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Capacity-prediction models for organic anode-active materials of lithium-ion batteries: advances in predictors using small data

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Capacity-prediction models for organic anode-active materials of lithium-ion batteries: advances in predictors using small data†

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Organic energy storage has attracted a lot of interest in enhancing performance and reducing the consumption of resources. If performance predictors are prepared, the exploration of new compounds can be accelerated without consumption of time, energy, and effort. In the present work, a new straightforward capacity predictor is constructed for the exploration of organic anode-active materials. Sparse modeling for small data (SpM-S) combining machine learning (ML) and our chemical insights was used to construct linear regression models of specific capacity. In our previous work, two predictors (models G1 and G2) were prepared using small datasets. However, the descriptors and prediction accuracy of these models were not validated. In the present work, a new improved model (model G3) has been constructed with the addition of new data. These three models were studied in terms of data science: namely, prediction accuracy, validity of the descriptors, amount of training data used, and effect of ML algorithms. The straightforward, generalizable, and interpretable model G3 can be applied to explore new organic anode-active materials. Moreover, these data-scientific approaches to model construction and validation can be used to explore new energy-related materials even with small data.

1. Introduction

Organic electrode-active materials are needed to achieve next-generation high-performance and resource-saving energy storage.[1–9] One significant process is the exploration and discovery of new compounds for electrode-active materials. If a potential compound, *e.g.* a lead compound in the field of drug discovery, is found, we can design molecules, nanostructures, and electrodes to enhance performance. However, it is not easy to discover new compounds in a wide search space of organic compounds. Exploration based only on experience and intuition with trial and error encounters limitations. If predictors of electrochemical performance, such as reaction potential, capacity, and cyclability, are prepared, the efficient exploration of new compounds can be achieved. In the present work, a new

capacity prediction model (model G3) was constructed to explore organic anode-active materials for lithium-ion batteries using SpM-S (Fig. 1), a data-driven method based on small data.[10–14] The validity of model G3 was studied in a data-scientific manner and compared with that of the previous models G1 and G2.

Organic anode-active materials exhibit high specific capacity compared with conventional graphite.[1–9] In previous work, conductive polymers with redox reactions in the range of 2.0–0.5 V *vs.* Li/Li$^+$ were studied as a classical organic anode-active material.[15–18] Tarascon *et al.* reported a new scheme for the lithium alkoxylation of carbonyl groups in π-conjugated molecules.[19] Sun *et al.* found the uptake of multiple lithium ions (Li$^+$) in a π-conjugated framework,[20] *i.e.* superlithiation, drastically enhancing specific capacity.[21–29] Although π-conjugated molecules have potential for superlithiation, not all such compounds show high specific capacity. In recent years, known compounds with high specific capacity were introduced into polymers and covalent organic frameworks to enhance performance.[30–32] The exploration and discovery of new compounds depending only on professional experience encounter limitations. A more specific design strategy is required to discover new anode-active materials efficiently. If the correlations between molecular structure and capacity are elucidated, a predictor can be constructed to accelerate the exploration of new compounds. Redox potentials were

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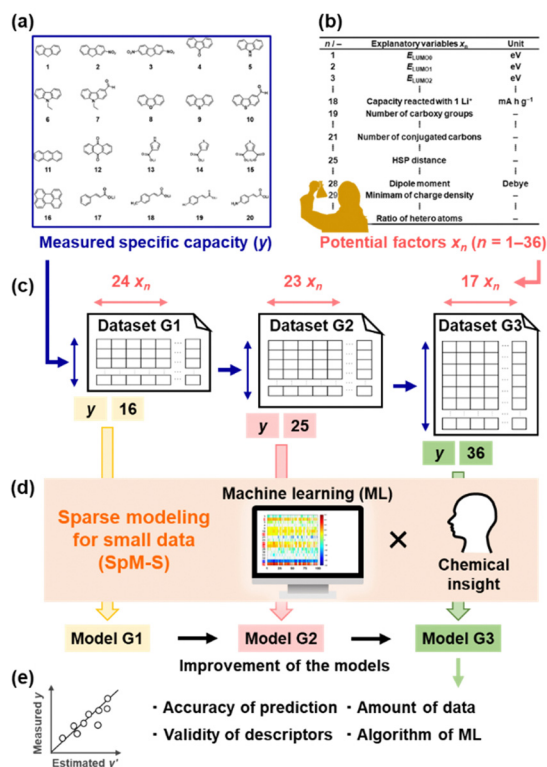
Fig. 1 Construction of prediction models G1–G3 from small data and their data-scientific validation. (a) Measured specific capacity (y: objective variables) for an organic anode-active material from charge−discharge curves. (b) Examples of the explanatory variables (x_n) as potential descriptors. (c) Successive small training datasets G1–G3 including y and x_n. (d) SpM-S with a combination of ML and chemical insight for the extraction of descriptors and construction of models G1–G3. (e) Data-scientific validation of the successive prediction models.

calculated to design organic electrode-active materials by computational chemistry.[33,34] The reactivity of organic anode-active materials with multiple lithium ions was studied by calculation.[20,28] However, specific capacity is not easily predicted by computational chemistry alone because various factors, such as conductivity, size, and shape of the particles, are related to capacity. Therefore, we have focused on machine learning (ML) to extract the significant factors and construct the capacity predictors.

Data-driven approaches have been rapidly developed in recent materials science.[35–40] ML has been used to predict the structures and functions of molecules and materials. In general, bigger training data is preferred to construct more accurate predictors. Big data sufficient for conventional ML algorithms is not easily prepared based on experimental studies in the laboratory. New ML schemes applicable to small data have been studied in recent years.[10,41–43] In addition, automated, robotic, and combinatorial methods are used to obtain big training data efficiently.[44–47] However, not all experiments including synthesis and characterization are integrated in an automated system. Although training data can be collected from the literature, the reported values include differences and errors depending on the experimental conditions of an individual research group. Experimental scientists need a new methodology

to use ML for small data. Our group has developed SpM-S, a new scheme of ML for small data.[10–14] Sparse modeling (SpM) is a general concept to describe whole high-dimensional data using a limited number of significant descriptors extracted by ML. In SpM-S, the extraction of the descriptors using ML is followed by further selection based on our chemical insight. Combination with our chemical insight contributes to avoiding overtraining caused by the small data and improving generalizability.[10,14] Therefore, SpM-S provides straightforward, interpretable, and generalizable linear regression models using a limited number of descriptors. Our group constructed performance predictors for organic cathode-active and anode-active materials using SpM-S.[48–50] Although two predictors (G1 and G2) for the specific capacity of an anode were prepared in our previous work (Fig. 1a–d),[48,49] their prediction accuracy was not sufficient. Moreover, the validity of the predictors and extracted descriptors were not studied in terms of data science. In the present work, a new improved model G3 was prepared with the addition of new experimental data (Fig. 1c and d). The validity of the prediction models G1–G3 was studied in terms of prediction accuracy, extracted descriptors, amount of training data, and ML algorithm (Fig. 1e).

2. Results and discussion

The capacity predictors of organic anode-active materials were constructed using small data based on our own charge–discharge measurements (Fig. S1 in ESI†).[48,49] Predictors G1 and G2 were prepared in our previous work (Fig. 2).[48,49] In the present work, predictor G3 was constructed to improve the prediction accuracy with the addition of new data (Fig. 3). The objective variable (y) was the measured specific capacity of commercially available compounds **1–54**, such as conjugated molecules and heteroaromatic compounds, at a current density of 10 mA g^{-1} for model G1 and 100 mA g^{-1} for models G2 and G3 (Table 1 and Scheme S1 in the ESI†).[48,49] New data was added in the training data for the construction of model G3 (note # in Table 1 and Fig. S1 in the ESI†).

The explanatory variables (x_n) were the potential descriptors related to capacity prepared based on our chemical insight (Table 2). The following parameters were used as x_n (Table 2):[48,49] the energy levels (E) of LUMO (x_1: E_{LUMO0}), four energy levels higher than the LUMO (x_2–x_5: E_{LUMOj}, $j = 1–4$), the absolute values of the differences in the energy levels

Fig. 2 Relationship between the estimated and measured capacity in the training (black) and test (red) data for models G1 (a) and G2 (b).
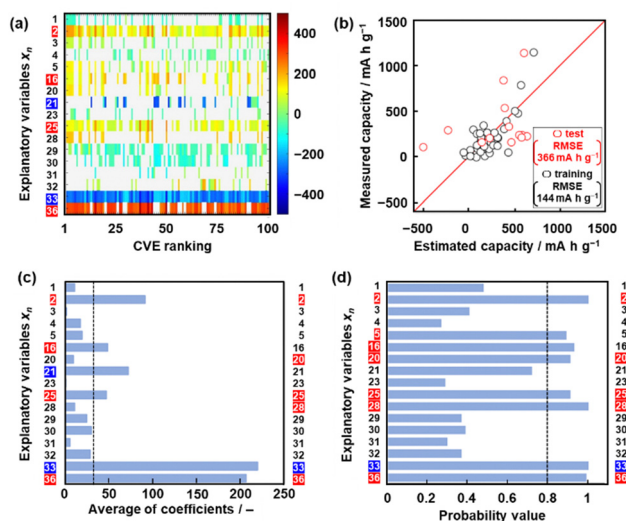
Fig. 3 Construction of model G3. (a) Weight diagram representing the coefficients of x_n (vertical axis) in 100 regression models with the smallest CVE values (the colored x_n on the left-hand axis: extractable descriptors). (b) Relationship between the estimated and measured capacity in the training (black) and test (red) data for model G3. (c) Average coefficients of each x_n in 100 regression models with the smallest CVE values (the colored x_n on the left-hand axis: extractable descriptors in the chart, the colored x_n on the right-hand axis: selected descriptors in the model G3). (d) Probability values of each x_n as a descriptor estimated from ES-BMA (the colored x_n on the left-hand axis: extractable descriptors in the chart, the colored x_n on the right-hand axis: selected descriptors in model G3).

Table 1 List of the objective variables (y)

[a]No.	Specific capacity/ mA h g^{-1}	[b]G1	[b]G2	[b]G3	Ref.	[a]No.	Specific capacity/ mA h g^{-1}	[b]G1	[b]G2	[b]G3	Ref.
1	0	G1			48	**28**	490		G2	G3	49
2	0	G1			48	**29**	6		G2		49
3	0	G1			48	**30**	178		G2	G3	49
4	0	G1			48	**31**	30		G2	G3	49
5	0	G1			48	**32**	798		G2	G3	49
6	19	G1			48	**33**	55		G2		49
[d]**7**	732/0	G1	G2		48, 49	**34**	513		G2	G3	49
[d]**8**	126/221	G1	G2	G3	48, 49	**35**	109		G2	G3	49
9	0	G1			48	**36**	56			G3	[c]#
[d]**10**	478/28	G1	G2	G3	48, 49	**37**	105			G3	[c]#
11	0	G1			48	**38**	0		G2		49
12	0	G1			48	**39**	277		G2	G3	49
13	84	G1			48	**40**	0		G2		49
[d]**14**	135/64	G1	G2	G3	48, 49	**41**	201			G3	[c]#
[d]**15**	178/1147	G1	G2	G3	48, 49	**42**	277		G2	G3	49
16	0	G1			48	**43**	141		G2	G3	49
17	355		G2	G3	49	**44**	134			G3	49
18	175			G3	49	**45**	15			G3	49
19	24			G3	[c]#	**46**	267			G3	[c]#
20	105		G2	G3	49	**47**	73			G3	49
21	0		G2		49	**48**	318			G3	49
22	142		G2	G3	49	**49**	63			G3	[c]#
23	405			G3	49	**50**	229			G3	[c]#
24	227		G2	G3	49	**51**	133			G3	49
25	91			G3	[c]#	**52**	279			G3	49
26	310		G2	G3	49	**53**	23			G3	[c]#
27	0		G2		49	**54**	273			G3	[c]#

[a] The molecular structures of **1–54** are displayed in Scheme S1 in the ESI. [b] The specific capacity refers to the training and test datasets in our previous work.[48,49] [c] The specific capacity was measured in the present work (Fig. S1 in the ESI). [d] The differences in the specific capacity are caused by the differences in the current density. The former and latter values are the measured capacity in the datasets G1 and G2, respectively.[48,49]

(x_6–x_{15}: $\Delta E_{\text{LUMO}j-k}$: j, k = 0–4), molecular weight (x_{16}), expected maximum (theoretical) capacity (x_{17}), theoretical specific capacity for reaction with one Li$^+$ (x_{18}), the number of carboxy groups (x_{19}), the number of carbonyl groups (x_{20}), the number of conjugated carbons (x_{21}), the number of occupied orbitals (N_{orb}) lower than the work function of lithium and energy level (E) E = 0 (x_{22}: N_{orb}, $E_{\text{LUMO0}} \leq E < \Phi_{\text{Li}}$, x_{23}: N_{orb}, $E_{\text{LUMO0}} \leq E < 0$), the sum of absolute values of E for the orbitals in the range from E_{LUMO0} to E = 0 ($\Sigma|\text{E}|$, $E_{\text{LUMO0}} \leq E < 0$, x_{24}), Hansen solubility-(similarity-)parameter (HSP) distance between the target compound and electrolyte solution (x_{25}), melting point (x_{26}), the number of sulfur (S) atoms in the heteroaromatic rings (x_{27}), dipole moment (x_{28}), the minimum and maximum values of the partial charge density (x_{29}, x_{30}), HSP dispersion (δD), polarity (δP), and hydrogen-bonding (δH) terms (x_{31-33}, respectively), the number of nitrogens and oxygens in the heteroaromatic rings (x_{34} and x_{35}, respectively), the ratio of the number of heteroatoms (N, S, O) to the total number of carbon, N, S, and O (x_{36}). In SpM-S, the significant descriptors were extracted by ML and then selected in combination with our experience and chemical insight. Linear regression models were constructed using the selected descriptors. After predictors G1 and G2 were introduced, the validity of predictor G3 and the advances in the processes of these predictors were studied in terms of data science.

2.1. Prediction model G1

Model G1 was constructed using the training data (training dataset G1) containing 24 x_n (n = 1–17, 19, 21–26, Table 2) and

16 y (compounds **1–16** in Table 1 and Scheme S1 in the ESI†) by SpM-S (Tables S1 and S2 in the ESI†).[48] The descriptors were initially extracted using a minimax concave penalty and penalized linear unbiased selection algorithm (MCP) and then selected according to our chemical insight.[48] The predicted y (y') was described by (eqn (1)) using three x_n with root mean square error (RMSE) of 162 mA h g^{-1} for the training data (black circles in Fig. 2a). Here the coefficients are converted to a normalized frequency distribution such that the mean is 0 and the standard deviation is 1. The coefficients of x_n quantitatively represent the contribution to y'.[48]

$$y' = 64.6x_{23} + 67.3x_{25} - 98.2x_{26} + 109.5 \qquad (1)$$

The test data including compounds **A–M** was prepared using literature values (Table 3 and Scheme S2 and Table S2 in the ESI†).[21–29] As predictor G1 needs the melting point (x_{26}) to calculate y', only nine compounds (**A, B, C, E, F, G, H, L, M**) with melting point data were used for the test (test dataset G1, Table S2 in the ESI†). Predictor G1 had an RMSE of 629 mA h g^{-1} for the test data (red circles in Fig. 2a). The black and red plots are not in the diagonal line of the y–y' plots representing the relationship between the predicted and measured values. A couple of new potential compounds, such as benzodithiophene,

Table 2 List of explanatory variables (x_n: n = 1–36)

No.	Explanatory variable x_n	Unit	G1[c]	G2[c]	G3[c]
1[a]	E_{LUMO0}	eV	G1	G2	G3
2[a]	E_{LUMO1}	eV	G1	G2	*G3*
3[a]	E_{LUMO2}	eV	G1	G2	G3
4[a]	E_{LUMO3}	eV	G1	*G2*	G3
5[a]	E_{LUMO4}	eV	G1	G2	G3
6[a]	$E_{LUMO1-0}$	eV	G1		
7[a]	$E_{LUMO2-0}$	eV	G1		
8[a]	$E_{LUMO3-0}$	eV	G1		
9[a]	$E_{LUMO4-0}$	eV	G1		
10[a]	$E_{LUMO2-1}$	eV	G1		
11[a]	$E_{LUMO3-2}$	eV	G1		
12[a]	$E_{LUMO3-1}$	eV	G1		
13[a]	$E_{LUMO4-3}$	eV	G1		
14[a]	$E_{LUMO4-2}$	eV	G1		
15[a]	$E_{LUMO4-1}$	eV	G1		
16	Molecular weight	g mol^{-1}	G1	**G2**	G3
17	Expected maximum capacity	mA h g^{-1}	G1		
18	Capacity reacted with 1 Li$^+$	mA h g^{-1}		G2	
19	Number of carboxy groups	—	G1	G2	
20	Number of carbonyl groups	—			*G3*
21	Number of conjugated carbons	—	G1	G2	G3
22[a]	N_{orb}, $E_{LUMO0} \le E < \Phi_{Li}$	—	G1	*G2*	
23[a]	N_{orb}, $E_{LUMO0} \le E < 0$	—	*G1*	**G2**	G3
24[a]	$\Sigma|E|$, $E_{LUMO0} \le E < 0$	eV	G1	G2	
25[b]	HSP distance	—	*G1*	*G2*	*G3*
26	Melting point	°C	**G1**	G2	
27	Number of S	—		G2	
28[a]	Dipole moment	Debye		G2	*G3*
29[a]	Minimum of charge density	—		G2	*G3*
30[a]	Maximum of charge density	—			*G3*
31[b]	HSP-δD	—		G2	G3
32[b]	HSP-δP	—		G2	G3
33[b]	HSP-δH	—		G2	**G3**
34	Number of N	—		G2	
35	Number of O	—		*G2*	
36	Ratio of heteroatoms	—		G2	*G3*

[a] DFT calculation values. [b] HSP calculation values. [c] x_n values shown in bold and italics were used as descriptors in models G1–G3 with positive and negative correlations, respectively.

Table 3 Specific capacity of compounds **A–M** in the test data

No.	Specific capacity/ mA h g^{-1}	Ref.	No.	Specific capacity/ mA h g^{-1}	Ref.
A	549	21	**H**	176	26
B	851	21	**I**	306	27
C	1143	21	**J**	253	28
D	125	22	**K**	344	28
E	254	23	**L**	242	29
F	178	24	**M**	230	29
G	222	25			

The molecular structures of **A–M** are displayed in Scheme S2 in the ESI.

were successfully found using predictor G1 in a limited number of experiments.[48] However, the predictor needs improvement for the following reasons. The measured capacity is higher than the estimated value, as indicated by the red arrow (Fig. 2a). This fact means that the capacity is underestimated by model G1. The underestimation is caused by the unbalanced small training data because nine of the 16 compounds had a specific capacity of 0 (Table 1). In addition, the melting point (x_{26}) is not always available for unknown new compounds. Therefore, model G1 is not easily applied to the practical exploration of new compounds.

2.2. Prediction model G2

Model G2 was constructed using the training data (training dataset G2) containing 23 x_n (n = 1–5, 16, 18, 19, 21–29, 31–36 in Table 2) and 25 y (compounds 7, 8, 10, 14, 15, 17, 20–22, 24, 26–35, 38–40, 42, 43 in Table 1, Scheme S1 in the ESI†) by SpM-S (Tables S3 and S4 in the ESI†).[49] As the specific capacity was measured at a current density of 100 mA g^{-1} to accelerate the collecting of y for the construction of models G2 and G3 (Table 1), the capacity (y) of some compounds was different from that used for model G1. In addition, compounds with specific capacity 0 (1–5, 9, 11, 12, 16) were removed to adjust the balance of the training data. The descriptors were extracted using an exhaustive search with linear regression (ES-LiR) and then selected according to our chemical insight, as explained later (Section 2.3). Predictor G2 was described by (eqn (2)) using six x_n with an RMSE of 217 mA h g^{-1} for the training data (black circles in Fig. 2b).[49]

$$y' = 20.4x_4 - 307.6x_{16} + 303.2\ x_{22} - 9.13x_{23} + 12.4\ x_{25}$$
$$+ 40.3x_{35} + 218.9 \tag{2}$$

The RMSE for the test data including 13 compounds **A–M** was 338 mA h g^{-1} (red circles in Fig. 2b and Table 3 and Scheme S2 and Table S4 (test dataset G2) in ESI†).[21–29] The black and red plots approach the diagonal line of the y–y' plots compared with those in model G1. A new potential active material with high specific capacity and cycle stability, namely 5-formylsarytilic acid, was found using predictor G2.[49] However, predictor G2 still needs an improvement in accuracy.

2.3. Prediction model G3 and its data scientific validity

Model G3 was constructed using the training data (training dataset G3) containing 17 x_n (n = 1–5, 16, 20, 21, 23, 25, 28–33, 36 in Table 2) and 36 y (compounds 8, 10, 14, 15, 17–20, 22–26, 28, 30–32, 34–37, 39, 41–54 in Table 1) by SpM-S (Tables S5 and S6 in the ESI†). The measured specific capacity of new compounds was added to dataset G3 (# in Table 1 and Fig. S1 in the ESI†). The descriptor was extracted from the weight diagram of ES-LiR and then considered based on our chemical insights (Fig. 3a). In ES-LiR, linear regression models are exhaustively prepared with all the possible combinations of x_n (n = 1, 2, 3, . . ., n). Here a total of $2^{17}-1$ ($\approx$ 1.3 × 10^5) patterns of the regression models are available whether or not each x_n (n = 1–17) is used as a descriptor. The coefficients of each model are visualized by the color in the weight diagram in ascending order of cross validation error (CVE) (Fig. 3a). In the weight diagram, x_n with more densely colored bands are used as descriptors more frequently. A deeper color indicates a larger coefficient of the descriptor, implying a larger contribution. The warm and cool colors correspond to positive and negative correlations, respectively. The coefficients of 100 models with the smallest CVE (top 0.08% of a total of 1.3 × 10^5 models) are summarized in the weight diagram (Fig. 3a). In general, a full state search (2^n-1 patterns) of the regression models is not performed to find a

sparse regression model, because evaluating each model results in a computational explosion. Computational explosion is prevented by replacing the task with a relaxation scheme, such as L1 regularization, and its optimization.[51,52] The methodology can end up with an exponential amount of computation with a realistic computation time of polynomial order. However, only a limited number of models are obtained by the optimization. In addition, the solution has no guarantee that it will be the optimal one for real data analysis. In recent years, all models with dozens of descriptors can be searched in a realistic amount of time through improved computing power, although ES-LiR needs an exponential amount of computation. Therefore, the search is exhaustively achieved for all possible models unlike optimization depending on relaxation problems.[53] This method visualizes the contribution of each x_n in the weight diagram, as shown in Fig. 3a.

We visually extracted seven x_n ($n = 2, 16, 21, 25, 33, 36$) from the weight diagram (the left-hand axis in Fig. 3a) and then studied their validity as descriptors. The positive correlation of x_{25} (HSP distance) and negative correlation of x_{33} (HSP-δH) imply that rigid molecular frameworks with low solubility to the electrolyte enable a stable redox reaction leading to high specific capacity. The positive correlation of x_{36} (ratio of the heteroatoms) implies that charge localization in the molecules promotes the introduction of Li$^+$. These x_n ($n = 2, 25, 33, 36$) are consistent with our chemical insight. Although the positive correlation of x_2 (E_{LUMO1}) is not directly explained, the positive correlation of the LUMO levels was used as the results of ML in model G2.[49] In the present work, x_2 is also adopted as a descriptor in model G3. Further studies including a calculation study are needed to elucidate the correlation between the LUMO level and capacity. The positive correlation of x_{16} (molecular weight) and the negative correlation of x_{21} (number of conjugated carbons) are not simply consistent with our chemical insight. In principle, the correlation of these descriptors is inverse. A higher specific capacity (mA h g^{-1}) is achieved by compounds with a lower molecular weight. More conjugated carbons enhance superlithiation, leading to an increase in specific capacity. Therefore, these x_n ($n = 16, 21$) are not selected for model G3. On the other hand, two x_n ($n = 20, 28$) are added as descriptors according to our chemical insight. The positive correlation of x_{20} (the number of carbonyl groups) means an increase in the reactivity of Li$^+$. In addition, carbonyl groups were reported to be reaction sites in previous work.[3–6] The positive correlation of x_{28} (dipole moment) means charge localization of the molecule enhances the introduction of Li$^+$. In this manner, six x_n ($n = 2, 20, 25, 28, 33, 36$) were selected as descriptors in combination with ES-LiR and our chemical insights. Predictor G3 was described by (eqn (3)) using six x_n with RMSE 144 mA h g^{-1} for the training data (black circles in Fig. 3b).

$$y' = 164.6x_2 + 58.0x_{20} + 116.8x_{25} + 98.5x_{28} - 280.1x_{33}$$
$$+ 296.9x_{36} + 229.9 \quad (3)$$

When five-fold cross validation was performed using (eqn (3)) in training dataset G3, the average RMSE values were 194 ± 12.6 mA h g^{-1} for the training and 218 ± 113 mA h g^{-1}

for the test data. Model G3 showed an RMSE of 366 mA h g^{-1} for the test data, including compounds **A–M** (red circles in Fig. 3b, Table 3 and Scheme S2 in the ESI†). Although the RMSE value of model G3 is smaller than that of model G2 for the training dataset (the black circles in Fig. 2b and 3c), model G3 shows a larger RMSE value than model G2 for the test dataset (the red circles in Fig. 2b and 3c). The relationship between the estimated and measured capacity of model G3 more accurately represents the trend of high and low capacity compared with that of models G1 and G2 (Fig. 2b and 3b), because more plots are on the diagonal line in the true-error plots. The overall accuracy and generalizability of the prediction model are evaluated not only by the RMSE values but also by the true-error plots. These results imply that model G3 can be used for an exploration of new unknown compounds.

The validity of the extracted descriptors was studied in terms of data science. The averaged absolute values of the coefficients were calculated for each x_n in 100 models with the smallest CVE values (Fig. 3c). The averages were larger than 35 for the visually extracted x_n ($n = 2, 16, 21, 25, 33, 36$) from the weight diagram. The chart quantitatively supports the validity of the visually extracted x_n from the weight diagram (Fig. 3a). However, the selected x_n ($n = 20, 28$) based on our chemical insight were not supported by the chart (Fig. 3c). In addition, the chart indicates that x_n ($n = 16, 21$) are potential descriptors. The validity of the six selected descriptors is not fully supported by ES-LiR alone. In general, ES-LiR has the following two problems which need to be solved. CVE is used to evaluate the prediction accuracy of the models. As this CVE-based model selection causes over-fitting the training data, a true model is not always obtained.[53] The other problem is the visual and qualitative extraction process of the descriptors from the weight diagram displaying the coefficients of the models in order of lowest CVE. The weight diagram represents not only a model with a specific CVE, such as the lowest one, but also multiple models with low CVE in the ranking. The visual effect of the weight diagram depends on the threshold of the CVE ranking defined by researcher. A more quantitative scheme including reliability is needed to extract the descriptors more appropriately.

Here reliability assessment and subsequent extraction of descriptors based on Bayesian model averaging (BMA) were carried out in the data.[54] Bayesian inference was applied to a linear regression model in our previous work.[55] In Bayesian inference,[56] the likelihood of each linear regression model using various descriptors is expressed by a probability value, assuming that noise is added to each of the experimental data. This evaluation method based on probability value approaches a true model, avoiding overtraining in training data compared with that based on the CVE value.[57] The model with the highest probability value can be selected to explain the experimental data. BMA is introduced in the selection process because the influence of the training data is significant. All possible models for each descriptor are integrated with weighting by the probability values explaining the experimental data. Then, the probability that each x_n is a descriptor is calculated (Fig. 3d). This ES-BMA method provides more quantitative information in the extraction processes

of the descriptors, whereas the descriptors are visually extracted from the weight diagram of ES-LiR (Fig. 2 and 3a–c). ES-BMA analysis indicates that the selected descriptors x_n (n = 2, 20, 25, 28, 33, 36) have a probability higher than 0.8. Therefore, ES-BMA supports the validity of the descriptors in model G3.

In this manner, the appropriate descriptors were extracted and selected in model G3 by ES-LiR in combination with our chemical insight. The validity of the model and its descriptors is supported by ES-BMA. These results imply that a straightforward and interpretable linear predictor can be constructed in small data using ES-LiR and ES-BMA in combination with our chemical insight.

2.4. Dataset independence of model G3

Cross-validation by merging the training and test datasets was carried out to study whether the selected descriptors are not extracted only from the specific training data.[14] The original training dataset G3 and test dataset G3 contained 36 y and 13 y, respectively. These datasets were mixed and then divided into ten segments. One segment and the remaining nine segments were assigned to test and training data, respectively. Validation was performed by changing the assignments of the test data in the total ten patterns. The average RMSE was 194 $\pm$ 12.6 mA h g^{-1} for the training dataset and 219 $\pm$ 114 mA h g^{-1} for the test datasets (Table S7 and Fig. S2 in the ESI†). The same ten-fold cross validation with merging of training and test data was performed for models G1 and G2. In model G1, the average RMSE was 280 $\pm$ 18.2 mA h g^{-1} for the training dataset and 303 $\pm$ 150 mA h g^{-1} for the test datasets (Table S7 and Fig. S3 in the ESI†). In model G2, the average RMSE was 240 $\pm$ 12.1 mA h g^{-1} for the training dataset and 261 $\pm$ 105 mA h g^{-1} for the test datasets (Table S7 and Fig. S4 in the ESI†). The smallest RMSE values for model G3 indicate that model G3 is constructed without dependence on the datasets compared with models G1 and G2.

2.5. Effect of the data quantity on the extractability of the descriptors

The effect of data size on the validity and extractability of the descriptors in model G3 was studied with a reduction in the size of the datasets (Fig. 4). The reduced training datasets G1′ and G2′ including the same compounds (y) in training dataset G1 (16 y) and training dataset G2 (25 y) were prepared from training dataset G3, respectively (Tables S8 and S9 in the ESI†). ES-LiR and ES-BMA were performed on the reduced training datasets G1′ and G2′ to study whether the same six descriptors in model G3 (x_n: n = 2, 20, 25, 28, 33, 36) are extractable or not (Fig. 4). The same x_n in model G3 were not fully extracted from datasets G1′ and G2′ (Fig. 4).

In training dataset G1′, six x_n (n = 1, 21, 23, 25, 28, 36) were visualized and extractable based on the weight diagram of ES-LiR and a chart displaying the averaged absolute values of the coefficients in the 100 models with the smallest CVE (the left-hand axes in Fig. 4a and c). The probability from ES-BMA indicates the potential descriptors x_n (n = 1, 23, 25, 28) (the left-hand axis in Fig. 4e). However, x_n (n = 2, 20, 23) were not extractable by ES-LiR and/or ES-BMA in dataset G1′. In training

Fig. 4 Extractability of the descriptors in the reduced datasets G1′ (a, c and e) and G2′ (b, d and f) (left-hand axis: extractable descriptors in the corresponding chart, right-hand axis: selected descriptors in model G3). (a and b) Weight diagram of ES-LIR. (c and d) Averaged absolute values of the coefficients in 100 models with the smallest CVE. (e and f) Probability values based on ES-BMA.

dataset G2′, x_n (n = 1, 2, 4, 16, 21, 28, 36) were extractable based on the weight diagram of ES-LiR and the averaged coefficients (the left-hand axis in Fig. 4b and d). The ES-BMA analysis indicates potential descriptors x_n (n = 1, 2, 20, 28, 29) with a probability higher than 0.8 (Fig. 4f). However, x_n (n = 25, 23) were not extractable by ES-LiR and/or ES-BMA in dataset G2′. These analyses imply that the data sizes in datasets G1 and G2 were insufficient to extract the descriptors.

The effect of the data was studied by another method (Table 4). Dataset G3 containing 36 y was reduced in six random patterns (Fig. S5–S9 in the ESI†). The weight diagrams were prepared by ES-LiR using the reduced datasets containing 35, 34, 33, 30, and 27 y to study the extractability of the descriptors. The number of extractable x_n (N_x) in the six x_n (n = 2, 20, 25, 28, 33, 36) of model G3 was counted in each weight diagram (Figs. S5–S9 in the ESI†). The average N_x ($N_{x,\text{ave}}$) of the six weight diagrams was calculated in the reduced datasets (Table 4). In addition, the numbers in the weight diagram (N_{wd}) satisfied with N_x = 6 and $N_x \geq 5$ are summarized in Table 4. The extractability of x_n distinctly decreases for y

Table 4 Extraction behavior of x_n in the reduced datasets

y in the reduced dataset	35	34	33	30	27
N_{ave}	1	2	0	0	0
$N_{wd}|N_x = 6$	3	4	3	2	0
$N_{wd}|N_x \geq 5$	4.17	4.83	4.17	3.50	3.00

Fig. 5 RMSE of the prediction models constructed with SpM-S, LASSO, and ML-R in the training (gray) and test (red) datasets.

lower than 33 (Table 4). When the data size is $y = 30$ or 27, the extractable x_n from the weight diagram depend on the datasets. The results support model G3 being constructed on a sufficient amount of training data $y = 36$.

2.6. Construction of predictors using other ML algorithms

Other prediction models were constructed using training dataset G3 by different ML algorithms, namely least absolute shrinkage and selection operate (LASSO) and multiple linear regression without variable selection (ML-R). The constructed predictors were validated using the test dataset including compounds **A–M** (Table 3 and Scheme S2 in the ESI†). The accuracy was evaluated by the RMSE values for the training data (dataset G3) and test data. The reference models comprised 13 x_n for LASSO and 17 x_n for ML-R. The RMSE values of these reference models for the training data were smaller than that of model G3 (gray bars in Fig. 5). The lower RMSE values imply that the reference models have higher prediction accuracy than model G3. Although the number of descriptors used is limited to six, model G3 has sufficient prediction accuracy. The RMSE value of model G3 for the test data was the smallest compared with that of the reference models (red bars in Fig. 5). The large differences in the RMSE values between the training and test datasets imply overtraining. As the difference is smallest for model G3, overtraining is avoided compared with the other models. These results indicate that SpM-S provides a straightforward, generalizable, and interpretable model G3 even in a small dataset.

3. Conclusions

Capacity prediction models for organic anode-active materials (models G1–G3) were constructed by SpM-S combining ML and our chemical insight for small experimental data. Models G1–G3 have been developed with the addition of training data. In the present work, the validity of these models was studied in terms of data science. Whereas the previous models G1 and G2 needed improvements in prediction accuracy, model G3 had sufficient prediction accuracy. The extracted and selected descriptors in model G3 were supported by a combination of

ES-LiR and ES-BMA. On the other hand, the same descriptors were not extracted from the datasets for models G1 and G2 even in combination with ES-LiR and ES-BMA. In other words, generalizable and appropriate descriptors were not extractable in the training datasets of models G1 and G2 for the exploration of new compounds because of the lack of training data. The required amount of data was studied using the weight diagrams of ES-LiR with a reduction in the size of the training data. Model G3 was constructed on a sufficient amount of training data compared with that of models G1 and G2. In addition, SpM-S provided generalizable model G3 compared with other ML algorithms. The straightforward, interpretable, and generalizable predictor G3 can be applied to the exploration of new organic anode-active materials in a wide search space. Our methods for model construction and validation, SpM-S combined with ES-LiR, ES-BMA, and our chemical insight, can be applied to other small-data-driven material exploration.

Conflicts of interest

There are no conflicts to declare.

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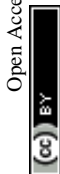
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