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## Thermodynamic mechanism of controllable growth of two-dimensional uniformly ordered boron-doped graphene†

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Two-dimensional (2D) boron-doped graphene (B–G) exhibits remarkable properties for advanced applications in electronics, sensing and catalysis. However, the synthesis of large-area uniformly ordered 2D B–G remains a grand challenge due to the low doping level and uncontrolled distribution of dopants or even the phase separation from the competitive growth of boron polymorphs and graphene. Here, we theoretically explored the mechanism of the epitaxial growth of 2D uniformly ordered B–G on a metal substrate *via ab initio* calculations. We show that, by establishing the substrate-mediated thermodynamic phase diagrams, the controllable growth of 2D ordered B–G with different B/C stoichiometry can be achieved on appropriate substrates within distinct chemical potential windows of the feedstock by beating the competitive growth of graphene and other impurity phases. It is suggested that a suitable substrate for the controllable epitaxial growth of 2D ordered B–G can be efficiently screened based on the symmetry match and interaction between 2D B–G and the surfaces. Importantly, by carefully considering the chemical potential of boron/carbon as a function of temperature and partial pressure of the feedstock with the aid of the standard thermochemical tables, the optimal experimental parameters for the controllable growth of 2D ordered B–G are also suggested accordingly. This work provides a comprehensive and insightful understanding of the mechanism of controllable growth of 2D B–G, which will guide future experimental design.

### Introduction

Doping of heteroatoms with different electron configurations can efficiently tailor the chemical and electronic properties of two-dimensional (2D) graphene, which will lead to diverse applications of doped graphene.<sup>1,2</sup> Since boron (B) has one

### New concepts

The growth of large-area 2D uniformly ordered boron-doped graphene (B–G) is a grand challenge due to the low doping level and phase separation issue. Here we show that, by establishing the substrate-mediated thermodynamic phase diagrams, the controllable growth of 2D ordered B–G with different B/C stoichiometry can be achieved on a pre-selected substrate within distinct chemical potential windows of the feedstock by beating the competitive growth of graphene and other impurity phases, where a suitable substrate is efficiently screened based on the symmetry match and surface interaction with 2D B–G. More importantly, the optimal experimental parameters for the controllable growth of 2D ordered B–G are also suggested according to the standard thermochemical tables. This work not only provides a comprehensive and insightful understanding of the mechanism of controllable growth of 2D B–G but also can be reasonably extended to guide the controllable growth of other 2D doped systems.

valence electron less than the carbon host but similar atomic radii, B doping in graphene will act like an electron deficiency or hole additive and thus has been suggested to be an efficient way to tune the electronic properties of graphene while avoiding significant structural changes.<sup>3–5</sup> Previous studies have confirmed the characteristics of p-type semiconductors of boron doped graphene (B–G)<sup>6,7</sup> and explored the potential usage of B–G in electronic devices,<sup>8</sup> where B doping is usually conducted through *ex situ* processes experimentally.<sup>9</sup>

It was shown that B–G can be applied as a channel material for high-performance field effect transistors (FETs) or as cathode material for high-power lithium-ion batteries.<sup>8,10</sup> B–G also exhibits great prospects in the fields of photocatalysis and photo-electronics. For example, the reduction of highly active and selective oxygen to H<sub>2</sub>O<sub>2</sub> with B–G as the catalyst can achieve higher productivity than the most advanced carbon oxide catalysts in industrial production.<sup>11</sup> B–G can also be adopted as an efficient metal-free electrocatalyst for the electrochemical reduction of nitrogen in aqueous solution.<sup>12</sup> In addition, complexes of B–G and TiO<sub>2</sub> nanoparticles have shown

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potential application in CO<sub>2</sub> photo-reduction since the holes in B–G can be effectively transferred to TiO<sub>2</sub>.<sup>13</sup> Furthermore, it was also experimentally demonstrated that B doping in graphene could lead to a much-enhanced sensitivity for detecting trace amounts of molecules of toxic gases.<sup>14</sup> Besides, *ab initio* molecular dynamics simulations elucidate that B doping can significantly improve the gas adsorption performance of graphene, thus promoting the hydrogen storage capacity.<sup>15</sup>

Obviously, the properties and applications of B–G are highly dependent on the doping concentration and distribution of B atoms.<sup>7</sup> For instance, it was theoretically predicted that 2D uniformly ordered BC<sub>5</sub> shows metallic characters while BC<sub>3</sub> behaves as a semiconductor. Therefore, the preparation of large area high-quality 2D uniformly ordered B–G structures with effective control over the concentration and distribution of B doping is crucial for their real application. However, the substitutional doping of B atoms into the honeycomb-like carbon sp<sup>2</sup> network of graphene is rather difficult due to the strong C–C bonds. Density functional theory (DFT) calculations revealed that displacing C atoms from the graphene lattice with boron atoms is associated with a large activation energy barrier of ~1.3 eV.<sup>16</sup> In addition, it is suggested theoretically that the presence of three or more boron atoms within a single six-member ring leads to conspicuous deformations, while one or two boron atoms per hexagonal ring were found to be able to form stable heteroatomic nanostructures.<sup>17</sup> For this reason, the experimentally realized doping level of B atoms in graphene is fairly low. Moreover, a significant characteristic of the boron element is its polymorphism.<sup>18,19</sup> Actually, a variety of planar or quasi-planar boron clusters with medium sizes have been predicted, such as B<sub>12</sub>, B<sub>13</sub>, B<sub>19</sub> and B<sub>36</sub>, where the B<sub>12</sub> appears as the energetically more preferred one.<sup>20–26</sup> Hence, due to the competitive formations of graphene and boron polymorphs, phase separation is highly expected in the growth of B–G, which will lead to the uncontrolled doping concentration and distribution of B atoms.<sup>27</sup>

A few initial attempts at the synthesis of B–G have been conducted recently with some prototype devices based on B–G being demonstrated. For example, B–G nanoribbons have been prepared *via* surface assisted reaction by using organic-boron as the precursor<sup>28</sup> or *via* the reactive microwave plasma method by using B(CH<sub>3</sub>)<sub>3</sub> as the precursor.<sup>8</sup> The chemical vapor deposition (CVD) method, which was widely employed to produce large-area high quality graphene, has also been used for the growth of B–G.<sup>10,12,15,28,29</sup> However, the controllable growth of large-area 2D uniformly ordered B–G film has not yet been experimentally realized due to the low doping level and phase separation issues, which severely hinder the theoretical and experimental studies of 2D ordered B–G. A comprehensive mechanistic study with atomic-level insight into the controllable growth of 2D uniformly ordered B–G is urgently needed. Here, we theoretically explore the mechanism of the controllable growth of two uniformly ordered phases of 2D B–G, namely, BC<sub>3</sub> and BC<sub>5</sub>, on catalytic metal surfaces based on *ab initio* DFT calculations. Our study indicates that the controllable growth of 2D uniformly ordered BC<sub>3</sub> and BC<sub>5</sub> can be

reasonably realized by choosing an appropriate substrate and carefully adjusting the experimental conditions.

## Method and models

All the DFT calculations were performed by using the Vienna Ab initio Simulation Package (VASP).<sup>30,31</sup> The Perdew–Burke–Ernzerhof (PBE) functional<sup>32</sup> was used to describe the exchange and correlation, and the electronic interaction was described by the projector augmented wave (PAW) potential. The Monkhorst–Pack *k*-point sampling<sup>32</sup> parameters were carefully tested to produce convergent results. The DFT-D3 scheme was applied to treat the interlayer van der Waals (vdW) interactions.<sup>33</sup> All structures were fully optimized until the force component on each atom was less than 0.02 eV Å<sup>−1</sup> with an energy convergence of 10<sup>−4</sup> eV. The energy cutoff of the plane-wave basis was 400 eV.

When calculating the formation enthalpy of 2D B–G on both C<sub>2v</sub> and C<sub>6v</sub> surfaces, slab models consisting of three atomic layers with bottom layer atoms fixed were constructed to mimic the epitaxial substrate. The supercells of 2D B–G and epitaxial substrates are carefully constructed to ensure that the lattice mismatch is less than ~5%.<sup>34</sup> In addition, the 2D B–G was slightly stretched or compressed to match that of the substrates. The initial distance between the 2D B–G sheets and surfaces was set to 3.00 Å during the calculations. A vacuum space of >15 Å was set to separate images along the vertical direction of the supercell to avoid suspicious interactions between adjacent images.

## Results and discussion

There are a variety of possible ordered phases of 2D B–G with distinct B/C stoichiometry. However, it is suggested by the previous literature that the presence of three or more boron atoms within one six-member ring leads to conspicuous deformations.<sup>17</sup> In other words, over high B/C ratio (high B concentration) renders the 2D B–G system highly hole-rich and therefore highly active/unstable. In contrast, 2D ordered B–G compounds with low B concentration are predicted to show better stability. Indeed, our calculations reveal that there is no imaginary frequency band in the phonon spectrum of BC<sub>3</sub> and BC<sub>5</sub>, both of which are representative examples of 2D uniformly ordered 2D B–G with low B concentration. We thus mainly focus on BC<sub>3</sub> and BC<sub>5</sub> in the present work. In addition, another 2D B–G compound, BC<sub>11</sub>, with lower boron concentration as well as negligible phonon spectrum imaginary frequency bands was also considered (Fig. 1). Thermodynamic competitions among distinct phases of 2D B–G with different B/C ratios are expected to play vital roles during epitaxial CVD growth. Moreover, the elementary substance of carbon and boron, graphene and B<sub>12</sub> molecules, would also be the competitive phases to disturb the controllable growth of ordered 2D B–G. To figure out the thermodynamic competitions, which depend on the chemical potential of the carbon and boron source, we define

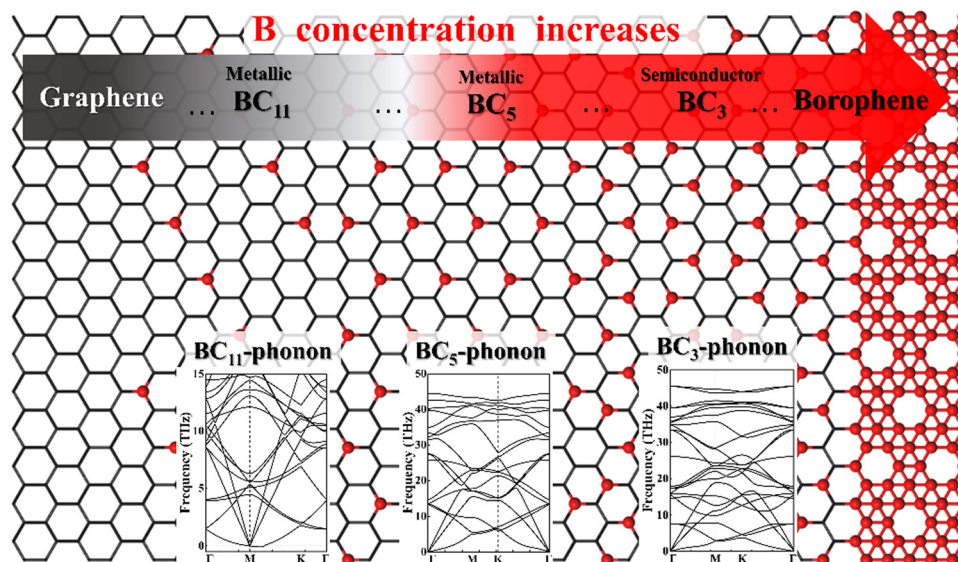


Fig. 1 The structures and calculated phonon spectra of 2D B-G with increased B concentrations (from left to right:  $\text{BC}_{11}$ ,  $\text{BC}_5$  and  $\text{BC}_3$ ). The carbon and boron atoms are denoted by the black sticks and red balls, respectively.

the formation enthalpy ( $\Delta H$ ) of dangling 2D B-G at 0 K as (1):

$$\Delta H = \frac{E_{\text{B}_x\text{C}_y} - x\mu_{\text{C}(\text{graphene})} - y\mu_{\text{B}(\text{B}_{12})}}{x + y} \quad (1)$$

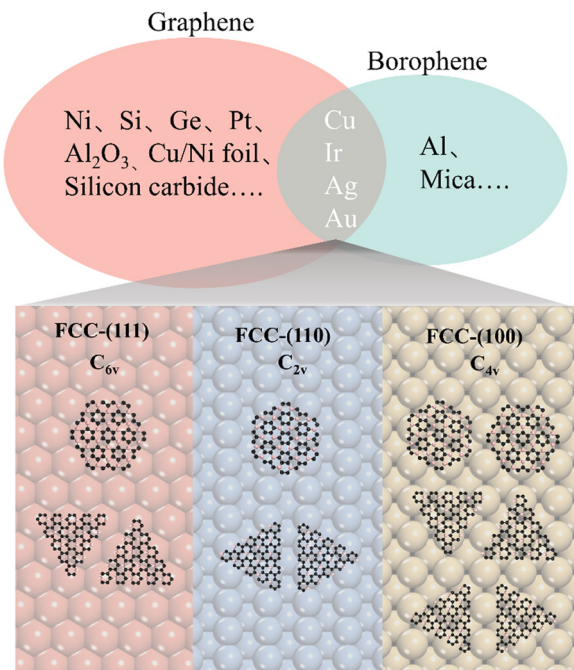
where  $E_{\text{B}_x\text{C}_y}$  is the energy of 2D B-G,  $x:y$  refers to the B/C stoichiometry of ordered 2D  $\text{B}_x\text{C}_y$  compounds, which will be 1:3, 1:5 or 1:11.  $\mu_{\text{C}(\text{graphene})}/\mu_{\text{B}(\text{B}_{12})}$  is the chemical potential of the carbon/boron atoms in graphene/ $\text{B}_{12}$  molecules. The  $\Delta H$  of graphene/ $\text{B}_{12}$  at 0 K equals zero based on such a definition. In order to stimulate the growth of 2D B-G, the chemical potential of carbon and boron  $\mu_{\text{C}}/\mu_{\text{B}}$  from the feedstock<sup>35</sup> must satisfy the following eqn (2) as required in thermodynamics:

$$\Delta H < \frac{x\Delta\mu_{\text{C}} + y\Delta\mu_{\text{B}}}{x + y} \quad (2)$$

The phase diagram of suspending  $\text{BC}_3$  and  $\text{BC}_5$  under vacuum is attained accordingly as shown in Fig. S1 (ESI†) based on the thermodynamic conditions of eqn (2). Each line in the phase diagram divides the  $\mu_{\text{C}} - \mu_{\text{B}}$  phase space into two sectors, where the upper sector favors the formation of the corresponding 2D B-G while the lower sector is unfavorable for the formation. Obviously, the unmarked upper sector of the phase diagram allows the formation of both  $\text{BC}_3$  and  $\text{BC}_5$  while the unmarked lower part rejects both. The marked in-between sector of the phase diagram may lead to the selective formation of either  $\text{BC}_3$  or  $\text{BC}_5$ . The areas painted in pink and blue denote the selective formation windows of  $\text{BC}_3$  and  $\text{BC}_5$ , respectively. Note that the reference phase of carbon and boron, namely the graphene (vertical dash line  $\mu_{\text{C}} = 0$ ) and  $\text{B}_{12}$  (horizontal dash line  $\mu_{\text{B}} = 0$ ), may also be formed in the condition of  $\mu_{\text{C}} > 0$  eV and  $\mu_{\text{B}} > 0$  eV, respectively. Thus, the graphene and  $\text{B}_{12}$  molecule will serve as main competitors to disturb the growth of 2D B-G. The formation of graphene and  $\text{B}_{12}$  will inevitably introduce solid impurities in 2D B-G and may even cause the

phase separation issue. The thermodynamic phase diagram of suspending 2D B-G indicates that controllable growth of  $\text{BC}_3$  and  $\text{BC}_5$  is feasible within certain chemical potential windows of  $\mu_{\text{C}}$  and  $\mu_{\text{B}}$ , which may be achieved by selecting proper epitaxial substrates and carefully tuning the experimental parameters.

It is known that an epitaxial substrate is very important for the CVD growth of 2D materials in terms of surface interaction and symmetry match.<sup>36,37</sup> Since the interaction between the substrate and carbon or boron atoms would be different, it is thus reasonably suggested that the intersection group of substrates used for both graphene and borophene growth could be more suitable for the epitaxial growth of 2D B-G. According to this simple theoretical assumption, four metal substrates Cu, Au, Ag,<sup>38</sup> Ir<sup>27</sup> have been successfully picked out from the intersection group to serve as the potential epitaxial substrates for the growth of 2D B-G, as shown in Fig. 2. Furthermore, a previous report suggested that the interplay between the symmetries of the epitaxial substrates and 2D materials is of vital significance to determine the crystal orientation, morphology and domain size in the epitaxial growth of 2D materials.<sup>39</sup> Consequently, the symmetry match between possible epitaxial substrates and 2D B-G must be well concerned to attain the single crystal growth of 2D B-G. Surfaces with six-fold or two-fold symmetry may be employed for the epitaxial growth of the single crystal of 2D B-G in light of the theoretical analysis of the symmetry rules of preferential alignment of 2D materials on epitaxial substrates,<sup>39</sup> as  $\text{BC}_3$  presents six-fold symmetry while  $\text{BC}_5$  exposes three-fold symmetry. As shown in Fig. 2,  $\text{BC}_3$  tends to unidirectionally align on either six-fold or two-fold surfaces whereas two/four energetically equivalent antiparallel orientations appear for the nucleation of  $\text{BC}_3/\text{BC}_5$  on four-fold symmetric epitaxial surfaces due to the symmetry mismatch, which is more unfavorable for the single crystal growth. Accordingly, the single crystal growth of  $\text{BC}_3$  and less crystalline orientation



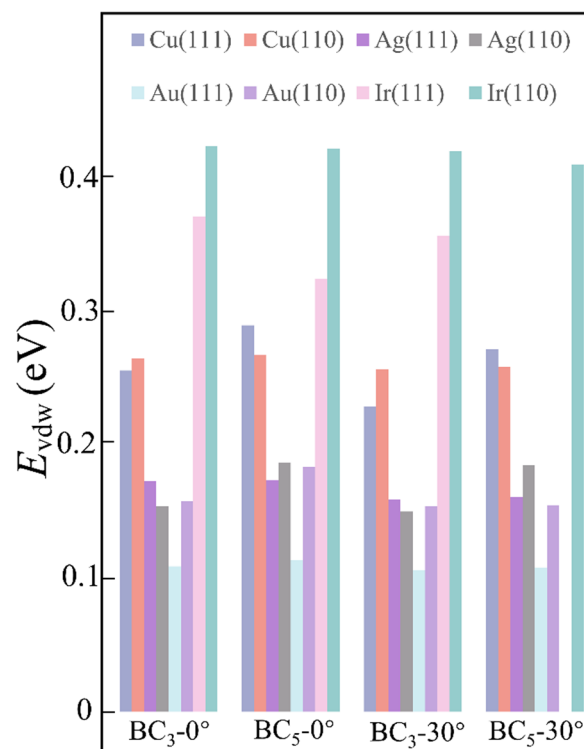
**Fig. 2** Schematic diagram of the process of screening suitable epitaxial growth substrates for 2D B-G. The epitaxial substrates used for graphene and borophene growth are marked with pink and light green background, respectively. The gray part represents the intersection of substrates, which are Cu, Ag, Ir and Au. The carbon and boron atoms are denoted by black balls and pink balls, respectively. The bottom half of the image shows the alignment of single-crystalline 2D B-G islands on (a)  $C_{6v}$ , (b)  $C_{2v}$ , and (c)  $C_{4v}$  epitaxial substrates. The three-fold symmetric  $BC_5$  and six-fold symmetric  $BC_3$  islands are in the shape of triangles and hexagons, respectively. The orientation of the island indicates the alignment of 2D B-G on the substrates.

growth of  $BC_5$  could be possible on the six-fold and two-fold epitaxial substrates. What's more, Al is excluded as a result of the incompatibility between Al and the common boron source  $B_2H_6$ . Thus, we consider the face-centered cubic (fcc) Cu(111), Ag(111), Au(111) and Ir(111) surfaces with six-fold symmetry and Cu(110), Ag(110), Au(110) and Ir(110) surfaces with two-fold symmetry to act as the potential epitaxial surfaces for the growth of 2D B-G in this work.

The strong surface interaction will be beneficial for the epitaxial growth of 2D B-G. Therefore, we extract the vdW interaction ( $E_{vdW}$ ) between 2D B-G and epitaxial surfaces *via* DFT calculations, which is defined as:

$$E_{vdW} = \frac{E_{B_xC_y} + E_{sub} - E_{B_xC_y@sub}}{x + y} \quad (3)$$

By considering the symmetry of both 2D B-G and metal surfaces, we calculated the vdW interactions of various configurations where the 2D B-G shows different rotation angles  $\theta = 0^\circ$  (zigzag (ZZ)//substrate  $\langle 110 \rangle$ ) and  $30^\circ$  (armchair (AC)//substrate  $\langle 110 \rangle$ ) with respect to the 8 types of substrate except for the case of  $BC_5-30^\circ$  on the Ir(111) surface as the



**Fig. 3** The vdW interaction between 2D B-G and various metal surfaces with rotation angle of  $0^\circ$  and  $30^\circ$ , respectively.

corresponding supercell is too large to be computationally affordable. Here the lattice mismatch is defined as eqn (4):

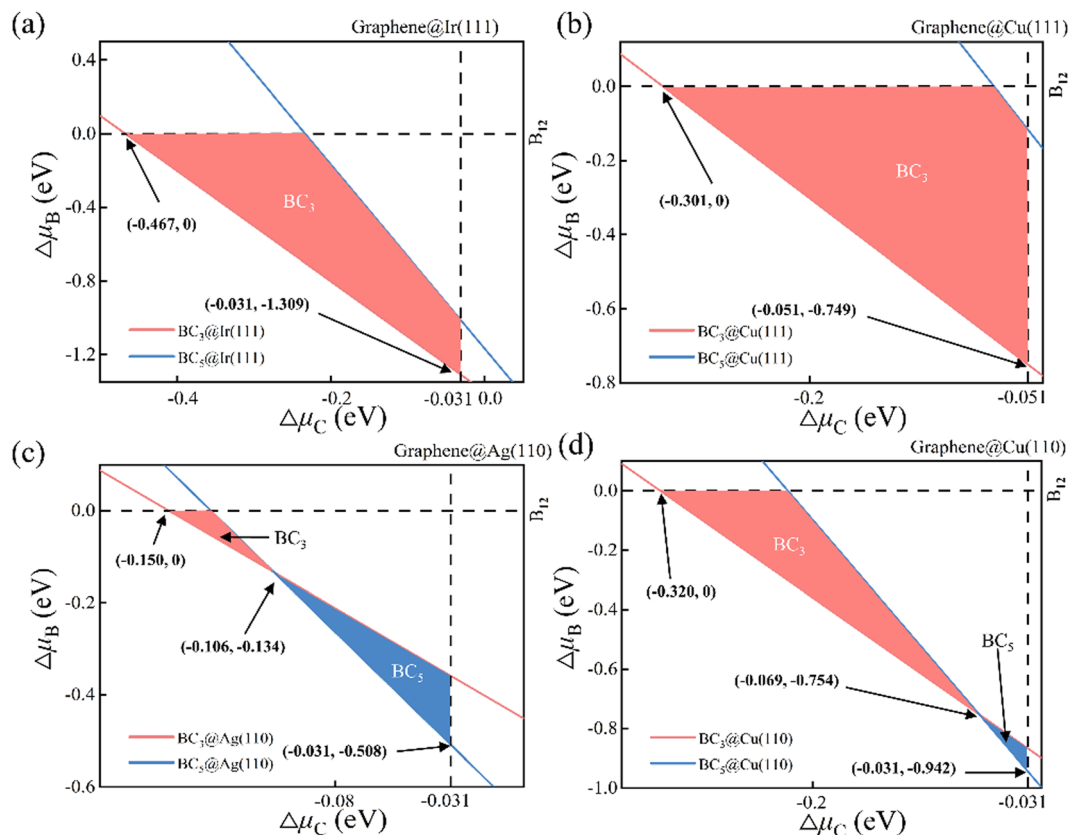
$$f = \frac{m+1}{n+1} - 1 \quad (4)$$

where  $m/n$  is a positive integer and denotes the minimum number of periodic supercells for substrate/2D B-G, respectively. The vdW interactions between 2D B-G and various metal surfaces are presented in Fig. 3. Noteworthy, it is indicated that the lower the lattice mismatch, the higher the vdW interaction between 2D B-G and various metal surfaces. In addition, the calculations indicate that the  $\theta = 0^\circ$  configuration is more energy favorable compared to the  $\theta = 30^\circ$  configuration, suggesting that the high-symmetric ZZ orientation of a 2D B-G prefers to align along the high-symmetric direction of the metal substrates, regardless of the lattice-match between the 2D material and the substrate.<sup>39</sup> Meanwhile, the vdW interactions between 2D B-G and Cu/Ir surfaces are generally stronger than that of Ag/Au, which can be attributed to the stronger surface catalytic activity of Cu/Ir. In this sense, the Cu and Ir substrates are expected to be more suitable for the selective growth of 2D B-G.

To investigate the thermodynamic equilibrium of 2D B-G on epitaxial surfaces, eqn (1) can be modified as:

$$\Delta H = \frac{E_{B_xC_y@sub} - x\mu_{C(graphene@sub)} - y\mu_{B(B_{12})} - E_{sub}}{x + y} \quad (5)$$

where  $E_{B_xC_y@sub}$  and  $E_{sub}$  represent the energies of the substrate with and without the 2D B-G, respectively.



**Fig. 4** Thermodynamic phase diagrams of 2D B-G on two typical  $C_{6V}$  surfaces (a) Ir(111), (b) Cu(111) and two  $C_{2V}$  surfaces (c) Ag(110), (d) Cu(110). The chemical potential ranges that allowed for the controllable growth of 2D B-G are painted in pink and blue, respectively. The coordinates of the intersection of the critical lines of distinct 2D B-G are denoted by arrows. The horizontal and vertical dashed lines denote the chemical potential per atom of  $B_{12}$  molecules and graphene on various substrates, respectively.

The thermodynamic phase diagrams of 2D B-G on different metal surfaces are shown in Fig. 4 and Fig. S2 (ESI<sup>†</sup>) according to eqn (2) and (5). It is suggested that the selective growth of  $BC_3$  is feasible on Cu(111), Ir(111), Ir(110) and Au(111) surfaces while the growth of  $BC_5$  may only be feasible on the Ag(111) surface. Note that the controllable growth of both  $BC_3$  and  $BC_5$  can be achieved on Cu(110), Ag(110) and Au(110) surfaces by beating the competition growth of graphene, where the product's transition between  $BC_3$  and  $BC_5$  on Cu(110), Ag(110) and Au(110) surfaces occurs around certain  $\mu_C$  and  $\mu_B$  (see Fig. 4(c), (d) and Fig. S2d, ESI<sup>†</sup>). Our calculations demonstrated that the eight investigated surfaces are all possible for the single crystal growth of  $BC_3$  or  $BC_5$  with appropriate  $\mu_B$  and  $\mu_C$ .

So far, B-G has been experimentally synthesized by using reactive microwave plasma with  $B(CH_3)_3$  as the precursor,<sup>8</sup> by the surface chemical reaction with organoboron as the precursors<sup>28</sup> or *via* simultaneous reduction of boron-doped graphene oxide at high annealing temperatures,<sup>40</sup> *etc.* However, none of these methods can accurately control the coordination environment of boron compared to chemical vapor deposition (CVD), which is a more effective method for the synthesis of B-G films, such as growing on polycrystalline copper foils using a mixture of  $CH_4$ ,  $H_2$  and  $B_2H_6$  gases at 1000 °C.<sup>41</sup> The doped

graphene film produced by CVD is utilized mainly for the thin film-based electronic devices, which prefer a clean and pollution-free environment. Therefore, the CVD manufacturing process of using gas as the feedstock of doping atoms and carbon is more preferred, which can reduce the difficulty of cleaning the generated impurities. Here,  $B_2H_6$  and  $CH_4$  are considered as the feedstock of boron and carbon in our calculations, respectively.

Actually, in practical CVD growth the  $\mu_C$  or  $\mu_B$  will be variable in a wide range as a function of temperature and pressure of the feedstock. Nevertheless, the previously mentioned formation enthalpy of 2D B-G is calculated by using the static energy of the graphene sheet and  $B_{12}$  molecule at 0 K as the reference of  $\mu_C$  and  $\mu_B$ , which cannot be utilized to directly guide the experimental study. To fill this gap, it would be highly desirable to provide the optimal experimental conditions for the controllable growth of high-quality 2D B-G by probing the thermal equilibrium between the grown 2D B-G and feedstock. To this end, we manage to establish the relationship between the chemical potential of carbon/boron and the typical experimental growth parameters, temperature and partial pressure of the feedstock, based on the NIST-JANAF thermochemical tables. At the given partial pressure ( $P$ ) and temperature ( $T$ ), the chemical potential of carbon from the hydrocarbon ( $CH_4$ )

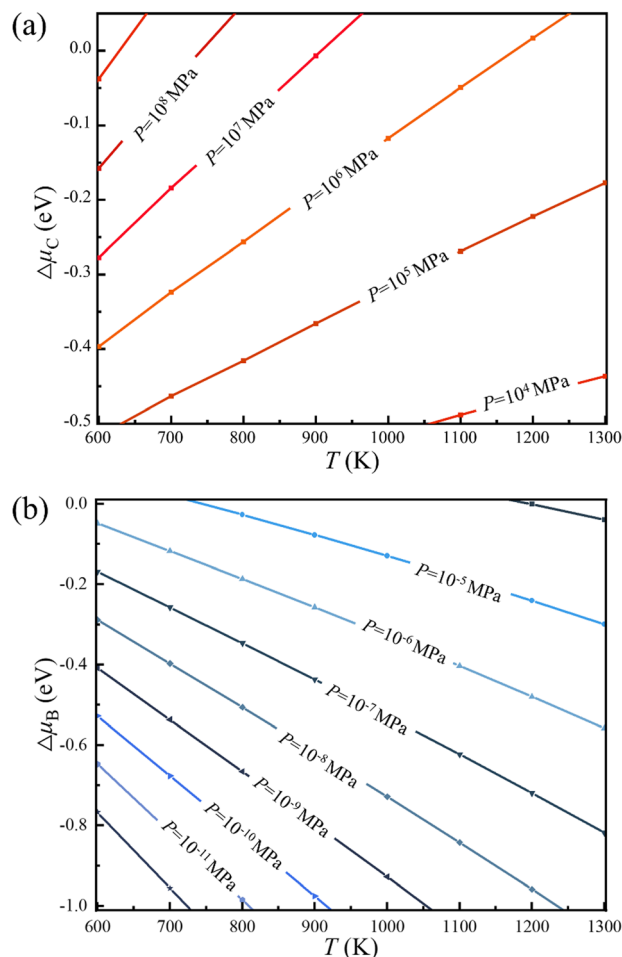


Fig. 5 Chemical potential of (a) carbon and (b) boron under specific experimental parameters of temperature and partial pressure ( $P_{H_2} = 10$  MPa), respectively.

feedstock, by using the chemical potential of graphene per atom as the reference, can be defined as (see ESI† for more details):

$$\begin{aligned}\Delta\mu_{C(CH_4)}(T, P) &= \mu_{C(CH_4)}(T, P) - \mu_{C(\text{Graphene})}(0) \\ &= \left[ H_{\text{Graphene}}^0(T) - TS_{\text{Graphene}}^0(T) - H_{\text{Graphene}}^0(0) \right] \\ &\quad + \Delta_f G_{CH_4}^0(T) + RT \ln \left[ \frac{P_{CH_4}}{P^0} \left( \frac{P^0}{P_{H_2}} \right)^2 \right]\end{aligned}\quad (6)$$

Similarly, at the given partial pressure and temperature, the chemical potential of boron from the feedstock of  $B_2H_6$ , by taking the energy of the  $B_{12}$  molecule per atom as the reference, is expressed as (see ESI† for more details):

$$\begin{aligned}\Delta\mu_{BB_2H_6}(T, P) &= \mu_{B(B_2H_6)}(T, P) - \mu_{B(B_{12})}(0) \\ &= \left[ H_{B_{12}}^0(T) - TS_{B_{12}}^0(T) - H_{B_{12}}^0(0) \right] \\ &\quad + \Delta_f G_{B_2H_6}^0(T) + RT \ln \left[ \frac{P_{B_2H_6}}{P^0} \left( \frac{P^0}{P_{H_2}} \right)^2 \right]\end{aligned}\quad (7)$$

Thus, the optimal experimental conditions for the controllable growth of high quality 2D B-G can be easily obtained according to eqn (6) and (7). As presented in Fig. 5, the selective growth of 2D B-G can be achieved under appropriate temperatures and moderate partial pressure by using  $CH_4$  and  $B_2H_6$  as feedstocks. It is found that the appropriate experimental parameters can be straightforwardly figured out from the chart for realizing the controllable growth of targeted 2D B-G. In other words, the experimental condition data where the selective growth of  $BC_3$  and  $BC_5$  on distinct surfaces can be realized, where the required temperature range can be easily grabbed at a certain partial pressure. Taking the case of  $BC_3$  on  $Ag(110)$  as an example, the selective growth can be realized when the partial pressure of  $B_2H_6 \sim 10^{-6}$  MPa and that of  $CH_4 \sim 10^7$  MPa under the temperature range of 750–1000 K.

## Conclusion

To conclude, we theoretically investigate the thermodynamic mechanism of epitaxial growth of 2D uniformly ordered B-G,  $BC_3$  and  $BC_5$ , on metal substrates by means of DFT calculations. It is suggested that the controllable growth of 2D ordered B-G on metal substrates can be achieved under distinct chemical potential windows of B/C feedstock by carefully considering the interfacial interaction and symmetry match between 2D B-G films and the metal substrates. Our results indicate that the 2D  $BC_3$  can be grown on almost all the investigated substrates except for the  $Ag(111)$  surface while the selective growth of  $BC_5$  may be possible on  $Cu(110)$ ,  $Ag(110)$ ,  $Ag(111)$  and  $Au(110)$  surfaces. Furthermore, the optimal experimental parameters, including the temperature and partial pressure, for the controllable growth of 2D ordered B-G are also proposed by taking the thermal equilibrium between the 2D B-G and feedstock into consideration. Our study provides useful guidelines for the future experimental design of the epitaxial controllable growth of 2D ordered B-G.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

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