

**Layered Electrides as Fluoride Intercalation Anodes**

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# Layered Electrides as Fluoride Intercalation Anodes

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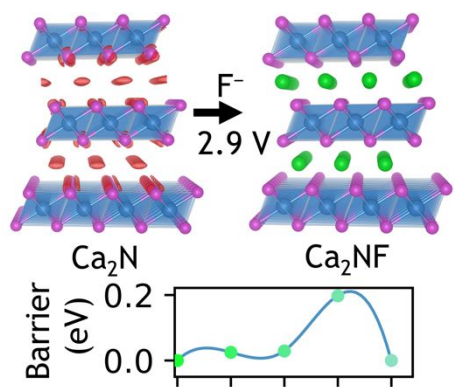
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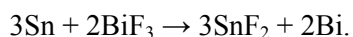
**ABSTRACT:** The fluoride ion is well suited to be the active species of rechargeable batteries, due to its small size, light weight, and high electronegativity. While existing F-ion batteries based on conversion chemistry suffer from rapid electrode degradation with cycling, those based on fluoride intercalation are currently less attractive than cation intercalation battery chemistries due to their low reversible energy densities. Here, using first-principles density-functional-theory calculations, we predict that layered electrides, such as  $\text{Ca}_2\text{N}$  and  $\text{Y}_2\text{C}$  — that have an electron occupying a lattice site — are promising hosts for fluoride intercalation, since their anionic electrons create large interstices. Our calculations indicate that anodes made from layered electrides can offer voltage up to  $-2.86$  V vs.  $\text{La}_2\text{CoO}_4$  cathode, capacity  $>250$  mAh/g, and fast diffusion kinetics with migration barriers as low as  $0.15$  eV. These metrics compare favorably to popular Li-ion intercalation cathodes such as  $\text{LiCoO}_2$ . Electrides open up a new space for designing fluorine intercalation batteries with good performance and cyclability.

#### TOC GRAPHIC



Rechargeable batteries enable crucial modern technologies, such as mobile phones, electric cars, and aerial drones, and will be required in even larger numbers for the rapidly growing automotive fleets and grid-scale storage of electricity generated by intermittent renewable sources. Currently, the market is dominated by Li-ion batteries, which shuttle lithium ions between two intercalation electrodes such as graphite and LiCoO<sub>2</sub>. In these electrodes, the Li ions move into empty spaces in a host material without significantly disrupting the host's structure. While this design has achieved high energy density and adequate cycling stability, the supply risk of lithium and cobalt<sup>1</sup> is predicted to create obstacles for the surge in battery usage. Current Li-ion batteries also pose safety concerns due to Li dendrite growth and thermal runaway.<sup>2</sup> Therefore, it is desirable to find other high-performance battery chemistries besides Li-ion.

The search for alternative chemistries has primarily been limited to light cations such as Na<sup>+</sup>,<sup>3</sup> K<sup>+</sup>,<sup>4</sup> Mg<sup>2+</sup>,<sup>5</sup> Zn<sup>2+</sup>,<sup>6</sup> and Al<sup>3+</sup>.<sup>7</sup> A handful of studies have instead focused on using anions as the active species.<sup>8, 9</sup> Amongst the various candidates for active anion batteries, fluoride (F<sup>-</sup>) is especially attractive due to its earth-abundance, light weight, high electronegativity, and reasonably fast diffusion in liquid or solid electrolytes.<sup>10-17</sup> In contrast to the success of Li batteries using two intercalation electrodes, most research on fluoride-ion batteries (FiBs) has followed a different path involving conversion reactions,<sup>18, 19</sup> pairing metals with metal fluorides, such as:<sup>11</sup>



The theoretical current capacity of conversion electrodes can be very high, such as 669 mAh/g for Ca/CaF<sub>2</sub>, compared to 294 mAh/g for LiCoO<sub>2</sub>. However, these high capacities are difficult to achieve in practice. The phase transformation of the metal to its fluoride during charge/discharge cycles is typically a slow reaction which requires a large overpotential; furthermore, if the resulting volume change is large, the electrode can crumble and degrade during repeated cycling.<sup>20</sup> In addition, the pure metal electrode sometimes dissolves into the electrolyte, further degrading it.<sup>19</sup> These effects are also seen in Li-ion conversion batteries, which have not found commercial success despite extensive research.<sup>21</sup> Therefore, prior experience suggests the value of intercalation FiBs, but high-capacity, fluoride intercalation electrodes

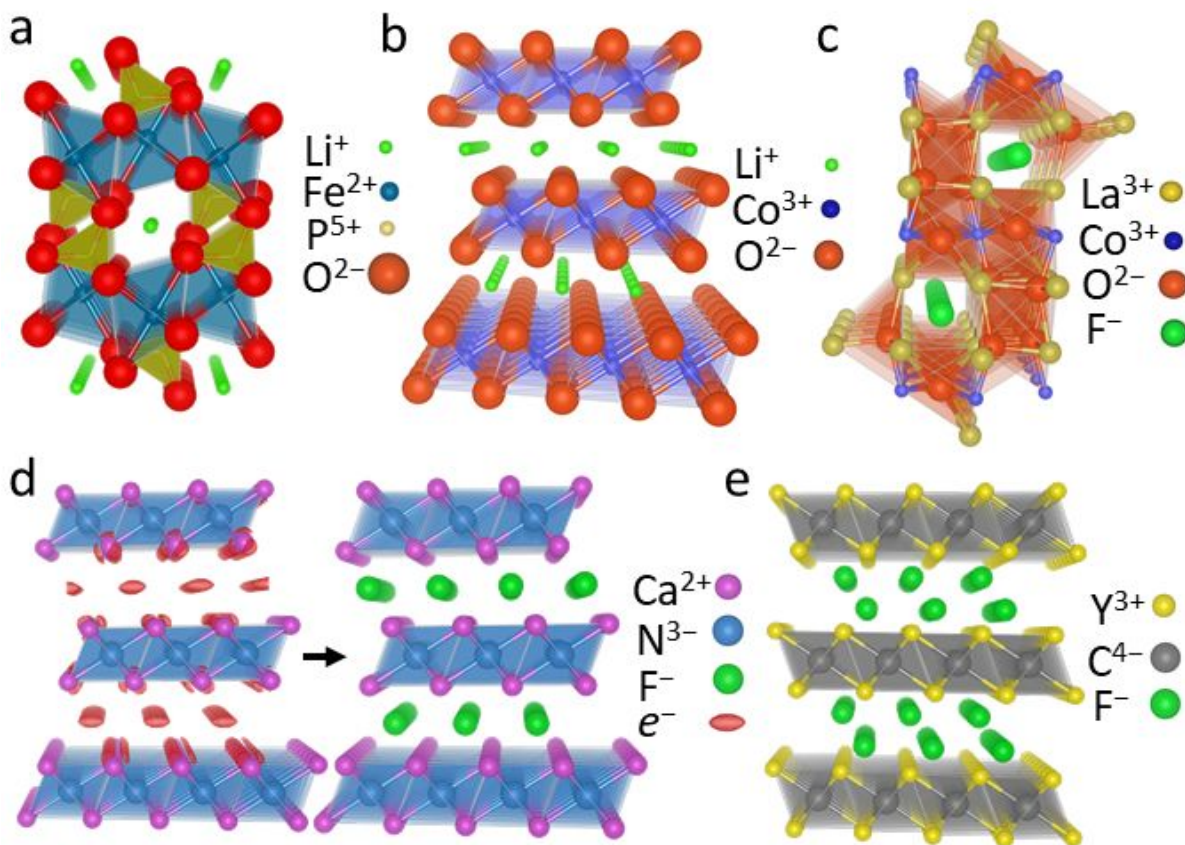
have been not been reported. The first  $F^-$  intercalation electrode to be tested was  $LaSrMnO_4/LaSrMnO_4F_2$ ,<sup>13</sup> which offered a moderate theoretical capacity of 172 mAh/g, but proved to have very limited reversibility due to destructive side reactions and overpotentials  $>1$  V.  $La_2CoO_4/La_2CoO_4F$  later provided improved cycling durability, but at the cost of low theoretical capacity (67 mAh/g).<sup>18, 22</sup> These electrodes have relatively little driving force for fluoride intercalation, making them suitable for cathodes, while  $FiB$  intercalation anodes have not yet been demonstrated.

In this Article, we take a new approach to design intercalation  $FiBs$ , which is to use the unconventional chemistry of electride crystals to our advantage. These inorganic electrides have interstices occupied by free electrons that act as anions, due to their unusual stoichiometries, which are not charge-balanced in common oxidation states.<sup>23</sup> We use first-principles density-functional-theory (DFT) calculations to show that electrides can intercalate fluoride stably by replacing the free electron with a  $F^-$ . Among the 12 known or predicted electrides which we have examined, we predict  $Ca_2N$  and  $Y_2C$  as promising candidates for intercalation anodes with theoretical gravimetric capacities  $\sim 280$  mAh/g, volume change during cycling  $<15\%$ , voltage  $<-2.5$  V vs.  $La_2CoO_4$  cathode, and low kinetic barriers  $<0.2$  eV for fluoride ion transport. These values approach the performance of popular Li-ion electrodes such as  $LiCoO_2$ , which has a theoretical capacity 295 mAh/g, calculated voltage 3.7 V vs. graphite, and migration barriers  $\sim 0.3$  eV,<sup>24</sup> and  $Ca_2N$  in particular is much more earth-abundant than  $LiCoO_2$ . The excellent performance metrics of  $Ca_2N$  and  $Y_2C$ , if realized experimentally, will be a major step toward the practical use of  $FiBs$ .

First, we consider the crystal structures of Li-intercalation electrodes, to see if the proven design principles can be transferred directly to  $FiBs$ . Two of the most successful  $Li^+$  intercalation cathodes,  $LiFePO_4$ <sup>25</sup> and  $LiCoO_2$ ,<sup>26</sup> are shown in Figures 1a and b, respectively. They are characterized by anionic polyhedra that are centered on small, highly charged cations (Shannon radius of 0.65 Å for  $Fe^{3+}$ , 0.17 Å for  $P^{5+}$ , and 0.53 Å for  $Co^{4+}$ ). The  $Li^+$  ions rest in the interstices between these polyhedra. The transition metal ions, besides providing the redox activity by changing their oxidation state, also serve to hold the crystal together when the  $Li^+$  is absent (in the charged state). Thanks to these framework-preserving cations,

$\text{LiCoO}_2$  and  $\text{LiFePO}_4$  have calculated volume changes of only 3% and 7 %, <sup>24</sup> respectively, as Li is removed, promoting durability over many cycles.

Based on these examples, to intercalate  $\text{F}^-$ , we ought to invert the paradigm and have cationic polyhedra centered on some other anion, to maintain the structural integrity in the absence of  $\text{F}^-$  ions. However, we immediately notice that anions are generally larger than cations, <sup>27</sup> with  $\text{F}^-$  having the smallest Shannon radius of 1.33 Å. In addition to making fluoride intercalation more challenging, the large size of anions also restricts the construction of anion-centered polyhedra. Therefore, the best candidates for anion-centered polyhedra are the first-row species  $\text{N}^{3-}$  (1.46 Å),  $\text{B}^{3-}$ ,  $\text{C}^{4-}$ , and possibly  $\text{O}^{2-}$  (1.4 Å). <sup>28, 29</sup> As for the surrounding cations, they should be large enough to create stable polyhedra with spacious interstices between them. They should also have a low charge to achieve charge balance, since they are more numerous than the central anion even if the polyhedra share many edges and faces. The cation also needs to be light for good gravimetric capacity, and inexpensive. Finally, it ought to be redox-active, with several stable oxidation states.



**Figure 1. Structural principles for fluorine intercalation electrode design.** **a.** The popular Li-ion intercalation electrode  $\text{LiFePO}_4$ , in which  $\text{Li}^+$  (green) occupies distorted octahedral sites between  $\text{PO}_4$  tetrahedra and  $\text{FeO}_6$  distorted octahedra. **b.**  $\text{LiCoO}_2$ , with  $\text{Li}^+$  sitting in octahedral interstices between layers of edge-sharing  $\text{CoO}_6$  octahedra. **c.** The previously known  $\text{F}^-$  intercalation electrode  $\text{La}_2\text{CoO}_4\text{F}$ , with  $\text{F}^-$  (green) in tetrahedral interstices between strongly distorted  $\text{La}_5\text{CoO}$  octahedra. **d.** The newly proposed  $\text{Ca}_2\text{NF}$  electrode, with  $\text{F}^-$  in octahedral interstices between layers of edge-sharing  $\text{Ca}_6\text{N}$  octahedra. The localized electrons between the  $\text{Ca}_2\text{N}$  layers are shown with isosurfaces of the electron localization function.  $\text{Ca}_2\text{NF}$ 's structure is the inverse of  $\text{LiCoO}_2$ 's structure in **b.** **e.**  $\text{Y}_2\text{CF}_2$ , with  $\text{F}^-$  in tetrahedral interstices between layers of edge-sharing  $\text{Y}_6\text{C}$  octahedra.

These constraints are not easily satisfied by a single cation, and indeed all existing fluoride intercalation electrodes combine two or more cation species. Figure 1c shows the most successful electrode to date,  $\text{La}_2\text{CoO}_4\text{F}$ ,<sup>18,22</sup> which uses the larger  $\text{La}^{3+}$  cations (1.16 Å) to create large tetrahedral sites for  $\text{F}^-$  in the rock-salt structured  $\text{LaO}$  layers. The smaller  $\text{Co}^{2+}$  (0.65 Å) occupies  $\text{CoO}_2$  layers which provide the redox activity, as  $\text{F}^-$  intercalation onto the  $\text{LaO}$  layers oxidizes  $\text{Co}$  to 3+. However, the gravimetric capacity is low (67 mAh/g theoretically) because the heavy  $\text{La}$  is “dead weight” from an electrochemical perspective. This is

generally true for similar electrodes such as  $\text{MgFeSb}_4\text{O}_8\text{F}$  (39 mAh/g)<sup>30</sup> or  $\text{FeSb}_2\text{O}_4\text{F}$  (74 mAh/g)<sup>31</sup> although it can be mitigated by using cations lighter than La or Sb, such as Sr (1.26 Å) in  $\text{Sr}_2\text{TiO}_3\text{F}_2$  (197 mAh/g), which has been proposed as a FiB anode but not yet tested.<sup>32</sup>

We conclude that to keep the electrode light, yet retain large interstitial sites, it should ideally have only one type of cation. Alkali and alkaline earth metals are light, large, inexpensive, and have low charge, satisfying all the constraints except redox activity, so we can expect good results if these metals can be stabilized in oxidation states besides +1 and +2, respectively. Such materials are rare, but a small group of suboxides, subnitrides, and hypocarbides are stable with fewer anions than would be expected by charge balance.<sup>33</sup> One well-studied example is the electride  $\text{Ca}_2\text{N}$ , which from a chemical perspective can be represented as  $\text{Ca}_2^{2+}\text{N}^{3-}e^-$ , where  $e^-$  is an electron localized at an empty anion site. We show the structure of  $\text{Ca}_2\text{N}$  in Figure 1d.  $\text{Ca}_2\text{N}$  has an inverse  $\text{LiCoO}_2$  structure, with  $\text{Ca}_6\text{N}$  octahedra instead of  $\text{CoO}_6$ , and Li replaced by anionic electrons. This suggests the following half-reaction can proceed topochemically, with little volume change:



While  $\text{Ca}_2\text{N}$  is referenced as a possible FiB electrode in a patent application,<sup>34</sup> any related studies remain unpublished beyond a single voltammogram, so a detailed theoretical study offers the first opportunity to understand the  $\text{F}^-$  intercalation properties of  $\text{Ca}_2\text{N}$ .

To assess the intercalation of  $\text{Ca}_2\text{N}$  with  $\text{F}^-$  ions, we have calculated the stability of the products and reactants for a variety of fluoride intercalation reactions along with the associated change in voltage and volume using DFT. For details of these calculations, see the section on Computational Methods. We find that both  $\text{Ca}_2\text{N}$  and  $\text{Ca}_2\text{NF}$ , with their structures shown in Figure 1d, are on the convex hull, and hence, stable against decomposition into known competing phases present in the Materials Project database.<sup>24</sup> The fluoride ion occupies the octahedral site between  $\text{Ca}_2\text{N}$  layers, while the tetrahedral sites, which are twice as many as the octahedral sites, are unoccupied. Placing fluoride into the tetrahedral site costs 0.34 eV more than the octahedral site. Upon geometry optimization, we find that  $\text{Ca}_2\text{NF}$  retains the same rhombohedral  $R$



$\bar{3}m$  phase as  $\text{Ca}_2\text{N}$ . For this structure, we can calculate its gravimetric capacity to be 285 mAh per gram of  $\text{Ca}_2\text{N}$  according to Eqn. 1:

$$\frac{1 \text{ mol Ca}_2\text{N}}{94 \text{ g Ca}_2\text{N}} \times \frac{1 \text{ mol e}^-}{1 \text{ mol Ca}_2\text{N}} \times \frac{96485 \text{ A} \times \text{s}}{1 \text{ mol e}^-} \times \frac{1000 \text{ mA}}{1 \text{ A}} \times \frac{1 \text{ h}}{3600 \text{ s}} = \frac{285 \text{ mAh}}{1 \text{ g}} \quad [2]$$

We note that while  $\text{Ca}_2\text{NCl}$  and  $\text{Ca}_2\text{NBr}$  are experimentally reported to exist in the  $R\bar{3}m$  phase,<sup>35,36</sup>  $\text{Ca}_2\text{NF}$  has only been made in the  $I4_1/amd$  phase,<sup>37</sup> which we find is 5 meV/atom higher in energy than the  $R\bar{3}m$  phase. Therefore, we expect that low-temperature fluoridation, which has emerged as a successful strategy to produce fluoride structures topochemically,<sup>38,39</sup> should yield  $R\bar{3}m$   $\text{Ca}_2\text{NF}$  from  $R\bar{3}m$   $\text{Ca}_2\text{N}$ . Space groups  $I4_1/amd$  and  $R\bar{3}m$  do not have a group-subgroup relationship, so any transformation from one to the other would be a reconstructive transition,<sup>40</sup> requiring many chemical bonds to break and re-form. Once  $\text{Ca}_2\text{NF}$  is kinetically trapped in the layered structure, the strength of the metal-nitride bonds will hinder the formation of other competing phases during cycling. We note that the isostructural  $\text{LiCoO}_2/\text{CoO}_2$  electrode is metastable with respect to non-layered phases at both ends of the phase diagram,<sup>24</sup> using the same computational methods we use here.  $\text{CoO}_2$ 's layered phase is metastable by 6 meV/atom relative to an  $I4/m$  phase, while  $\text{LiCoO}_2$  has an  $Fd\bar{3}m$  phase which is 193 meV/atom more stable, but careful management of the cycling can preserve the useful layered phase. The  $R\bar{3}m$  phase of  $\text{Ca}_2\text{NF}$  shrinks 13% by volume during fluoridation, and the electromotive force is  $-2.86$  V vs.  $\text{La}_2\text{CoO}_4/\text{La}_2\text{CoO}_4\text{F}$ , calculated with:

$$\frac{E_{\text{Ca}_2\text{NF}} + E_{\text{La}_2\text{CoO}_4} - E_{\text{Ca}_2\text{N}} - E_{\text{La}_2\text{CoO}_4\text{F}}}{1} = -2.86 \text{ V}, \quad [3]$$

where  $E_{\text{Ca}_2\text{NF}}$  and  $E_{\text{La}_2\text{CoO}_4}$  are the calculated energies of the products,  $E_{\text{Ca}_2\text{N}}$  and  $E_{\text{La}_2\text{CoO}_4\text{F}}$  are the energies of the reactants, and 1 is the number of electrons transferred in the reaction.  $-2.86$  V is the same calculated potential as the  $\text{Li}/\text{LiF}$  half-reaction, indicating that  $\text{Ca}_2\text{N}$  is highly electropositive, consistent with its experimentally known sensitivity to air and moisture.<sup>41</sup> Charge-balanced  $\text{Ca}_2\text{NF}$  can be further fluoridated to  $\text{Ca}_2\text{NF}_2$  at  $-0.78$  V vs.  $\text{La}_2\text{CoO}_4/\text{La}_2\text{CoO}_4\text{F}$ , which corresponds to an oxidation of nitride to the unstable  $\text{N}^{2-}$ . We do not include this in  $\text{Ca}_2\text{N}$ 's theoretical capacity, since it is not clear if the anion-redox capacity is accessible without degrading the electrode. The  $\text{Ca}_2\text{NF}_2$  phase is 237 meV/atom above the Materials

Project convex hull, excluding species such as  $\text{CaN}_6$  which are poorly described by DFT,<sup>42</sup> and it might decompose by nitrogen gas evolution to produce  $\text{Ca}_2\text{NF}$  and  $\text{CaF}_2$ . Therefore, it is likely necessary to cut off the reaction after the first fluoridation, such as by using a small excess of anode material.

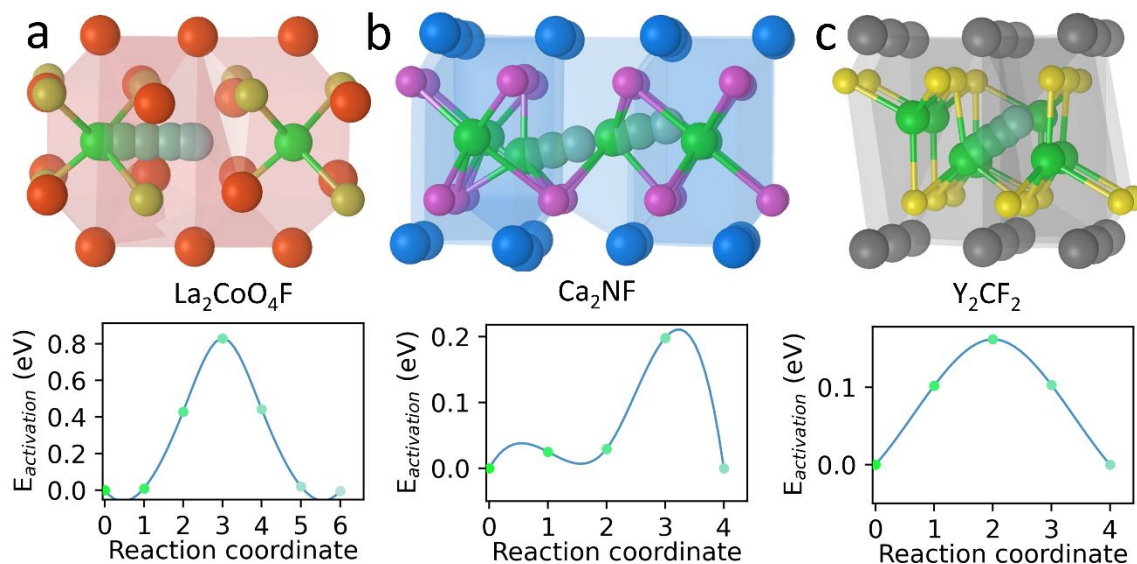
Another electride isostructural to  $\text{Ca}_2\text{N}$ ,  $\text{Y}_2\text{C}$ ,<sup>43</sup> is also a promising candidate for FiB anodes.  $\text{Y}_2\text{C}$ , as shown in Figure 1e, can be represented as  $\text{Y}_2^{3+}\text{N}^{3-}2e^-$  with  $2e^-$  nominally residing at the octahedral sites. Recently, Druffel et al. reported the formation of  $\text{Y}_2\text{CF}_2$  using a high-temperature solid-state reaction of  $\text{Y}$ ,  $\text{YF}_3$ , and graphite.<sup>44</sup>  $\text{F}^-$  ions are observed to occupy the tetrahedral sites between the  $\text{Y}_2\text{C}$  layers of  $\text{Y}_2\text{CF}_2$ , and the  $\text{Y}_2\text{C}$  layers re-stack from their original *ABC* stacking pattern to an *AAA* stacking in  $\text{Y}_2\text{CF}_2$  with space group  $P\bar{3}m1$ , as shown in Figure 1e. The *AAA* stacking of  $\text{Y}_2\text{C}$  is only 28 meV/atom less stable than *ABC*, so it may appear as a metastable phase during charge/discharge cycles. The structural restacking may also create a significant interfacial strain between the fluoridated and unfluoridated phases, which is an important matter for further investigation. We find that  $\text{Y}_2\text{CF}_2$  expands by 9% in volume relative to  $\text{Y}_2\text{C}$ , in good agreement with the 8% volume difference found experimentally. We also calculate the fluoridation voltage to be  $-2.56$  V vs.  $\text{La}_2\text{CoO}_4/\text{La}_2\text{CoO}_4\text{F}$ , and a gravimetric capacity of 282 mAh/g.

The intermediate  $\text{Y}_2\text{CF}$  phase, with  $\text{F}^-$  in octahedral sites, is unstable by 81 meV/atom with respect to  $\text{Y}_2\text{C}$  and  $\text{Y}_2\text{CF}_2$ , indicating that  $\text{Y}_2\text{C}$  is likely to fluoridate in a one-step process without staging. Further evidence for a one-step reaction is provided by the formation energy of the neutral  $\text{F}^-$  vacancy, which we calculate to be 0.14 eV at the chemical potential defined by the  $\text{Y}_2\text{C}/\text{Y}_2\text{CF}_2$  equilibrium. Creating two adjacent fluoride vacancies costs 0.46 eV. Neglecting entropy, it is easier to defluorinate  $\text{Y}_2\text{CF}_2$  all at once, than to remove one or two  $\text{F}^-$  at a time. Most Li-ion batteries discharge in stages because the electrostatic repulsion between  $\text{Li}^+$  gradually reduces the driving force to insert additional  $\text{Li}^+$ ,<sup>45</sup> but the empty octahedral  $\text{F}^-$  sites of the electrides can still be occupied by a negatively charged electron, so an electrostatic repulsion still occurs in the empty state. We have calculated the electrostatic interactions using VESTA,<sup>46</sup> assuming that all anionic free electrons are localized in the octahedral interstitial site.  $\text{Y}_2\text{CF}_2$  has a total Madelung energy of  $-174$  eV/f.u., compared to  $-185$  eV/f.u. for  $\text{Y}_2\text{C}$ . This includes the contribution of the re-stacking;

$\text{Ca}_2\text{NF}$  does not re-stack, and has a Madelung energy of  $-89.5$  eV/f.u., much closer to the  $-87.8$  eV/f.u. of  $\text{Ca}_2\text{N}$ . As a comparison, the Madelung energy of  $\text{LiCoO}_2$  is  $-110$  eV/f.u. and that of  $\text{CoO}_2$  is  $-140$  eV/f.u..

Based on these thermodynamic calculations, we expect the layered electrifieds to have good energy storage capacity, but the diffusion kinetics are also important. To achieve high power density, a battery electrode must conduct the active ion rapidly. Since the layered structures of  $\text{Ca}_2\text{NF}$  and  $\text{Y}_2\text{CF}_2$  match  $\text{LiCoO}_2$  so closely, it is reasonable to expect them to have fast two-dimensional ion transport kinetics, which we calculate using the climbing-image nudged elastic-band (NEB) technique.<sup>47</sup> To provide a benchmark, we first calculate the vacancy diffusion mechanism of the known cathode material  $\text{La}_2\text{CoO}_4\text{F}$ , which is shown in Figure 2a, with a barrier to fluoride migration of  $0.83$  eV. For the layered electrifieds, we consider three mechanisms: vacancy-assisted diffusion, direct interstitial diffusion, and interstitialcy (kick-out) diffusion. The lowest barrier for  $\text{Ca}_2\text{NF}$  is the interstitialcy diffusion mechanism, in which a tetrahedral interstitial  $\text{F}^-$  displaces an octahedrally coordinated  $\text{F}^-$ , forcing it into an adjacent tetrahedral interstitial site. The high-energy transition state, with a saddle point barrier height of only  $0.2$  eV, is associated with a configuration where the two diffusing  $\text{F}^-$  ions pass through triangular openings in the  $\text{Ca}^{2+}$  sublattice.  $\text{Y}_2\text{CF}_2$  is more likely to exhibit vacancy diffusion, with a barrier of  $0.16$  eV as the  $\text{F}^-$  passes directly between the two  $\text{Y}^{3+}$  that are shared between the starting and ending tetrahedral sites. Both of these barriers compare favorably to the calculated barrier of  $0.2$ - $0.3$  eV for  $\text{Li}^+$  diffusion in  $\text{LiCoO}_2$ .<sup>48</sup>

The NEB barriers assume the existence of an empty defect site (interstitial for  $\text{Ca}_2\text{NF}$  and F-vacancy for  $\text{Y}_2\text{CF}_2$ ), but the total activation energy  $E_A$  for diffusion is the formation energy of the relevant electrically neutral defect, plus the kinetic barrier height. When calculating the formation energy of the defects, we can assume either fluorine-rich and fluorine-poor conditions, which are the fluoride chemical potentials required to defluoridate or further fluoridate the electrified. In  $\text{Ca}_2\text{NF}$ , the dominant mechanism switches from interstitialcy to vacancy diffusion when the



**Figure 2: NEB study of  $\text{F}^-$  diffusion kinetics.** **a.** Vacancy diffusion in  $\text{La}_2\text{CoO}_4\text{F}$ . A tetrahedral  $\text{F}^-$  moves to an adjacent vacant tetrahedral site in the LaO layer. The plot shows the diffusion barrier for the motion of  $\text{F}^-$ . **b.** Interstitialcy mechanism in  $\text{Ca}_2\text{NF}$ . A tetrahedral  $\text{F}^-$  interstitial displaces an octahedral  $\text{F}^-$ , which moves to a tetrahedral interstitial site on the opposite side as the original. **c.** Vacancy diffusion mechanism in  $\text{Y}_2\text{CF}_2$ . A tetrahedral  $\text{F}^-$  moves to an adjacent tetrahedral site.

fluoride chemical potential is reduced, because the fluoride interstitial costs 2.3 eV to form under fluoride-poor conditions while the  $\text{F}^-$  vacancy only costs 0.3 eV. The vacancy diffusion has a barrier of 1.34 eV which occurs as the moving  $\text{F}^-$  passes through the tetrahedral site. In contrast, we predict that  $\text{Y}_2\text{CF}_2$  favors vacancy diffusion under any stable fluoride potential, since the  $\text{F}^-$  vacancy's formation energy never exceeds 0.6 eV. The total calculated activation energies are 1.61-1.64 eV for  $\text{Ca}_2\text{NF}$  and 0.30-0.71 eV for  $\text{Y}_2\text{CF}_2$ , indicating that  $\text{Y}_2\text{CF}_2$  is likely to have much faster kinetics. We estimate the diffusivity  $D$  using Eqn. 3:<sup>48</sup>

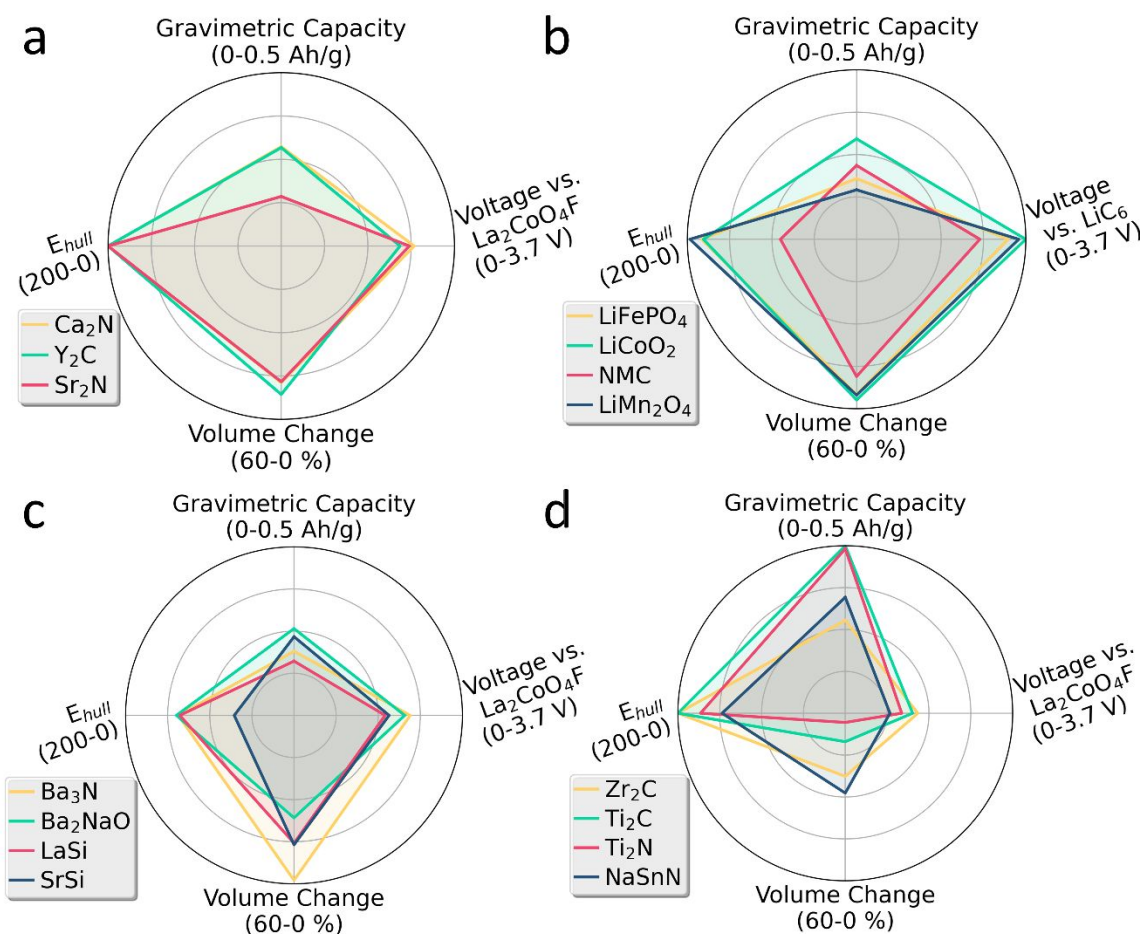
$$D = \frac{l^2 v_0}{2n} \exp\left(-\frac{E_A}{kT}\right) \quad [4]$$

Here the dimensionality  $n = 2$ ,  $l$  is the length of a single jump, and  $k$  is the Boltzmann constant. We approximate the attempt frequency,  $v_0 = 10^{13}/\text{s}$ , a fairly typical value for fluorides; for example, the attempt frequency of  $\text{BaF}_2$  was estimated to be  $0.6 \times 10^{13}/\text{s}$  from the frequency of the transverse optical phonon

mode.<sup>49, 50</sup> We obtain a negligible value of  $D = 2.4 \times 10^{-30} \text{ cm}^2/\text{s}$  for  $\text{Ca}_2\text{NF}$  at 298 K and F-poor conditions, while  $\text{Y}_2\text{CF}_2$  has  $D = 1.4 \times 10^{-8} \text{ cm}^2/\text{s}$ .

We have also used ab-initio molecular dynamics (AIMD) calculations as an alternate method to calculate the intrinsic activation energy and diffusivity of stoichiometric  $\text{Y}_2\text{CF}_2$  without artificially imposed defects. We run the calculations at elevated temperatures to obtain a meaningful number of diffusion events in a computationally affordable timescale. By running for 35 ps at 1700 K, 1800 K, 1900 K, 2000 K, and 2100 K, we obtain the mean-squared displacement (MSD) over time, and the diffusivity, at each temperature. Fitting the temperature-dependent diffusivities to an Arrhenius relationship provides the total activation energy.<sup>51, 52</sup> We find that the total activation energy of  $\text{F}^-$  diffusion in  $\text{Y}_2\text{CF}_2$  is  $0.75 \text{ eV} \pm 0.25$ , which yields a diffusivity at 300 K of  $6.9 \times 10^{-16} \text{ cm}^2/\text{s}$ . These values agree well with the NEB-calculated values for the fluoride-rich condition, where F vacancies have higher formation energy and are present only at lower concentrations. In the AIMD simulations, we observe both the vacancy and interstitialcy diffusion mechanisms. However, the AIMD supercells are stoichiometric, so the defects must be generated as interstitial/vacancy pairs. For this reason, many of the hopping events we observe either create or annihilate defects, as opposed to the defect-conserving mechanisms we calculate with NEB.

Experimentally, sample characteristics such as grain size will also influence the experimental diffusivity.<sup>53</sup> Since the majority of the total activation energy is the vacancy formation cost, doping  $\text{Y}_2\text{CF}_2$  with a small amount of  $\text{Ca}^{2+}$  ought to improve the diffusion kinetics by introducing additional  $\text{F}^-$  vacancies to compensate charge. Likewise,  $\text{Ca}_2\text{NF}$ 's interstitialcy diffusion has a low kinetic barrier height  $< 0.2 \text{ eV}$ , so we expect the diffusion can be enhanced by doping with  $\text{Y}^{3+}$  to increase  $\text{F}^-$  interstitial concentration.



**Figure 3: Comparison of structural families for intercalation electrodes.** Gravimetric capacity and voltage are normalized with respect to the highest score in each category. The voltage is the average voltage for the complete reaction with  $\text{La}_2\text{CoO}_4\text{F}$  or  $\text{LiC}_6$ , not accounting for any steps in the voltage profile. Thermodynamic stability is measured with the hull energy  $E_{\text{hull}}$ , in meV/atom, of whichever electrode state (charged or discharged) is less stable, and plotted from 200 meV above the hull to 0. Likewise, the magnitude of the volume change of the intercalated phase with respect to the de-intercalated phase is plotted from 60% to 0%. Calculated data for these and other electrodes are in Supporting Information. **a.** The layered electrides which are the focus of this work. **b.** Commercially successful Li-ion battery cathodes, for comparison. **c.** Other predicted electrides with different structures than  $\text{Ca}_2\text{N}$ . **d.** 2D mxenes, and the closely related material  $\text{NaSnN}$ .

While  $\text{Ca}_2\text{N}$  and  $\text{Y}_2\text{C}$  are the most promising electrides for use in FIBs identified in this study, we have also calculated the  $\text{F}^-$  intercalation properties of several other electrides, including  $\text{LaSi}$ ,  $\text{SrSi}$ ,  $\text{Ba}_3\text{N}$ , and  $\text{Ba}_2\text{NaO}$ ,<sup>54-56</sup> for comparison. In addition, we have calculated the stability and capacity of several known MXenes,<sup>29</sup> which are structurally related to the layered electrides, although their chemical properties are

different. We compare the theoretical performance of these different structural families in Figure 3, with popular Li-ion electrodes shown as a reference.  $\text{Ca}_2\text{N}$  and  $\text{Y}_2\text{C}$  have calculated performances closest to that of their structural analogue  $\text{LiCoO}_2$ , with excellent thermodynamic stability and current capacity. The other electrifieds are not as promising, since their structures do not allow fluoride intercalation with the same stability as the layered electrifieds. However, the structure alone is not enough without the electrified chemistry. The isostructural MXenes have high gravimetric capacity — up to 497 mAh/g for  $\text{Ti}_2\text{C}$  — due to their light weight, but also have low voltage and experience large volume changes. The electrified chemistry turns out to be essential because the free anionic electrons have a very low work function  $\sim 2.5$  eV,<sup>57</sup> the same as Li metal.<sup>58</sup> Because electrifieds give up electrons easily, they have a higher voltage vs. the cathode. The anionic electrons also improve the cycling stability by acting in combination with the large  $\text{Ca}^{2+}$  and  $\text{Y}^{3+}$  cations to maintain large interstices even in the unfluoridated state.

Our calculations suggest that  $\text{Ca}_2\text{N}$  and  $\text{Y}_2\text{C}$  can perform very well as FiB anodes. Going forward, there are several other FiB components which require improvement for these anodes to be used at their full capability. The most important target for further research is the voltage stability window of the electrolyte and the conductive additive.  $\text{Ca}_2\text{N}$  is likely to form a solid-electrolyte interphase (SEI) in contact with solid fluoride electrodes such as  $\text{La}_{1-x}\text{Ba}_x\text{F}_{3-x}$  (LBF), since Li/LiF has the same potential of  $-2.86$  V and is known to reduce LBF,<sup>59</sup> while  $\text{Y}_2\text{C}$  is right on the edge of the stability window. The effect of this SEI is not yet known, and it might be preferable to find an electrolyte which is stable against  $\text{Ca}_2\text{N}$ . At the other end of the voltage window,  $\text{La}_2\text{CoO}_4$  is the highest-voltage practical cathode, at 2.86 V vs.  $\text{Ca}_2\text{N}/\text{Ca}_2\text{NF}$ . Higher-voltage cathodes are known, such as  $\text{MgFeSb}_4\text{O}_4$  (3.37 V)<sup>30</sup> or  $\text{FeSb}_2\text{O}_4$  (3.49 V)<sup>31</sup> but at those voltages the commonly used conductive additive, carbon black, reacts irreversibly with  $\text{F}^-$ .<sup>13, 30, 59</sup> The carbon fluoridation may be avoided in the future through the introduction of improved conductors such as  $\text{SnO}_2$  or carbon nanotubes;<sup>20</sup> success in this endeavor would increase the operating voltage up to 20% if  $\text{FeSb}_2\text{O}_4$  can be used, and this material is also likely to have excellent kinetics even at low temperature. In order to compete with Li-ion batteries, the accessible voltage range must be expanded to  $>3$  V, and intercalation cathodes with higher capacities than  $\text{La}_2\text{CoO}_4$  or  $\text{LaSrMnO}_4$  are required.

In summary, we have calculated the properties of different FiB intercalation electrodes, and find that  $\text{Ca}_2\text{N}$  and  $\text{Y}_2\text{C}$  can offer an excellent combination of energy density, power density, and cycling stability. Their useful properties are due to the unique chemistry of layered electrides, which have free anionic electrons occupying vacant anion sites in the defluorinated state. Both materials intercalate  $\text{F}^-$  with very low kinetic barriers for  $\text{F}^-$  diffusion, and less volume change than most conversion electrodes, which is ideal for fast and reversible charge/discharge cycles. We expect that these new anodes will significantly advance FiBs' energy storage capability.

AUTHORS' NOTE: During final revision of this manuscript, a new theoretically calculated  $\text{Ca}_2\text{NF}$  phase was added to the Materials Project database. This phase has symmetry  $Cm$ ; while the cation sublattice is the same as the  $R\bar{3}m$  phase we identify in this work, the nitride and fluoride anions in the octahedral sites are ordered in a non-layered fashion. The  $Cm$  phase is calculated to be 26 meV/atom more stable than  $R\bar{3}m$ , so future work may need to consider if the nitride anions are mobile enough to re-order at battery operating temperatures.

## COMPUTATIONAL METHODS

We performed all DFT calculations using the VASP software,<sup>60,61</sup> and chose our calculation parameters to be compatible with the Materials Project database.<sup>24,62</sup> Certain calculations could not be converged using the tetrahedron method for electronic smearing, so these were completed using Gaussian smearing with a small SIGMA of 0.01, to minimize the discrepancy compared to the tetrahedron method. To maintain compatibility with the Materials Project, we did not include van der Waals corrections (see Supporting Information for tests of the effects of vdW corrections). All gravimetric capacities were calculated with respect to the mass of the defluorinated or delithiated state, and the reported voltage is the electromotive force driving the complete reaction, which does not include the "steps" seen in many experimental discharge curves due to intermediate phases. The initial locations of fluoride atoms were selected manually,



a procedure which is unambiguous for the layered electrides with their clearly defined octahedral and tetrahedral sites.

We used 3x3x1 supercells for the NEB calculations of Ca<sub>2</sub>NF and Y<sub>2</sub>CF<sub>2</sub>, which contained 81 atoms plus the added fluorine. Ionic positions were relaxed to a force convergence criterion of 0.02 eV/Å, with two exceptions. The Y<sub>2</sub>CF<sub>2</sub> interstitial diffusion was terminated after 200 steps because the F<sup>-</sup> could not fit through the saddle point, and was taking an alternate route with very high energy. The saddle-point image of Ca<sub>2</sub>NF's interstitialcy mechanism was well-converged, but the first image could not be converged even after several hundred ionic steps. The fluorine-poor limit is defined by the Ca<sub>2</sub>N/Ca<sub>2</sub>NF or Y<sub>2</sub>C/Y<sub>2</sub>CF<sub>2</sub> equilibrium, while the fluorine-rich limit is the Ca<sub>2</sub>NF/(2CaF<sub>2</sub> + 0.5N<sub>2</sub>) or Y<sub>2</sub>CF<sub>2</sub>/(2YF<sub>3</sub> + C) equilibrium.

For the AIMD calculations, we used a slightly larger 120-atom supercell of pristine Y<sub>2</sub>CF<sub>2</sub> with no defects, and used only the K-point at gamma to keep the calculations affordable. We used a plane-wave cutoff of 400 eV, a timestep of 2 fs, and kept the cell size and shape fixed. We first heated the cell from 100K to the desired temperature over 2 ps, then allowed 5 ps for the system to reach thermal equilibrium before we began collecting diffusion data. We then calculated the diffusivity as:

$$D = \lim_{t \rightarrow \infty} \left[ \frac{1}{2dt} \left\langle \left[ \vec{r}(t) \right]^2 \right\rangle \right] \quad [5]$$

Where  $d = 2$  is the dimension of the diffusion lattice,  $t$  is the simulation time, and  $\langle [r(t)]^2 \rangle$  is the time-averaged mean square displacement (MSD) of the F<sup>-</sup> ions.<sup>63</sup> We obtained the activation energy by fitting the temperature-dependent diffusivity data points to an Arrhenius model:

$$D = D_0 \exp\left(-\frac{E_a}{kT}\right) \quad [6]$$

where  $D_0$  is a constant pre-factor,  $E_a$  is the activation energy,  $k$  is Boltzmann's constant, and  $T$  is the temperature. All AIMD analysis was done using the Mo group aimd post-processing script.<sup>51</sup> Plots of the data are shown in Supporting Information S4.

ASSOCIATED CONTENT

**Supporting Information:** Performance metrics of other anode materials investigated in this study; effect of van der Waals corrections; decomposition pathways; AIMD data.

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