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Poroviscoelasto-plasticity of agarose-based hydrogels

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Keywords: Agarose gels, Multi-step stress relaxation, Creep, Poroviscoelasto-plasticity, Abaqus, Transient Network Theory

ABSTRACT

Agarose gels are excellent candidates for tissue engineering as they are tunable, viscoelastic, and show a pronounced strain-stiffening response. These characteristics make them ideal to create *in vitro* environments to grow cells and develop tissues. As many other biopolymers, viscoelasticity and poroelasticity coexist as time-dependent behaviors in agarose gels. While the viscoelastic behavior of these hydrogels has been considered using both phenomenological and continuum models, there remains a lack of connection between the underlying physics and the macroscopic material response. Through a finite element analysis and complimentary experiments, we evaluated the complex time-dependent mechanical response of agarose gels in various conditions. We then conceptualized these gels as a dynamic network where the global dissociation/association rate of intermolecular bonds is described as a combination of a fast rate native to double helices forming between aligned agarose molecules and a slow rate of the agarose molecules present in the clusters. Using the foundation of the transient network theory, we developed a physics-based constitutive model that accurately describes agarose behavior. Integrating experimental results and model prediction, we demonstrated that the fast dissociation/association rate follows a nonlinear force-dependent response, whose exponential evolution agrees with Eyring's model based on the transition state theory. Overall, our results establish a more accurate understanding of the time-dependent mechanics of agarose gels and provide a model that can inform design of a variety of biopolymers with a similar network topology.

1. INTRODUCTION

Biopolymers are used extensively as both commodity materials and for specialized applications[1–3]. For example, chitin is important for medical devices and wound-healing dressings[4], carrageenan films play an important role in extending the shelf life of foods[5], alginate is used to prevent dehydration of meats[6], and agar is common for culturing cells[7–9]. Biopolymers are selected for their ease of manufacture from natural precursor materials as well as for their ability to bear loads over long time scales. However, biopolymers also exhibit complex behaviors that may influence their durability and function. An accurate characterization of these materials is thus critical to guide material selection and design, yet many aspects of how biopolymers respond to loads applied over time remain poorly understood. Their physical behaviors are complex and vary across multiple length scales[10], where many behave as semiflexible networks. Typically, these polymeric systems have supramolecular assemblies which can vary between about one nanometer and tens of nanometers. Of particular interest are agarose-based hydrogels, which are commonly used as scaffolds in tissue engineering due to their low cost, biodegradability, and highly controllable elastic properties[11]. Agarose gels are viscoelastic semiflexible biopolymer hydrogels whose mechanical response depends on the polymer concentration[12] and has been demonstrated to exhibit a strain stiffening response that is likely to influence cellular responses[13,14]. While bulk properties are important to bear loads, cells respond directly to the small-length scale properties and behavior of their host scaffolds. Modulus, viscoelasticity, plasticity, and nonlinear elasticity of substrates and scaffolds influence cells and alter the fundamental processes of growth, proliferation, migration, and differentiation[15,16].

To better understand the characteristic mechanics and time-dependent response of agarose gels, let us first describe its network features. Below the gelation point, double helices are formed through the conglomeration of agarose molecules.

44 Each agarose molecule participates in more than one double helix. Supramolecular fibers form from the aggregation of
45 double helices through hydrogen bonding. These bonds govern the self-gelation of agarose gels (Figure 1.A) and enable the
46 network to be dynamic through bond formation and dissociation which dissipates elastic stored energy when exposed to
47 mechanical stimuli. The agarose molecules within the supramolecular fibers of the network structure thus possess a solid-
48 like behavior that has been proposed to be capable of fast energy dissipation. In contrast, agarose molecules present in the
49 clusters or junctions and that are not aligned can dissipate energy much more easily as they slide over adjacent molecules
50 thus generating a fluid-like behavior[17]. Hence, it has been proposed that bond exchange processes taking place in the
51 junctions will correspond to longer relaxation times or slower dissipation of the stored elastic energy. Clusters formed by
52 several suprafibers within agarose networks increase the number of connected bonds under deformation. The adjacent
53 agarose molecules that are not part of the cluster in a stress-free configuration are then able to form new crosslinks which
54 increases the size of the cluster and strengthens the network. This process enables agarose to dissipate stress when loaded
55 over long time periods. Elucidating the complex behavior of agarose gels is crucial to design more controllable materials,
56 but also to elucidate the factors leading to cell responses when subjected to externally applied loads. In addition, a deeper
57 understanding of agarose behavior will provide novel insight into many biological materials which present similar network
58 topology (i.e., actin filaments and collagen gels) (Figure 1.B).

59 The behavior of agarose gels, and many other biopolymers, is considered to be poroviscoelastic because of their high-water
60 content[18–20]. Fluid movement and mass transport through the solid network influence behavior. However, existing
61 poroviscoelastic models fail to connect the network topology with the mechanical response of the solid phase within
62 hydrogels. Such models lack accuracy as they do not account for the movement and rearrangement of molecules within the
63 polymer network. Generally, existing mathematical models used to characterize the macroscopic mechanical response of
64 agarose are empirical. Most either describe the mechanical response by approximating its structure as a combination of
65 simple linear elements (i.e., Maxwell or Kelvin-Voigt model) or describe the stress-strain relations from the stored elastic
66 energy expressions (i.e., Neo-Hookean or Holzapfel model). Studies using a linear combination of phenomenological
67 models, such as Prony series viscoelastic model[21], can broadly be found in literature to describe the time-dependent response
68 of agarose-based hydrogels. For example, Chen *et al.* (2011)[22] used this approach to study the deformation of chondrocytes
69 seeded in agarose gels while Pauly *et al*. (2017)[23] investigated the effects of additives on the mechanical properties of
70 agarose hydrogels. On the other hand, Caccavo and Lamberti (2017)[24] used fundamental balance laws to describe the
71 poroviscoelastic behavior of hydrogels under large deformation, and applied it to agarose-based hydrogels[25]. This latter
72 model provided an important step towards the development of refined models for biopolymers; however, this modeling
73 approach is empirical which limits its use for design purposes. High-precision atomistic simulations, such as molecular
74 dynamics, have been the subject of an increasing developments in the last two decades. The molecular modeling of
75 hydrogels incorporates into a model every single element that is part of the system (i.e., atomic positions, velocities, and
76 forces). In this context, Casalini (2013)[26] developed a molecular model of an agarose-carbomer hydrogel to explore the
77 effect of mesh size on solvent diffusion at low solute concentration. Although atomistic models remove all the assumptions
78 that limit the application of a specific model, they are still computationally expensive and difficult to apply to polymeric
79 networks models at large time scales. Thus, while viscoelasticity in agarose networks have been studied extensively, no
80 studies to date evaluate if the time-dependent response of hydrogels can be accurately described by dynamic bond evolution.
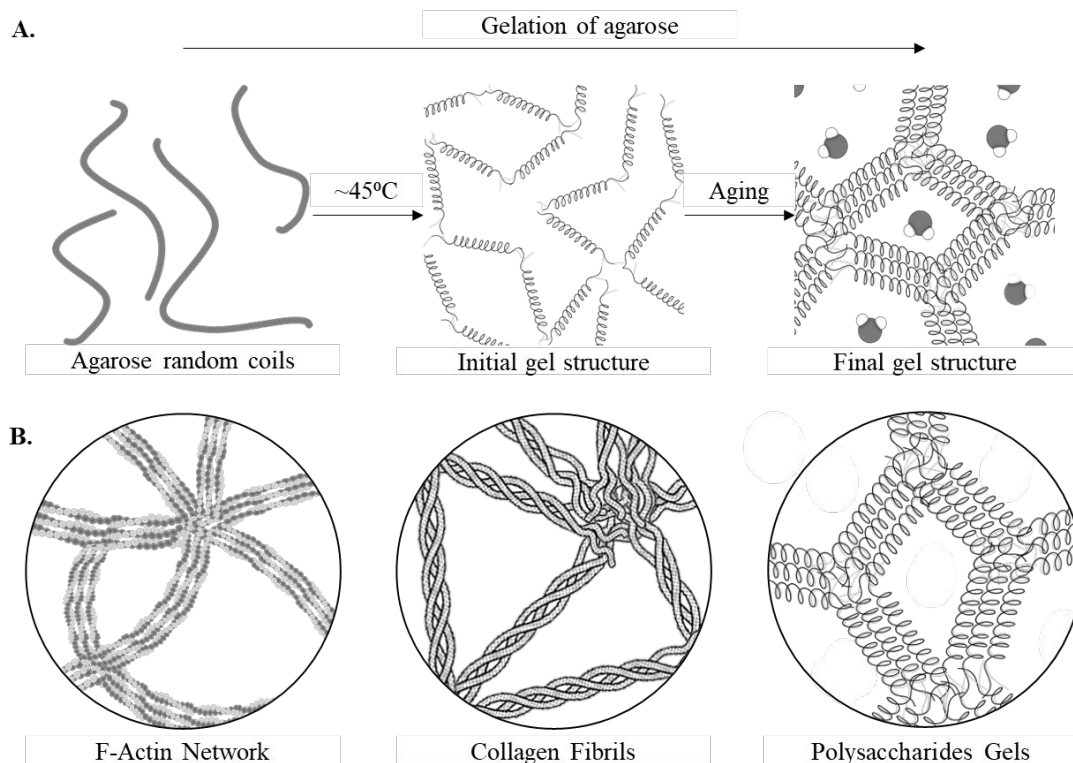
A.

B.

Figure 1. A. Gelation mechanism of agarose, from left to right: When water is added to agarose and it is heated up, agarose untangle and forms random coils. As the agarose cools (~45°C), coils pair to form helices. As the temperature continues to drop, the helices bundle and form higher-order assemblies (suprafibers) that are coincident with water inside the gel. **B**. Schematic representation of different biopolymer network showing cluster and thick fibers structure.

81   In this study, we connect the viscoelastic macroscopic response with the chain-level physics of agarose-based hydrogels.
82   This work seeks to establish a fundamental understanding of mechanisms responsible for nonlinear viscoelasticity of agarose
83   hydrogels by adapting the Transient Network Theory (TNT)[27] to the case of agarose networks. More specifically, the TNT
84   is modified to capture the force-dependent response of the fast bond dynamics observed during creep and to capture the
85   nonlinear plastic flow-like behavior observed during the multi-step stress-relaxation experiment. We propose bond
86   dynamics as a novel mechanism for describing strain-stiffening and force-dependent viscoelastic material behavior of
87   agarose. With new data we sought to better understand the time-dependent mechanics of agarose gels to inform their design
88   and to provide a model that may be extended to a range of biopolymers which share similar network topology. The
89   manuscript is organized as follows. In Section 2, we present and analyze experimental results on the behavior of agarose
90   subjected to unconfined compression and study the poroelastic contribution on the overall time-dependent response. In
91   Section 3 we review the main elements of the TNT to model the response of dynamic polymer networks and introduce the
92   nonlinear bond dynamics of agarose-based gels based on network topology. We then modify the TNT to capture the
93   experimental observations reported in Section 2. Finally, in Section 4, we provide a comprehensive overview of the model.

2. CHARACTERIZATION OF THE TIME-DEPENDENT RESPONSE OF AGAROSE UNDER UNCONFINED COMPRESSION

In this section, we present and analyze experimental results on the behavior of agarose subjected to unconfined compression. We described the time-dependent mechanical response of agarose gels for multi-step stress-relaxation and steady creep conditions with the objective of establishing a connection with chain-level physics. Because agarose is a biphasic material comprised of a solvent-filled biopolymer network, we first aimed to characterize the role of poroelastic effects, i.e., the time dependence of the response related to solvent transport, on the gel's overall response. Thus, finite element analysis (FEA) was used to model and reproduce fluid transport in experimental specimens during loading over time.

2.1 Experimental methodology

Agarose Gel Fabrication. Hydrogels were prepared by dissolving 5%, 7.5% and 10%, (w/w) agarose (Sigma A9539) into phosphate buffered saline (PBS, pH 7.4, Invitrogen), and while stirring the agarose powder was slowly added to prevent clumping. The solution was weighed, covered with aluminum foil to reduce evaporation, and boiled (~95°C) and magnetically stirred to maintain homogeneity for 5-10 minutes until agarose was dissolved. Agarose solutions were drawn into 3-, 5-, and 10-ml syringes cooled at room temperature. The hydrogels were removed from the syringes and cut into 8.66 mm, 12 mm and 16 mm lengths, respectively, to create 1:1 cylinders (height:diameter ratio).

Unconfined Compressive Multi-step Stress-Relaxation Test. A total of 15 samples were swelled to equilibrium in PBS for 48 h. Unconfined Compressive stress-relaxation testing (*n* = 3 samples/composition/dimension) was conducted on a Mechanical Testing System (MTS Insight II; Eden Prairie, MN; 250 N load cell; data recorded at 1 Hz) at room temperature; testing was performed with samples immersed in PBS. Aluminum compression platens were rigid, impermeable, and smooth. A minimum contact force of 30 mN ensured full contact between platen and sample (Figure 2.A). A USB-camera (Dino-Lite 1.3MP EdgePLUS AM4117MZT) was used to assess for full contact prior to testing as well as to evaluate uncompressed, fully compressed, and recovered (48 hours of swelling after testing) dimensions to calculate lateral expansion. The test profile included four incremental steps in strain ϵ = {5%, 10%, 15%, 20%}. Each of these stages was divided into a compression phase and a relaxation phase. Samples were deformed at a strain rate of $\dot{\epsilon}$ = 0.05/s over 1 s, and then each strain was held for 5 h to reach an equilibrium stress state (Figure 2.B).

Water absorption/release quantification. After swelling in PBS for 48 hours, 5% w/w samples (*n* = 3) were weighed for initial mass m_0 (before mechanical testing and final mass m_f (after stress-relaxation experiments). Samples were weighed quickly to avoid water reabsorption and minimize evaporation, and the amount Δm of solvent exchanged with the media Δm was calculated. This procedure was used for the lower agarose concentration gels since their higher porosity (Table 1) made them best candidates to have larger values for Δm. Samples were next re-submerged in PBS and weighed after 48 hours to assess for mass of fluid reabsorbed.

Unconfined Compressive Creep Test. Unconfined compressive creep tests were also conducted to evaluate short-term time-dependent responses. Creep testing was performed in PBS at room temperature on an MTS with closed-loop load control. A total of 9, cylindrical, 12x12 mm samples (*n* = 3/group) were subjected to constant compressive stress based on the overall strains achieved after a fast-loading stage ($\dot{\epsilon}_l$ = 0.05/s.). The overall strains achieved during the loading stage were ϵ_l = {1%, 2.5%, 5%, 7.5%, 10%, 15%}. The loading stage was followed by a 120 s creep hold at ϵ_l.

2.2 Experimental approach: multi-step stress-relaxation

The multi-step stress relaxation depicted in Figure 2. C-E shows the mean stress versus time response of the three different sample sizes for each of the three agarose gels compositions. At each level of applied strain, the stress increased immediately after the step-strain application, followed by a relaxation stage that reaches a quasi-steady value, referred to as the plateau stress σ_p in the remainder of the manuscript. We observed that this value increases with the applied strain while being independent of specimen size. Equilibrium values for the stress at the end of the stress-relaxation testing were determined

136   to be 0.028 ± 0.00082 MPa, 0.055 ± 0.0011 MPa and 0.083 ± 0.0005 MPa for 5% w/w, 7.5% w/w and 10% w/w respectively.
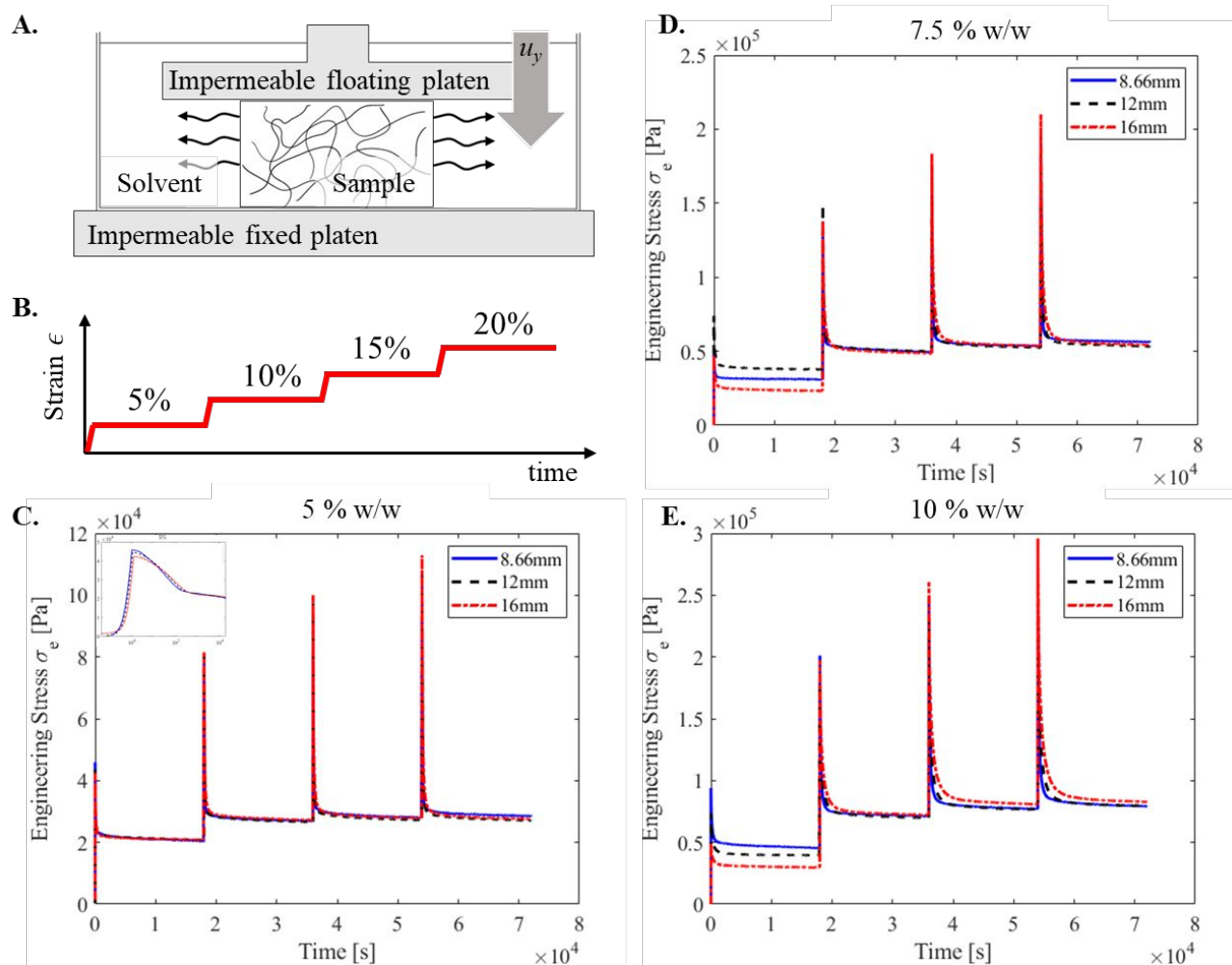137   The stress relaxation data were consistent between different samples showing a small variability.

Figure 2. **A**. Schematic of the unconfined compression test of a cylindrical disk of hydrated hydrogel. **B**. Strain vs. time function features multiple steps with holding times to observe relaxation. **C**, **D,** and **E.** Experimental results obtained from multi-step stress-relaxation (8.66 mm, 12 mm, and 16 mm) for 5%, 7.5%, and 10% w/w agarose compositions, respectively. For each dimension, the averaged data is represented. For each composition, agarose gels showed the same long-term stress-relaxation response independent of the sample size. The inset in **C**. shows the stress evolution for the first loading and relaxation step in a semilogarithmic scale along the x-axis.

138   A similar "stress-plateau effect" behavior was observed in multi-step stress relaxation testing (with a 30 minute relaxation
139   period) on the data reported by Roberts *et al.* (2011)[12] in their comparative study of the viscoelastic mechanical behavior of
140   agarose and poly(ethylene glycol) hydrogels. Because of the relatively short time used between step strains in this previous
141   study, the stress does not plateau as clearly as reported here although general trends are constant between the two studies.

142   *2.3. Experimental approach: steady-state creep.*

143   When subjected to a constant compressive load, the agarose sample displayed a combination of elastic deformation and
144   creep as described below and as shown in Fig. 3.A. First, following a period of fast elastic deformation, the specimen
145   displayed a transitory regime where creep rate first substantially decreased with respect the loading rate $\dot{\epsilon} = 0.05$/s and then
146   later increased before reaching a steady-state creep (Figure 3.C). We also observed a convergence of the strain rate to a
147   constant over time, which indicated steady-state creep and not consolidation effects from fluid transport out of the gel. We
148   further noted that the average creep rate increased with applied stress (Figure 3.B), suggesting that the creep response of

5

149   agarose is force dependent. At higher loads, however, creep could only be sustained for a while before the specimen ruptures.
150   We finally did not notice major differences between the creep response of agarose with different compositions.
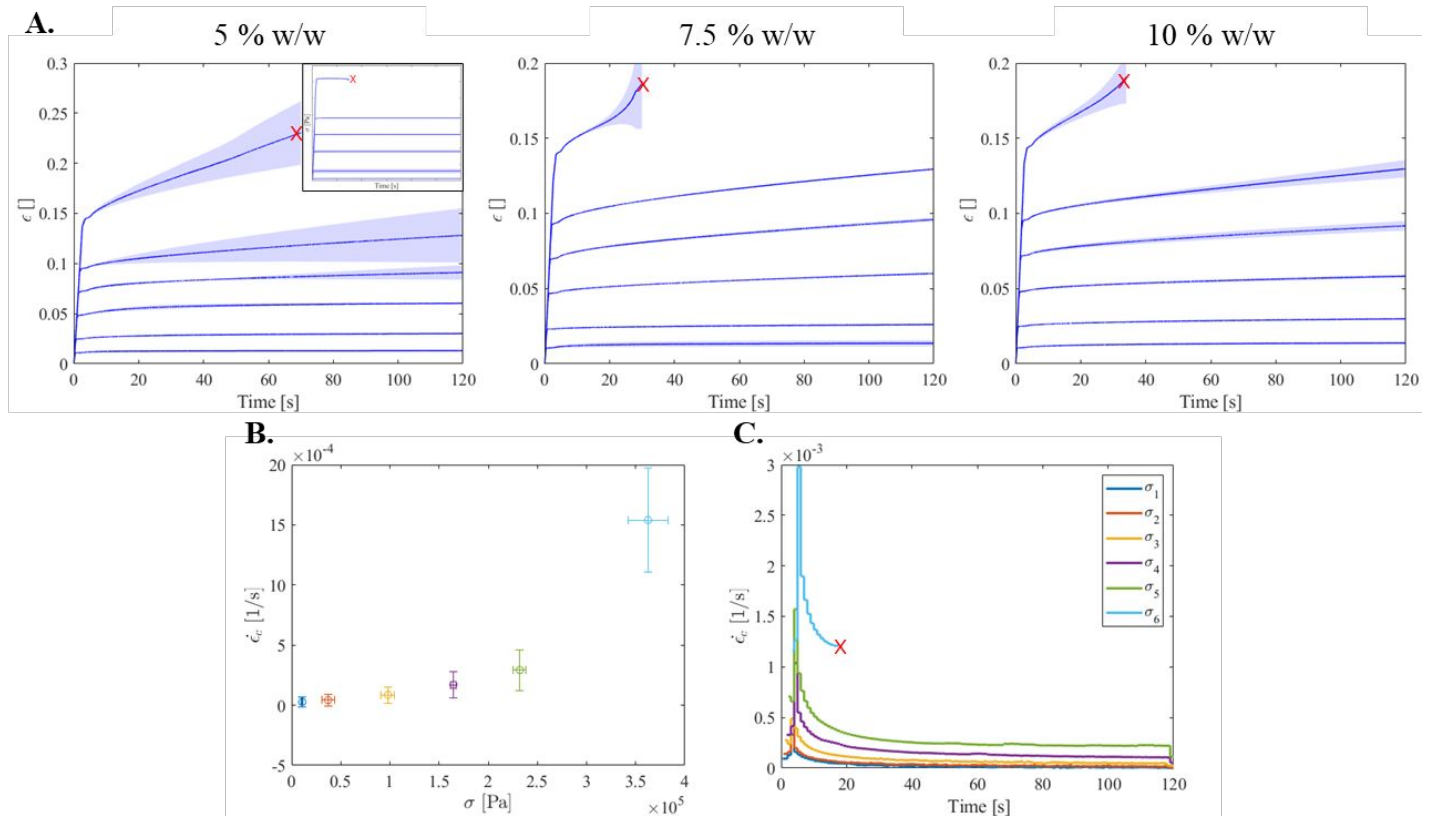
A.

Figure 3. A. Experimental results obtained from creep tests of 12 mm height (and diameter) samples for each of the agarose compositions (n = 3/composition). Data is reported using a solid blue line (average values from samples tested), and a blue region (± standard deviation). The red-cross indicates mechanical failure. Agarose gels showed same creep response independent of agarose composition. **B.** Evolution of the average data for the creep strain rate $\dot{\epsilon}_c$ respect the average data of the constant stress applied σ_i ($\sigma_1 < ... < \sigma_6$) during the creep test. **C.** Evolution of the average data for the creep strain rate $\dot{\epsilon}_c$ over time for the different constant stresses applied σ_i. Red-cross indicates the mechanical failure.

151   *2.4. Poromechanical effects*

152   As most biopolymers, agarose can be considered as a biphasic mixture consisting of two constituents: a solid skeleton phase
153   that is intermixed with a fluid phase. In the following, we therefore use superscripts s and f to denote the solid and fluid
154   phases, respectively[18,28,29]. For simplicity, the solid matrix is assumed to have an isotropic and uniform pore distribution on
155   the whole domain while the mixture is assumed to have reached its equilibrium swollen state so it can be considered fully
156   saturated. During deformation, however, the fluid can move relative to the solid skeleton, producing an effective time-
157   dependence of the mixture, independently of the material response of the polymer matrix. This poroelastic effect brings a
158   challenge to data interpretation as it is difficult to decouple the viscoelastic and poroelastic origins of the material's time
159   behavior[30–33]. The volume fraction $n^\alpha(\boldsymbol{X},t)$ of phase α ($\alpha = s$ or f) is defined as $n^\alpha(\boldsymbol{X},t) = \frac{dv_\alpha}{dv}$, where $\boldsymbol{X}$ is the material
160   coordinate, t is the time, and dv_α is the differential volume fraction of constituent α. The saturation condition implies that n^s
161    $+ n^f = 1$ and the total Cauchy stress can be decomposed into a solid and fluid component as[34]:

$$\boldsymbol{\sigma} = \boldsymbol{\sigma}^s + \boldsymbol{\sigma}^f = \boldsymbol{\sigma}^s - p^f \boldsymbol{I} \qquad\qquad 1$$

162 Here, p^f stands for the fluid pressure, $\boldsymbol{\sigma}^s$ is partial stress of solid skeleton[35] and $\boldsymbol{I}$ is the identity tensor. Interstitial fluid flow
163 is modeled based on isotropic Darcy's law as $\nabla p^f = -\frac{1}{K}\frac{e}{1+e}(v^f - v^s)$[36] where e is the void ratio, K is the hydraulic
164 conductance, v^s is the velocity of the solid phase and v^f is the velocity of the fluid phase, as before.

165 To explore the extent of these effects on material response, we implemented the above linear poromechanics model into a
166 general-purpose FEA software Abaqus 2019 (Dassault Systèmes Simulia Corp., USA). The specimen was modeled as an
167 axisymmetric cylinder around its axis of revolution ($r = 0$) (Figure 5.B). Solvent transport was assumed isotropic and
168 modeled by defining the hydraulic conductance of the fluid K, the void ratio e and the specific weight of the fluid γ_s. Gu *et*
169 *al.* (2003)[37] described the evolution of K and e as a function of the deformation applied to agarose gels (detailed description
170 on Appendix I). The compression step was run using the SOILS analysis in Abaqus, which accounts for the pore pressure
171 response and permeability. Because large deformation was used on our tests, the nonlinear geometric option (NLGEOM)
172 was applied. To avoid discontinuities on the step resolution, the maximum pore pressure change per increment was set to
173 10 Pa.

174 Regarding boundary conditions, the fluid pore pressure p^f was set to zero on the cylindrical periphery (right side) to allow
175 the fluid flow in the radial direction. Furthermore, to simulate the rigid and impermeable platen, all displacements and
176 rotations were constrained using an encastre boundary condition on the bottom platen. The contact with the platens
177 compressing the hydrogels was assumed to be perfectly lubricated and defined as a frictionless contact. Two different
178 predefined fields were created on the initial step. The first one was used to initialize the internal state variables, which were
179 set to zero. The second one defined the initial void ratio of the sample and was set to e_0 (see Appendix I).

180 Nonlinear analysis was performed using the Newton-Raphson algorithm. The hydrogel sample was modeled by the coupled
181 pore-fluid/stress CAX8P elements, 8-node quadrilateral axisymmetric elements that considers biquadratic displacement and
182 bilinear pore pressure. By subsequent mesh refinements, the results presented here were demonstrated to be mesh-size
183 independent.

184 This model was used to simulate the two different tests conducted for this study: multi-step stress-relaxation and creep. To
185 simulate stress-relaxation, a displacement u_y was prescribed on the top platen using a tabular amplitude to match the strain
186 previously described in Section 2.1. To simulate creep, a range of pressures P_y were prescribed to the top platen with its
187 respective tabular amplitude as well to simulate a constant strain ratio during the compression stage. To assess the role of
188 poromechanics alone, we first assumed that the solid skeleton behaves as a compressible Neo-Hookean hyperelastic solid.
189 In this context, the sample deformation is measured by the deformation gradient $\boldsymbol{F}(t) = d\boldsymbol{x}(t)/d\boldsymbol{X}$ which represents the
190 linear mapping between the position vector $\boldsymbol{X}$ of a material point in the reference configuration and its position $\boldsymbol{x}(t)$ in the
191 current configuration (Figure 4). In the case of unconfined compression, this tensor takes the simple form $\boldsymbol{F}(t) = diag[\lambda, \lambda_l,$
192 $\lambda_l]$, where $0 < \lambda \le 1$ is the length ratio along the vertical direction and $\lambda_l \ge 1$ represents the lateral length ratio.
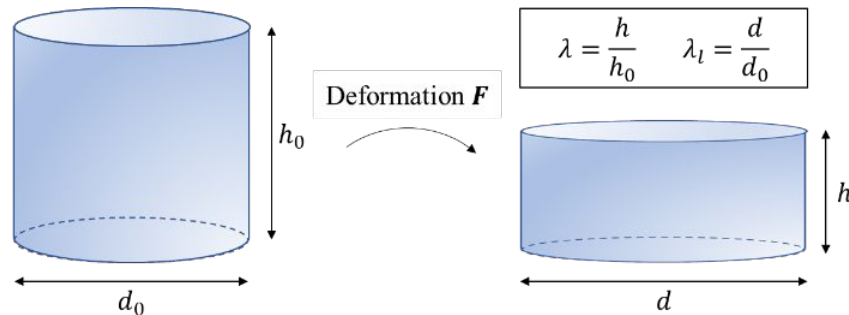

Figure 4. Conceptual diagram of deformation gradient tensor $\boldsymbol{F}$, the length ratio along the axial direction λ and the lateral
length ratio λ_l.

193   The material strain is defined by the Finger deformation tensor (or left Cauchy-Green deformation tensor) $\boldsymbol{b} = \boldsymbol{F}\boldsymbol{F}^T$, which

194   may further be decomposed into a volumetric component $J_e = \sqrt{\det \boldsymbol{b}}$ and an isochoric component $\overline{\boldsymbol{b}} = J_e^{-\frac{2}{3}}\boldsymbol{b}$. With these

195   definitions, the strain energy density (per reference volume) of our compressible Neo-Hookean model is provided by

$$\psi = c_{10}(\operatorname{tr}\overline{\boldsymbol{b}} - 3) + \frac{1}{D_1}(J_e - 1)^2 \qquad\qquad 2$$

196

197   The material constant c_{10} and D_1 can further be written in terms of the more familiar elastic modulus E_s and the Poisson's

198   ratio v_s of the solid network respectively:

$$c_{10} = \frac{E_s}{4(1 + v_s)} \ and \ D_1 = \frac{6(1 - 2v_s)}{E_s} \qquad\qquad 2.b$$

199   The true (Cauchy) stress tensor can then be derived as:

$$\boldsymbol{\sigma} = \frac{2}{J_e}\boldsymbol{b}\frac{\partial\psi}{\partial\boldsymbol{b}} = \frac{2}{J_e}c_{10}\operatorname{Dev}\overline{\boldsymbol{b}} + \frac{2}{D_1}(J_e - 1)\boldsymbol{I} \qquad\qquad 3$$

200   where the deviatoric part of $\overline{\boldsymbol{b}}$ is given by $\operatorname{Dev}(\overline{\boldsymbol{b}}) = \left(\overline{\boldsymbol{b}} - \frac{\operatorname{tr}\overline{\boldsymbol{b}}}{3}\boldsymbol{I}\right)$. The Poisson's ratio v_s for the solid network was

201   experimentally determined by imaging and measuring dimensions of each sample before compression and 50 minutes after

202   the load was applied. Poisson's ratio was found to be $v_s = 0.17$, which is in good agreement with previous studies[19,38]. The

203   Poisson's ratio in this study was assumed to remain constant during testing.

204   To obtain the elastic modulus E_s of the network, an optimization algorithm was developed to directly compare the contact

205   force from modeling results and the experimental data (see Appendix III). In this case, contact force obtained from first

206   compression stage ($\epsilon = 0.05$) on the multi-step stress-relaxation on 5% w/w agarose gels was used. E_s is set to be equal to

207   0.81 MPa.

208   Numerical simulations together with experimental findings indicate that poromechanics plays only a minor role stress

209   relaxation. From simulations, we can state fluid transport occurred within the first 2000 s ($\sim$ 35 min) (Figure 5.C and 5.D);

210   then stress remained constant until the end of the simulation.

211   *2.5. Experimental confirmation of poromechanical effects*

212   We next sought to experimentally confirm our finding that poroelasticity did not dominate the behavior of agarose under

213   the parameters applied in our computational analysis. Mass loss from samples was performed to experimentally confirm the

214   minor role of energy-dissipation from poromechanics (Table 1). The amount of water released increased with increasing

215   sample diameter due to the higher water content in the initial state. In relative terms, Table 1 shows that the amount of water

216   loss remained constant with respect the initial gel mass $\left(\|\Delta\overline{m}\| = \left\|\frac{\Delta m}{m_1}\right\| = 10.1\%\right)$, independently of sample size.

d [mm]	m_1 [g]	Δm [g]
8.66	0.57 ± 0.022	$- 0.05 \pm 0.028$ (-9.34%)
12	1.32 ± 0.084	$- 0.14 \pm 0.033$ (-10.7%)
16	3.43 ± 0.17	$- 0.35 \pm 0.069$ (-10.3%)

Table 1. The initial mass of the agarose gels is shown as m_1. Mass variation on gels due to the water mass loss, is reported as Δm and is calculated as $\Delta m = m_2 - m_1$, where m_1 initial mass of the sample and m_2 is the mass measured after the experimental test.

217   The effect of water loss was also assessed through the diametrical contraction of the sample during stress-relaxation testing
218   (Figure 5.E). When compression is held, pressurized pore fluid slowly leaves the system in the radial direction of the sample
219   while pores within it collapse reducing its volume. When diametrical contraction stops due to this phenomenon, it can be
220   understood as the end of the poromechanics contribution to the energy dissipation. The experimental data recorded
221   dissipated energy after the poroelastic model (Section 2.4) plateaued which increased the difference between the equilibrium
222   forces. Based on this observation, the purely poroelastic computational model was insufficient to explain the behavior of
223   agarose in response to unconfined compression observed during the relaxation stage. However, for lower agarose
224   concentrations, agarose network may become poorly crosslinked (i.e., near the percolation threshold). Arbabi and Sahimi
225   (1993) concluded that for networks with low connectivity, the capabilities of continuum models may be limited since the
226   affine deformation assumption can no longer be applied[39]. Due to the network's decreased cross-link density, viscoelasticity
227   might not be as dominant in that situation as for higher agarose concentration.
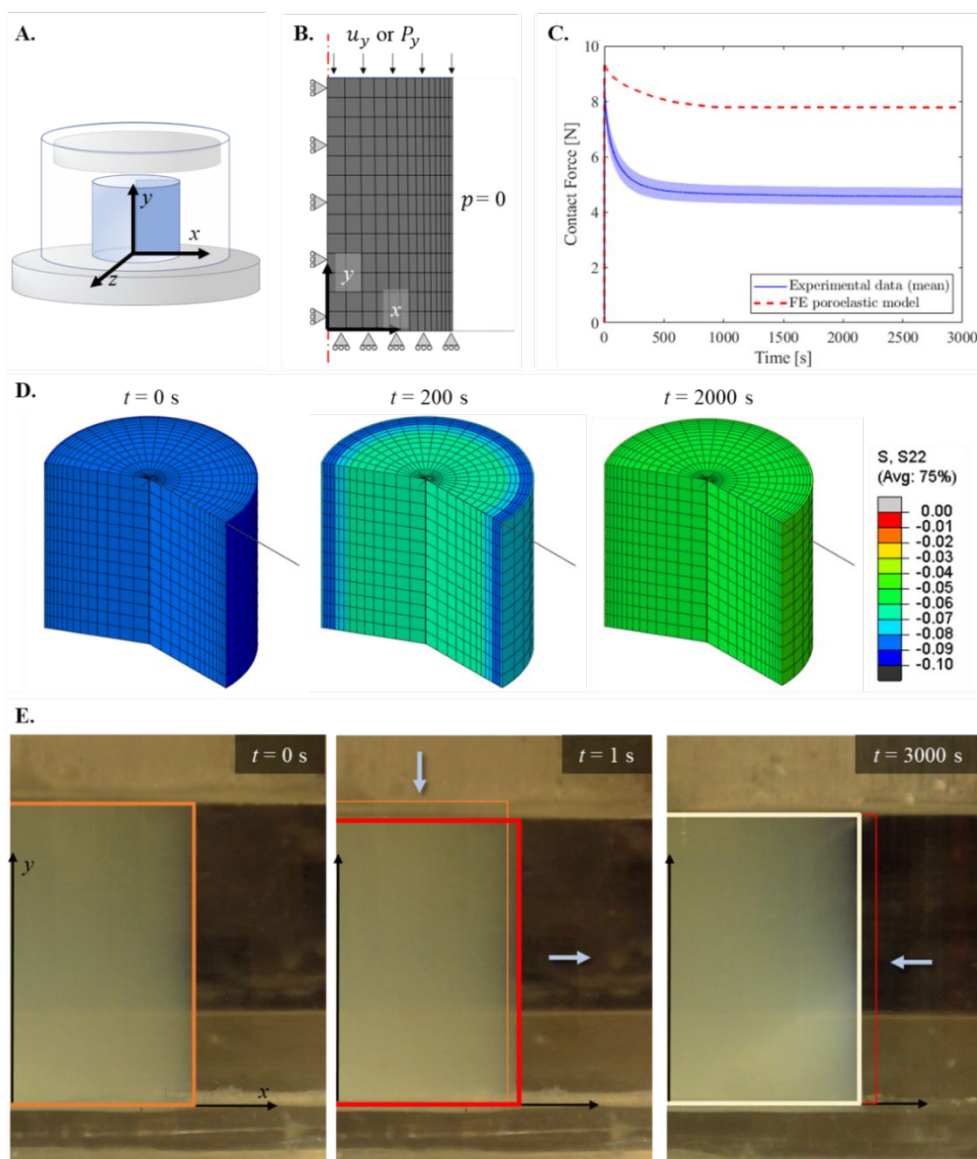

Figure 5. **A**. Schematic of unconfined compression of a cylindrical agarose sample. **B**. The computational domain along with the mesh and the boundary conditions implemented. In the boundary conditions, p is the pore pressure and u_y the axial displacement applied when multi-step stress-relaxation is simulated or P_y the axial pressure applied when creep is

simulated. **C**. Abaqus poroelastic model prediction results (red dashed line) for stress-relaxation test for 16 mm, 5% w/w agarose gels versus experimental data (solid blue line -average value from the different samples tested- and a blue region -average ± standard deviation). **D.** Three different time frames (from top to bottom, 1 s, 200 s and 2000 s) are plotted to show the stress distribution in the axial direction. It is possible to observe how the poroelastic effect generates a gradient on the stress distribution. After the fluid transport ceased, the stress field became uniform and the solid network was the only part of the system dissipating energy. **E**. Photographs were taken during stress-relaxation test on 16 mm, 5% w/w agarose gels to experimentally quantify the Poisson's ratio of the solid skeleton and determine the order of magnitude of the characteristic time corresponding to the fluid leaving the system. The compression stage had a duration of 1 s where the gel expanded laterally. The relaxation process was recorded while the gel contracted laterally due to the fluid leaving the system. The gel stopped shrinking at 3000 s after the compression stage.

228   3.   AGAROSE AS A NONLINEAR TRANSIENT NETWORK

229   The time-dependent inelastic response of agarose samples in this study was dominated by viscoelasticity, rather than
230   poroelasticity. In the literature, the mechanical behavior of agarose have generally been characterized by an elastic and a
231   time-dependent or viscous component using phenomenological viscoelastic models[21–23] (i.e., the simplest being the Maxwell
232   model). These models however remain mostly empirical, which motivates the current work as an attempt to build a
233   connection between the gel's network topology and its mechanical response.

234   3.3. Preliminaries: the transient network theory

235   Let us start by introducing a theoretical framework to describe the nonlinear viscoelasticity of polymer networks, known as
236   the transient network theory (TNT)[27,40]. Due to the presence of physical crosslinks in agarose structure[41], the network is
237   assumed to be dynamic, wherein the polymer chains associate and dissociate over time.

238   The polymer is thus idealized as a network of polymer strands with the end-to-end vector $\boldsymbol{r}$ which represents as the segment
239   between two nodes or crosslinks. For convenience, we introduce the normalized end-to-end vector $\boldsymbol{\lambda} = \dfrac{\boldsymbol{r}}{r_0}$ where r_0 is the
240   natural (force-free) length of a strand. In the TNT, a statistical description of the network is provided by the density c of
241   connected strands and the so-called strand conformation tensor, with indices μ_{ij} given by

$$\boldsymbol{\mu}(t) = 3\langle\boldsymbol{\lambda}\otimes\boldsymbol{\lambda}\rangle \qquad\qquad 4$$

242   where the operation $\langle\ \rangle$ denotes the average chain deformation of all connected strand within a representative volume
243   element. If the network is initially isotropic, it verifies $\boldsymbol{\mu}(0) = \boldsymbol{I}$. Under the affine deformation assumption[42], the change in
244   stretch of a connected strand verifies $\dot{\boldsymbol{\lambda}} = \boldsymbol{L} \cdot \boldsymbol{\lambda}$ where $\boldsymbol{L}$ is the velocity gradient $\boldsymbol{L} = \dot{\boldsymbol{F}}\boldsymbol{F}^{-1}$. Therefore, it is possible to
245   construct an evolution equation for the strand conformation tensor if the rates of chain association and dissociation
246   previously described are known[27].

$$\dot{\boldsymbol{\mu}} = \boldsymbol{L}\boldsymbol{\mu} + \boldsymbol{\mu}\boldsymbol{L}^{T} - k_d\boldsymbol{\mu} + k_a\frac{C-c}{c}\boldsymbol{I} \qquad\qquad 5$$

247   where C is the total number of strands per unit volume the network (including both connected and dangling contributions),
248   and k_a and k_d are the kinetic rates describing polymer chains association and dissociation, respectively. For simplicity, we
249   assume there is a perfect bond exchange within the network, meaning each detachment event is immediately followed by
250   an attachment event[43]. We also consider the case of incompressible plastic flow. The evolution equation becomes the
251   following[44]:

$$\dot{\boldsymbol{\mu}} = \boldsymbol{L}\boldsymbol{\mu} + \boldsymbol{\mu}\boldsymbol{L}^{T} - k_d\left(\boldsymbol{\mu} - \frac{3}{\operatorname{tr}\boldsymbol{\mu}^{-1}}\boldsymbol{I}\right) \qquad\qquad 6$$

252   From this relation, it is straightforward to show that for a covalently cross-linked network ($k_d = 0$) the conformation tensor
253    $\boldsymbol{\mu}$ is equivalent to the left Cauchy-Green tensor $\boldsymbol{b}$, i.e. $\boldsymbol{\mu} = \boldsymbol{b} = \boldsymbol{F}\boldsymbol{F}^{T}$[27]. Similarly to Equation 3, the true stress tensor can
254   then be derived in terms of the conformation tensor as[40,45]

$$\boldsymbol{\sigma} = \frac{2}{J_e}\boldsymbol{\mu}\frac{\partial\psi}{\partial\boldsymbol{\mu}} = \frac{2}{J_e}c_{10}\mathrm{Dev}\,\overline{\boldsymbol{\mu}} + \frac{2}{D_1}(J_e - 1)\boldsymbol{I}$$

7

255   where the deviatoric part of $\overline{\boldsymbol{\mu}}$ is given by $\mathrm{Dev}\,\overline{\boldsymbol{\mu}} = \overline{\boldsymbol{\mu}} - \frac{\mathrm{tr}\,\overline{\boldsymbol{\mu}}}{3}\boldsymbol{I}$. Material constants c_{10} and D_1 were defined in Equation 2b.

256   This model describes a material that displays a linear elastic response (through its Neo-Hookean form), and a linear

257   viscoelastic response (since the rate constant k_d remains constant). Note that this model may however still capture nonlinear

258   geometrical effects since it is valid for large strains. The viscoelasticity of agarose was however observed to be quite

259   nonlinear, which motivates the development of a more physical model regarding the relaxation mechanisms occurring

260   within the polymer structure. Such a theoretical improvement must therefore involve a rate constant k_d that changes with

261   stress as previously discussed in Hui *et al.* (2021)[46].

262   3.4. *Nonlinear bond dynamics of agarose-based gels*

263   Hydrogen bonding not only governs the self-gelation of agarose gels, but it also facilitates the complex dynamics of the

264   resulting network. Hydrogen-bonding side groups found in agarose facilitate the formation of transient supramolecular

265   structures with viscoelastic responses[47]. It is theorized that there are two main microstructural features that contributes to

266   agarose viscoelastic behavior. First, aligned agarose molecules that form double helices have a limited mobility in

267   comparison with single agarose molecules. This dynamic gel structure has been proposed to occur at short relaxation times.

268   In contrast, agarose molecules present in clusters that are not aligned with each other can dissipate energy much more easily

269   as they slide over adjacent molecules, corresponding to a fluid-like behavior[17]. This behavior is illustrated in Figure 6.
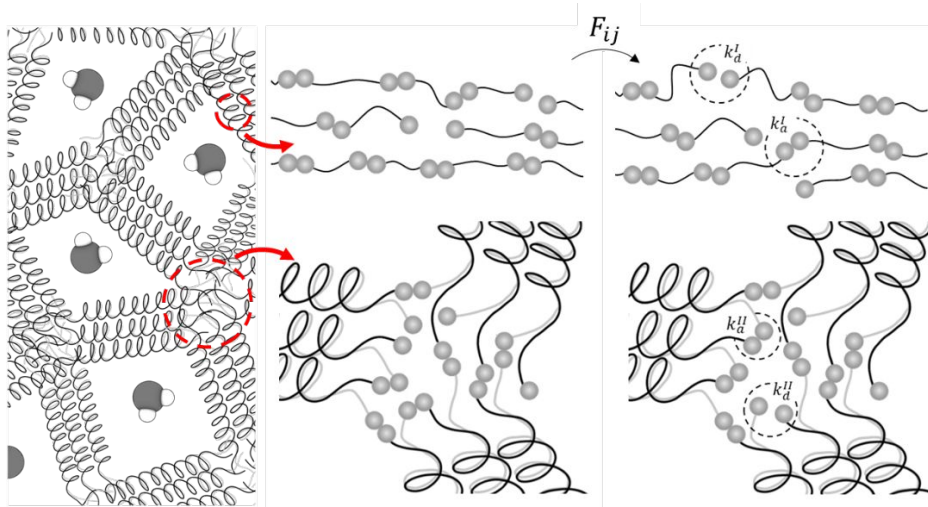

Figure 6. Schematic of the short relaxation time on agarose corresponding to the fast bond dynamics (k_d^I and k_a^I) of the strands aligned on the double helices (top) and of the long relaxation times associated to the slow bond dynamics (k_d^{II} and k_a^{II}) where agarose molecules presented in the suprafibers clusters can dissipate energy much more easily as the they slide over adjacent molecules (bottom).

270   Our experimental results suggest that agarose networks have two different dissipation mechanisms when subjected to an

271   external stress[48]. To construct a model for this network, we first assume each mechanism has its own characteristic

272   dissociation rate such that global the kinetic rate k_d is decomposed as:

$$k_d = k_d^I + k_d^{II}$$

8

273   Here k_d^I is the fast dissociation rate associated to the rearrangement of the strands aligned forming the double helix structure

274   and k_d^{II} is the slow dissociation rate associated with the bond exchange in the suprafiber junctions. A closer look at

275   experimental data suggests that the transition between the above two relaxation mechanisms is smooth and a function of the

276   overall stress-state of the specimen. The fast rates k_d^I is assumed to change with the level of stress, or alternatively, the level

277 of elastic deformation while the slow constant k_d^{II} is assumed to remain constant over the time scale of the experiments. For
278 simplicity, we follow classical plasticity theory and assume that volumetric deformation does not affect inelastic flow[49].
279 This model assumption can easily be relaxed in future implementation of the model if further experiments show it to be
280 inaccurate. We can therefore define a scalar measure of the isochoric elastic deformation via an "effective elastic strain"
281 defined as:

$$\bar{\mu} = \sqrt{\frac{3}{2} \text{Dev}(\overline{\boldsymbol{\mu}}){:}\text{Dev}(\overline{\boldsymbol{\mu}})} \ ,$$

282

283 such that the fast relaxation rate is defined with a generic function $f(\bar{\mu})$ in the form:

$$k_d^I = k_{d0}^I f(\bar{\mu}) \hspace{3cm} 9$$

284 The scalar function $f(\bar{\mu})$ need to be derived based on the experimental data collected. Observation of the creep test data
285 suggests that agarose does not show significant creep for $\bar{\mu} < \beta$. However, for values of $\bar{\mu} > \beta$ (Figure 8.A), creep suddenly
286 accelerates and the function k_d^I maybe assumed to follow the relation $k_d^I = k_d^0 \exp{(\gamma \bar{\mu})}$. This exponential relation is in line
287 with the theoretical model presented by Eyring experiencing force-dependent bond dynamics[50–52]. Combining this statement
288 along with the observation made from multi-step stress relaxation tests, the evolution of k_d is hypothesized to follow a
289 generalized logistic function with the following expression:

$$f(\bar{\mu}) = \frac{e^{\gamma\bar{\mu}}}{1 + e^{-\alpha(\bar{\mu} - \beta)}} \hspace{3cm} 10$$

290 where β represents the elastic strain trigger for bond dynamics, and γ is defined as the stress-sensitivity of bond dynamics.
291 In addition, as depicted in Figure 7, coefficient α describes the sharpness of the transition between the two energy dissipation
292 mechanisms; if $\alpha \rightarrow \infty$, the transition is very steep and converges to a step function while $\alpha \rightarrow 0$ indicates a very smooth
293 transition showing a perfect coupling between the two relaxation mechanisms during the whole relaxation process. The
294 coefficient β follows the evolution of the equilibrium or plateau stress σ_p point seen in Figure 2.C-D-E.
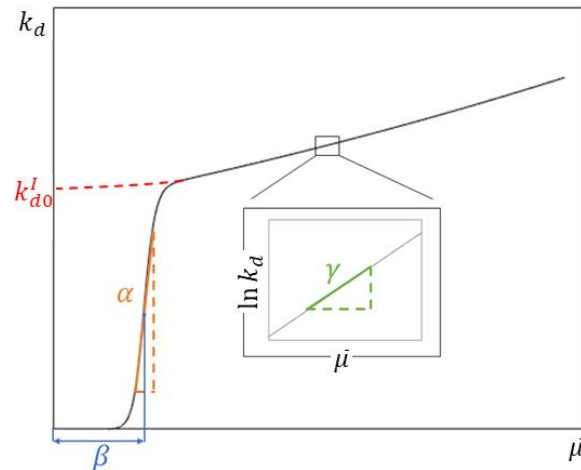

Figure 7. Physical interpretation of the fitting parameters used to describe the bond dynamic evolution: α is the bond
dynamics transition steepness, β is the elastic strain trigger for bond dynamics, γ is the stress-sensitivity of bond dynamics
and k_{d0}^I is the spontaneous dissociation once the stress threshold is triggered.

295   *3.5. Implementation and experimental validation*

296 The above viscoelastic model was implemented into a UMAT Abaqus subroutine requiring the calculation of the Cauchy
297 stress $\boldsymbol{\sigma}(\overline{\boldsymbol{\mu}})$ and tangent stiffness matrix $\boldsymbol{C}(\overline{\boldsymbol{\mu}})$. Using expressions provided in Appendix II, Equation **Error! Reference**

298   **source not found.** was invoked to enforce the evolution of the conformation tensor as a function of the dissociation ratio of
299   the network. To summarize, the material behavior of the hydrogel depends on two physical processes that are captured by
300   (a) a UMAT subroutine for the solid matrix based on the TNT to control the viscoelasticity of the skeleton, and (b) an
301   Abaqus material library to describe the poroelasticity due to the pore fluid flow of the solvent.

302   Running the optimization procedure detailed on Appendix III on the creep data and, separately, on the multi-step stress-
303   relaxation data, it was further possible to accurate calculate model parameters α, β, γ and k_{d0}^l. Using data from the creep
304   test, it was further possible to accurate calculate the exponential evolution of k_d^l where, independently of the concentration
305   of agarose used, we found mean values of $k_{d0}^l = 0.001164$ 1/s and $\gamma = 2.412$ (Figure 8.A); this expression accurately
306   predicts the values for k_d^l when $\bar{\mu} < \beta$.

307   Using data from the multi-step stress-relaxation and our optimization algorithm, the parameters α and β were empirically
308   fitted for various agarose composition and applied strain (see Figure 8.B). Different initial guess values were used as an
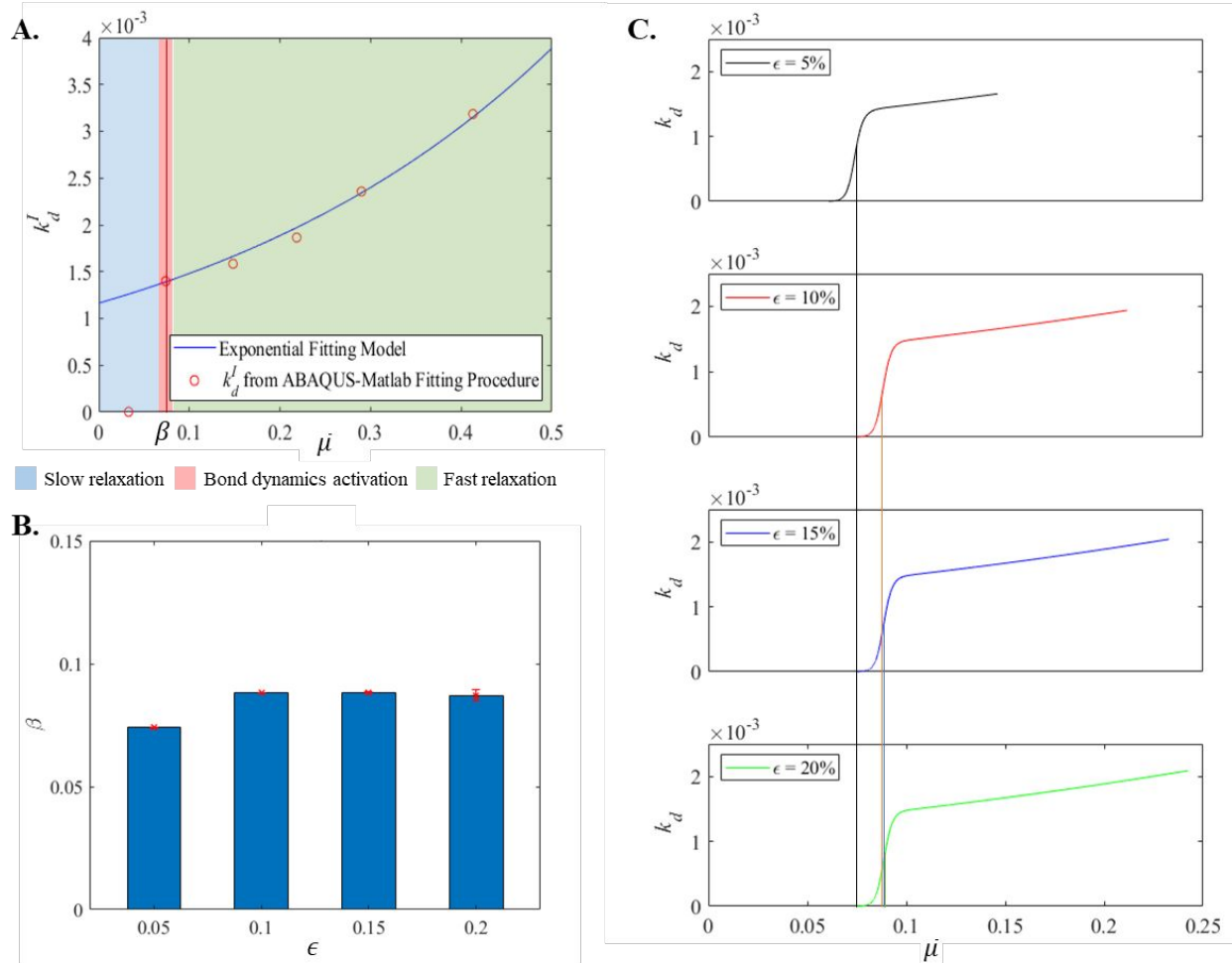309   input to the optimization algorithm.

Figure 8. A. Dissociation rate exponential evolution obtained from the optimization algorithm ran on the experimental creep test data on 12 mm, 5% w/w agarose gels. Graphing the results shows three different zones: slow relaxation domain (blue zone), fast relaxation domain (green zone) and the elastic strain trigger, β, zone for bond dynamic activation (red zone). **B.** For $\alpha = 500$, average values for the different agarose concentrations of the evolution of the elastic strain trigger for bond dynamics β at different applied strains during the multi-step unconfined compression test. **C.** For 10% w/w agarose, evolution of the bond exchange rate as a function of $\bar{\mu}$. Vertical lines represent the values for the bond dynamic trigger parameter β.

310

311 This data suggests that while the sharpness of the bond dynamics transition remains constant across the multiple
312 compression steps, the elastic strain trigger, β, changes its values to account for the stress plateauing during the whole test
313 (Figure 8.B). Therefore, β follows the plateau point evolution. For the 5% w/w case, β decreases for the last stress-relaxation
314 step. This agrees with the experimental data of Figure 2.C where the plateau stress σ_p measured in the last compression step
315 (20% strain), is below the one measured for 15% strain. For 7.5% and 10% w/w agarose, the same fitting parameter were
316 used for strains > 5%. In these cases, the sharpness of the transition remains constant, but β slightly increases its value at
317 each deformation step. Taken together, these results suggest that the evolution of bond dynamics is independent of agarose
318 concentration.

319 The dissociation constant k_d^{II} of the cluster was obtained using the optimization algorithm. We found that k_d^{II} is generally
320 insensitive to stress and agarose concentration which confirms it can be kept constant. We estimated the mean rate constant
321 as $k_d^{II} = $ 2.76E-6 1/s (i.e., $k_d^{II} \ll k_d^{I}$). In the remainder of our analysis (i.e., that concentrates on shorter time scales), this rate
322 can therefore be neglected compared to k_d^{I}, and a general evolution equation for the general kinetic rate is $k_d \approx k_d^{I} = k_{d0}^{I} f(\bar{\mu})$
323 . Therefore, as an input for the UMAT subroutine five parameters are necessary to describe the solid matrix behavior: the
324 elastic modulus E_s of the solid network, Poisson's ratio ν_s of the solid matrix and the empirical variables α, β, γ and k_{d0}^{I}.

325 Figure 9. demonstrates agreement between the poroviscoelastic model and the time-dependent mechanical response of
326 agarose gels during experimental creep (5% w/w agarose) and multi-step stress relaxation (5, 7.5, 10% w/w agarose) testing.
327 Figure 8.B. and Figure 9.B-D. also verify the evolution of bond exchange rate behaves independently of agarose
328 concentration. Inset plot in panel A in Figure 9 corroborates the model captures the three creep regimes (primary, secondary
329 and tertiary creep) in experimental data. Insets plots in panels B-D in Figure 9, shows the model captures the short-term
330 experimental response of agarose gels. We notice energy is dissipated faster on the experimental data than on the
331 computational model for short time scales, yet such difference does not affect the equilibrium response.
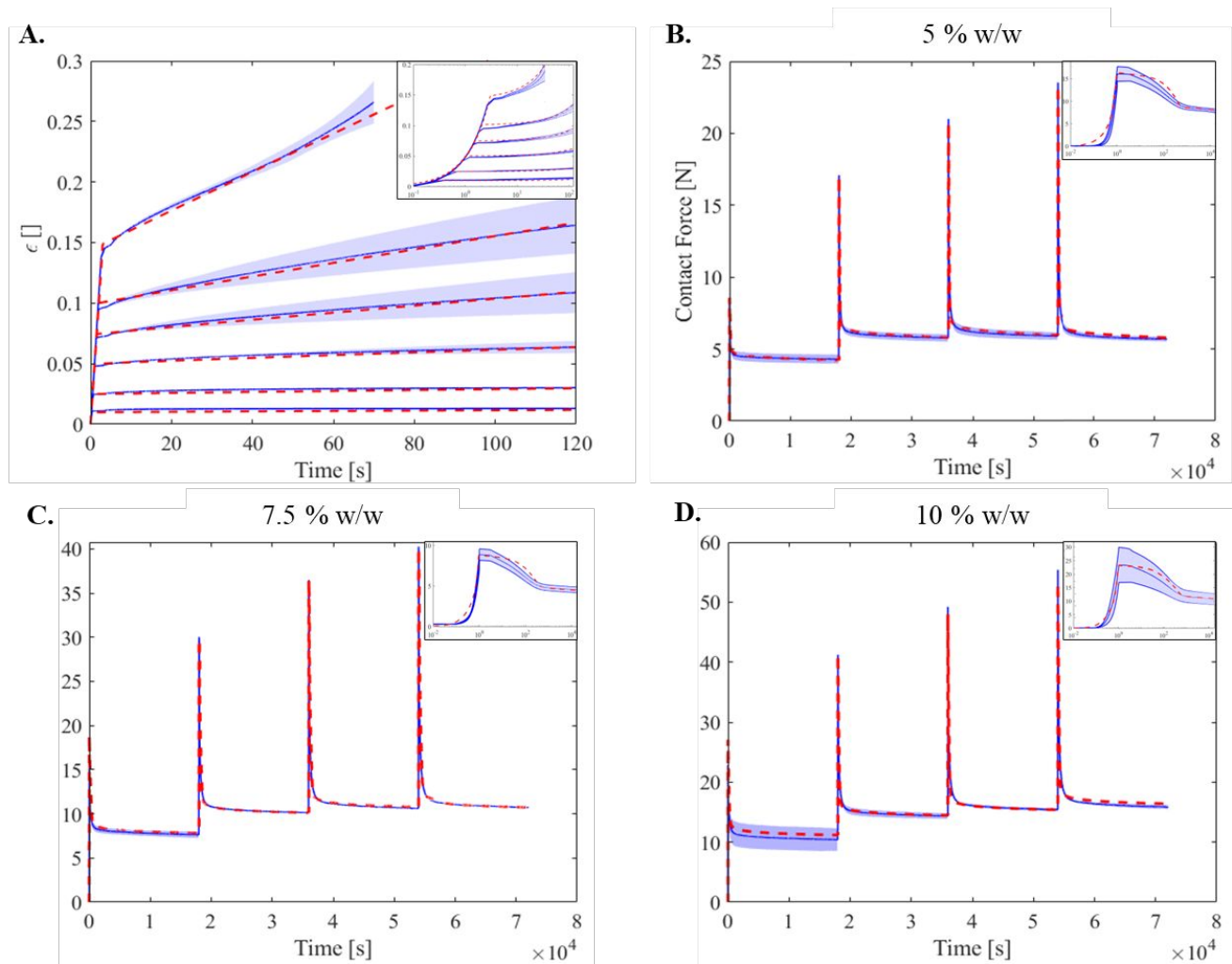
Figure 9. Comparison of the prediction from finite element predictions against experimental measurements for tested samples. Abaqus simulation results are represented by red dotted line, and experimental results are reported as a blue solid line (mean values from experimental tests) and blue region (average ± standard deviation). **A.** Results of creep test for 12mm, 5% w/w agarose gels. The inset in **A**. shows creep test results in a semilogarithmic scale along the x-axis. **B.**, **C.**, and **D**. Results of multi-step stress relaxation tests for 5%, 7.5% and 10% w/w agarose gels respectively. The inset in **B-D**. shows the stress evolution for the first loading and relaxation step in a semilogarithmic scale along the x-axis.

4. DISCUSSION

We developed a physically based model to describe and predict the time-dependent behavior of agarose networks under unconfined compression. Unlike prior phenomenological and continuum models describing viscoelasticity, our approach considers the time-dependent evolution of the stress-dependent variables that result from bond-exchange within the polymer network. This work provides a reinterpretation of agarose network viscoelastic behavior using the transient network theory (TNT). Using the characterization of the two main microstructural features that contribute to agarose viscoelastic behavior, which are based on dissociation and reassociation of molecular bonds within agarose, we demonstrated that the network deforms over time through non-linear force-dependent evolution of bond dynamics.

Agarose gels are formed from hydrogen (e.g., dynamic) bonds that re-attach after disengaging which imparts gels with viscoelastic behavior. Here, viscoelasticity was assumed to follow the two main characteristic microstructures of the gel network described by Labropoulos *et al.* (2001)[48]. Assuming perfect bond exchange, we hypothesized that the overall dissociation rate (k_d) results from a linear combination of the dissociation rate corresponding to double helices forming between aligned agarose molecules (k_d^I) and the dissociation rate of the agarose molecules present in the clusters (k_d^{II}). Due to the degree of mobility of the agarose, these factors are responsible for the short ($1/k_d^I$) and longer ($1/k_d^{II}$) relaxation times,

15

346 respectively. The present work incorporated these topologically based phenomena into a mathematical model, the TNT,
347 thus enabling a novel quantitative understanding of the relationships between molecular physics and overall mechanical
348 response. This methodology may be extrapolated to other biopolymer networks with similar topologies (i.e., collagen and
349 fibrin networks) to predict their emerging material response as a function of bond kinetics.

350 The fast bond dynamics of agarose network (k_d^l) associated to the aligned agarose molecules exhibited significant force-
351 sensitive dynamics. In the creep test, we observed that the magnitude of the applied stress had the effect of weakening the
352 solid-like behavior of the network associated to the fast energy dissipation mechanism. We interpreted this behavior as a
353 reorientation of the agarose network along the direction of applied compression which is a particular property of semiflexible
354 networks. Our model suggested an exponential force-dependent response of the fast dissociation rate, which agrees with
355 Eyring's theory[50]. Capturing this phenomenon revealed a novel insight in agarose viscoelastic properties: i.e., the lifetime
356 of a bond depends on the force applied to that bond.

357 We further demonstrated the non-linear viscoelasticity of agarose hydrogels throughout the implementation of a non-
358 constant dissociation rate. In our study, the nonlinear viscoelasticity could be observed by a stress-plateauing effect during
359 a multi-step stress relaxation test. In particular, the equilibrium stress at the end of the relaxation phase plateaued and reached
360 the same value independent of the applied deformation. We developed a master equation to describe the bond exchange
361 (Equation **Error! Reference source not found.**) based on physics-based parameters such as the elastic strain trigger for
362 bond dynamics and the stress-sensitivity of the bond rate. The same behavior was observed in multi-step stress relaxation
363 testing (with a 30 minute relaxation period) reported by Roberts *et al.* (2011)[12] in their comparative study of the viscoelastic
364 mechanical behavior of agarose and poly(ethylene glycol) hydrogels. Because of the relatively short time used between step
365 strains in their study, the stress did not plateau as reported herein; however, the trends in both studies are consistent.

366 Following the stability of adhesion clusters model presented by Erdmann and Schwarz (2004)[53], we hypothesized that the
367 clusters formed by several suprafibers within agarose networks increased the number of connected bonds during the
368 deformation process (Figure 10). Cluster adhesion was presented in previous literature as a likely mechanism for stress
369 relaxation in biopolymers[54–56]. For example, Prechtel *et al.* (2002) studied cluster dissociation under a linear ramp of force
370 and described the strength of the adhesion of living cells to model membranes[57]. Briefly, Erdmann and Schwarz postulated
371 a detailed theoretical analysis of the stochastic dynamics of a cluster of parallel bonds under shared constant loading and
372 with rebinding. The adjacent agarose molecules that are not part of the cluster in a stress-free configuration may be available
373 to later form new crosslinks with the initial components of the cluster. This theory provides a mechanism for increasing
374 cluster size and a strengthening of the network. Following this theory, we found the elastic modulus of agarose slightly
375 increased with elastic deformation which indicated a mild strain stiffening effect during sustained compression (Appendix
376 IV). Future investigations should further evaluate our hypothesis for a potential relationship between the elastic strain trigger
377 for bond dynamics and cluster size and should also consider other possible competing mechanisms such a viscoelastic
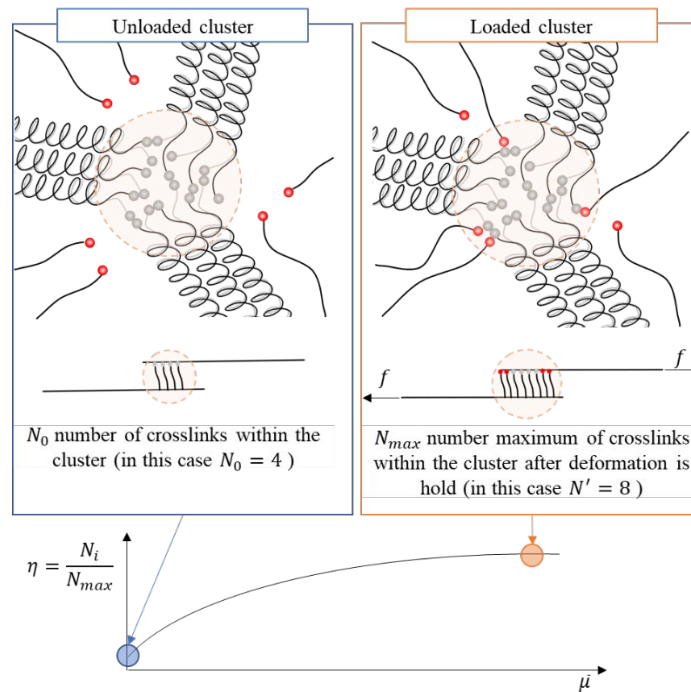378 elongation of the network chains[58,59].

379

Figure 10. Schematic representation of the number of bonds N_i within a cluster in agarose network before and after a stress field is applied. Unbonded agarose molecules join the cluster as the external force increases. Variable η is defined to represent the cluster bond saturation plateauing after the force f held by the cluster exceed a certain threshold value.

380   Poromechanical effects in agarose did not significantly contribute to energy dissipation during stress-relaxation. These
381   results followed the well-studied poroelastic material behavior of agarose in the literature[37,60–64]. We observed that the
382   influence of time-dependent fluid displacement on the gel's response to be small. However, we still incorporated it in our
383   analysis for the following reasons. First, we observed a reduction of the initial hydrogel mass during long-duration
384   compression tests; this effect can only be captured by poromechanics. Second, the incorporation of fluid transport during
385   loading allowed for a more general formulation that may explain coupling of poromechanics with network relaxation; this
386   point can be used to better understand poroviscoelastic behavior of agarose gels. Demonstrating the minor role of
387   poromechanics in agarose supported the use of the TNT to control and predict the macroscopical time-dependent response
388   of physically crosslinked gels.

389   Unlike prior applications of the TNT in 2D[40], our study demonstrated the application of the TNT into a commercial FEA
390   software. This approach will allow for future 3D modeling of complex polymer behavior (i.e., crack propagation or cavity
391   generation[65]) using an underlying mechanism-based material model. We also demonstrated an initial step that will enable a
392   continuum approach of the TNT to be applied to more complex geometries (i.e., 3D printed hydrogels) than the cylindrical
393   geometry presented in this study. The computational implementation of the TNT into a commercial FEA package, combined
394   with experimental testing, allowed us to assess the influence of poroelastic and viscoelastic effects in the overall
395   macroscopic response of agarose to time-dependent experiments.

396   Finally, we emphasize that the model presented in this study can be used to provide control guidance on the material design
397   in numerous applications, many of which are applicable to bioengineering, that necessitate the use of agarose and similar
398   gels. The TNT model also offers the possibility to design and fabricate gels based on their bond dynamic to obtain a specific
399   time-sensitive behavior. One important future effort is to extend the current model to different biopolymers with similar
400   network topology and to determine if the TNT can be universally applied to describe behavior of similar biopolymers.
401   Finally, our work may also support a variety of tissue engineering applications and provide physical insights to understand
402   the force-dependent viscoelastic behavior. For instance, understanding how the yielding behavior of agarose gels may be
403   crucial for a wide range of biomedical applications where gels are subjected to loads over long periods of times.

409 **CONFLICT OF INTEREST**

410 There are no conflicts of interest.

411 **APPENDIX I: INTRINSIC PERMEABILITY AND VOID RATIO EVOLUTION IN AGAROSE GELS**

412 The intrinsic permeability κ for agarose gels was defined using the evolutions equations described by Gu *et al.* (2003)[37].

$$\kappa = \kappa_0\left(\frac{J_e - \phi_0}{1 - \phi_0}\right)^n, \phi = \frac{\phi_0}{J_e} \tag{11}$$

413 Therefore, in this study, the intrinsic permeability κ and the solid volume fraction ϕ were assumed to be a function of the
414 macroscopic deformation applied on the gel, in this case using the Jacobian J_e of the elastic deformation gradient tensor $\boldsymbol{F_e}$.

415 The initial permeability was defined as $\kappa_0 = p_1\left(\frac{1-\phi_0}{\phi_0}\right)^{p_2}$ where p_1 and p_2 were fitting parameters. Here, the initial solid

416 volume fraction ϕ_0 was obtained using the relationship established by Pluen *et al.* (1999)[60]; $\phi_0 = \frac{1}{\rho_{agarose}\omega_{agarose}}c_o$ where c_o

417 is the agarose concentration, $\rho_{agarose}$ = 1.64 g/ml is the dry agarose density[61] and $\omega_{agarose}$ = 0.625 is the mass fraction of
418 agarose in a fiber[62].

419 The initial hydraulic conductance K was defined as $K = \frac{\gamma_s}{\mu}\kappa$ where μ is the dynamic viscosity of the fluid and γ_s is the
420 specific weight of the fluid. Since the fluid was a PBS solution, μ = 1E-9 N·s/mm² and γ_s = 9.81E-06 N/mm³. Once ϕ was
421 calculated and assuming the porosity $\theta = 1 - \phi$, the void ratio was defined as $e_0 = \frac{\theta_0}{1-\theta_0} = \frac{J_e}{\phi_0} - 1$. Values were summarized
422 in Table 2 and assumed to remain constant during the whole deformation process.

c_o[%]	ϕ_0[%]	e_0	κ_0 [mm²]	K_0 [mm/s]
5	4.88	19.5	2.32E-11	2.56E-07
7.5	7.32	12.67	1.22E-11	1.22E-07
10	9.76	9.25	7.75E-12	7.60E-08

Table 2. Parameters used to describe poromechanics for each agarose composition used in the study.

423 **APPENDIX II: CAUCHY STRESS AND TANGENT STIFFNESS MATRIX DERIVATION**

424 To derive the required expressions for the implementation of the TNT into Abaqus, we first rewrote the elastic energy as:

$$\psi = c_{10}\left(\overline{I_1} - 3\right) + \frac{1}{D_1}(J_e - 1)^2 \tag{12}$$

425 We here assumed elastic compressibility but inelastic incompressibility (from Equation 6). Consequently, in the remainder
426 of our derivations, $J_e = J$. The constitutive equation for the Cauchy stress can be written directly in terms of the deformation
427 gradient[45]:

$$\sigma_{ij} = \frac{2}{J}\mu_{ik}\frac{\partial\psi}{\partial\mu_{kj}}$$

13

428   Now we compute the derivatives of the invariants $\overline{I_1}$, $\overline{I_2}$ and J with respect to the conformation tensor $\boldsymbol{\mu}$ components

$$\frac{\partial\psi}{\partial\mu_{ij}} = \frac{\partial\psi}{\partial\overline{I_1}}\frac{\partial\overline{I_1}}{\partial\mu_{ij}} + \frac{\partial\psi}{\partial\overline{I_2}}\frac{\partial\overline{I_2}}{\partial\mu_{ij}} + \frac{\partial\psi}{\partial J}\frac{\partial J}{\partial\mu_{ij}},$$

14

429   and obtain the stress expression

$$\sigma_{ij} = \frac{2}{J}\left[\frac{1}{J^{\frac{2}{3}}}\left(\frac{\partial\psi}{\partial\overline{I_1}} + \overline{I_1}\frac{\partial\psi}{\partial\overline{I_2}}\right)\mu_{ij} - \frac{1}{3}\left(\overline{I_1}\frac{\partial\psi}{\partial\overline{I_1}} + 2\overline{I_2}\frac{\partial\psi}{\partial\overline{I_2}}\right)\delta_{ij} - \frac{1}{J^{\frac{4}{3}}}\frac{\partial\psi}{\partial\overline{I_2}}\mu_{ik}\mu_{kj}\right] + \frac{\partial\psi}{\partial J}\delta_{ij}$$

15

430   In our case

$$\sigma_{ij} = \frac{2}{J}c_{10}\left(\overline{\mu}_{ij} - \frac{1}{3}\delta_{ij}\overline{\mu}_{kk}\right) + \frac{2}{D_1}(J-1)\delta_{ij}$$

16

431   To obtain the tangent stiffness matrix we first need to define virtual rate of deformation

$$\delta D_{ij} = \frac{1}{2}\left(\delta F_{im}F_{mj}^{-1} + F_{im}^{-1}\delta F_{jm}\right) = \frac{1}{2}(L_{ij} + L_{ji})$$

17

432   The Kirchhoff stress is

$$\tau_{ij} = J\,\sigma_{ij}$$

18

433   The material Jacobian derives from the variation in Kirchhoff stress.

$$\tau_{ij} = J\,C_{ijkl}\,\delta D_{kl}$$

19

434   then

$$C_{ijkl} = \frac{2}{J}c_{10}\left[\frac{1}{2}(\delta_{ij}\overline{\mu}_{jl} + \overline{\mu}_{ik}\delta_{jl} + \delta_{il}\overline{\mu}_{jk} + \overline{\mu}_{il}\delta_{jk}) - \frac{2}{3}\left(\delta_{ij}\overline{\mu}_{kl} + \overline{\mu}_{ij}\delta_{kl} + \frac{1}{3}\delta_{ij}\delta_{kl}\overline{\mu}_{mm}\right)\right] + \frac{2}{D_1}(J_e - 1)\delta_{ij}\delta_{kl}$$

20

$$c_{10} = \frac{E}{4(1+v)} \text{ and } D_1 = \frac{6(1-2v)}{E}$$
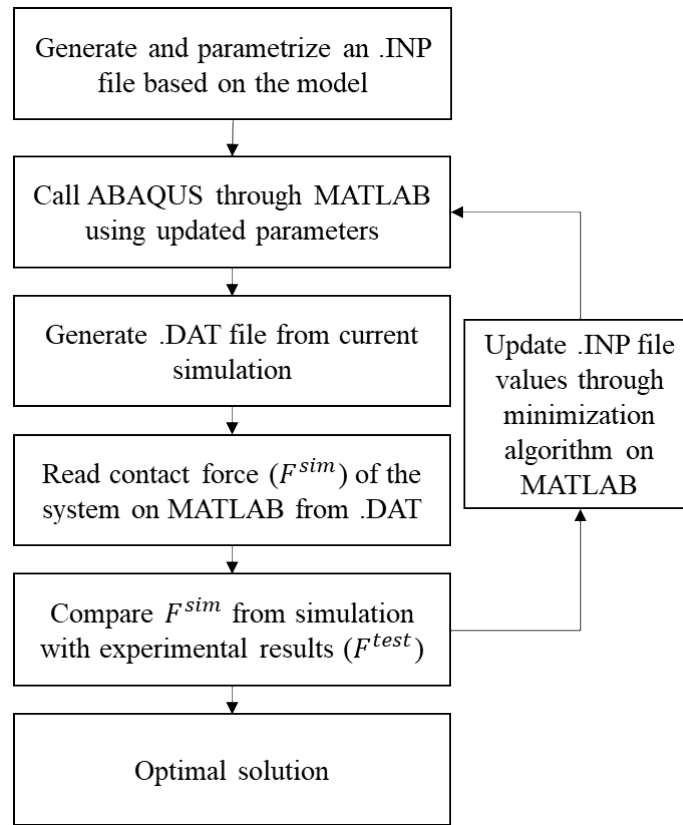
435

APPENDIX III: FITTING PROCEDURE LINKING ABAQUS AND MATLAB

436

437   To estimate the input material parameters (k_d^I, k_d^{II}, α, β, γ and k_{d0}^I) of agarose gels, an optimization procedure linking
438   Abaqus and MATLAB (MathWorks, Natick, MA, USA) was developed. Briefly, initial guess values of the material
439   parameters were assigned in the input file model and the Abaqus run was executed to compute the system contact force
440   response F^{sim}. Then, the sum of root-mean-square error in the contact force was defined as

$$SE = min\sum_{i=1}^{n}\left(F_i^{test} - F_i^{sim}\right)^2$$

21

441   where n is the number of iterations. Subsequently, an optimization algorithm was used to iteratively calculate the value of
442   the input variables by minimizing the objective function SE. For solving the optimization problem, the in-house code was
443   used based on the MATLAB function *fminsearch*. The lower and upper bounds in the function were properly chosen to
444   accommodate a wide range of values for each of the material properties.

19

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┌─────────────────────────────┐
│ Generate and parametrize an .INP │
│      file based on the model     │
└─────────────────────────────┘
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│  Call ABAQUS through MATLAB  │◄──────────┐
│    using updated parameters  │           │
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┌─────────────────────────────┐  │  values through   │
│ Generate .DAT file from current │ │   minimization    │
│          simulation          │  │  algorithm on     │
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│ Read contact force ($F^{sim}$) of the │  │
│ system on MATLAB from .DAT   │           │
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│ Compare $F^{sim}$ from simulation │──────┘
│ with experimental results ($F^{test}$) │
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│       Optimal solution       │
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445

446 **APPENDIX IV: ELASTIC MODULUS OF THE SOLID NETWORK E_S AND AGGREGATE MODULUS H_A**

447   Once the Poisson's ratio was properly determined and set to $\nu_s = 0.17$; the elastic modulus of the solid network E_s was
448   obtained using the fitting procedure described on Appendix III. This procedure was repeated for each of the four loading
449   steps for every sample. Fully swollen agarose gels exhibited an elastic response with a strong correlation between
450   stress/strain ($R^2 \approx 1$). Most studies in the literature report the aggregate modulus H_A instead of the elastic modulus of the
451   solid network. The aggregate modulus for different agarose composition can however be obtained directly from E_s and ν_s
452   as:

$$H_A = \frac{3(1 - 2\nu_s)}{2\,(1 - \nu_s)} E_s \qquad\qquad 22$$

453   At 5% strain and before relaxation, the mean aggregate modulus values could therefore be estimated as 0.97 MPa, 1.7 MPa,
454   and 2.43 MPa for 5%, 7.5% and 10% w/w agarose respectively. These results were in excellent agreement with the
455   previously reported by Normand *et al.* (2000)[66]. During the compressive stage that followed stress relaxation, we further
456   observed an increase in the aggregate modulus with respect to its initial value. In this study, H_A was observed to
457   exponentially increase with applied deformation in the following fashion ($R^2 \approx 1$) (Figure 11):

$$H_A = a(\bar{\mu})^b + c \qquad\qquad 23$$

458   Values for fitting parameters were summarized in Table 3.

c_o	a	b	c
5% w/w	7.27E5	10.86	0.97
7.5% w/w	1.92E6	11.31	1.70
10% w/w	3.65E6	11.76	2.44

Table 3. Control parameters a, b, and c as a function of the agarose concentration c_o used in the samples.
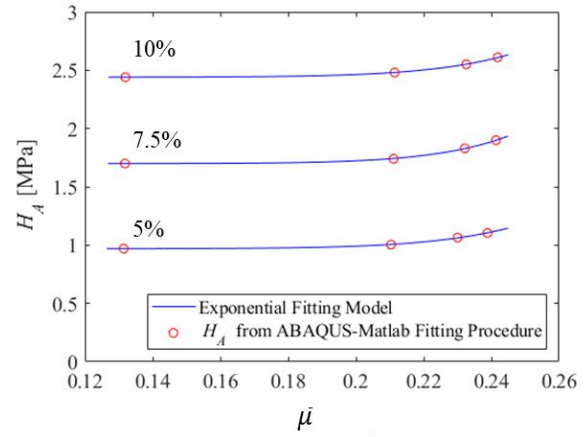

Figure 10. Evolution of the aggregate modulus H_A as a function of the second invariant of the conformation tensor $\bar{\mu}$.

459   The parameter c was directly related to the elastic modulus found at 5% strain (H_A^0) before the network had time to relax.
460   This fact motivated the idea of finding the following master equation as a function of the agarose concentration c_o.

$$H_A = H_A^0\left[\frac{3}{2}10^6 c_o(\bar{\mu})^b + 1\right]$$

24

461   The master Equation 27 shows that agarose network becomes stiffer as the overall deformation is increased and held during
462   large periods of time. Parameter b increases as the concentration of agarose in the samples increases. However, we found
463   that assuming parameter b constant and equal to the average of the values shown on Table 3 $(\bar{b} = 11.3)$ did not have major
464   differences in the fitted curves shown in Figure 9.

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