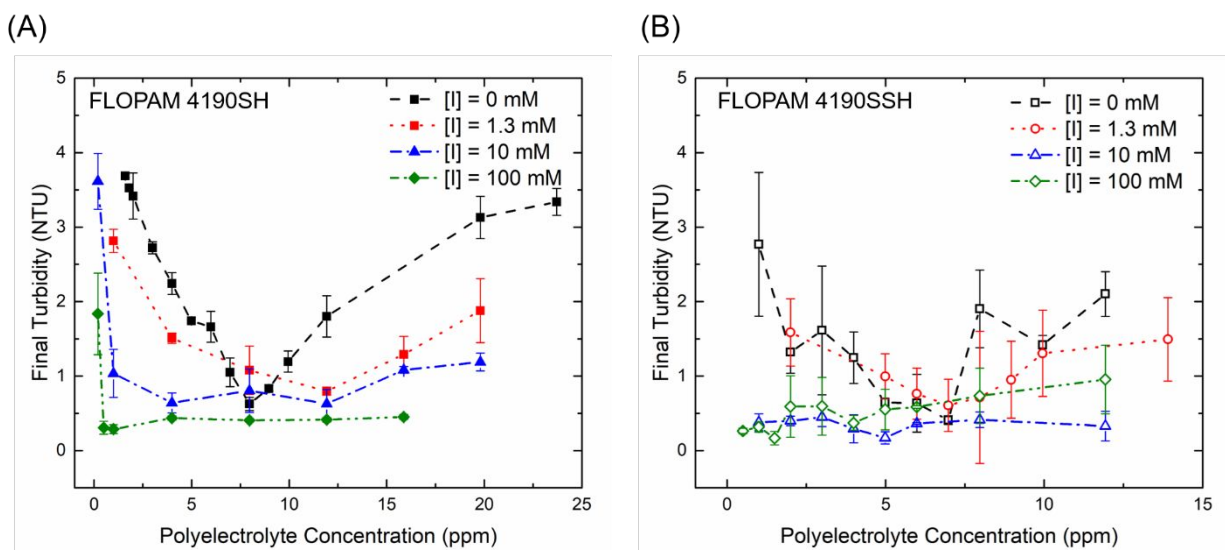
118 1.1 Materials

119 The polymer flocculants, or organic polyelectrolytes, used in this study are both  
120 commercially available cationic polyacrylamides (FLOPAM FO 4190SH and FLOPAM FO  
121 4190SSH, SNF Polydyne) with 10 mol% of the monomer groups containing a quaternary  
122 ammonium cation with a permanent positive charge in solution. The FLOPAM 4190SH has a  
123 molecular weight of  $4\text{-}6 \times 10^6 \text{ g}\cdot\text{mol}^{-1}$  and the FLOPAM 4190SSH has a molecular weight of  $8\text{-}$   
124  $11 \times 10^6 \text{ g}\cdot\text{mol}^{-1}$ . For both cationic polyacrylamides (CPAM), a 0.2 wt% solution was made by  
125 mixing the solid polymer pellets with a Jiffy mixer attachment in distilled water for 30 min. The  
126 solutions rested in a refrigerator overnight prior to use and were remade every 2 weeks as  
127 necessary as indicated by the supplier. Before any experiment was performed, the solution was  
128 removed from the refrigerator and allowed to warm to room temperature ( $\sim 23^\circ\text{C}$ ). The distilled  
129 water was purchased from Premium Waters, Inc. Powdered Na-Bentonite and NaCl are ACS  
130 grade from Fisher Scientific and were used as received.

131 1.2 Methods: Jar Tests

132 To perform a jar test, the appropriate amount of NaCl needed to obtain ionic strengths,  
133  $[I]$ , of 0 mM (no NaCl), 1.3 mM, 10 mM, and 100 mM was added to 1 L of distilled water in a 2  
134 L Pyrex beaker, or jar. A VELP Scientifica JTL4 flocculator was used to mix the solutions for 5  
135 min at 300 RPM to fully dissolve the NaCl. The bentonite was then added to the jar to mix for 30  
136 min at 300 RPM to evenly distribute it. For all jar tests, the concentration of bentonite was kept  
137 constant at  $30 \text{ mg}\cdot\text{L}^{-1}$ . The mixing speed was then lowered to 200 RPM, and a pre-specified  
138 volume of polyelectrolyte flocculant was injected into the suspension and mixed for 3 min to  
139 disperse the flocculant. To allow the flocs to grow, the mixing speed was lowered to 30 RPM  
140 and the suspension was mixed for an additional 30 min. Once the mixing stopped, the jars sat for  
141 5 min before the final turbidity in nephelometric turbidity units (NTU) was measured with a

142 LaMotte turbidity meter. This was performed for a range of polyelectrolyte flocculant  
 143 concentrations in triplicate at each concentration to obtain the optimal dose, which is the global  
 144 minimum in a turbidity curve as shown in Figure 1. The optimal dose for each ionic strength and  
 145 polyelectrolyte type is shown in Table 1. The steady shear viscosities of each suspension with the  
 146 optimal dose of polyelectrolyte were measured using the cup and bob geometry fixture of an AR-  
 147 G2 rotational rheometer from  $1 \text{ s}^{-1}$  to  $250 \text{ s}^{-1}$  at  $23^\circ\text{C}$  as shown in Figure S1 and were found to be  
 148 Newtonian for the range of shear rates experienced in the annulus of the TC cell.



149

150 Figure 1: Jar test results as a function of solution ionic strength using the (A) lower molecular  
 151 weight cationic polyacrylamide flocculant (4190SH) and the (B) higher molecular weight  
 152 cationic polyacrylamide flocculant (4190SSH). The final turbidity in terms of nephelometric  
 153 turbidity units (NTU) is expressed as a function of the polyelectrolyte dose, or concentration, in  
 154 parts per million (ppm). The global minimum in each curve denotes the optimal dose for a set of  
 155 solution conditions. Error bars represent one standard deviation from the mean turbidity.

156 1.3 Methods: Suspension Loading into TC Cell Annulus and Spatial Calibration

157 The TC cell used in this study injects flocculant through a total of 16 precisely spaced  
 158 axial and azimuthal injection ports along the inner cylinder to smooth any azimuthal  
 159 concentration gradients. These injection ports do not protrude into the annulus and the port  
 160 covers are contour-matched to the inner cylinder so that the flow profile of the resultant vortices



161 are not modified during operation.<sup>38</sup> Additional details on the TC cell design, with inner cylinder  
162 diameter ( $D_i = 2R_i$ ) of  $13.5407 \pm 0.0025$  cm, gap width ( $d$ ) of 0.84 cm, and the injection  
163 assembly can be found elsewhere.<sup>37</sup> To make the bentonite suspensions, the appropriate amount  
164 of NaCl was added to two separate 2 L jars each filled with 1 L distilled water to obtain solutions  
165 with ionic strengths of 0 mM (no NaCl), 1.3 mM, 10 mM, or 100 mM. The NaCl was mixed  
166 using a VELP Scientifica JTL4 Flocculator for 5 min at 300 RPM. Once the NaCl was dissolved,  
167 30 mg of bentonite was transferred to each jar to have a total of 2 L of  $30 \text{ mg}\cdot\text{L}^{-1}$  bentonite  
168 suspensions. The bentonite was dispersed using the flocculator for 30 min at 300 RPM. The pH  
169 of the suspensions in all cases was approximately 6.6 due to the interaction of dissolved carbon  
170 dioxide in water and bentonite.<sup>42</sup> Once finished, the bentonite suspensions were immediately  
171 transferred to the annulus of the TC cell by way of tubing attached to the base of the cylinder  
172 assembly. A figure detailing this process can be found in a previous study by Metaxas et al.<sup>39</sup>

#### 173 1.4 Methods: Flocculation Experiment Protocol

174 A stepper motor (Applied Motion Products HT34-497 2 phase stepper motor with a  
175 STAC5-S-E120 controller) rotates the inner cylinder and is equipped with a 7:1 gear reducer  
176 (Applied Motion Products 34VL007) for inertial balance between the motor and the cylinder. A  
177 laser diode (Thorlabs, 450 nm, 1600 mW max) in combination with a laser line generator was  
178 used to create a laser light sheet tangential to the inner cylinder. The Basler Ace camera ( $1280 \times$   
179  $1024$  pixels, 60 fps maximum frame rate) with a Tamron 25 mm c-mount lens was vertically  
180 adjusted such that the field of view was between the third and fourth injection port covers from  
181 the bottom of the TC cell. The frame rate on the camera was set to 30 fps with an exposure time  
182 of 8 ms for all experiments. A LabView code was used to simultaneously inject the  
183 polyelectrolyte flocculant from the inner cylinder ports into the annulus and record the entire

184 flocculation process. For all experiments, the drive pressure was set to 30 psi to inject the 0.2  
185 wt% polyelectrolyte solution at a calibrated injection rate of  $1.115 \pm 0.089 \text{ g}\cdot\text{s}^{-1}$  for the 4190SH  
186 flocculant and  $0.772 \pm 0.039 \text{ g}\cdot\text{s}^{-1}$  for the 4190SSH flocculant. The calibration data can be found  
187 in the Supplementary Information (Figure S2). The injection time was based on the required  
188 mass of flocculant needed to obtain the concentrations shown in Table 1.

189 Many flocculation applications preform the mixing with a two-stage protocol. First, there  
190 is an initial faster “Mix” speed (Stage 1), followed by a slower “Growth” speed (Stage 2),  
191 although growth can occur during both Stage 1 and Stage 2. In this study, the Mix and Growth  
192 speeds were set to constant rotation speeds of  $0.50 \text{ s}^{-1}$  and  $0.46 \text{ s}^{-1}$ , respectively. To begin an  
193 experiment, the inner cylinder drive shaft and injection ports were primed with flocculant. The  
194 initial Stage 1 speed was set, and the recording was started. After a delay of 30 s, the polymer  
195 was injected from the inner cylinder into the annulus and mixed at this Stage 1 speed for 3 min.  
196 After this, a step change in speed occurred to reach the Stage 2. This stage was maintained for  
197 30 min to allow the flocs to grow. The speed of  $0.46 \text{ s}^{-1}$  was chosen as it was the slowest speed  
198 tested that allowed flocs to be suspended throughout the 30 min duration of Stage 2 mixing. The  
199 times (3 min for Stage 1 and 30 for min Stage 2) used here mimic those used in the jar tests  
200 described in Section 2.2. After completion, the TC cell was disassembled and cleaned.

## 201 1.5 Methods: Image Analysis

202 Physicochemical and hydrodynamic effects on final floc microstructure have been  
203 examined using techniques such as small angle light scattering, which yields final floc size and  
204 fractal dimensions.<sup>43–45</sup> The longer characterization length scales accessible by static light  
205 scattering typically work well to determine mass fractal dimension determination. However,  
206 interpretation of the scattering patterns can be difficult, and static light scattering works best for

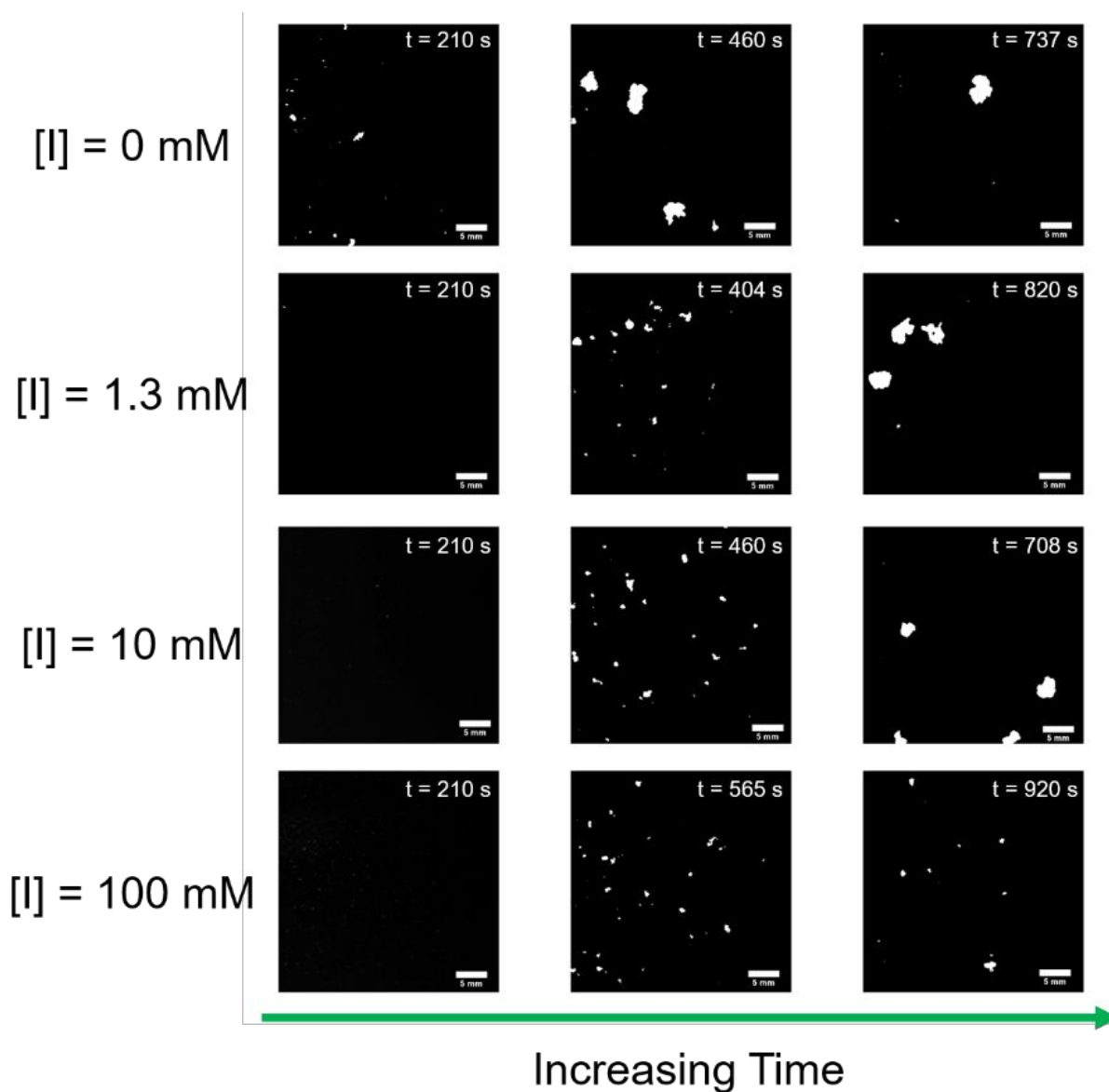
207 small aggregates with loosely packed structures, which is not always the case during  
 208 flocculation. In more recent years, advanced image analysis techniques have been used to study  
 209 the dynamic flocculation behavior using jar tests and impellers. Image analysis offers a non-  
 210 intrusive method of studying the flocs as compared to obtaining and preparing a sample for light  
 211 scattering experiments.<sup>46</sup>

212 To eliminate the curved glass surface of the outer cylinder during imaging, refractive  
 213 index-matching paraffin oil was poured into the Plexiglass tank surrounding the TC cell prior to  
 214 making the bentonite suspension. The cell was illuminated using a flicker-free LED light strip  
 215 (Metaphase 19 in Exo2 Light) to visualize the bottom-most port cover of the inner cylinder. An  
 216 image of the port cover was captured with the Basler camera. ImageJ was then used to determine  
 217 the pixel-to-mm ratio of the port cover for spatial calibration of the flocculation movies.

218 The movies were post-processed using MATLAB to obtain time-dependent floc size and  
 219 morphology based on an analysis by Vlieghe et al.<sup>47</sup> The raw movie frames were first binarized  
 220 to clearly show the floc (shown as white shapes in Figure 2 and Figure S3), and the centroid  
 221 position of each floc ( $x_c, y_c$ ) was determined. As a metric of floc size, the radius of gyration,  $R_g$ ,  
 222 of the non-spherical floc is calculated via

$$223 \quad R_g^2 = \frac{1}{N_p} \sum_{i=1}^{N_p} [(x_i - x_c)^2 + (y_i - y_c)^2] \quad \#(1)$$

224 where  $N_p$  is the number of pixels making up each floc with coordinate pair  $(x_i, y_i)$ . The resulting  
 225 radii of gyration were averaged for each 10 s interval (300 frames).



226

227 Figure 2: Time lapse of binarized images of bentonite-cationic polyacrylamide flocs (here, the  
 228 4190SH flocculant was used) as a function of ionic strength. The first image in each row is at  
 229 210 s, which is the onset of the inner cylinder speed change from Stage 1 to Stage 2 mixing. The  
 230 last image in each row occurs where the floc size plateaus. The middle image in each row occurs  
 231 at the midpoint time between the times associated with the first and last images. The white scale  
 232 bar in the lower right-hand corner of each image represents 5 mm. The movie frames have been  
 233 resized to comply with figure dimension limitations. The actual movie frames used in the  
 234 quantitative analysis are larger than what is shown here (actual dimensions of each frame are  
 235  $1280 \times 1024$  pixels).

236 A 2-D surface-based fractal dimension,  $D_{sf}$ , was used to quantify the morphology of the  
237 flocs. This quantity was calculated using the cross-sectional floc area,  $A$ , and the floc perimeter,  
238  $P$ , using the relationship from Vlieghe et al.<sup>47</sup>

$$239 \quad A \propto P^{2/D_{sf}} \quad \#(2)$$

240 The fractal dimension varies between the limits of 1, which indicates a circular floc cross-  
241 section, and 2, which indicates a rod-like floc cross-section. For each 10 s set of data, a linear  
242 regression was performed to determine  $D_{sf}$ . The number of flocs as a function of time were also  
243 calculated for each experiment. All experiments were conducted in triplicate for error analysis.  
244 All runs for both the 4190SH and 4190SSH flocculants are shown in Figures S4 and S5,  
245 respectively.

## 246 2 Results and Discussion

### 247 2.1 Optimal Dose Determination of Polyelectrolyte Flocculants

248 Jar tests were performed to determine the optimal dose of polyelectrolyte required as a  
249 function of both the solution ionic strength and the polyelectrolyte type. The optimal dose occurs  
250 where there is a global minimum in the turbidity curve. Determining the optimal dose is critical  
251 because under-dosing results in insufficient particulate removal and over-dosing results in  
252 particulate restabilization, both undesirable outcomes which can be cost-prohibitive in water  
253 treatment.<sup>48–50</sup> As discussed earlier, Figure 1 shows the results from these jar tests for both the  
254 lower molecular weight (4190SH) and higher molecular weight (4190SSH) cationic  
255 polyacrylamides. The optimal dose decreases as the ionic strength increases for both  
256 polyelectrolytes as reported in Table 1. The global minimum in the final turbidity indicates that  
257 more solid particulate (in this the case, bentonite) has settled out of solution because of the

258 presence of the flocculant and the increase in ionic strength of the solution. The shape of the  
259 turbidity curves also differs with ionic strength, where there is a distinct minimum in the curve  
260 below  $[I] = 10$  mM and a loss of the distinct minimum at  $[I] = 10$  mM and above. This suggests  
261 the restabilization of bentonite due to overdosing as previously mentioned.

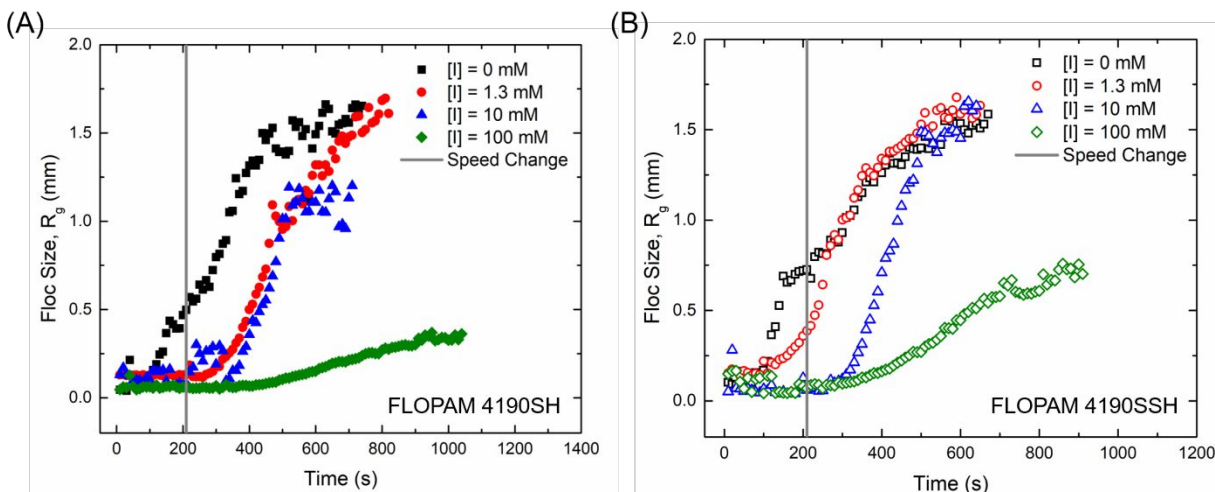
262 The previously mentioned study by Wilkinson et al.<sup>21</sup> showed that an increase in solution  
263 ionic strength resulted in an increase in the bentonite aggregate size from  $\sim 0.04$   $\mu\text{m}$  at  $[I] = 0$   
264 mM to  $\sim 9$   $\mu\text{m}$  at  $[I] = 100$  mM, which is attributed to the decrease in Debye length between  
265 bentonite sheets. In brief, the net negative charge of the bentonite platelets is screened by an  
266 increase in positive  $\text{Na}^+$  ions added as NaCl into solution, which decreases the repulsive,  
267 electrostatic force between the bentonite platelets, allowing them to aggregate to form larger  
268 bentonite aggregates.<sup>7,23</sup> Aggregation of the bentonite clay is aided just by the presence of  
269 additional NaCl in the solution, which means less of the polyelectrolyte is required to promote  
270 flocculation efficiency. The optimal doses of the higher molecular weight CPAM at each  
271 solution ionic strength were generally lower than those of the lower molecular weight CPAM.  
272 Because both polyelectrolytes in the study consist of the same monomer unit, the higher  
273 molecular weight polyelectrolyte is longer in length and therefore able to bridge more bentonite  
274 aggregates, requiring less of the polymer in solution to produce similar flocculation  
275 efficiencies.<sup>1,51</sup>

## 276 2.2 Ionic Strength and Molecular Weight Effects on Floc Size and Growth Rate

277 Once the optimal doses were determined for each polyelectrolyte at every solution ionic  
278 strength and the TC cell was calibrated to inject the correct mass of polyelectrolyte (see Figure  
279 S2), the flocculation experiments were conducted in the TC cell with radial injection capabilities.  
280 As described in the Methods section, during a routine flocculation processes, the flocculant is

281 first rapidly mixed (Stage 1) to disperse the polymer quickly, followed by a slower mix (Stage 2)  
282 to allow appreciable floc growth.<sup>52</sup> For this study, the inner cylinder rotational speed,  $\Omega_i$ , for  
283 Stage 1 and Stage 2 mixing were both kept constant at  $0.50 \text{ s}^{-1}$  and  $0.46 \text{ s}^{-1}$ , respectively.

284 While  $\Omega_i$  remained constant for both the Stage 1 and Stage 2 mixing, there is some  
285 variation in the non-dimensionalized velocity, given by the Reynolds number ( $Re_i = \Omega_i R_i d / \nu$ ),  
286 due to slight differences in the kinematic viscosity  $\nu$  of each suspension. The Stage 1  $Re_i$  range  
287 from 1517, 1518, 1956, and 1785 for the lower molecular weight CPAM and from 1593, 1822,  
288 1792, and 1709 for the higher molecular weight CPAM as ionic strength increases. The Stage 2  
289  $Re_i$  range from 1404, 1405, 1810, and 1654 for the lower molecular weight CPAM and from  
290 1474, 1687, 1659, and 1582 for the higher molecular weight CPAM as ionic strength increases.  
291 Even though the  $Re_i$  vary, they all fall within the range for the turbulent wavy vortex (TWV)  
292 flow type, which the  $Re_i$  range for TWV flow for this specific TC geometry falls between 1400  
293 and 2924. The prior TC flocculation study by Metaxas et al.<sup>39</sup> tested two different  $Re_i$  within a  
294 vortex flow type and found no statistical difference in the floc size, growth rate, and floc  
295 morphology, therefore it can be assumed that the same holds true in this study.



296

297 Figure 3: Floc size expressed as radius of gyration,  $R_g$ , as a function of ionic strength with time  
 298 for the (A) lower molecular weight cationic polyacrylamide flocculant (4190SH) and the (B)  
 299 higher molecular weight cationic polyacrylamide flocculant (4190SSH). The vertical gray line  
 300 depicts where the inner cylinder speed transitions from  $\Omega_i = 0.5 \text{ s}^{-1}$  to  $\Omega_i = 0.46 \text{ s}^{-1}$ .

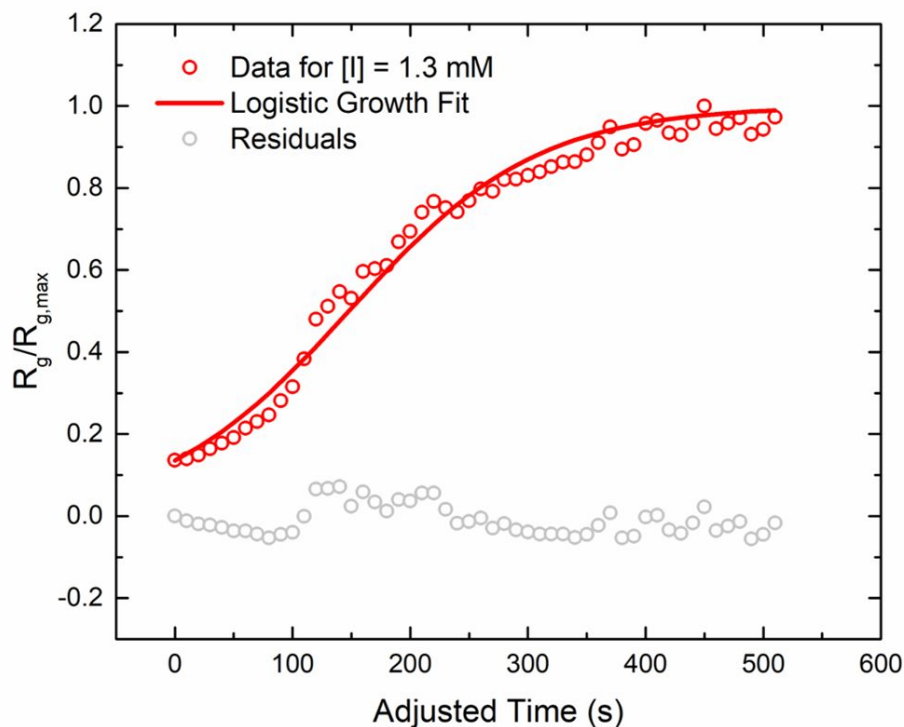
301 Figure 3 depicts a representative example of the transient floc size, expressed as the  
 302 radius of gyration  $R_g$ , as a function of solution ionic strength and polyelectrolyte molecular  
 303 weight. The radius of gyration of the flocs increases in all runs after the initial injection of  
 304 cationic polyacrylamide at 30 seconds until a plateau value of  $R_g$  is obtained. Shear gradients  
 305 present in the flow and a finite amount of bentonite and flocculant limit the maximum floc  
 306 size.<sup>8,34,46,53</sup> The maximum floc size generally decreases as ionic strength increases, from  $1.8 \pm$   
 307  $0.3 \text{ mm}$  at  $[I] = 0 \text{ mM}$  to  $0.4 \pm 0.1 \text{ mm}$  at  $[I] = 100 \text{ mM}$  for the lower molecular weight CPAM  
 308 (4190SH) and from  $1.9 \pm 0.2 \text{ mm}$  at  $[I] = 0 \text{ mM}$  to  $0.6 \pm 0.3 \text{ mm}$  at  $[I] = 100 \text{ mM}$  for the higher  
 309 molecular weight CPAM (4190SSH) as shown in Table 1. The floc sizes tend to be slightly  
 310 larger for the 4190SSH CPAM compared to the 4190SH CPAM as the 4190SSH variant is  
 311 higher in molecular weight and therefore is longer in length, allowing it to bridge more bentonite  
 312 aggregates.<sup>1,11,51</sup> All experimental runs can be found in the SI (Figures S4 and S5).



313 The floc growth rate can be calculated from the experimental data using a modified  
 314 version of the logistic growth equation

$$315 \quad \frac{R_g(t)}{R_{g,max}} = \frac{1}{1 + \left( \frac{1}{R_{g,0}/R_{g,max}} - 1 \right) e^{-rt}} \quad \#(3)$$

316 where  $R_g$  is the radius of gyration at a given time in mm,  $R_{g,max}$  is the maximum value of  $R_g$  in the  
 317 fitting range in mm,  $R_{g,0}$  is the initial value of  $R_g$  at the beginning of the fitting range in mm,  $r$  is  
 318 the growth rate in  $\text{mm s}^{-1}$ , and  $t$  is time in seconds. This model is typically used for quantifying  
 319 growth rates in microbial and ecological studies, but it can also be applied to quantify floc  
 320 growth rates as the flocs eventually plateau in growth due to finite concentrations of bentonite  
 321 and polyelectrolyte, which is akin to a “carrying capacity.”<sup>39,54–56</sup> The logistic growth equation  
 322 was fit to where there was a marked increase in the floc size with time. An example of the  
 323 logistic growth fit is shown in Figure 4, and all fits are shown in Figures S6-S7. In addition to the  
 324 fits, the residuals between the measured values and calculated values from the modified logistic  
 325 growth equation are presented to show how well the logistic growth equation fits the data points.



326

327 Figure 4: Representative example of the logistic growth fit to flocculation data over time using the  
 328 higher molecular weight polyelectrolyte (4190SSH) at a solution ionic strength of  $[I] = 1.3$  mM.  
 329 The open, red circles represent the  $R_g$  data points collected during the experiment normalized by  
 330 the maximum value of  $R_g$  in the fitting range, which is where the flocculation size plateaus. The solid,  
 331 red line indicates the logistic growth fit. The open, gray circles represent the residuals of the fit,  
 332 which is the data point calculated using the logistic growth model subtracted from the original  
 333 data at each corresponding time point. The time was adjusted such that the beginning of flocculation  
 334 growth occurs at time = 0 s. Logistic growth fits for all systems can be found in Figures S6-S7.

335 For both polyelectrolytes tested in this study, the flocculation growth rate initially increases from  
 336  $0.010 \pm 0.002$  mm s<sup>-1</sup> for 4190SH and  $0.008 \pm 0.004$  mm s<sup>-1</sup> for 4190SSH at  $[I] = 0$  mM to  $0.020$   
 337  $\pm 0.003$  mm s<sup>-1</sup> for 4190SH and  $0.020 \pm 0.002$  mm s<sup>-1</sup> for 4190SSH at  $[I] = 10$  mM as shown in  
 338 Table 1. Once the solution ionic strength is increased to  $[I] = 100$  mM, the growth rates decrease  
 339 to  $0.008 \pm 0.005$  mm s<sup>-1</sup> for 4190SH and  $0.009 \pm 0.005$  mm s<sup>-1</sup> for 4190SSH. This initial increase  
 340 in growth rate followed by a decrease as the solution ionic strength increases is due to the  
 341 interplay of two factors: (1) the bentonite aggregate size increases with ionic strength and (2) the  
 342 persistence length, and therefore how stretched out the polyelectrolyte conformation is in

343 solution, decreases.<sup>3,21</sup> In particular, the change in persistence length of the polyelectrolytes  
344 affects how effectively the polyelectrolyte bridges multiple bentonite aggregates. When there are  
345 no or very few additional ions in solution (i.e.  $[I] = 0$  mM and  $[I] = 1.3$  mM), the positive  
346 charges of the quaternary ammonium cation functional groups on the polyelectrolyte backbone  
347 repulse each other, forcing the polyelectrolyte to adopt a more rigid, expanded conformation  
348 with a larger persistence length compared to those at higher ionic strengths.<sup>3,25,57</sup>

349 Similarly to the bentonite sheets and aggregates, as the solution ionic strength increases  
350 ( $[I] = 10$  mM and  $[I] = 100$  mM), the positive charges of the quaternary ammonium functional  
351 groups on the polymer backbone are increasingly screened due to an increase in negative  $\text{Cl}^-$  ions  
352 present in solution. This then allows for the polyelectrolyte to adopt a more flexible, coiled  
353 conformation and the persistence length therefore decreases.<sup>3,25</sup> Walldal and Åkerman<sup>25</sup> found  
354 that for the same CPAM with a molecular weight in the same range as the ones used in this study  
355 ( $5 \times 10^6 \text{ g}\cdot\text{mol}^{-1}$ ), the persistence length decreased from  $\sim 8.5$  nm at  $[I] = 0$  mM to  $\sim 5.5$  nm at  $[I]$   
356  $= 10$  mM until it finally plateaued to  $\sim 2$  nm at  $[I] = 45$  mM. The  $[I] = 10$  mM appears to be an  
357 inflection point as at that point the bentonite aggregates prior to the addition of CPAM are two  
358 orders of magnitude larger than those at  $[I] = 0$  mM as shown by Wilkinson et al.,<sup>21</sup> but the  
359 persistence lengths of the polyelectrolytes are not so small that the bridging capability of the  
360 CPAM is significantly decreased, which could explain why the growth rate has increased and  
361 why there is a delay in the growth at  $[I] = 100$  mM compared to the other ionic strengths tested.  
362 At  $[I] = 100$  mM, the bentonite aggregate size prior to the addition of CPAM is another order of  
363 magnitude larger than that at  $[I] = 10$  mM, but the persistence lengths of the polyelectrolytes  
364 have continued to decrease, and the polymer chains cannot bridge the now much larger bentonite  
365 aggregates as effectively, leading to smaller floc sizes and growth rates. The images in Figure 2

366 and Figure S3 illustrate this point as the flocs are visibly larger at the lower ionic strengths and  
367 smaller at the higher ionic strengths.

368 As the flocs are formed and grow during the flocculation process, they can eventually  
369 break due to fluid shear forces.<sup>46,47</sup> After some time, the flocs will approach a steady state  
370 between floc growth and breakage.<sup>58-61</sup> Prior studies have shown that the maximum floc size is  
371 on the order of the Kolmogorov microscale, and floc size decreases with increasing global  
372 velocity gradient via the global dissipation rate of turbulent kinetic energy.<sup>34,39,46,62</sup> However, the  
373 global velocity gradient in this study does not significantly vary, if at all, because the kinematic  
374 viscosities of the suspensions are quite similar to each other ( $\sim 1$  cSt to  $\sim 1.2$  cSt) and the same  
375 inner cylinder speed and vortex flow type were used in all experiments. Here, the global velocity  
376 gradient,  $G \approx 2\pi R_i \Omega_i / d$ , is  $25.1 \text{ s}^{-1}$  for Stage 1 mixing for 3 min and  $23.3 \text{ s}^{-1}$  for Stage 2 mixing  
377 for 30 min. It is known that the maximum floc size,  $d_{max}$ , scales with inverse square root of the  
378 global velocity gradient ( $d_{max} \propto G^{-1/2}$ ), although to do this analysis would require subsequent  
379 studies run at different speeds, which was not the focus of this study.<sup>27,46,61</sup> For even more  
380 specific information on the local velocity gradients and stress distribution, a particle imaging  
381 velocimetry (PIV) setup would be needed. Because the global velocity gradient does not vary  
382 between experiments, the differences in floc size and floc growth rate are largely due to the  
383 interplay between increasing bentonite aggregate size and less expanded polyelectrolyte  
384 conformation from decreased persistence length as the solution ionic strength increases.

385 What is interesting to note is that there is no appreciable difference in the growth rates  
386 between the lower and higher molecular weight polyelectrolytes. This largely has to do with  
387 using TWV flow for all experiments, which implies that the intervortex mass transfer during

388 mixing does not significantly vary. Intervortex mass transfer can be quantified by an effective  
 389 dispersion coefficient determined for this particular TC cell by Wilkinson and Dutcher,<sup>38</sup> which  
 390 can be expressed as

$$391 \quad D_z^* = 2\lambda k_{cb} \#(4)$$

392 where  $D_z^*$  is the effective dispersion coefficient in  $\text{m}^2 \cdot \text{s}^{-1}$ ,  $\lambda$  is the axial wavelength of the vortex  
 393 ( $\sim 1$  cm for vortices present here), and  $k_{cb}$  is the intermixing coefficient in  $\text{m s}^{-1}$ .<sup>38,63</sup> The values of  
 394  $D_z^*$  vary from  $5.3 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 0$  mM and 1.3 mM,  $6.7 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 10$  mM, and  
 395  $6.2 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 100$  mM for 4190SH and from  $5.6 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 0$  mM,  $6.3 \times 10^{-5}$   
 396  $\text{m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 1.3$  mM,  $6.2 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 10$  mM, and  $5.9 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 100$  mM for  
 397 4190SSH for Stage 1 mixing. The trend is similar during Stage 2 mixing, where the values of  $D_z^*$   
 398 vary from  $5.0 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 0$  mM to  $5.8 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 100$  mM for 4190SH and  
 399 from  $5.2 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 0$  mM to  $5.5 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$  at  $[\text{I}] = 100$  mM for 4190SSH. The  
 400 effective dispersion coefficient is highest at  $[\text{I}] = 10$  mM and correlates with this case having the  
 401 highest growth rate well, which indicates that the solution properties do indeed affect the trends  
 402 described previously. There is a small delay in the floc growth curves for the 4190SH case at  $[\text{I}]$   
 403  $= 0$  mM and  $[\text{I}] = 1.3$  mM compared to the 4190SSH by approximately 30 s and 100 s,  
 404 respectively, which is due to the small increase in the effective dispersion coefficient for the  
 405 4190SSH case during Stage 1 mixing.

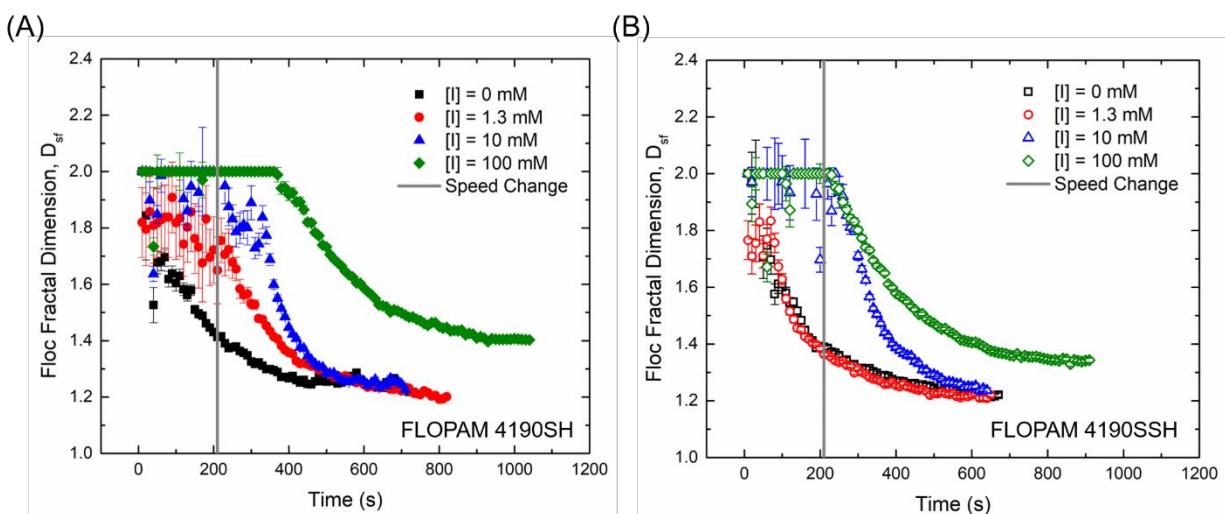
### 406 2.3 Ionic Strength and Molecular Weight Effects on Floc Morphology and Number

407 Another key parameter to examine in addition to floc size and floc growth rate is floc  
 408 morphology as a function of ionic strength and polyelectrolyte molecular weight. Sedimentation  
 409 and filtration of flocs for effective separation from water depend on the floc morphology and is  
 410 related to both floc size and density.<sup>27</sup> Shear gradients present during the mixing process can

411 alter the floc structure with time, which can also have consequences for removal efficiency. Floc  
412 morphology can be quantified using a non-dimensional parameter known as a fractal dimension.  
413 To obtain a three-dimensional mass fractal dimension, light scattering techniques are typically  
414 used, which requires the removal of sample flocs from their native environment.<sup>58,64,65</sup> One of the  
415 major advantages of the TC cell used in this study is that the combination of the optically clear,  
416 glass outer cylinder and the radial injection capabilities of the inner cylinder allows for  
417 determination of the fractal dimension throughout the duration of the flocculation process via  
418 image analysis without floc removal. The only difference between determining a fractal  
419 dimension with image analysis and light scattering is that image analysis yields a two-  
420 dimensional, rather than a three-dimensional, fractal dimension.<sup>27,47,66</sup>

421 The two-dimensional fractal dimension,  $D_{sf}$ , was obtained by linearly regressing the log  
422 of the cross-sectional floc area against the log of the floc perimeter for each ten second data set.  
423 The closer the  $D_{sf}$  value is to 1, the more circular in cross-section the floc is whereas the closer  
424  $D_{sf}$  is to 2, the less circular and more rod-like the cross-section of the floc is. Figure 5 shows the  
425 evolution of  $D_{sf}$  with time during Stage 1 and Stage 2 mixing as a function of ionic strength and  
426 polyelectrolyte molecular weight. The flocs are initially less circular (i.e.  $D_{sf}$  is closer to 2 than to  
427 1) due to increased aggregate-aggregate collisions from orthokinetic aggregation, which is the  
428 driving force behind flocculation.<sup>7,59,66</sup> The fractal dimension asymptotically decreases toward  
429 unity in all cases, indicating that the floc morphology is more circular. This suggests that shear-  
430 induced rounding dominates aggregate-aggregate collisions, particularly because a turbulent  
431 flow type was used throughout the duration of the experiment, which echoes what was observed  
432 in a prior study by Metaxas et al.<sup>39</sup> This shear rounding trend also correlates to results observed  
433 from Spicer et al.<sup>61</sup> for the temporal evolution in the floc structure with varying the shear rates in

434 a baffled stir tank. In their study, they also observed a decrease in the 2-D fractal dimension until  
 435 it asymptotes to a steady state value, indicating that there is preferential breakage of the flocs at  
 436 weaker points (i.e. their edges) from subjecting the flocs for extended periods of time to shear  
 437 forces present in the flow.



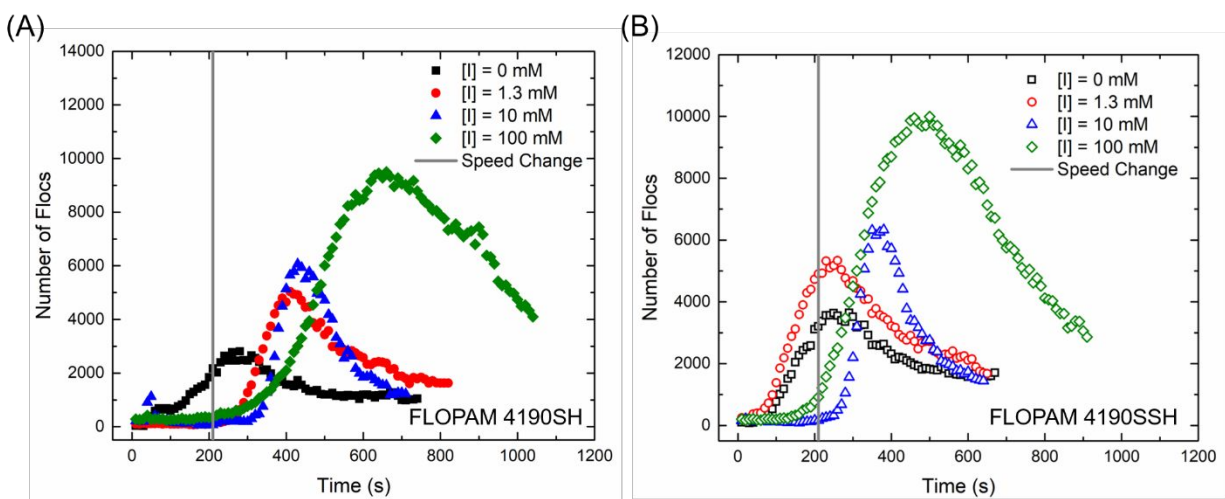
438

439 Figure 5: Floc morphology quantified as a 2-D perimeter-based fractal dimension,  $D_{sf}$ , as a  
 440 function of ionic strength with time for the (A) lower molecular weight cationic polyacrylamide  
 441 flocculant (4190SH) and the (B) higher molecular weight cationic polyacrylamide flocculant  
 442 (4190SSH). The vertical gray line depicts where the inner cylinder speed transitions from  $\Omega_i =$   
 443  $0.50 \text{ s}^{-1}$  to  $\Omega_i = 0.46 \text{ s}^{-1}$ .

444 Another factor to consider here is how the individual bentonite sheets interact with each  
 445 other prior to the addition of CPAM. It was previously mentioned that bentonite sheets adopt a  
 446 porous, edge-face structure at lower ionic strengths. As the ionic strength increases, the bentonite  
 447 sheets adopt a more edge-edge structure to ultimately, a denser, face-face packed structure.<sup>16,17</sup>  
 448 Figure 5 and

449 show that the  $D_{sf}$  values increase with increasing ionic strength, indicating that the flocs  
 450 are less circular in cross-section. At the end of the logistic growth fits, the  $D_{sf}$  values increased  
 451 from  $1.21 \pm 0.01$  at  $[I] = 0 \text{ mM}$  to  $1.4 \pm 0.1$  at  $[I] = 100 \text{ mM}$  for 4190SH, and increased from

452  $1.22 \pm 0.06$  at  $[I] = 0$  mM to  $1.4 \pm 0.1$  at  $[I] = 100$  mM for 4190SSH. This implies that flocs at  
 453 higher ionic strengths are more resistant to shear-induced rounding, which is most likely due to  
 454 the denser nature of the bentonite aggregates at higher ionic strengths. Interestingly, these results  
 455 contradict what Wilkinson et al.<sup>21</sup> found, where the flocs at  $[I] = 100$  mM had smaller fractal  
 456 dimensions than those at  $[I] = 10$  mM. However, it should be noted that the fractal dimension for  
 457 flocs at  $[I] = 0$  mM or  $[I] = 1.3$  mM were not measured in the Wilkinson study, and jar tests  
 458 were used, where the flow field is not nearly as homogeneous as the TWV flow used in the  
 459 present study.<sup>34</sup> Between the two polyelectrolytes used, there was a statistically insignificant  
 460 difference between the fractal dimension values at injection, at the speed change, and at the end  
 461 of the logistic growth fit. This result further suggests that the initial bentonite aggregate structure,  
 462 which differs because of changes in the ionic strength of the solution, determines the fractal  
 463 dimension trends.



464

465 Figure 6: Number of flocs as a function of solution ionic strength with time for the (A) lower  
 466 molecular weight cationic polyacrylamide flocculant (4190SH) and the (B) higher molecular  
 467 weight cationic polyacrylamide flocculant (4190SSH). The vertical gray line depicts where the  
 468 inner cylinder speed transitions from  $\Omega_i = 0.50$  s<sup>-1</sup> to  $\Omega_i = 0.46$  s<sup>-1</sup>.



469 In addition to differences in floc morphology as a function of ionic strength, the number  
 470 of flocs present in the suspension differs with ionic strength. Because the persistence lengths of  
 471 the polyelectrolytes are longer and therefore adopt a less expanded conformation in solution, and  
 472 the initial bentonite aggregate sizes are lower at lower ionic strengths as compared to higher  
 473 ionic strengths, more of the bentonite aggregates present in the suspension can be incorporated to  
 474 form a floc. This is reflected in the larger floc sizes observed at lower ionic strengths in Figure 2,  
 475 Figure 3, and Table 1. Larger floc sizes indicate less flocs in the suspension, which is what is  
 476 observed in Figure 6. The maximum number of flocs increases from  $\sim 3000$  flocs up to  $\sim 9000$   
 477 flocs for 4190SH and from  $\sim 3500$  flocs up to  $\sim 10,000$  flocs for 4190SSH as ionic strength  
 478 increases. The numbers are slightly higher for the 4190SSH as its longer length compared to  
 479 4190SH allows it to adsorb to more bentonite aggregates in the suspension.

480 Table 1: Summary of relevant parameters of the flocculation studies including the solution ionic  
 481 strength, the polyelectrolyte concentration used with optimal dose or overdose indicated in  
 482 parentheses, the maximum floc size, the floc growth rate, and the fractal dimension where the  
 483 polyelectrolyte is injected (30 s), at the speed change from Stage 1 to Stage 2 mixing (210 s), and  
 484 at the end of the region where growth plateaus (varies for each condition). The errors for the  
 485 mean values represent 95% confidence intervals.

	Ionic Strength (mM)	Polyelectrolyte Concentration (ppm)	Max. Floc Size, $R_g$ (mm)	Floc Growth Rate, $r$ ( $\text{mm}\cdot\text{s}^{-1}$ )	$D_{sf}$ at Injection	$D_{sf}$ at Speed Change	$D_{sf}$ at End of Fit
FLOPAM 4190SH (MW = 4-6 x $10^6$ g $\cdot$ mol $^{-1}$ )	0	8.0 (optimal dose)	$1.8 \pm 0.3$	$0.010 \pm 0.002$	$1.8 \pm 0.6$	$1.5 \pm 0.1$	$1.21 \pm 0.01$
	1.3	11.9 (optimal dose)	$1.5 \pm 0.5$	$0.011 \pm 0.001$	$1.8 \pm 0.4$	$1.7 \pm 0.2$	$1.24 \pm 0.06$
	10	4.0 (optimal dose)	$1.5 \pm 0.5$	$0.020 \pm 0.003$	$2.0 \pm 0.1$	$2.0 \pm 0.0$	$1.25 \pm 0.09$
	100	1.0 (optimal dose)	$0.4 \pm 0.1$	$0.008 \pm 0.005$	$1.9 \pm 0.1$	$1.8 \pm 0.2$	$1.4 \pm 0.1$
	100	8.0 (overdose)	$0.7 \pm 0.4$	$0.0101 \pm 0.0001$	$2.0 \pm 0.0$	$1.55 \pm 0.06$	$1.36 \pm 0.08$

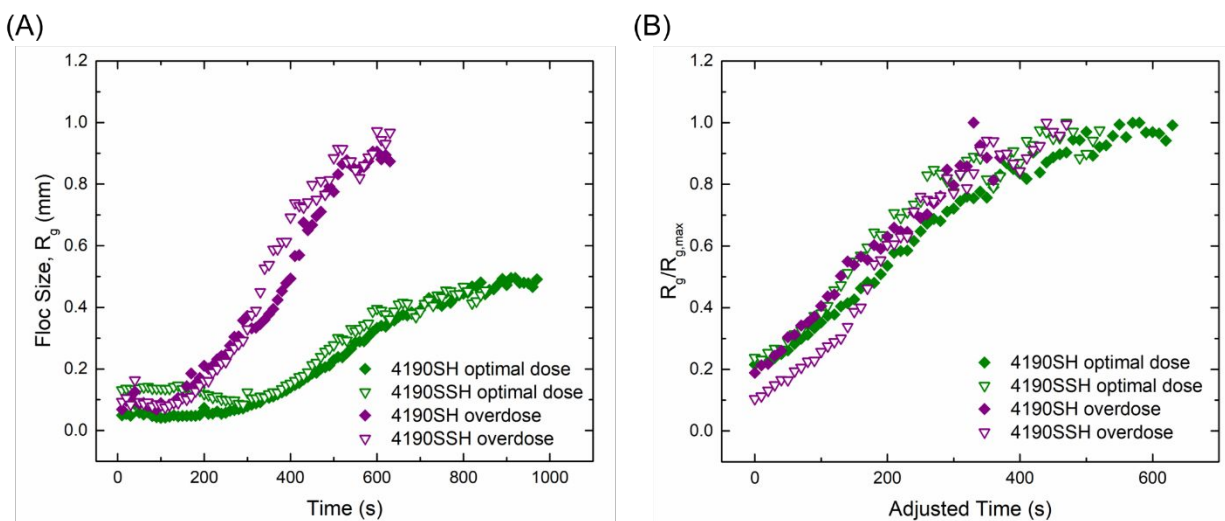
	Ionic Strength (mM)	Polyelectrolyte Concentration (ppm)	Max. Floc Size, $R_g$ (mm)	Floc Growth Rate, $r$ ( $\text{mm}\cdot\text{s}^{-1}$ )	$D_{sf}$ at Injection	$D_{sf}$ at Speed Change	$D_{sf}$ at End of Fit
FLOPAM 4190SSH	0	7.0 (optimal dose)	$1.9 \pm 0.2$	$0.008 \pm 0.004$	$2.0 \pm 0.2$	$1.41 \pm 0.04$	$1.22 \pm 0.06$
(MW = $8\text{-}11 \times 10^6 \text{ g}\cdot\text{mol}^{-1}$ )	1.3	7.0 (optimal dose)	$1.7 \pm 0.6$	$0.012 \pm 0.001$	$1.9 \pm 0.3$	$1.4 \pm 0.1$	$1.3 \pm 0.1$
	10	5.0 (optimal dose)	$1.6 \pm 0.1$	$0.020 \pm 0.002$	$2.0 \pm 0.0$	$2.0 \pm 0.0$	$1.22 \pm 0.03$
	100	1.5 (optimal dose)	$0.6 \pm 0.3$	$0.009 \pm 0.005$	$1.9 \pm 0.3$	$1.8 \pm 0.3$	$1.4 \pm 0.1$
	100	7.0 (overdose)	$0.9 \pm 0.8$	$0.010 \pm 0.005$	$2.0 \pm 0.0$	$1.7 \pm 0.3$	$1.33 \pm 0.07$

486

## 487 2.4 Effects of Optimal Dosing and Overdosing on Floc Growth

488 To further illustrate the effects of overdosing a suspension with polyelectrolyte  
489 flocculant, an experiment was conducted to compare the floc size and floc growth rates between  
490 the optimal dose required for  $[I] = 100 \text{ mM}$  as determined from Figure 1 for both  
491 polyelectrolytes used in this study. Figure 7(A) shows the floc size for the optimal dose cases  
492 (green symbols) with the corresponding overdose cases (purple symbols) for the lower molecular  
493 weight CPAM (closed diamonds) and the higher molecular weight CPAM (open triangles). The  
494 concentrations for the overdose case are  $8.0 \text{ ppm}$  for 4190SH and  $7.0 \text{ ppm}$  for 4190SSH, which  
495 are the concentrations used for the  $[I] = 0 \text{ mM}$  case as shown in Table 1. There is no statistical  
496 difference in the maximum floc size and the floc growth rate between the optimal and overdose  
497 cases for both polyelectrolytes according to Table 1. To make it more apparent that there is no  
498 appreciable difference between the optimal and overdose cases, the floc size normalized by the  
499 maximum floc size was plotted against the adjusted time (where all growth starts at 0 s) in Figure  
500 7(B). Using a higher concentration polyelectrolyte does not result in an increased flocculation  
501 performance compared to the smaller, optimal dose. Using more of the polyelectrolyte could  
502 potentially result in restabilization of the particulate as described earlier.<sup>1</sup> At an industrial scale,

503 using more flocculant than needed can be cost-prohibitive as more polyelectrolyte would be used  
 504 and any excess polyelectrolyte would have to be filtered downstream prior to discharging the  
 505 water.<sup>48</sup>



506

507 Figure 7: (A) Comparison of optimal dose (green symbols) and overdose (purple symbols) floc  
 508 growth with time using the lower (4190SH, solid diamonds) and higher (4190SSH, open  
 509 triangles) molecular weight polyelectrolyte flocculants at  $[I] = 100$  mM. To better compare the  
 510 floc growth of the optimal dose to overdose conditions, (B) shows the time adjusted such that all  
 511 growth curves start at 0 s and the floc sizes normalized by the maximum floc size ( $R_g/R_{g,max}$ ).  
 512 There is no statistical difference in floc size or growth rate between optimal dose and overdose  
 513 conditions for both flocculants studied.

### 514 3 Conclusion

515

516 The unique ability to non-intrusively inject one fluid into another fluid while harnessing  
 517 the precise mixing capabilities of a TC cell offers unprecedented access to the entire flocculation  
 518 process without having to remove flocs for further analysis. In this study, the ionic strength was  
 519 varied in a bentonite suspension and two different molecular weights of polyelectrolyte  
 520 flocculant were used at the same turbulent wavy vortex flow state generated by the TC cell to  
 521 obtain the floc size, floc growth rate, 2-D floc fractal dimension ( $D_{sf}$ ), and floc numbers with  
 522 time. As the ionic strength increased, the floc size generally decreased while the floc growth rate

523 initially increased then decreased. This was due to charge screening effects, where the initial  
524 bentonite aggregate size increases but the polyelectrolyte persistence length decreases and its  
525 conformation is less expanded, hindering its ability to adsorb to and bridge multiple bentonite  
526 aggregates. The  $D_{sf}$  values increased (became less circular in cross-section) with ionic strength  
527 due to densification of bentonite aggregates because of charge screening, rendering the flocs  
528 more resistant to shear-induced breakage. An increase in ionic strength resulted in an increased  
529 in the number of flocs due to the inability of the polyelectrolytes to effectively bridge multiple  
530 bentonite aggregates as their respective persistence lengths decrease with increasing ionic  
531 strength, resulting in a less expanded conformation in solution. There were no appreciable  
532 differences with respect to maximum floc size, growth rate, and floc structure between the two  
533 molecular weights of CPAM tested in this study, with the exceptions of smaller optimal doses  
534 and slightly higher effective dispersion coefficients for the larger molecular weight  
535 polyelectrolyte. In summary, the solution ionic strength is a critical process variable to consider  
536 in a flocculation process as it can have ramifications for the solution behavior of both the  
537 particulate system and the flocculant.

538 Flocculation is a highly dynamic process, with results that depend on both the  
539 physicochemical properties of the solution, as well as the hydrodynamic properties of the mixing  
540 environment. With respect to the myriad of factors affecting polyelectrolyte-mediated  
541 flocculation, this study only begins to scratch the surface. Here, only one turbulent vortex type  
542 (TWV) was used to study the flocculation of bentonite with cationic polyacrylamide as a  
543 function of ionic strength and polymer molecular weight. It would be of interest to study how the  
544 results presented here compare with a different turbulent flow state or with a laminar flow state,  
545 such as laminar wavy vortex flow. Fundamental understanding of the effect of solution

546 properties and flow parameters can potentially be used to optimize processes that utilized  
547 polymer-driven flocculation of a solid particulate, such as water treatment operations.

#### 548 4 Conflicts of Interest

549

550 There are no conflicts to declare.

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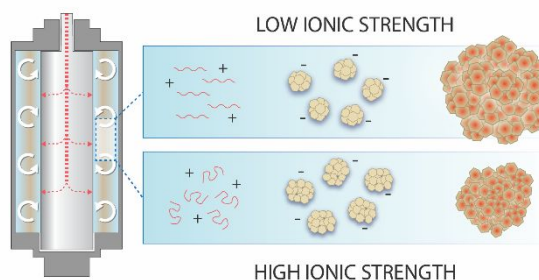
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728 Graphical Abstract



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731 Graphical abstract summary: Increased charge screening from increased ionic strength of a  
732 bentonite-laden suspension for flocculation in a Taylor-Couette cell capable of radial injection  
733 results in an interplay between increased bentonite aggregate size and decreased ability for the  
734 polyelectrolyte to bridge multiple aggregates due to decreasing persistence length, resulting in a  
735 less expanded polymer conformation in solution.

736