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# Variations in $\gamma'$ formers and refractory elements for enhanced creep resistance and phase stability of an advanced Ni-based superalloy†‡

Rui Feng,<sup>ab</sup> Chang-Yu Hung,<sup>ab</sup> Stoichko Antonov,<sup>a</sup> Jonathan D. Poplawsky,<sup>id c</sup>  
Ke An,<sup>id d</sup> Paul D. Jablonski<sup>a</sup> and Martin Detroy<sup>id \*a</sup>

The strong demands on increasing fuel efficiency have continuously driven the optimization of superalloys for high-performance applications. In this study, modifications to the chemistry and heat treatment of HAYNES<sup>®</sup> 282<sup>®</sup> alloy (H282) were performed by varying  $\gamma'$  formers and refractory elements. It was found that increasing Ti and substituting W for some of the Mo in the newly designed alloy (Q) resulted in a significant improvement of creep resistance, up to 130% increase in creep life, compared to standard H282. It was found that Orowan loops and dislocation climb were the dominant creep deformation mechanisms in alloy Q, while extensive dislocation tangling as an additional configuration was observed in the baseline alloy. Moreover, phase stability investigations for up to 5000 h at 800 °C and 900 °C revealed a reduced formation of detrimental  $\sigma$  and  $\mu$  phases in alloy Q when compared to H282. Atom-probe tomography (APT) revealed that the formation and growth of those phases were responsible for a decrease in Mo content in the matrix, thereby leading to a decrease in solid-solution strengthening in H282 over time. Furthermore, the coarsening of  $\gamma'$  precipitates was retarded by the substitution of W for Mo, particularly under creep stress. The theoretical and experimental understanding of precipitation strengthening unraveled that higher optimal strengthening occurs at larger particle size for alloy Q, compared to the commercial formulation, further explaining the origin of enhanced creep resistance in the modified alloy.

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## 1. Introduction

Nickel-based superalloys have been widely used to manufacture turbine blades and discs for use in both aero- and land-based gas turbines due to their remarkable high-temperature strength, creep

resistance, and oxidation and corrosion resistance.<sup>1</sup> The exceptional mechanical properties of Ni-based superalloys at high temperatures are primarily governed by a microstructure consisting of L1<sub>2</sub>-ordered  $\gamma'$  precipitates coherently embedded in the face-centered cubic (FCC)  $\gamma$  matrix. To further enhance the performance of Ni-based superalloys, many efforts have been made to optimize their chemical compositions and tailor microstructural features such as the  $\gamma'$  precipitate size, volume fraction, and morphology.<sup>2–9</sup> An example can be seen in HAYNES<sup>®</sup> 282<sup>®</sup> alloy (H282), whose chemical composition was designed to achieve a favorable combination of creep strength, thermal stability, fabricability, and weldability.<sup>2,3</sup> In the alloy-design principles of H282, the  $\gamma'$  forming elements (*i.e.*, Ti and Al) are balanced to obtain a relatively low  $\gamma'$  volume fraction ( $\sim 19\%$ ) for improved fabricability. Moreover, an optimal content of Mo ( $\sim 8.5$  wt%) is added to provide significant solid-solution strengthening and retain high creep strength, because of its relatively large atomic size and slow diffusion kinetics in Ni.<sup>3,10,11</sup>

Although H282 exhibits attractive fabricability compared to other superalloys, its creep performance still needs further improvement to meet the increasing global demands for energy efficiency and potential use in next-generation energy systems,

<sup>a</sup> National Energy Technology Laboratory, 1450 Queen Avenue SW, Albany, OR 97321, USA. E-mail: martin.detrois@netl.doe.gov

<sup>b</sup> NETL Support Contractor, 1450 Queen Avenue SW, Albany, OR 97321, USA

<sup>c</sup> Center for Nanophase Materials Sciences, Oak Ridge National Laboratory, 1 Bethel Valley Road, Oak Ridge, TN 37831, USA

<sup>d</sup> Neutron Scattering Division, Oak Ridge National Laboratory, 1 Bethel Valley Road, Oak Ridge, TN 37831, USA

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such as those using hydrogen as fuel. To this end, research efforts have been spurred to further optimize the chemical composition of H282 to enhance its creep strength while still maintaining its exceptional fabricability. In this regard, varying the concentration of  $\gamma'$  forming elements, Al and Ti, has been explored as the ratio between these element is crucial for maintaining a low  $\gamma/\gamma'$  misfit and thus enhancing the stability of  $\gamma'$  at high temperatures.<sup>6,12</sup> According to a previous report, it was observed that a low Ti/Al ratio (1.26) H282 variant coarsens more rapidly than a high Ti/Al ratio (1.748) variant.<sup>6</sup> Another common strategy for improving the creep resistance is to add refractory elements, such as Mo, W, Ta or Re, because these refractory elements can effectively enhance the thermal stability and solid-solution strengthening due to their sluggish diffusivities in Ni and large atomic sizes.<sup>13</sup> For example, Re can significantly enrich the  $\gamma$  phase and thus obviously strengthen it, while also stabilizing the  $\gamma/\gamma'$  interfaces.<sup>8,14,15</sup> Although primarily used for single-crystal superalloys, Wadowski *et al.*<sup>16</sup> studied the effect of Re addition on the atomic interactions in H282 by *ab initio* calculations. They found that the addition of Re to H282 can preserve the character of the atomic interactions in the alloy,<sup>16</sup> however, the effect of Re on creep resistance and thermal stability has not been reported for H282 yet. More importantly, Re is a scarce strategic element, which can lead to high alloy costs despite small additions in Ni-based superalloys.<sup>17</sup> More common solid-solution strengtheners for polycrystalline Ni-based superalloys are Mo and W. Tungsten has the highest melting temperature and is among the slowest diffusers in Ni, which can not only impart significant solid-solution strengthening but also effectively reduce the  $\gamma'$  precipitates' growth and coarsening rate in Ni-based superalloys.<sup>18</sup> To the best of our knowledge, no studies on the effect of W addition on the creep and thermal stability behaviors of H282 alloy have been reported so far.

Therefore, we designed variants of alloy H282 by increasing the content of  $\gamma'$  formers and by substituting W for Mo. The present work provides a systematic study on understanding the role of Ti, Al, and W on the creep resistance and phase stability of H282. Specifically, using targeted Ti addition and W substitution, the creep life of the best performing alloy was increased by 130% compared to the commercial alloy tested at 760 °C and 259 MPa. The underlying creep deformation mechanisms were evaluated by examining the microstructures and dislocation configurations of the designed alloy variants. Moreover, the effect of W on the coarsening kinetics and thermal stability after thermal exposure up to 5000 h was investigated by characterizing the morphological evolution, spatial correlations, and temporal evolution of  $\gamma'$  precipitates. The effects of W addition on the elemental partitioning, solid-solution strengthening, and precipitation strengthening were also analyzed by atom probe tomography (APT) and theoretical calculation. The insights obtained from this thorough study can provide valuable guidance to optimize the alloying design strategies in Ni-based superalloys for achieving enhanced long-term creep resistance.

## 2. Materials and methods

The alloys for this investigation were fabricated using vacuum induction melting (VIM). Three formulations are reported for this investigation, alloys STD (which is a nominal chemistry for H282), P, and Q. High-purity raw materials were used to cast 8 kg cylindrical ingots with a diameter of 75 mm. The phase diagrams of the three alloys were predicted by Thermo-Calc using TCNi8 to determine the liquidus and solidus temperatures. Melting was performed with 50 °C superheat above the Thermo-Calc predicted liquidus temperature and at a partial pressure of 200 Torr Ar. After casting, the top of each ingot was cut into 5 mm thick slices for chemistry analysis. Major elements were determined using X-ray fluorescence (XRF) on a Rigaku ZSX Primus II, while carbon (C) was measured using combustion analysis on LECO systems (Table 1). The ingots were homogenized using a computationally optimized homogenization heat treatment.<sup>19</sup> Subsequently, the homogenized ingots underwent steps of hot forging and hot rolling to form plates with a thickness of approximately 10 mm. The standard aging heat treatment (referred to as SA) of 1010 °C/2 h + 788 °C/2 h as specified for H282 was used to heat treat the plates. It was later found that the first step of the heat treatment was too low for alloy Q as the solvus temperature of the  $\gamma'$  phase increased which resulted in a bimodal precipitate size. Thus, the alternate single-step aging heat treatment (SSA) consisting of 800 °C for 4 h was also investigated for alloy Q. To investigate the phase stability and coarsening behavior, phase stability studies at 800 °C and 900 °C were conducted in air with exposure times of 100 h, 500 h, 1000 h, 2000 h, and 5000 h on the as-solutioned alloys.

The precipitates of the aged samples from at least three different grains were characterized on a JEOL JSM-IT700HR scanning electron microscope (SEM). The SEM specimens were prepared using standard metallographic techniques with a final vibratory polishing using 0.05  $\mu\text{m}$  colloidal silica. Scanning/transmission electron microscopy (S/TEM) observations on  $\gamma'$  precipitates and dislocation configurations were carried out on a JEOL 2100Plus TEM equipped with energy-dispersive X-ray spectroscopy (EDS) detector operated at 200 kV. Discs measuring 3 mm in diameter for TEM characterization were extracted from the thread region and gauge section of tensile samples for as-aged and interrupted crept conditions, respectively. The 3 mm diameter discs were mechanically thinned down to about 50  $\mu\text{m}$ , followed by twin-jet electropolishing on a Struers TenuPol-5 with an electrolyte solution of 20% Perchloric acid and 80% Ethanol maintained at −16 °C and with an applied voltage of 20 V. The size, volume fraction, and spatial

**Table 1** Compositions of the alloys STD, P and Q from XRF (major elements), combustion analysis (C), and measured from addition to the melt (B) in wt%

| Alloy | Ni   | Mn   | Si   | Cr   | Co  | Mo  | W    | Ti  | Al  | C    | B     |
|-------|------|------|------|------|-----|-----|------|-----|-----|------|-------|
| STD   | Bal. | 0.11 | 0.04 | 19.9 | 9.7 | 8.5 | —    | 2.1 | 1.7 | 0.06 | 0.004 |
| P     | Bal. | 0.20 | 0.05 | 19.9 | 9.7 | 8.5 | —    | 2.5 | 2.1 | 0.06 | 0.004 |
| Q     | Bal. | 0.21 | 0.05 | 19.9 | 9.8 | 4.5 | 3.85 | 2.5 | 1.7 | 0.06 | 0.004 |



correlation of  $\gamma'$  precipitates were determined from SEM or TEM images using ImageJ software analysis. The average  $\gamma'$  precipitate size,  $d$ , was defined by an area-equivalent diameter (*i.e.*, diameter =  $2\sqrt{\text{area}/\pi}$ ). The volume fraction of precipitates,  $\phi$ , was determined by  $\phi = A_f$ , where  $A_f$  is the projected areal fraction of precipitates.<sup>20</sup> The number density,  $n_v$ , calculated by  $n_v = n_a/d$ , where  $n_a$  is the areal density of precipitates.<sup>20</sup>

Time-of-flight (TOF) neutron diffraction measurements on the as-aged STD and Q samples were conducted on the VULCAN Engineering Materials Diffractometer at the Spallation Neutron Source (SNS) of the Oak Ridge National Laboratory (ORNL).<sup>21,22</sup> Rietveld refinements on the diffraction profiles were performed to determine lattice parameters of  $\gamma'$  precipitates and  $\gamma$  matrix.

The APT measurements were performed using a CAMECA LEAP 4000XHR local electrode atom probe.<sup>23</sup> Sharp-tip specimens for APT were prepared using a FEI Nova 200 dual beam SEM/focused ion beam (FIB).<sup>24</sup> The APT acquisition was performed in laser mode at 30 K with a pulse frequency of 200 kHz and a 60 pJ laser pulse energy. The APT data was reconstructed and analyzed using CAMECA's IVAS 3.8 software.

Creep testing was performed using constant load creep frames on specimens machined from the plates following aging. The overall length measured 76.2 mm with a gauge section of 31.75 mm and a reduced diameter of 6.25 mm. Testing was performed according to ASTM E-139 Standard.<sup>25</sup> Interrupted creep tests were carried out at 760 °C and 259 MPa, and the samples were cooled under load to preserve the dislocation structures. Vickers hardness was performed at room temperature (RT) on the 800 °C aged samples with different aging times, using a Buehler Micromet II Microhardness Tester. The testing load was 300 gf with a holding time of 10 s. Measurements were repeated eight times at different regions to ensure repeatability.

## 3. Results

### 3.1. Phase diagram prediction

Fig. 1 shows the predicted phase fractions as a function of temperature and the values of liquidus, solvus temperatures and  $\gamma'$  fractions at selected temperatures are listed in Table 2. Alloy P was designed so that the fraction of  $\gamma'$  precipitates at

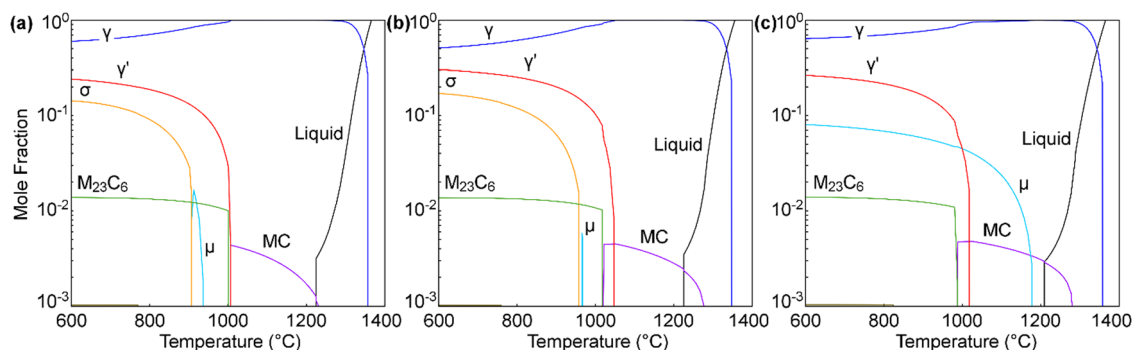
**Table 2** Liquidus temperature,  $\gamma'$  and  $\mu$  solvus temperatures and  $\gamma'$  mole fraction from Thermo-Calc

| Alloy | Liquidus (°C) | $\gamma'$ Solvus (°C) | $\mu$ Solvus (°C) | $\gamma'$ at 800 °C (%) | $\gamma'$ at 900 °C (%) |
|-------|---------------|-----------------------|-------------------|-------------------------|-------------------------|
| STD   | 1366          | 1010                  | 940               | 18.8                    | 13.3                    |
| P     | 1355          | 1051                  | 975               | 25.3                    | 20.0                    |
| Q     | 1365          | 1026                  | 1186              | 21.6                    | 16.2                    |

900 °C in P equals that in alloy STD at 800 °C. The predictions, however, revealed a higher fraction of  $\gamma'$  precipitates in P at 900 °C compared to STD at 800 °C, which was attributed to the fact that the simulations were performed using the measured, and not nominal, alloy compositions. The solvus temperatures for  $\gamma'$  and  $\mu$  phases slightly increased in alloy P, compared to alloy STD. Alloy Q was designed not only to increase the fraction of  $\gamma'$  precipitates but also to improve the phase stability of the alloy. Compared to alloy STD, only the Ti content was increased by 0.4 wt% and 3.85 wt% W was substituted for Mo. This led to a predicted fraction of  $\gamma'$  in Q in between those for STD and P. The similar liquidus temperatures were predicted between STD and Q, while higher solvus temperatures of  $\gamma'$  and  $\mu$  were predicted for alloy Q compared to STD, particularly for  $\mu$  phase (246 °C higher). It is noted that a major difference between the predicted phase diagrams is the absence of  $\sigma$  phase in alloy Q compared to alloys STD and P. The predicted fraction of topologically close-packed (TCP) phases ( $\sigma$ ,  $\mu$ ) was less in alloy Q compared to the other alloys, however, the solvus temperature of the  $\mu$  phase was higher in alloy Q. The predicted compositions of the precipitate phases  $\sigma$ ,  $\mu$ , and  $M_{23}C_6$  are listed in Table 3 for each alloy.

### 3.2. Microstructural phase stability

Fig. 2 presents the SEM microstructures of STD, P, and Q alloys at their triple junctions of GBs after aging at 800 °C and 900 °C for different durations. It can be found that a higher amount of TCP phases – Mo-rich  $\mu$  phase (bright contrast) and occasionally Mo-rich  $\sigma$  phase (also bright contrast) – is precipitated in alloy P compared to STD and Q (EDS analysis for specimens exposed to 800 °C for 5000 h is given in the ESI†). Overall, it can be concluded that phase stability was significantly improved in



**Fig. 1** Thermo-Calc phase prediction for mole fraction between 0.001 and 1 and temperature between 600 °C and 1400 °C for alloys (a) STD, (b) P, and (c) Q.

**Table 3** Phase compositions from Thermo-Calc in wt%

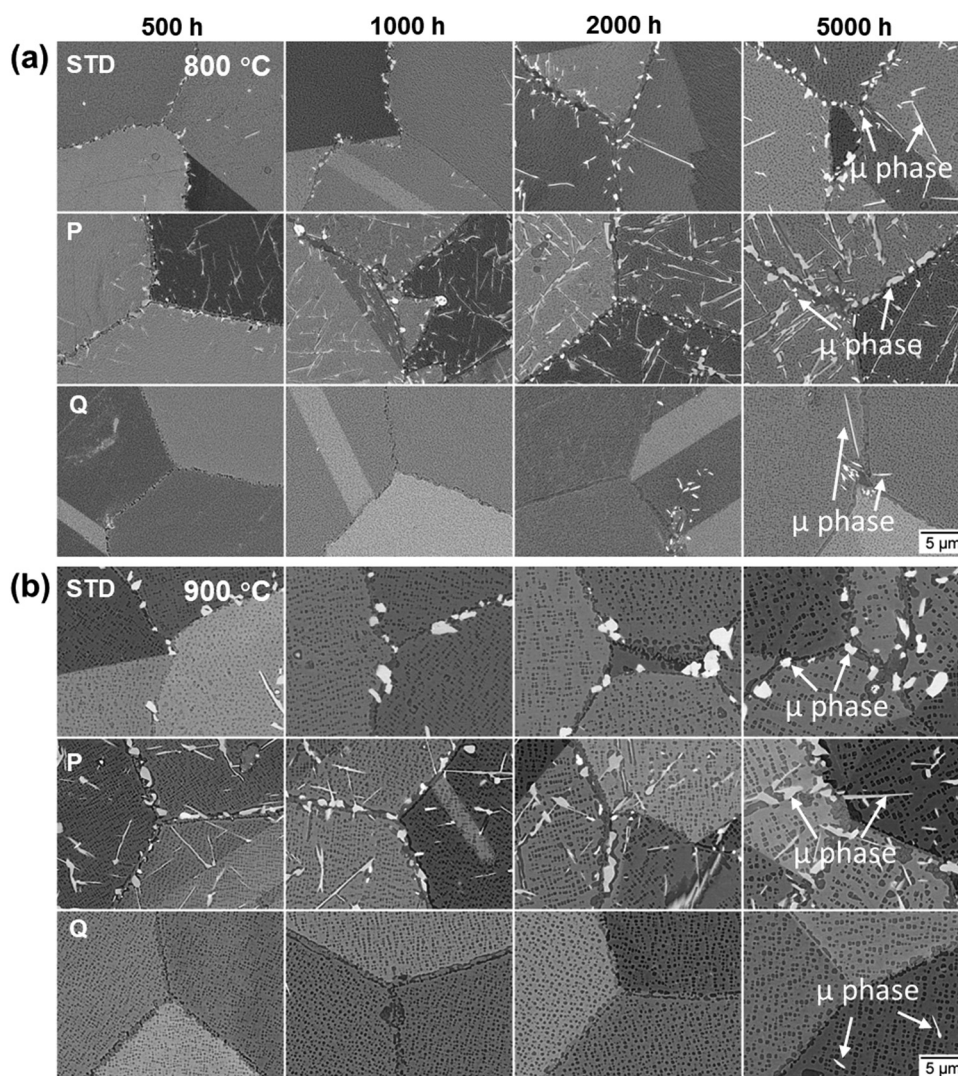
| Alloy | Phase       | Temperature (°C) | Ni  | Cr | Co  | Mo  | W   | C  |
|-------|-------------|------------------|-----|----|-----|-----|-----|----|
| STD   | $\sigma$    | 800              | 28  | 38 | 6.9 | 27  | —   | —  |
|       | $\mu$       | 920              | 22  | 33 | 12  | 33  | —   | —  |
|       | $M_{23}C_6$ | 800              | 2.8 | 66 | 0.7 | 9.5 | —   | 21 |
| P     | $\sigma$    | 800              | 27  | 41 | 8.5 | 24  | —   | —  |
|       | $\mu$       | 960              | 21  | 34 | 12  | 33  | —   | —  |
|       | $M_{23}C_6$ | 800              | 2.5 | 67 | 0.7 | 9.4 | —   | 21 |
| Q     | $\mu$       | 900              | 11  | 35 | 8   | 31  | 14  | —  |
|       | $M_{23}C_6$ | 800              | 2.5 | 69 | 0.5 | 6.9 | 0.4 | 21 |

alloy Q, *i.e.*, reducing the formation of TCP phases, using the addition of W and by lowering the Mo content. The extensive formation of the TCP phase in alloys STD and P after 2000 h exposure at 800 °C is a result of more Mo diffusing from the  $\gamma$  matrix to GBs, which can easily trigger the formation of the TCP phase. In alloy P, the addition of Ti and particularly Al, promoted the formation of  $\gamma'$  precipitates, which resulted in a matrix with lower Ni, or in other words more TCP phase

forming elements, *e.g.*, Cr, Mo, compared to the matrix of alloy STD. TCP phases are detrimental to the thermomechanical properties of Ni-based superalloys and are generally avoided.<sup>26</sup> Due to the poor phase stability results of alloy P, this formulation was not explored further. Furthermore, one can notice that some differences indeed exist between the experimental results and predicted phase diagrams, which could be due to inaccurate predictions from available databases.

### 3.3. Microstructures

Fig. 3(a) and (b) show the representative grain microstructures of alloys STD and Q. Both alloys have equiaxed grains with similar grain sizes of about  $68 \pm 12 \mu\text{m}$  for alloy STD and  $65 \pm 6 \mu\text{m}$  for alloy Q, measured using the linear intercept technique. The neutron diffraction patterns at the high-resolution detector bank for both alloys are given in Fig. 3(c) and (d). According to the indexed Bragg peaks,  $\gamma'$  (L1<sub>2</sub>) and  $\gamma$  (FCC) structures are identified in both alloys, while no other precipitated phases are detected.



**Fig. 2** BSE SEM images of alloys STD, P, and Q at the triple junctions of grain boundaries following exposure at 800 °C and 900 °C for 500, 1000, 2000, and 5000 h, showing more precipitated TCP phase in alloys P and STD than alloy Q.



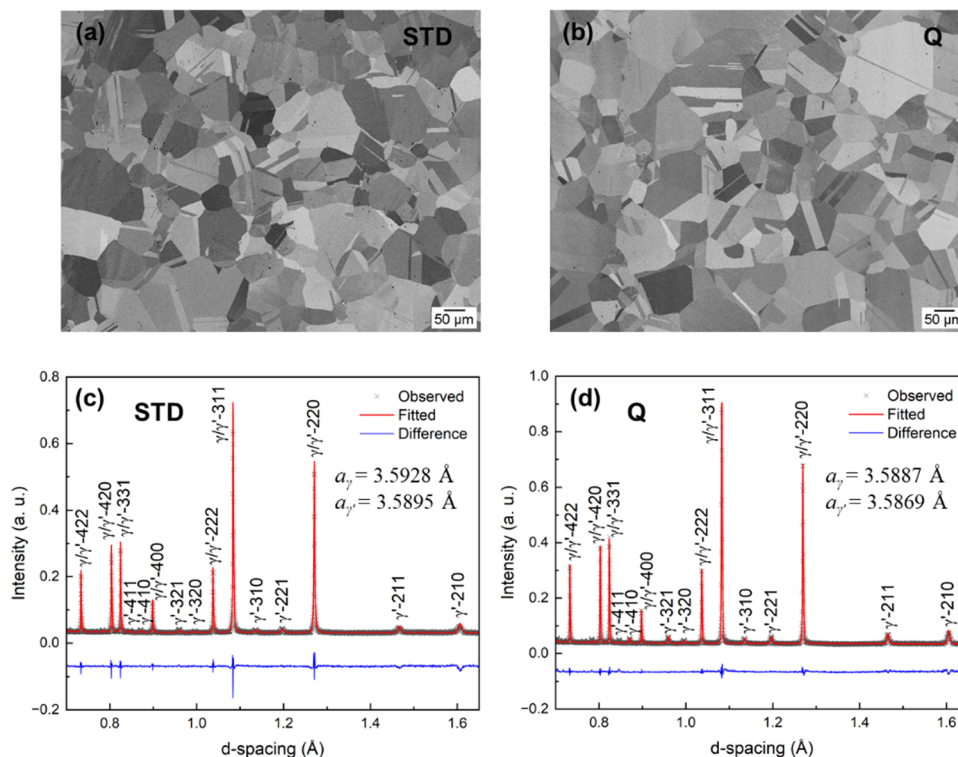


Fig. 3 (a) and (b) Backscattered electron (BSE) SEM images of the as-aged microstructures of alloys STD and Q, respectively. (c) and (d) Neutron diffraction patterns of alloys STD and Q, respectively.

Using Rietveld refinement, the lattice parameters of the  $\gamma'$  and  $\gamma$  phases are determined to be 3.5895 Å and 3.5928 Å, respectively, for alloy STD, and 3.5869 Å and 3.5887 Å, respectively, for alloy Q. As a result, the lattice misfits,  $\delta$ , between the  $\gamma'$  and  $\gamma$  phases are calculated as  $-0.09\%$  for alloy STD and  $-0.05\%$  for alloy Q using the following equation:

$$\delta = \frac{2(a_{\gamma'} - a_{\gamma})}{a_{\gamma'} + a_{\gamma}} \quad (1)$$

where  $a_{\gamma'}$  and  $a_{\gamma}$  are the lattice parameters of  $\gamma'$  and  $\gamma$ , respectively. Note that this corresponds to the constrained lattice misfit, which is affected by both phase chemistry and the elastic strains resulting from the coherency constraint.

To identify  $\gamma'$  precipitates and quantify their size, TEM was performed for both alloys in their as-aged and crept (gauge section) conditions with the SA heat treatment for alloy STD and SSA for alloy Q. Fig. 4(a) and (c) display the representative TEM dark-field (DF) images of the  $\gamma'$  precipitates in both alloys

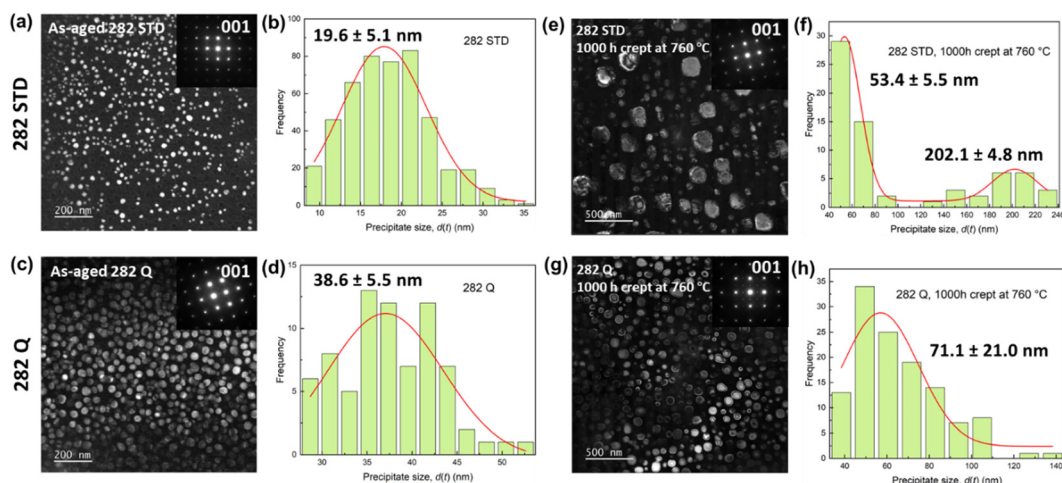


Fig. 4 TEM DF images and  $\gamma'$  precipitate size distributions of the alloys STD (a)–(d) and Q (e)–(h) in their as aged conditions and their 1000 h crept at 259 MPa and 760 °C conditions, respectively.

in their as-aged conditions, exhibiting the spherical shape. From the precipitate size distribution analysis (Fig. 4(b) and (d)), the average particle size for alloy STD ( $\sim 19.6 \pm 5.1$  nm) is about half that of alloy Q ( $\sim 38.6 \pm 5.5$  nm). In addition, the  $\gamma'$  precipitates after 1000 h in creep at 259 MPa and 760 °C were also characterized. As shown in Fig. 4(e)–(h), coarser and unimodal spherical  $\gamma'$  precipitates ( $\sim 70.1 \pm 21.0$  nm) are uniformly dispersed in the  $\gamma$  matrix in alloy Q. In contrast, a bimodal  $\gamma'$  precipitate distribution is observed in alloy STD, comprising fine spherical  $\gamma'$  precipitates of about  $53.4 \pm 5.5$  nm and coarse cuboidal  $\gamma'$  precipitates of about  $202.1 \pm 4.8$  nm, implying lower resistance to coarsening during creep for alloy STD compared to alloy Q. The bimodal  $\gamma'$  size distribution is likely related to the formation of secondary  $\gamma'$  precipitates upon cooling from 760 °C to room temperature at the end of the interrupted creep test.

### 3.4. Coarsening behavior of $\gamma'$ precipitates

**3.4.1. Morphology of  $\gamma'$  precipitates.** To evaluate the thermal stability of  $\gamma'$  precipitates and understand the creep behavior, heat treatments at 800 °C and 900 °C for different times ranging from 100 h to 5000 h were performed for alloys STD and Q. The size, morphology, and distribution of  $\gamma'$  precipitates in both alloys after different exposure times are presented in BSE SEM images (Fig. 5). The temporal evolutions of  $\gamma'$  precipitates in terms of size, number density, and volume fraction are quantified and listed in Table 4. The average size of  $\gamma'$  precipitates increases significantly as the exposure time

increases at both temperatures. At 800 °C, the size of  $\gamma'$  particles is about  $47.8 \pm 4.1$  nm after 100 h in alloy STD, while it increases to an average size of  $144.5 \pm 13.2$  nm after 5000 h (Fig. 5(a)). Similarly, the  $\gamma'$  precipitates in alloy Q have an average size of about  $48.4 \pm 4.5$  nm after 100 h but increases to  $149.3 \pm 13.8$  nm after 5000 h. Likewise, the average particle size increases from  $134.0 \pm 10.7$  nm to  $349.1 \pm 35.4$  nm in alloy STD after exposure to 900 °C from 100 h to 5000 h. In alloy Q, the average particle size is  $126.7 \pm 9.7$  nm after exposure to 900 °C for 100 h, and grows to  $334.7 \pm 33.8$  nm after 5000 h. Compared to the particle sizes in alloy STD, the precipitate sizes in alloy Q are slightly smaller after exposure to 900 °C for different durations.

On the other hand, the number density of precipitates decreases as the exposure time increases, indicating the coarsening stage in both alloys. Specifically, the number density decreases from  $(2.8 \pm 0.2) \times 10^{21} \text{ m}^{-3}$  to  $(8.8 \pm 0.8) \times 10^{19} \text{ m}^{-3}$  and from  $(2.7 \pm 0.2) \times 10^{21} \text{ m}^{-3}$  to  $(9.8 \pm 0.9) \times 10^{19} \text{ m}^{-3}$  for STD and Q alloys, respectively, when the exposure time increases from 100 h to 5000 h at 800 °C. A similar decrease in number density can be also seen in both alloys after exposure to 900 °C with time increasing from 100 h to 5000 h (Table 4). In addition, the  $\gamma'$  precipitates for alloy STD exposed to 800 °C for 100 h and 500 h appear spheroidal and uniformly distributed throughout the  $\gamma$  matrix, while the  $\gamma'$  precipitates become cuboidal after exposure to 800 °C for 1000 h (Fig. 5(a)), indicating the onset of the elastically induced sphere-to-cube morphological transition. After 5000 h exposure to 800 °C, the

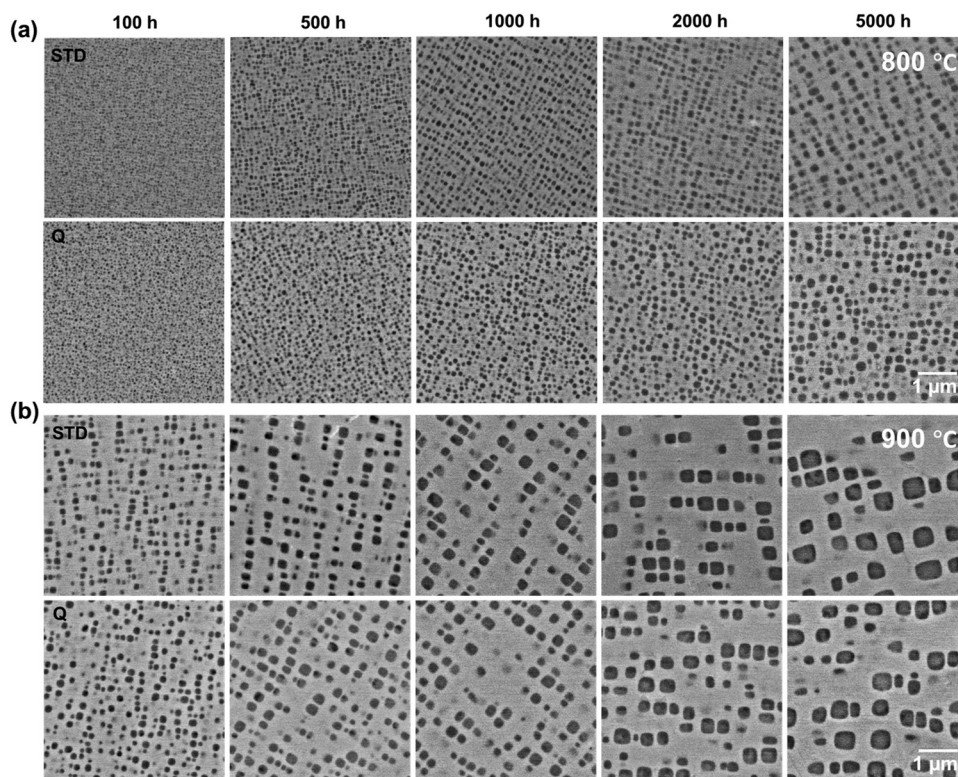


Fig. 5 BSE SEM images of  $\gamma'$  precipitates in both alloys STD and Q after exposure to 800 °C (a) and 900 °C (b) for 100, 500, 1000, 2000, and 5000 h.



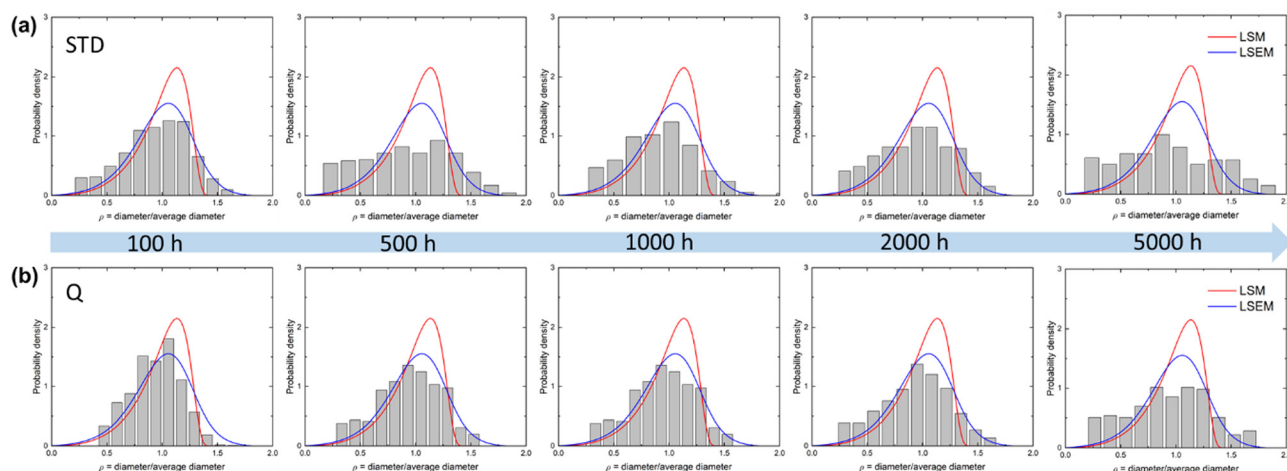
**Table 4** Temporal evolution of nanostructural properties of the  $\gamma'$  precipitates in alloys STD and Q exposed to 800 °C and 900 °C for various durations

| Alloy | Temperature (°C) | Time (h) | $d$ (nm)     | $\phi$ (%) | $N_v \times 10^{20}$ (m <sup>-3</sup> ) |
|-------|------------------|----------|--------------|------------|-----------------------------------------|
| STD   | 800              | 100      | 47.8 ± 4.1   | 23.7 ± 0.1 | 28.7 ± 2.4                              |
|       |                  | 500      | 71.6 ± 6.0   | 23.9 ± 0.3 | 8.3 ± 0.7                               |
|       |                  | 1000     | 94.9 ± 7.0   | 23.2 ± 0.4 | 3.5 ± 0.3                               |
|       |                  | 2000     | 114.5 ± 9.0  | 22.7 ± 0.6 | 1.9 ± 0.2                               |
|       |                  | 5000     | 144.5 ± 13.2 | 23.0 ± 1.2 | 0.9 ± 0.1                               |
|       | 900              | 100      | 134.0 ± 10.7 | 18.6 ± 0.3 | 1.06 ± 0.08                             |
|       |                  | 500      | 193.5 ± 15.4 | 18.6 ± 0.5 | 0.32 ± 0.02                             |
|       |                  | 1000     | 226.8 ± 18.3 | 17.8 ± 0.9 | 0.20 ± 0.02                             |
|       |                  | 2000     | 275.2 ± 21.7 | 18.5 ± 1.3 | 0.11 ± 0.01                             |
|       |                  | 5000     | 349.1 ± 35.4 | 17.1 ± 1.6 | 0.05 ± 0.005                            |
| Q     | 800              | 100      | 48.4 ± 4.5   | 23.6 ± 0.1 | 28.5 ± 2.49                             |
|       |                  | 500      | 73.4 ± 7.1   | 24.5 ± 0.3 | 6.85 ± 0.66                             |
|       |                  | 1000     | 91.0 ± 7.6   | 22.2 ± 0.4 | 3.75 ± 0.31                             |
|       |                  | 2000     | 115.1 ± 10.3 | 24.4 ± 0.7 | 2.05 ± 0.18                             |
|       |                  | 5000     | 149.3 ± 13.8 | 25.6 ± 1.3 | 0.98 ± 0.09                             |
|       | 900              | 100      | 126.7 ± 9.7  | 20.2 ± 0.4 | 1.27 ± 0.13                             |
|       |                  | 500      | 191.2 ± 15.4 | 20.5 ± 0.6 | 0.37 ± 0.03                             |
|       |                  | 1000     | 225.4 ± 18.1 | 21.5 ± 0.9 | 0.24 ± 0.02                             |
|       |                  | 2000     | 264.2 ± 22.8 | 21.0 ± 1.3 | 0.15 ± 0.01                             |
|       |                  | 5000     | 334.7 ± 33.8 | 19.2 ± 1.1 | 0.07 ± 0.006                            |

precipitates in alloy STD start to show a more-faceted cube-like shape. The cuboidal precipitates align along the  $\langle 100 \rangle$  matrix direction, which is the elastically soft crystallographic direction. In contrast, the  $\gamma'$  precipitates in alloy Q remain spheroidal even after being exposed for 2000 h at 800 °C (Fig. 5(a)). Only after 5000 h exposure time the cuboidal morphology of the  $\gamma'$  precipitates began to appear, but many particles still retain their spheroidal shape. The late onset of sphere-to-cube morphological transition in alloy Q compared to alloy STD was also present when exposing the specimens to 900 °C (Fig. 5(b)). For example, the  $\gamma'$  precipitates remain spheroidal in alloy Q after 100 h, while the  $\gamma'$  particles in alloy STD already show clearly faceted cuboids after 100 h. The different responses to sphere-to-cube morphological transition between the alloys suggest the difference in elastic strain energy controlled by lattice misfit in both alloys during coarsening.

**3.4.2. Precipitate size distribution.** Precipitate size distribution (PSD) histograms for STD and Q alloys after exposure to 900 °C for different durations are plotted in Fig. 6. The PSDs were generated by plotting the normalized particle size ( $\rho$  = diameter/average diameter) on the x-axis, and the number of  $\gamma'$  precipitates for a given interval width divided by the total precipitates count and the scaled interval width on the y-axis.<sup>27</sup> From Fig. 6, it can be seen that PSDs become broadened with the reduced peak height as exposure time increases for both alloys. Moreover, the PSDs evolve temporally and are not very self-similar, indicating that steady-state coarsening might have not yet been achieved.<sup>28</sup> The experimentally measured PSDs were further compared with the predictions according to Lifshitz-Slyozov-Wagner (LSW).<sup>29,30</sup> Since the LSW theory assumes that the volume fraction of precipitates tends to zero and the particle-particle interactions are not considered, the Lifshitz-Slyozov Encounter Modified (LSEM) theory that takes account of the encounter of growing particles during coarsening was also superimposed over each histogram.<sup>31</sup> The LSW gives an asymmetric (left-skewed), sharp, and tall PSD, while the LSEM produces a flattened, broader, and more symmetric PSD. From the fitted curves shown in Fig. 6, the experimental PSDs in both alloys fit well to the prediction of LSEM rather than LSW after exposure to 900 °C from 100 h to 2000 h, suggesting that LSEM can be concluded as a far more appropriate description for the precipitate coarsening in both alloys. When the aging time increases to 5000 h, the PSDs in both alloys become more cluttered and make the fitting to LSEM worse, indicating that remarkable coalescence of  $\gamma'$  precipitates occurred at this stage causing the discrepancy,<sup>8,32</sup> as evidenced by SEM results (Fig. 5(b)).

**3.4.3. Temporal evolution of  $\gamma'$  precipitates.** The temporal evolution of average size ( $d(t)$ ), number density ( $n_v(t)$ ), and volume fraction ( $\phi(t)$ ) of  $\gamma'$  precipitates in both alloys exposed to 800 °C and 900 °C is given in Fig. 7. As shown in Fig. 7(a) and (d), the average size,  $d(t)$ , of  $\gamma'$  precipitates increases with exposure time, following a power-law relationship. The temporal power-law



**Fig. 6** The evolution of scaled PSDs for  $\gamma'$  precipitates after exposure to 900 °C for different durations, compared with the prediction of the LSW model (red line) and the LSEM model (precipitate volume fraction = 20%, blue line) (a) alloy STD and (b) alloy Q.



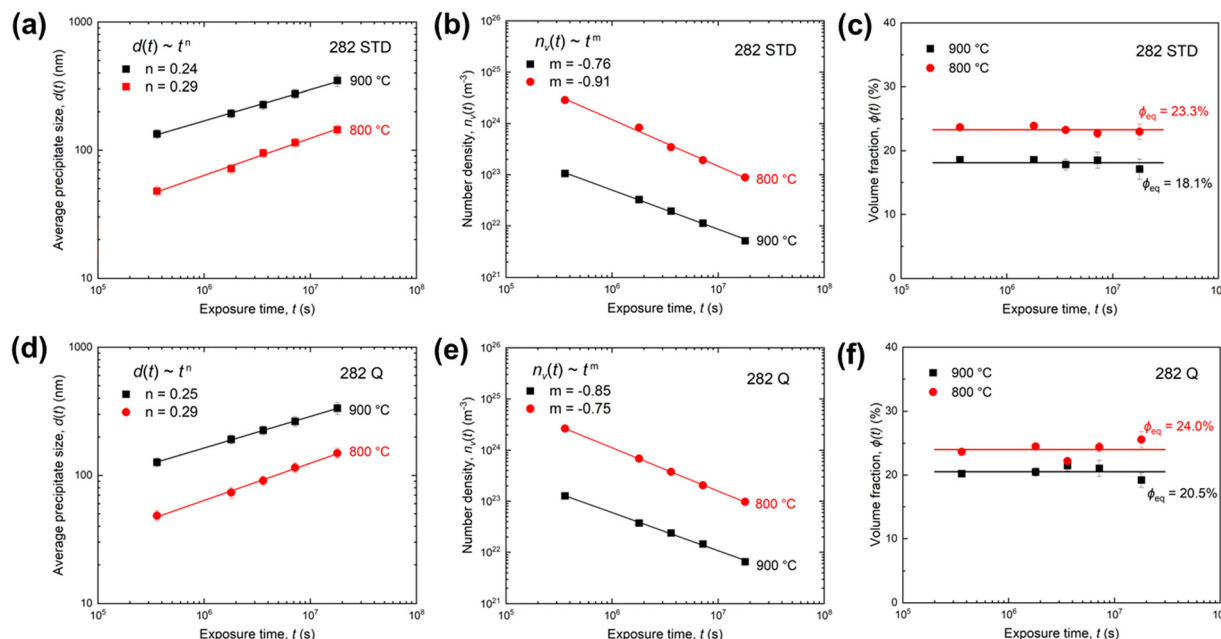


Fig. 7 The temporal evolution of (a) average size ( $d(t)$ ), (b) number density ( $n_v(t)$ ), and (c) volume fraction ( $\phi(t)$ ) of  $\gamma'$  precipitates in alloys STD and Q exposed to 800 °C and 900 °C. Solid lines in the above figures represent the linear fits and average values of the experimental data, respectively.

exponents are determined to be 0.29 for STD and Q alloys at 800 °C, and 0.24 and 0.25 for STD and Q alloys at 900 °C, respectively. The power-law exponents for both alloys roughly align with the predicted of 1/3 for a coarsening mechanism in accordance with the LSW model,<sup>29,30</sup> although it is not an exact match.

Fig. 7(b) and (e) plot the power-law relationship of precipitate number density,  $n_v(t)$ , as a function of the exposure time in STD and Q alloys at 800 °C and 900 °C. The precipitate number density,  $n_v(t)$ , decreases with exposure time, indicating that the alloys are well into the coarsening stage. The power-law exponents for  $n_v(t)$  are determined to be -0.76 and -0.91 for alloy STD at 800 °C and 900 °C, respectively, and -0.85 and -0.75 for alloy Q at 800 °C and 900 °C, respectively. Similar temporal exponents for the number density have also been observed in other Ni-based superalloys.<sup>33</sup>

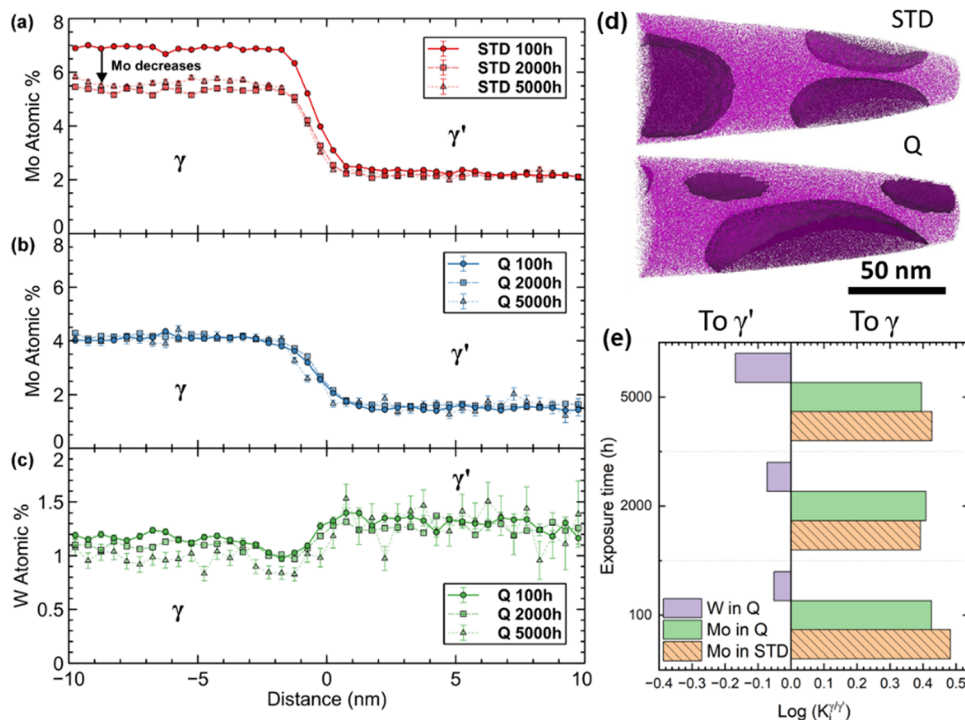
Fig. 7(c) and (f) display the evolution of volume fraction,  $\phi(t)$ , of  $\gamma'$  precipitates as a function of exposure time. The values of  $\phi(t)$  in both alloys are nearly constant with respect to exposure time from 100 h to 5000 h at each temperature, indicating that the alloys appear to be at their equilibrium value ( $\phi_{eq}$ ). Moreover, as the aging temperature increases from 800 °C to 900 °C, the equilibrium volume fractions ( $\phi_{eq}$ ) decrease from 23.3% to 18.1% and 24.0% to 20.5% for STD and Q alloys, respectively. The reached  $\phi_{eq}$  also implies that the alloys are within the coarsening regime.

**3.4.4 Elemental partitioning across  $\gamma/\gamma'$  interface.** APT measurements were performed on selected conditions of both alloys to investigate the elemental partitioning between the  $\gamma$  and  $\gamma'$  phases over time. Fig. 8 displays the concentration profiles of Mo and W in the STD and Q alloys across the  $\gamma/\gamma'$  interface following exposure to 800 °C for 100 h, 2000 h, and

5000 h. It can be readily seen that Mo is partitioned to the  $\gamma'$  matrix and is depleted in the  $\gamma'$  precipitates. It is worth noting that the Mo content in the  $\gamma$  matrix decreases as the exposure time increases in alloy STD, while it retains a constant level in the  $\gamma'$  precipitates. This partitioning behavior of Mo across the  $\gamma/\gamma'$  interface suggests that Mo diffuses elsewhere over time, *i.e.*, diffuses to the TCP phases. Nevertheless, no noticeable changes in the Mo contents of the  $\gamma$  matrix and  $\gamma'$  precipitates are observed in alloy Q after different thermal exposures. In the case of W in the Q alloy, it preferentially partitions towards the  $\gamma'$  precipitates, and becomes lean in the  $\gamma$  matrix. Such a W partitioning trend becomes relatively clearer as aging time increases; however, this evolution is minimal compared to the variations in Mo content observed in alloy STD. To better describe the partitioning behavior across the  $\gamma/\gamma'$  interface, the partitioning coefficient,  $K_i^{\gamma/\gamma'}$ , is plotted in Fig. 8(e), which is defined as  $K_i^{\gamma/\gamma'} = C_i^{\gamma}/C_i^{\gamma'}$ , where  $C_i^{\gamma}$  and  $C_i^{\gamma'}$  represent the atomic concentrations of element  $i$  in the  $\gamma$  and  $\gamma'$  phases, respectively. In Fig. 8(e), the columns on the left (right) mean that the element partitions to  $\gamma'$  ( $\gamma$ ) phase. Similarly, it can be clearly seen that W partitions to  $\gamma'$  precipitates in alloy Q, while Mo is enriched in the  $\gamma$  matrix.

**3.4.5. Effect of  $\gamma'$  precipitates coarsening on hardness evolution.** The effect of coarsening of  $\gamma'$  precipitates on hardness evolution was also investigated. Fig. 9 plots the relationship of the measured hardness *versus* exposure time for alloys STD and Q exposed to 800 °C. It is evident that alloy Q with alloying W exhibits higher hardness values than those in alloy STD across the entire exposure time range. A hardness peak is observed in each alloy but occurs at different times, *i.e.*, 100 h in alloy STD and 1000 h in alloy Q. The much longer exposure





**Fig. 8** (a)–(c) Proximity histograms of Mo and W in the alloys STD (Mo only) and Q across the  $\gamma/\gamma'$  interface defined by 5 at. % Ti isoconcentration surfaces after exposure to 800 °C for 100 h, 2000 h, and 5000 h. (d) APT atom maps with Cr (light purple) and Ti (dark purple) atoms and 5 at% Ti isoconcentration surfaces for the alloys STD and Q exposed to 800 °C for 100 h. (e) W and Mo partitioning coefficients  $\log(K_i^{\gamma/\gamma'})$  between the  $\gamma$  and  $\gamma'$  phases in alloys STD and Q after exposure to 800 °C for 100 h, 2000 h, and 5000 h.

time required to reach peak hardness in alloy Q compared to STD indicates that the optimal size of  $\gamma'$  precipitates requires longer exposure time to achieve than that of alloy STD.

### 3.5. Creep properties

To examine the alloying effect on the designed H282 variant alloy Q, creep-rupture testing was performed in its standard and single-step aging conditions (SA and SSA, respectively). Fig. 10(a) exhibits the creep lives of STD and Q alloys in a

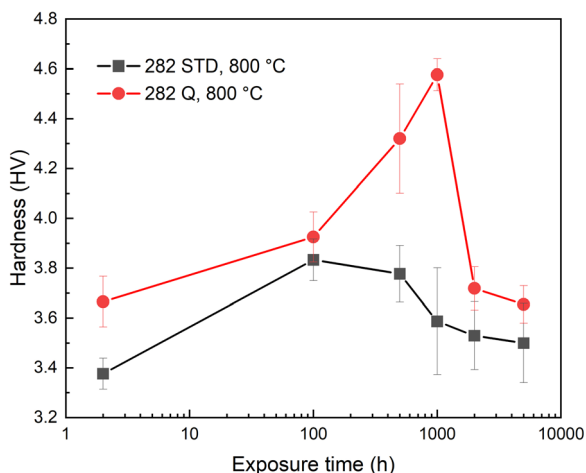
Larson–Miller plot, which is defined by eqn (2), in comparison to that of the ORNL H282 code case,<sup>34</sup>

$$\text{LMP} = T[20 + \log(t) \times 10^3] \quad (2)$$

where  $T$  is the absolute temperature in Kelvin and  $t$  is the creep time to rupture in hours. From Fig. 10(a), the LMP values of alloy STD and ORNL H282 code case are located at the bottom-left side of the Larson–Miller data points of alloy Q, indicating a superior creep performance of alloy Q compared to others. Intuitively, the outperforming creep life of Q alloy can be seen in the plots of creep strains as a function of time collected at 259 MPa and 760 °C and at 124 MPa and 900 °C in Fig. 10(b) and (c). In terms of 1% and rupture creep strains, alloy Q was found to have a significantly longer creep life than that of alloy STD at both temperatures. Alloy Q exhibits approximately 60% longer life to achieve 1% creep strain and 130% longer life to rupture with no loss of creep ductility at 760 °C, compared to alloy STD. Similarly, 150% and 83% increases in creep life of alloy Q are achieved for 1% and rupture creep strains at 900 °C, respectively, as compared to alloy STD.

### 3.6. Creep deformation microstructures

To understand the creep deformation mechanisms, TEM micrographs of dislocation configurations were imaged under two-beam conditions in both alloys after creep interrupted at 1000 h and ruptured at 760 °C and 259 MPa with a creep strain of  $\sim 0.23\%$ . Fig. 11 presents the bright-field (BF) TEM images of the dislocation configurations at the locations of grain interior



**Fig. 9** The measured hardness of alloys STD and Q as a function of aging time at 800 °C.

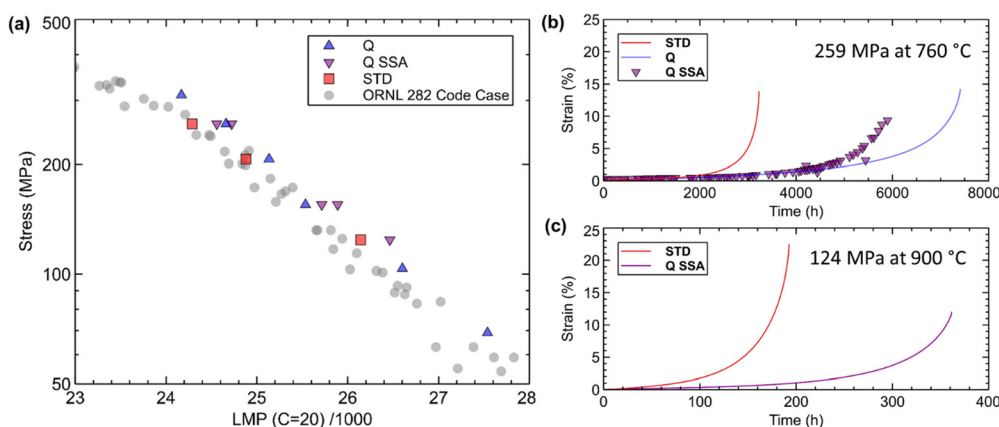


Fig. 10 (a) Larson–Miller parameter plot for alloys STD, Q and the H282 code case.<sup>32</sup> (b) and (c) Creep curves for creep testing at 760 °C and 259 MPa and 900 °C and 124 MPa, respectively.

and boundary in both alloys. In alloy STD, dislocation loops, marked by red arrows, were mainly observed within the grain interior and near the grain boundary (GB) after creep tests for 1000 h at 760 °C and 259 MPa (Fig. 11(a) and (b)). Orowan loops surrounding the  $\gamma'$  precipitates are generated when the gliding dislocations in the  $\gamma$  matrix cannot shear into the  $\gamma'$  precipitates but rather loop around them *via* the Orowan bypass process. Another feature of the dislocation sub-structure in STD alloy is the dislocation pile-ups lying on the  $\gamma/\gamma'$  interface, indicated by the green arrows (Fig. 11(a)). The formation of dislocation pile-ups is a result of the reaction of activated dislocations when they glide into the  $\gamma/\gamma'$  interface, which can serve to neutralize the misfit stress at the  $\gamma/\gamma'$  interface and also promote dislocation climb during creep.<sup>35,36</sup> In addition, dislocation pile-ups at GB and interacting dislocations with  $M_{23}C_6$  carbides were also observed in alloy STD (Fig. 11(b)). Interestingly, very few bowed dislocations surrounding the  $\gamma'$  precipitates in alloy Q were seen after creep, indicating a much stronger resistance to dislocation slip in the matrix of alloy Q than that in STD (Fig. 11(c)). Similarly, less dense dislocation pile-ups at GB were observed in alloy Q than in alloy STD (Fig. 11(d)), further correlating to the better creep resistance in alloy Q.

Fig. 12 displays the dislocation configurations after creep rupture at 760 °C and 259 MPa in alloys STD (creep time 3240 h) and Q (creep time 7410 h). Extensive Orowan loops and dislocation climbing evident by dislocations with bent morphology can be observed in the creep-ruptured samples of both alloys. Compared to STD and Q specimens subjected to interrupted creep tests, the pronounced appearance of dislocation climb in the ruptured specimens is attributed to the longer creep time, allowing enough time for dislocations to climb over the  $\gamma'$  precipitates. Moreover, in line with the TEM observation from the interrupted creep samples (Fig. 11), a distinct feature of dislocation tangles around the  $\gamma'$  precipitates was present in alloy STD, while it was barely seen in alloy Q. The more extensive dislocation tangling, *i.e.*, pile-ups, in alloy STD than that in alloy Q is likely resulting from the greater coarsening of the  $\gamma'$  precipitates in alloy STD during creep (Fig. 2(e) and (f)), creating more intense interactions between dislocations and  $\gamma'$

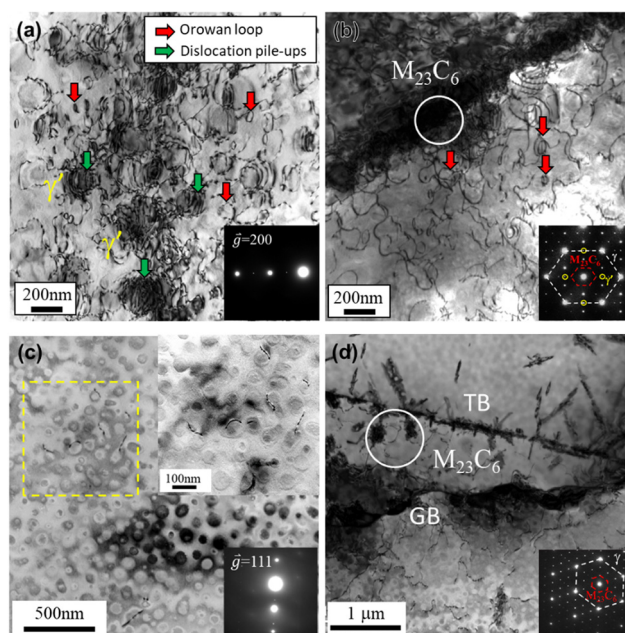


Fig. 11 TEM micrographs taken from the crept samples interrupted at 1000 h at 760 °C and 259 MPa under two-beam BF conditions. (a) and (b) alloy STD (creep strain  $\sim 0.23\%$ ). (c) and (d) alloy Q (creep strain  $\sim 0.23\%$ ). Insets at the right bottom in (a) and (c) are the corresponding two-beam conditions. Inset at the right top in (c) is the enlarged area of the marked yellow dashed box. Insets in (b) and (d) are the corresponding selected-area diffraction patterns (SAEDs) of  $M_{23}C_6$  carbides marked by white circles.

precipitates, as well as the larger  $\gamma/\gamma'$  misfit magnitude in alloy STD.

## 4. Discussion

### 4.1. Morphological evolution

The morphological evolution of  $\gamma'$  precipitates is critical to the mechanical performance of Ni-based superalloys during high-

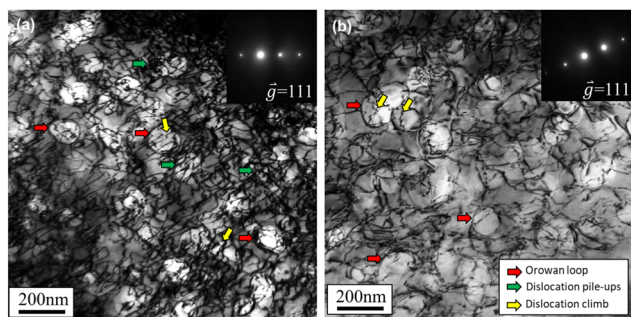


Fig. 12 BF TEM images under two-beam conditions of STD (a) and Q (b) alloys after creep rupture at 760 °C and 259 MPa (creep times of 3240 h and 7410 h for STD and Q, respectively), showing the dislocation configurations of Orowan loops (red arrows), dislocation pile-ups (green arrows), and climb (yellow arrows).

temperature service. The equilibrium morphology of  $\gamma'$  precipitates is determined by the minimization of the interfacial free energy and elastic free energy arising from lattice misfit.<sup>37,38</sup> Such a total free-energy minimization criterion gives a critical particle size,  $r_{\text{crit}}$ .<sup>38,39</sup> When the precipitate size is smaller than  $r_{\text{crit}}$ , the morphology of  $\gamma'$  precipitates is primarily dictated by the interfacial free energy, because the elastic strain energy caused by the lattice misfit between  $\gamma$  and  $\gamma'$  phases is negligible or lower. As the  $\gamma'$  precipitates grow larger than  $r_{\text{crit}}$ , elastic strain energy becomes more influential in determining the equilibrium shape of precipitates. The competition between the elastic energy and  $\gamma/\gamma'$  interfacial energy can be quantified by a dimensionless parameter,  $L$ :<sup>40</sup>

$$L = \frac{\varepsilon^2 C_{44} r}{\sigma} \quad (3)$$

where  $\varepsilon$  is the lattice parameter misfit strain, defined as  $\varepsilon = (a'_\gamma - a_\gamma)/a_\gamma$ , where  $a'_\gamma$  and  $a_\gamma$  are the lattice parameters of the  $\gamma'$  precipitate and  $\gamma$  matrix, respectively,  $C_{44}$  is an elastic constant for the  $\gamma$  matrix,  $r$  is the average precipitate radius, and  $\sigma$  is the interfacial energy between  $\gamma$  and  $\gamma'$  phases. For a precipitate with a purely dilatational misfit in Ni-based superalloy systems, as the precipitate size increases, the equilibrium shape of precipitates undergoes a gradual transition from a sphere ( $L = 0$ ) to a four-fold symmetric cuboid ( $L = 2-4$ ), and further, at a critical value of  $L$  ( $> 5.6$ ) bifurcates to a two-fold symmetric shape, like a platelet.<sup>40-43</sup>

For the studied alloys STD and Q,  $\varepsilon = -0.09\%$  and  $-0.05\%$  at RT in their as-aged conditions, average precipitate radii of 19.6 nm and 38.6 nm for alloys STD and Q, respectively,  $C_{44} = 100.5 \text{ GPa}$ <sup>44</sup> and  $\sigma = 0.02 \text{ J m}^{-2}$ <sup>45</sup> (assuming they are the same for both alloys) are used to calculate the value of  $L$ . Therefore,  $L$  values of 0.08 and 0.05 are yielded for alloys STD and Q, respectively. Such small  $L$  values (close to 0) of alloys STD and Q in their as-aged conditions correspond to the spherical shape of  $\gamma'$  precipitates, as shown in Fig. 2(a) and (c). After exposure to 800 °C for 5000 h,  $\varepsilon = -0.16\%$  and  $-0.11\%$  for alloys STD and Q, respectively, which were calculated based on APT phase chemistries in  $\gamma$  and  $\gamma'$  phases along with Vegard's

relation, and details can be seen in ref. 46, 47 After inserting average precipitate sizes of 144.5 nm (STD) and 149.3 nm (Q) into eqn (3),  $L$  values of 1.86 and 0.91 were obtained for alloys STD and Q, respectively, after exposure to 800 °C for 5000 h. For alloy STD, the calculated value of  $L$  to be 1.86 is in close agreement with the prediction of model for the four-fold symmetric cuboid, consistent with the experimental observation of cuboidal precipitates (Fig. 5(a)). For alloy Q, the yielded  $L$  value to be 0.91 also aligns with the observed spheroidal shape and the late onset of sphere-to-cube morphological transition (Fig. 5(b)), suggesting that interfacial energy is still dominated in favoring a four-fold symmetry. It should be noted that for alloys with negative lattice misfit at RT, it is expected that the magnitude of the misfit will increase (becoming more negative) at higher temperatures.<sup>48</sup> The different  $L$  values of alloys STD and Q after being exposed to 800 °C for 5000 hours suggest that the distinct morphology evolutions of  $\gamma'$  precipitates in these alloys primarily stem from differences in their lattice misfits. This discrepancy in lattice misfits is attributed to a notable compositional change in Mo in the matrix of alloy STD (approximately 1.5 at%), whereas there is minimal change in the composition of W and Mo in the matrix of alloy Q (Fig. 8). Therefore, it can be inferred that the partial substitution of W for Mo content can significantly improve the morphological resistance of  $\gamma'$  precipitates to thermal exposure in H282.

## 4.2. Coarsening kinetics

The coarsening kinetics and associated mechanisms of  $\gamma'$  precipitates in Ni-based superalloys have been extensively studied.<sup>49-51</sup> A classic theory to describe coarsening kinetics of  $\gamma'$  precipitates is the LSW model, following the Ostwald ripening process, which can be expressed by the following power-law equation:

$$d^3(t) - d^3(t_0) = K(t - t_0) \quad (4)$$

where  $K$  is the coarsening rate constant,  $d(t)$  is the average precipitate size at the thermal exposure time  $t$ ,  $d(t_0)$  is the average size of  $\gamma'$  precipitates at time  $t_0$ ,  $t_0$  is the time for the onset of quasi-stationary coarsening.

Fig. 13 plots the average precipitate size, ( $d^3(t)$ ), as a function of exposure time at 800 °C and 900 °C. Accordingly, the coarsening rates are determined from the slope values by linearly fitting to the experimental data using eqn (4). The measured data appear to be well fitted with the LSW model, giving the coarsening rate constants,  $K = 1.92 \times 10^{-28} \text{ m}^3 \text{ s}^{-1}$  and  $K = 2.67 \times 10^{-27} \text{ m}^3 \text{ s}^{-1}$  for alloy STD at 800 °C and 900 °C, respectively, and  $K = 1.94 \times 10^{-28} \text{ m}^3 \text{ s}^{-1}$  and  $K = 2.40 \times 10^{-27} \text{ m}^3 \text{ s}^{-1}$  for alloy Q at 800 °C and 900 °C, respectively. It is evident that the coarsening rate increases with exposure temperature for each alloy. At 800 °C, the coarsening rates are almost the same for both alloys. However, at 900 °C, the coarsening rate accelerates more rapidly in the STD alloy compared to alloy Q, suggesting the effective role of W addition in retarding the coarsening of  $\gamma'$  precipitates at higher temperatures. It should be emphasized that the effectiveness of W addition in slowing down the coarsening of  $\gamma'$  precipitates



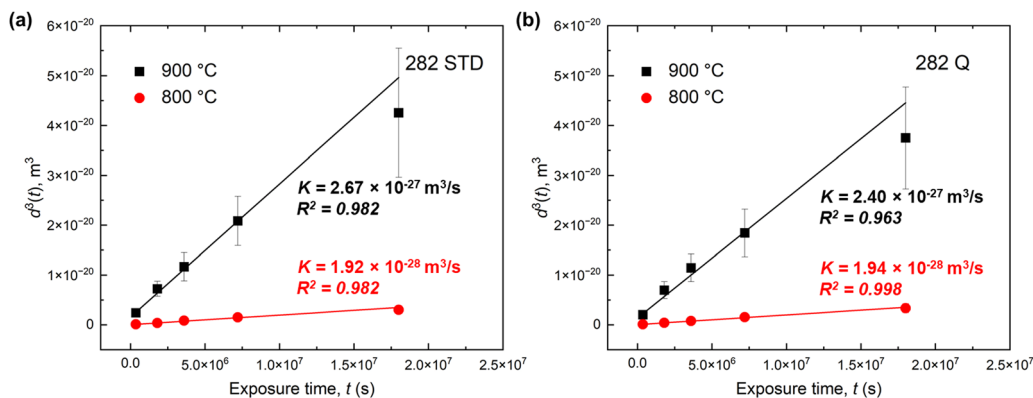


Fig. 13 Plots of average precipitate size,  $\overline{d^3(t)}$ , versus exposure time ( $t$ ) for alloy STD (a) and alloy Q (b) for temperatures of 800 °C and 900 °C. The coarsening rate constants are determined from the best linear fit of the experimental data.

becomes more significant under creep stress, which has been demonstrated by the much smaller  $\gamma'$  precipitate size in alloy Q than that in STD after 1000 h in creep at 259 MPa and 760 °C (Fig. 2).

In the diffusion-controlled coarsening mechanism, the diffusion species with the lowest mobility, in principle, govern the coarsening kinetics. Philippe and Voorhees (PV) extended the LSW model from the dilute binary systems to the multicomponent systems.<sup>52</sup> Accordingly, the PV model describes the coarsening rate constant of  $\gamma'$  precipitates as follows:<sup>52</sup>

$$K \approx \frac{8V_m\sigma Dc_i^M}{9RT(c_i^P - c_i^M)^2} \quad (5)$$

where  $V_m$  is the molar volume of the precipitate,  $\sigma$  is the interfacial energy between  $\gamma$  matrix and  $\gamma'$  precipitate,  $c_i^P$  and  $c_i^M$  are the equilibrium composition (in mole fraction) of the element  $i$  in the precipitates and matrix, respectively,  $R$  is the gas constant, and  $T$  is the absolute temperature.  $D$  is the diffusion coefficient of the slow element  $i$  in the matrix, which can be expressed by the Arrhenius equation,  $D = D_0 \exp\left(-\frac{Q}{RT}\right)$ , in which  $D_0$  is the pre-exponential factor and  $Q$  is the activation energy for diffusion of element  $i$  in the matrix. Inserting the Arrhenius equation into eqn (5), the activation energy for diffusion can be obtained from the fitted slope of  $\ln(KT)$  versus  $1/T$ , assuming that  $V_m$  and equilibrium composition in  $\gamma$  and  $\gamma'$  phases are temperature independent. Therefore, the element with the largest activation energy for diffusion is conducive to retard the coarsening process. In alloy STD, the controlling diffusing species should be Mo, considering its large diffusion activation energy ( $301.68 \text{ kJ mol}^{-1}$ ).<sup>53</sup> However, in alloy Q, W with the highest activation energy for diffusion ( $302.51 \text{ kJ mol}^{-1}$ ) can be the controlling diffusing element,<sup>53</sup> resulting in the enhanced coarsening resistance of  $\gamma'$  precipitate.

### 4.3. Strengthening mechanisms

In  $\gamma'$  precipitate strengthened Ni-based superalloys, the major strengthening mechanisms are solid-solution strengthening and precipitation strengthening.<sup>1,54</sup> Solid-solution strengthening during exposure to service temperatures is mainly impacted

by the alloying solutes in the  $\gamma$  matrix. The influence of alloying elements on the degree of solid-solution strengthening in the  $\gamma$  matrix ( $\Delta\sigma_\gamma$ ) and  $\gamma'$  precipitates ( $\Delta\sigma_{\gamma'}$ ) can be expressed by the following equations:<sup>55,56</sup>

$$\Delta\sigma_\gamma = \left( \sum_i k_i^2 c_i^\gamma \right)^{1/2} \quad (6)$$

$$\Delta\sigma_{\gamma'} = \sum_i (d\sigma/dc)_i c_i^{\gamma'} \quad (7)$$

where  $k_i$  and  $d\sigma/dc$  are the strengthening constant of alloying elements in  $\gamma$  and  $\gamma'$  phases, respectively.  $c_i^\gamma$  and  $c_i^{\gamma'}$  are the concentrations of element  $i$  in  $\gamma$  and  $\gamma'$  phases, respectively. In alloy Q, the only noticeable change of alloying elements was observed for W in the  $\gamma$  phase from the APT results ( $\sim 0.25$  at% decrease) after exposure to 800 °C for 5000 h. After employing the W strengthening constant of 977 MPa per atomic fraction<sup>1/2, 55,56</sup>, the decrease in solid-solution strengthening is only about 49 MPa in alloy Q even following 5000 h exposure at 800 °C. Moreover, unlike in alloy STD in which Mo becomes part of TCP phase formation, a small amount of W in Q segregates to the  $\gamma'$  phase from the  $\gamma$  matrix, as seen from the APT results shown in Fig. 8(e). This partitioning behavior can lead to an a slight increase in solid-solution strengthening within the  $\gamma'$  phase, as the strengthening constants for W in  $\text{Ni}_3\text{Al}$  are 25 MPa per at% compared to Mo's 16.8 MPa per at%.<sup>57</sup> In alloy STD, the major variation of alloying element is the decrease of Mo in the  $\gamma$  matrix (up to 1.5 at% decrease) after exposure for 100 h to 5000 h. Such a significant decrease in Mo content in the  $\gamma$  matrix can lead to a matrix strength decrease of  $\sim 124$  MPa, after considering Mo's strengthening constant of  $\sim 1015$  MPa per atomic fraction<sup>1/2, 55,56</sup>. This loss of solid-solution strengthening is directly related to the poor phase stability of alloy STD. As the TCP phases form over time, they deplete Mo from the  $\gamma$  matrix. As evident in the Fig. 11(a), the dislocations in the crept alloy STD interrupted at 1000 h at 760 °C undergo a sharp prefoliation in multiple slip planes due to the reduction of solid-solution strengthening, which facilitates easier dislocation glide in the matrix, and interact with each other into local dislocation pileups at  $\gamma/\gamma'$  interface, leading to the formation



of dislocation tangles surrounding the  $\gamma'$ . On the other hand, the superior phase stability in alloy Q preserves the refractory elements in solution and prevents a significant decrease in solid-solution strengthening over time. As such, dislocations with very low density induce less complex dislocation reactions and postpone the onset of “tertiary creep” stage (Fig. 11(c)).

In addition to solid-solution strengthening, precipitation strengthening is the primary strengthening mechanism in Ni-based superalloys, which can be divided into two categories, particle shearing or Orowan dislocation bypass mechanism.<sup>54</sup>

In Ni-based superalloys, the precipitate shearing mechanism, is controlled by anti-phase-boundary-coupled dislocation pairs, *i.e.*, pairwise cutting mechanism.<sup>1,58,59</sup> For small particles, dislocation pairs cutting through particles are usually weakly coupled, resulting in the ordering strength increment ( $\Delta\sigma_{OS}$ ) by the following equation:<sup>1,60</sup>

$$\Delta\sigma_{OS} = M \cdot \frac{\gamma_{apb}}{2b} \left[ \left( \frac{2\gamma_{apb}df}{\pi T} \right)^{1/2} - f \right] \quad (8)$$

where  $\gamma_{apb}$  is the antiphase boundary energy of the precipitates ( $\gamma_{apb} = 0.18 - 0.22 \text{ J m}^{-2}$ ).<sup>61,62</sup>  $T$  is the dislocation line tension, defined by  $T = Gb^2/2$ .<sup>63</sup> For large particles, dislocations cut through precipitates by forming strongly coupled pairs, which gives the strength increment as follows:<sup>1,64</sup>

$$\Delta\sigma_{OS} = M \cdot \sqrt{\frac{3}{2}} \left( \frac{Gb}{d} \right) f^{1/2} \frac{w}{\pi^{3/2}} \left( \frac{\pi d \gamma_{apb}}{wGb^2} - 1 \right)^{1/2} \quad (9)$$

where  $w$  represents a constant describing the elastic repulsion between the strongly coupled dislocation pairs, and it is approximately equal to 1.

When the precipitates are sufficiently large or incoherent within the matrix, the Orowan dislocation bypass mechanism governs the strength increment, which can be calculated by the following equation:<sup>60</sup>

$$\Delta\sigma_{Orowan} = M \cdot \frac{0.4Gb \ln(\bar{d}/b)}{\pi\sqrt{1-\nu} \lambda} \quad (10)$$

where  $G = 82 \text{ GPa}$  is the shear modulus of the matrix,<sup>65</sup>  $b$  is the magnitude of Burgers vector,  $\nu = 0.319$  is the Poisson's ratio,<sup>65</sup>  $\bar{d} = \sqrt{2/3} \cdot d$  is the average precipitate diameter on the slip planes,<sup>66</sup> and  $\lambda = \bar{d}(\sqrt{\pi/4\phi} - 1)$  is the average edge-to-edge interparticle spacing.<sup>67</sup>

The calculated strengthening contributions from the pairwise cutting mechanism or the Orowan bowing mechanism (involving the loss of solid-solution strengthening effect) are compared with the measured hardness increments ( $\Delta H$ ) via the conversion by  $\Delta H = \alpha\Delta\sigma$  ( $\alpha = 3$  is the Tabor factor). Fig. 14 plots the measured and calculated hardness increments resulting from precipitation strengthening as a function of the average precipitate size ( $d$ ) in alloys STD and Q during exposure to 800 °C. With a precipitate size of  $\sim 50 \text{ nm}$  (exposure duration of 100 hours), the hardness increment for alloy Q with alloying W is slightly higher than that in alloy STD. As the high-temperature exposure progresses, the hardness increment for alloy STD becomes less pronounced, while alloy Q, with W

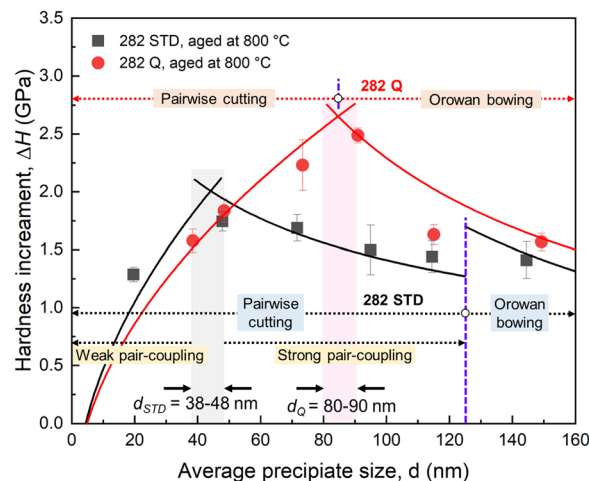


Fig. 14 Relationship between hardness increment ( $\Delta H$ ) as a function of average precipitate size ( $d$ ) for alloys STD and Q exposed to 800 °C for various durations. Experimental data points are derived from hardness measurements, while the solid lines represent the theoretical calculations.

substitution, maintains a robust hardness increment. As a result, an optimal hardness increment can be achieved when alloy is exposed up to 1000 hours with a precipitate size of 80–90 nm, twice that in alloy STD (38–48 nm). According to the calculated hardness increments, the pairwise cutting mechanism by forming weakly and strongly coupling pairs can be the dominant strengthening mechanism in alloy STD when the particle size is smaller than  $\sim 125 \text{ nm}$ . When the precipitate size is larger than  $\sim 125 \text{ nm}$ , Orowan bowing becomes the controlled strengthening mechanism. In alloy Q, the pairwise cutting mechanism at a small particle size ( $< \sim 85 \text{ nm}$ ) and the Orowan bowing mechanism at a large particle size ( $> \sim 85 \text{ nm}$ ) are the governing mechanisms. Based on these, the lower hardness increment in alloy STD can be attributed to the less pronounced precipitation strengthening effect and the loss of solid-solution strengthening due to the gradual depletion of strengthening element Mo in  $\gamma$  matrix. In contrast, the robust hardness increment in alloy Q is due to the significant precipitation strengthening effect and the negligible loss of solid-solution strengthening because of the enhanced compositional stability of  $\gamma/\gamma'$  by W substitution.

Note that the dominance of particle shearing at small particle sizes ( $< \sim 85 \text{ nm}$  for alloy Q and  $< \sim 125 \text{ nm}$  for alloy STD) is found in the hardness measurement at RT. However, during creep tests, particle shearing was not observed for the precipitates ranging from a few tens to one hundred nanometer regimes for both alloys (Fig. 11 and 12). Instead, dislocation bowing and its interaction with precipitates following Orowan bypass mechanism appears to be the major cause of the precipitate strengthening throughout the entire creep lifetime. This finding is consistent with previous reports that the deformation mode gradually transits from precipitate shearing at low temperatures to Orowan looping at high temperatures in various Ni-based superalloys, including H282.<sup>58,59,68</sup> At high temperatures, precipitate coarsening negatively affects the  $\gamma/\gamma'$  interface coherency leading to the change in deformation

behavior aforementioned. The superior creep performance of alloy Q compared to alloy STD can be partly attributed to the presence of W, which did not contribute as strongly as Mo to TCP phase formation, providing (i) more stable solid-solution strengthening of the  $\gamma/\gamma'$  microstructure, and (ii) slower diffusion kinetics in the  $\gamma$  matrix. As discussed in the section on solid-solution strengthening, the preservation of W in the matrix (in contrast to Mo in the matrix of STD) contributes to a more stable solid-solution strengthening of the matrix, rendering dislocation slip more challenging, as indicated by fewer observed dislocations in alloy Q during creep (Fig. 11 and 12). The high concentration of W in the  $\gamma'$  phase, which increases with thermal exposure times also strengthens the precipitates, increasing resistance to dislocation shearing and leading to Orowan bowing as the rate-controlling deformation mechanism. This phenomenon also elucidates why a larger optimal precipitate size is observed in alloy Q compared to alloy STD. Finally, the stable W content in the matrix of Q maintains slow diffusion kinetics, which can reduce vacancy-mediated dislocation processes. In contrast, the depletion of Mo from STD during thermal exposure can increase diffusion kinetics while reducing the matrix strength, making dislocation slip more facile. These contribute to alloy Q's superior resistance to creep deformation compared to alloy STD.

## 5. Conclusion

In this study, variants to H282 alloy were designed by varying the concentration of  $\gamma'$  formers and/or partially substituting W for Mo. The effects of variations in  $\gamma'$  formers and refractory elements on creep resistance, phase stability, and coarsening kinetics were systematically investigated. Several key conclusions are found and summarized as follows.

1. The increase of Ti and partial substitution of W for Mo in alloy Q resulted in a significant improvement of creep resistance, up to 130% increase in creep life, compared to the baseline alloy STD.
2. Orowan looping and dislocation climb were found to be the dominant creep deformation mechanism in alloy Q and STD, while extensive dislocation tangling was also observed in alloy STD.
3. Long-term phase stability investigations on alloys Q and STD were carried out at 800 °C and 900 °C (up to 5000 h), revealing the enhanced thermal stability in alloy Q from the reduced formation of detrimental TCP phases. The extensive formation of TCP phases in alloy STD led to a decrease in Mo content in the  $\gamma$  matrix and thus decreased amount of solid-solution strengthening and faster diffusion kinetics.
4. The investigation of coarsening kinetics of  $\gamma'$  precipitates in both alloys established that the coarsening constant rate of  $\gamma'$  precipitates was retarded by the partial substitution of W for Mo, which is particularly remarkable under creep stress.
5. The theoretical strengthening calculations found that the less pronounced loss of solid-solution strengthening and the significant precipitation strengthening with a larger optimal

strengthening particle size due to the substitution of W for Mo, compared to alloy STD, further explain the origin of enhanced creep resistance in Q alloy. The addition of W and its preservation in the matrix during thermal exposure also served to improve creep resistance in Q alloy *via* maintaining slow diffusion kinetics and retarding dislocation climb.

## Disclaimer

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## Data availability statement

All relevant data that support the study are reported in the paper.

## Conflicts of interest

The authors declare the following competing interests: authors M. Detrois and P. D. Jablonski are inventors on U.S. Patent Application 18/194,447 assigned unto the United States Government on some of the alloy compositions presented and heat treatment. The present manuscript, however, describes the research and fundamental aspects related to microstructure – thermomechanical processing – mechanical property relationships.

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